

WIMP direct detection: EFT and phenomenological analysis

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The University of Adelaide

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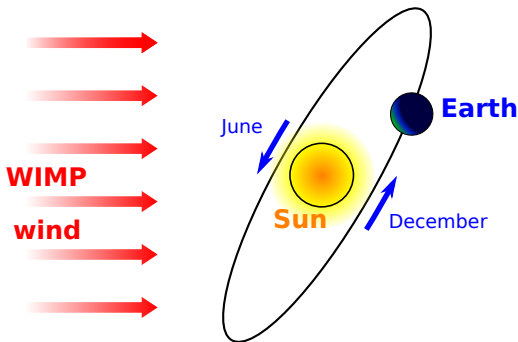


Part I: EFT in WIMP direct detection

Annual modulation of the event rate in direct detection is the key feature for a dark matter signal in direct detection experiments

K. Freese, Rev. Mod. Phys. **85** (2013) 1561

$$\frac{dR}{dE}(E, t) = S_0(E) + S_m(E) \cos \frac{2\pi}{T_0}(t - t_0) \quad (1)$$



Nal target

- DAMA
R. Bernabei *et al.*, Eur. Phys. J. C **56**, 333 (2008)
- DAMA/LIBRA phase-1
R. Bernabei *et al.*, Eur. Phys. J. C **73**, 2648 (2013)
- DAMA/LIBRA phase-2
R. Bernabei *et al.*, Universe **4**, 116 (2018).

Null experiments

- XENON100: Xenon
E. Aprile, Phys. Rev. Lett. **109**, 181301 (2012)
- CDMS: Germanium
Z. Ahmed, Science **327**, 1619 (2010);
- PICASSO: Fluorine
E. Behnke, Astropart. Phys. **90**, 85 (2017)
- COUPP, PICO-60: Fluorine-Iodine
E. Behnke, Phys. Rev. D **86**, 052001 (2012);
C. Amole, Phys. Rev. D **93**, 052014 (2016)
- CRESST-II: Calcium
G. Angloher, Eur. Phys. J. C **72**, 1971 (2012).

and more ...

The differential recoil rate in direct detection is given by

$$\frac{dR_{\chi T}}{dE_R} = \sum_T N_T \frac{\rho_\chi}{m_\chi} \int_{v_{\min}} d^3v f(\vec{v}, t) v \frac{d\sigma_{\chi T}}{dE_R}, \quad (2)$$

where

$$\frac{d\sigma_{\chi T}}{dE_R} = \frac{2m_T}{4\pi v^2} \left[\frac{1}{2j_\chi + 1} \frac{1}{2j_T + 1} \sum_{\text{spins}} |\mathcal{M}|_T^2 \right], \quad (3)$$

Calculation of $|\mathcal{M}|_T$ – NR EFT

- WIMP-**nucleon** operators, $\mathcal{O}_{\chi N} = \sum_i c_i \mathcal{O}_i$
- Embedding $\mathcal{O}_{\chi N}$ in **nucleus** states

N. Anand *et al.*, Phys. Rev. C **89**, 065501 (2014)

For dark matter spin 0 or 1/2,

$$\chi(p) + N(k) \rightarrow \chi(p') + N(k')$$

with $\vec{v} = \vec{v}_{\chi,\text{in}} - \vec{v}_{N,\text{in}}$ and $\vec{q} = \vec{p}' - \vec{p}$.

It is convenient to define

$$\vec{v}^\perp = \vec{v} + \vec{q}/2\mu_{\chi N}, \quad (4)$$

which satisfies $\vec{v}^\perp \cdot \vec{q} = 0$.

N. Anand *et al.*, Phys. Rev. C **89**, 065501 (2014)

In non-relativistic limit, the wavefunction of **free** nucleon,

$$U(p) = \sqrt{\frac{E+m}{2m}} \begin{pmatrix} \xi \\ \frac{\vec{\sigma} \cdot \vec{p}}{E+m} \xi \end{pmatrix} \rightarrow \begin{pmatrix} \xi \\ \frac{\vec{\sigma} \cdot \vec{p}}{2m} \xi \end{pmatrix}, \quad (5)$$

- $\mathcal{L} = c_1 \bar{\chi} \chi \bar{N} N \rightarrow c_1 \xi_X^\dagger \mathbf{1}_X \xi_X \xi_N^\dagger \mathbf{1}_N \xi_N + \mathcal{O}(p/m_N)$
 $\Rightarrow \mathcal{O}_1 = \mathbf{1}_X \mathbf{1}_N$
- $\mathcal{L} = c_4 \bar{\chi} \gamma_\mu \gamma_5 \chi \bar{N} \gamma^\mu \gamma_5 N \rightarrow -4c_4 \xi_X^\dagger (S_X) i \xi_X \xi_N^\dagger (S_N) i \xi_N$
 $\Rightarrow \mathcal{O}_4 = \vec{S}_X \cdot \vec{S}_N$

j	$\mathcal{L}_{\text{int}}^j$	NR Reduction in medium ($\xi^\dagger \mathcal{O}_{\text{eff}} \xi$)	$\sum_i c_i \mathcal{O}_i$
1	$\bar{\chi} \chi \bar{N} N$	$1_\chi 1_N \rightarrow \text{Standard SI}$	\mathcal{O}_1
2	$i \bar{\chi} \chi \bar{N} \gamma^5 N$	$i \frac{\vec{q}}{m_N} \cdot \vec{S}_N$	\mathcal{O}_{10}
3	$i \bar{\chi} \gamma^5 \chi \bar{N} N$	$-i \frac{\vec{q}}{m_\chi} \cdot \vec{S}_\chi$	\mathcal{O}_{11}
4	$\bar{\chi} \gamma^5 \chi \bar{N} \gamma^5 N$	$-(\frac{\vec{q}}{m_\chi} \cdot \vec{S}_\chi)(\frac{\vec{q}}{m_N} \cdot \vec{S}_N)$	\mathcal{O}_6
5	$\bar{\chi} \gamma^\mu \chi \bar{N} \gamma_\mu N$	$1_\chi 1_N$	\mathcal{O}_1
6	$\bar{\chi} \gamma^\mu \chi \bar{N} i \sigma_{\mu\alpha} \frac{q^\alpha}{m_M} N$	$\frac{\vec{q}^2}{2m_N m_M} 1_\chi 1_N + 2(\frac{\vec{q}}{m_\chi} \times \vec{S}_\chi + i\vec{v}^\perp) \cdot (\frac{\vec{q}}{m_M} \times \vec{S}_N)$	$\{\mathcal{O}_1, \mathcal{O}_3, \mathcal{O}_4, \mathcal{O}_6\}$
7	$\bar{\chi} \gamma^\mu \chi \bar{N} \gamma_\mu \gamma^5 N$	$-2\vec{S}_N \cdot \vec{v}^\perp + 2i\vec{S}_\chi \cdot (\vec{S}_N \times \frac{\vec{q}}{m_\chi})$	$\{\mathcal{O}_7, \mathcal{O}_9\}$
8	$\bar{\chi} i \gamma^\mu \chi \bar{N} \sigma_{\mu\alpha} \frac{q^\alpha}{m_M} \gamma^5 N$	$2i \frac{\vec{q}}{m_M} \cdot \vec{S}_N$	\mathcal{O}_{10}
9	$\bar{\chi} i \sigma^{\mu\nu} \frac{q_\nu}{m_M} \chi \bar{N} \gamma_\mu N$	$-\frac{\vec{q}^2}{2m_\chi m_M} 1_\chi 1_N - 2(\frac{\vec{q}}{m_M} \times \vec{S}_\chi) \cdot (\frac{\vec{q}}{m_N} \times \vec{S}_N + i\vec{v}^\perp)$	$\{\mathcal{O}_1, \mathcal{O}_4, \mathcal{O}_5, \mathcal{O}_6\}$
10	$\bar{\chi} i \sigma^{\mu\nu} \frac{q_\nu}{m_M} \chi \bar{N} i \sigma_{\mu\alpha} \frac{q^\alpha}{m_M} N$	$4(\frac{\vec{q}}{m_M} \times \vec{S}_\chi) \cdot (\frac{\vec{q}}{m_M} \times \vec{S}_N)$	$\{\mathcal{O}_4, \mathcal{O}_6\}$

11	$\bar{\chi}i\sigma^{\mu\nu}\frac{q_\nu}{m_M}\chi\bar{N}\gamma_\mu\gamma_5N$	$4i(\frac{\vec{q}}{m_M}\times\vec{S}_\chi)\cdot\vec{S}_N$	\mathcal{O}_9
12	$i\bar{\chi}i\sigma^{\mu\nu}\frac{q_\nu}{m_M}\chi\bar{N}i\sigma_{\mu\alpha}\frac{q^\alpha}{m_M}\gamma^5N$	$-[i\frac{\vec{q}^2}{m_M m_M} - 4\vec{v}^\perp\cdot(\frac{\vec{q}}{m_M}\times\vec{S}_\chi)](\frac{\vec{q}}{m_M}\cdot\vec{S}_N)$	$\{\mathcal{O}_{10}, \mathcal{O}_{12}, \mathcal{O}_{15}\}$
13	$\bar{\chi}\gamma^\mu\gamma^5\chi\bar{N}\gamma_\mu N$	$2\vec{S}_\chi\cdot\vec{v}^\perp + 2i\vec{S}_\chi\cdot(\vec{S}_N\times\frac{\vec{q}}{m_N})$	$\{\mathcal{O}_8, \mathcal{O}_9\}$
14	$\bar{\chi}\gamma^\mu\gamma^5\chi\bar{N}i\sigma_{\mu\alpha}\frac{q^\alpha}{m_M}N$	$4i\vec{S}_\chi\cdot(\frac{\vec{q}}{m_M}\times\vec{S}_N)$	\mathcal{O}_9
15	$\bar{\chi}\gamma^\mu\gamma^5\chi\bar{N}\gamma^\mu\gamma^5N$	$-4\vec{S}_\chi\cdot\vec{S}_N \rightarrow \text{Standard SD}$	\mathcal{O}_4
16	$i\bar{\chi}\gamma^\mu\gamma^5\chi\bar{N}i\sigma_{\mu\alpha}\frac{q^\alpha}{m_M}\gamma^5N$	$4i(\vec{S}_\chi\cdot\vec{v}^\perp)(\vec{S}_N\cdot\frac{\vec{q}}{m_M})$	\mathcal{O}_{13}
17	$i\bar{\chi}i\sigma^{\mu\nu}\frac{q_\nu}{m_M}\gamma^5\chi\bar{N}\gamma_\mu N$	$2i\frac{\vec{q}}{m_M}\cdot\vec{S}_\chi$	\mathcal{O}_{11}
18	$i\bar{\chi}i\sigma^{\mu\nu}\frac{q_\nu}{m_M}\gamma^5\chi\bar{N}i\sigma_{\mu\alpha}\frac{q^\alpha}{m_M}N$	$(\frac{\vec{q}}{m_M}\cdot\vec{S}_\chi)[i\frac{\vec{q}^2}{m_N m_M} - 4\vec{v}^\perp\cdot(\frac{\vec{q}}{m_M}\times\vec{S}_N)]$	$\{\mathcal{O}_{11}, \mathcal{O}_{15}\}$
19	$i\bar{\chi}i\sigma^{\mu\nu}\frac{q_\nu}{m_M}\gamma^5\chi\bar{N}\gamma_\mu\gamma^5N$	$-4i(\vec{S}_\chi\cdot\frac{\vec{q}}{m_M})(\vec{S}_N\cdot\vec{v}^\perp)$	\mathcal{O}_{14}
20	$i\bar{\chi}i\sigma^{\mu\nu}\frac{q_\nu}{m_M}\gamma^5\chi\bar{N}i\sigma_{\mu\alpha}\frac{q^\alpha}{m_M}\gamma^5N$	$4i(\frac{\vec{q}}{m_M}\cdot\vec{S}_\chi)(\frac{\vec{q}}{m_M}\cdot\vec{S}_N)$	\mathcal{O}_6

- There are 14 independent effective operators satisfying Galilean invariance, CPT symmetry, Hermitian
- Built out of the following four quantities

$$i\frac{\vec{q}}{m_N}, \quad \vec{v}^\perp, \quad \vec{S}_\chi, \quad \vec{S}_N. \quad (6)$$

where $\vec{v}^\perp = \vec{v} + \vec{q}/2\mu_{\chi N}$, which satisfies $\vec{v}^\perp \cdot \vec{q} = 0$.

- Inelastic scattering of spin 0 and 1/2 dark matter:
[G. Barello, PRD 90, 094027 \(2014\)](#)
- Higher dark matter spin:
[P. Gondolo, arXiv: 2008.05120](#)

Model independent, nucleus independent

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- Inelastic scattering of spin 0 and 1/2 dark matter:
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Model independent, nucleus independent

WIMPs interact with **bound** nucleon in a nucleus

The nuclear dynamics, notably the relativistic mean-fields, may modify these effective operators

M. Bolsterli *et al.*, Phys. Rev. C **10** (1974) 1225.

- model dependent
- nucleus dependent

Part II: Relativistic mean-field corrections

XGW and A. W. Thomas, arXiv: 2012.10144

In a nuclear medium, we assume that the wave function of a nucleon bound by Lorentz scalar and vector mean-fields satisfies the relativistic Dirac equation

$$\gamma^0 \left[-i\vec{\gamma} \cdot \nabla + M + V_s + \gamma^0 V_v \right] \psi(\vec{x}) = E\psi(\vec{x}), \quad (7)$$

where V_s corresponds to an attractive Lorentz scalar potential and V_v the repulsive fourth component of a four-vector.

$$\psi = \begin{pmatrix} u \\ v \end{pmatrix} \Rightarrow \begin{cases} u = \frac{1}{E-M-V_s-V_v} \vec{\sigma} \cdot \vec{p} v \\ v = \frac{1}{E+M+V_s-V_v} \vec{\sigma} \cdot \vec{p} u \end{cases} \rightarrow \frac{1}{2M[1+(V_s-V_v)/2M]} \vec{\sigma} \cdot \vec{p} u$$

j	$\mathcal{L}_{\text{int}}^j$	Non-relativistic Reduction in medium ($u^\dagger \mathcal{O}_{\text{eff}} u$)
1	$\bar{\chi}\chi\bar{N}N$	$1_\chi 1_N$
2	$i\bar{\chi}\chi\bar{N}\bar{\gamma}^5 N$	$i\frac{\vec{q}}{m_N} \cdot \vec{S}_N \frac{1}{1+(V_s-V_v)/2m_N}$
3	$i\bar{\chi}\bar{\gamma}^5\chi\bar{N}N$	$-i\frac{\vec{q}}{m_\chi} \cdot \vec{S}_\chi$
4	$\bar{\chi}\bar{\gamma}^5\chi\bar{N}\bar{\gamma}^5 N$	$-(\frac{\vec{q}}{m_\chi} \cdot \vec{S}_\chi)(\frac{\vec{q}}{m_N} \cdot \vec{S}_N) \frac{1}{1+(V_s-V_v)/2m_N}$
5	$\bar{\chi}\bar{\gamma}^\mu\chi\bar{N}\bar{\gamma}_\mu N$	$1_\chi 1_N$
6	$\bar{\chi}\bar{\gamma}^\mu\chi\bar{N}i\sigma_{\mu\alpha}\frac{q^\alpha}{m_M}N$	$\frac{q^2}{2m_N m_M} 1_\chi 1_N + 2(\frac{\vec{q}}{m_\chi} \times \vec{S}_\chi + i\vec{v}^\perp) \cdot (\frac{\vec{q}}{m_M} \times \vec{S}_M)$ $-[\frac{q^2}{2m_N m_M} 1_\chi 1_N - 2i\frac{\vec{k}' + \vec{k}}{2m_N} \cdot (\frac{\vec{q}}{m_M} \times \vec{S}_M)] \frac{V_s - V_v}{2m_N[1+(V_s-V_v)/2m_N]}$
7	$\bar{\chi}\bar{\gamma}^\mu\chi\bar{N}\bar{\gamma}_\mu\bar{\gamma}^5 N$	$-2\vec{S}_N \cdot \vec{v}^\perp + 2i\vec{S}_\chi \cdot (\vec{S}_N \times \frac{\vec{q}}{m_\chi}) - \vec{S}_N \cdot \frac{\vec{k}' + \vec{k}}{m_N} \frac{V_s - V_v}{2m_N[1+(V_s-V_v)/2m_N]}$
8	$\bar{\chi}i\bar{\gamma}^\mu\chi\bar{N}\bar{\sigma}_{\mu\alpha}\frac{q^\alpha}{m_M}\bar{\gamma}^5 N$	$2i\frac{\vec{q}}{m_M} \cdot \vec{S}_N$
9	$\bar{\chi}i\sigma^{\mu\nu}\frac{q_\nu}{m_M}\chi\bar{N}\bar{\gamma}_\mu N$	$-\frac{q^2}{2m_\chi m_M} 1_\chi 1_N - 2(\frac{\vec{q}}{m_M} \times \vec{S}_\chi) \cdot (\frac{\vec{q}}{m_N} \times \vec{S}_N + i\vec{v}^\perp)$ $+2(\frac{\vec{q}}{m_M} \times \vec{S}_\chi) \cdot (\frac{\vec{q}}{m_N} \times \vec{S}_N - i\frac{\vec{k}' + \vec{k}}{2m_N}) \frac{V_s - V_v}{2m_N[1+(V_s-V_v)/2m_N]}$
10	$\bar{\chi}i\sigma^{\mu\nu}\frac{q_\nu}{m_M}\chi\bar{N}i\sigma_{\mu\alpha}\frac{q^\alpha}{m_M}N$	$4(\frac{\vec{q}}{m_M} \times \vec{S}_\chi) \cdot (\frac{\vec{q}}{m_M} \times \vec{S}_M)$

- 11 $\bar{\chi}i\sigma^{\mu\nu}\frac{q_\nu}{m_M}\chi\bar{N}\gamma_\mu\gamma_5N$ $4i(\frac{\vec{q}}{m_M} \times \vec{S}_\chi) \cdot \vec{S}_N$
- 12 $i\bar{\chi}i\sigma^{\mu\nu}\frac{q_\nu}{m_M}\chi\bar{N}i\sigma_{\mu\alpha}\frac{q^\alpha}{m_M}\gamma^5N$ $-[i\frac{\vec{q}^2}{m_M m_M} - 4\vec{v}^\perp \cdot (\frac{\vec{q}}{m_M} \times \vec{S}_\chi)](\frac{\vec{q}}{m_M} \cdot \vec{S}_N)$
 $+4[\frac{\vec{k}'+\vec{k}}{2m_N} \cdot (\frac{\vec{q}}{m_M} \times \vec{S}_\chi)(\frac{\vec{q}}{m_M} \cdot \vec{S}_N) - \frac{\vec{k}'^2-\vec{k}^2}{2m_N m_M}(\frac{\vec{q}}{m_M} \times \vec{S}_\chi) \cdot \vec{S}_N]\frac{V_s-V_v}{2m_N[1+(V_s-V_v)/2m_N]}$
- 13 $\bar{\chi}\gamma^\mu\gamma^5\chi\bar{N}\gamma_\mu N$ $2\vec{S}_\chi \cdot \vec{v}^\perp + 2i\vec{S}_\chi \cdot (\vec{S}_N \times \frac{\vec{q}}{m_N}) + [\vec{S}_\chi \cdot \frac{\vec{k}'+\vec{k}}{m_N} - 2i\vec{S}_\chi \cdot (\vec{S}_N \times \frac{\vec{q}}{m_N})]\frac{V_s-V_v}{2m_N[1+(V_s-V_v)/2m_N]}$
- 14 $\bar{\chi}\gamma^\mu\gamma^5\chi\bar{N}i\sigma_{\mu\alpha}\frac{q^\alpha}{m_M}N$ $4i\vec{S}_\chi \cdot (\frac{\vec{q}}{m_M} \times \vec{S}_N)$
- 15 $\bar{\chi}\gamma^\mu\gamma^5\chi\bar{N}\gamma^\mu\gamma^5N$ $-4\vec{S}_\chi \cdot \vec{S}_N$
- 16 $i\bar{\chi}\gamma^\mu\gamma^5\chi\bar{N}i\sigma_{\mu\alpha}\frac{q^\alpha}{m_M}\gamma^5N$ $4i(\vec{S}_\chi \cdot \vec{v}^\perp)(\vec{S}_N \cdot \frac{\vec{q}}{m_M}) + 4i[(\vec{S}_\chi \cdot \frac{\vec{k}'+\vec{k}}{2m_N})(\vec{S}_N \cdot \frac{\vec{q}}{m_M}) - \frac{\vec{k}'^2-\vec{k}^2}{2m_N m_M}(\vec{S}_\chi \cdot \vec{S}_N)]\frac{V_s-V_v}{2m_N[1+(V_s-V_v)/2m_N]}$
- 17 $i\bar{\chi}i\sigma^{\mu\nu}\frac{q_\nu}{m_M}\gamma^5\chi\bar{N}\gamma_\mu N$ $2i\frac{\vec{q}}{m_M} \cdot \vec{S}_\chi$
- 18 $i\bar{\chi}i\sigma^{\mu\nu}\frac{q_\nu}{m_M}\gamma^5\chi\bar{N}i\sigma_{\mu\alpha}\frac{q^\alpha}{m_M}N$ $(\frac{\vec{q}}{m_M} \cdot \vec{S}_\chi)[i\frac{\vec{q}^2}{m_N m_M} - 4\vec{v}^\perp \cdot (\frac{\vec{q}}{m_M} \times \vec{S}_N)]$
 $-(\frac{\vec{q}}{m_M} \cdot \vec{S}_\chi)[i\frac{\vec{q}^2}{m_N m_M} + 4\frac{\vec{k}'+\vec{k}}{2m_N} \cdot (\frac{\vec{q}}{m_M} \times \vec{S}_N)]\frac{V_s-V_v}{2m_N[1+(V_s-V_v)/2m_N]}$
- 19 $i\bar{\chi}i\sigma^{\mu\nu}\frac{q_\nu}{m_M}\gamma^5\chi\bar{N}\gamma_\mu\gamma^5N$ $-4i(\vec{S}_\chi \cdot \frac{\vec{q}}{m_M})(\vec{S}_N \cdot \vec{v}^\perp) - 4i(\vec{S}_\chi \cdot \frac{\vec{q}}{m_M})(\vec{S}_N \cdot \frac{\vec{k}'+\vec{k}}{2m_N})\frac{V_s-V_v}{2m_N[1+(V_s-V_v)/2m_N]}$
- 20 $i\bar{\chi}i\sigma^{\mu\nu}\frac{q_\nu}{m_M}\gamma^5\chi\bar{N}i\sigma_{\mu\alpha}\frac{q^\alpha}{m_M}\gamma^5N$ $4i(\frac{\vec{q}}{m_M} \cdot \vec{S}_\chi)(\frac{\vec{q}}{m_M} \cdot \vec{S}_N)$

The large component $u(\vec{x})$ of the bound nucleon wave-function satisfies the Schrodinger equation

$$\left[\frac{1}{2m_N} p^2 + (V_s + V_v) + \frac{1}{2m_N} (V_s^2 - V_v^2) + \frac{B}{m_N} V_v - \underbrace{\frac{1}{4m_N^2} \frac{1}{r} \frac{d(V_s - V_v)}{dr} \vec{\sigma} \cdot \vec{l}}_{\text{spin-orbital}} - \underbrace{\frac{1}{8m_N^2} \nabla^2 (V_s - V_v)}_{\text{Darwin term}} \right] u(\vec{x}) = B u(\vec{x}),$$

One can define the effective potential

$$V_{\text{eff}} = V_s + V_v + \frac{V_s^2 - V_v^2}{2m_N} + \frac{B}{m_N} V_v. \quad (8)$$

J. V. Noble, Phys. Rev. C **17** (1978)2151

The correction induced by the RMF potentials involves a factor

$$1/[1 + (V_s - V_v)/2m_N] \quad (9)$$

- Quantum hydrodynamics:

$$V_s \approx -400 \text{ MeV}, \quad V_v \approx 350 \text{ MeV}$$

J. D. Walecka, *Int. J. Mod. Phys. E* 6, 515 (1997)

- Quark meson coupling (QMC) model:

$$V_s \approx -190 \text{ MeV}, \quad V_v \approx 130 \text{ MeV}$$

A. W. Thomas, *Prog. Part. Nucl. Phys.* 58, 1 (2007)

⇒ a boost for the effective interaction as large as 21-66%

- The standard SI/SD operators are unchanged
- Certain interactions will receive non-negligible corrections, which may significantly change the sensitivity of WIMP-nucleus cross sections to these operators
- It may help to study the nucleus-dependence of direct detection experiments
- This analysis can also be applied to the case of arbitrary dark matter spin, as well as inelastic scattering

Part III: Phenomenological analysis

Existing models

Either elastic or inelastic, single or two-component dark matter

VDF

DM response

Nuclear response

$$\frac{dR_{\chi T}}{dE_R} \propto$$

$$f(\vec{v}, t)$$

$$\otimes R_k \left(\vec{v} \frac{1}{T^2}, \{c_i^T c_j^{T'}\} \right)$$

$$\otimes W_k^{TT'}(\vec{q}^2 b^2)$$

SHM

SHM + Stream
Gaia Sausage

⋮

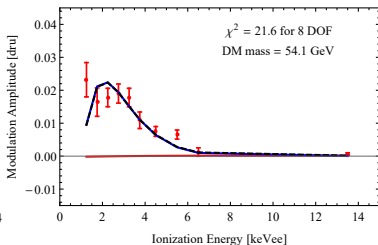
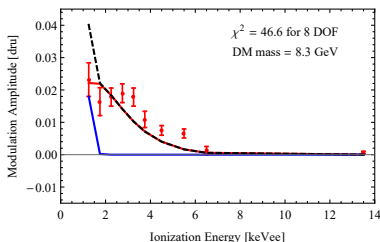
spin-1/2
SI/SD

Shell model

RMF
coupled – cluster

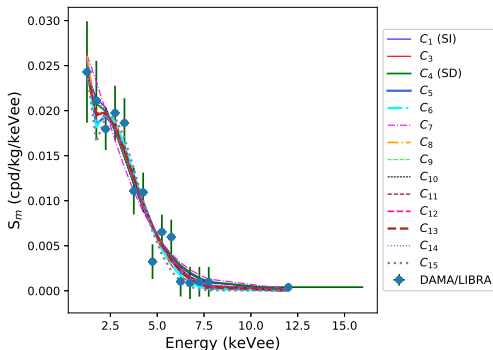
⋮

- SI/SD + elastic
S. Baum, PLB 789, 262 (2019)



- SI + isospin conserving is disfavored
- SI + isospin violating, or, SD ($c_n \neq c_p$) can provide a good fit

- Non-SI/SD + elastic
S. Kang, JCAP 07, 016 (2018)



- χ^2 ranging from 10.69 to 13.94 with 12 degree of freedom
- m_χ ranging from 7.32 ~ 13.41 GeV
- All the best fit solutions are in tension with XENON1T and PICO60.

- Two-component DM + SI + elastic
J. Herrero-Garcia, PRD 98, 123007 (2018)

$$\chi_i + N \rightarrow \chi_i + N, \quad (i = 1, 2)$$

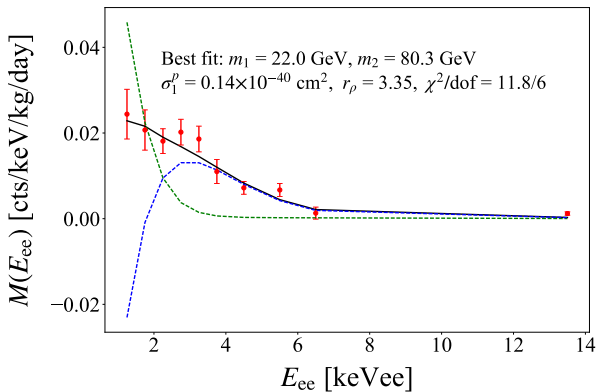


Figure: dotted green: DM 1; dashed blue: DM 2

Proton-philic + SD + inelastic:

S. Kang, PRD 99, 023017 (2019)

$$\chi_1(m_\chi) + N \rightarrow \chi_2(m_\chi + \delta) + N$$

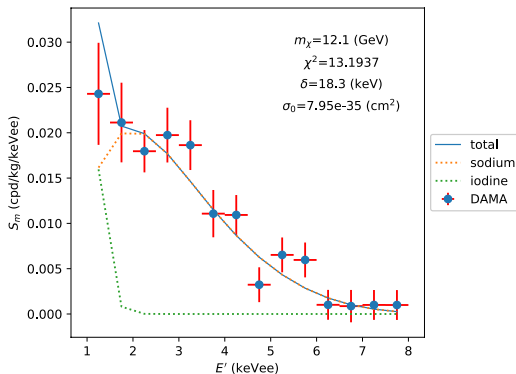


Figure: SHM + Best fit to DAMA/LIBRA

Relax experimental tensions

- tune SI coupling by large suppression
- tune SD couplings $c_n/c_p = -0.028$
Xe, Ge : unpaired neutron \rightarrow suppressed
Na, I, F: unpaired proton
- inelastic up-scatter

$$\chi_1(m_\chi) + N \rightarrow \chi_2(m_\chi + \delta) + N$$

$$v_{\min}^* = \sqrt{\frac{2\delta}{\mu_{\chi N}}},$$

$$v_{\min}^{*\text{Na}} < v_{\text{esc}}^{\text{lab}} < v_{\min}^{*\text{F}}$$

WIMP-Fluorine scattering is
kinematically suppressed

SHM + Best fit to
DAMA/LIBRA data
do **not** satisfy this
requirement.

SHM + Stream
[arXiv.org/abs/2005.10404](https://arxiv.org/abs/2005.10404)
(Madeleine)

Relax experimental tensions

- tune SI coupling by large suppression
- tune SD couplings $c_n/c_p = -0.028$
Xe, Ge : unpaired neutron \rightarrow suppressed
Na, I, F: unpaired proton
- inelastic up-scatter

$$\chi_1(m_\chi) + N \rightarrow \chi_2(m_\chi + \delta) + N$$

$$v_{\min}^* = \sqrt{\frac{2\delta}{\mu_{\chi N}}},$$
$$v_{\min}^{*\text{Na}} < v_{\text{esc}}^{\text{lab}} < v_{\min}^{*\text{F}}$$

WIMP-Fluorine scattering is
kinematically suppressed

SHM + Best fit to
DAMA/LIBRA data
do **not** satisfy this
requirement.

SHM + Stream
[arXiv.org/abs/2005.10404](https://arxiv.org/abs/2005.10404)
(Madeleine)

Tony Williams, Andre Scaffidi, Bill Loizos (Honours)

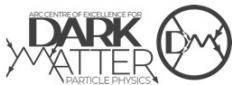
Our plan

- SHM + substructure
- two-component dark matter
- beyond SI interaction

Something else

- inelastic scattering model
- higher spin dark matter

Thanks!



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The University Of Sheffield.

