

# Axions and Wave Like Dark Matter



Michael Tobar



THE UNIVERSITY OF  
**WESTERN  
AUSTRALIA**

QDM

# Searching for Putative Wave-Like Dark Matter

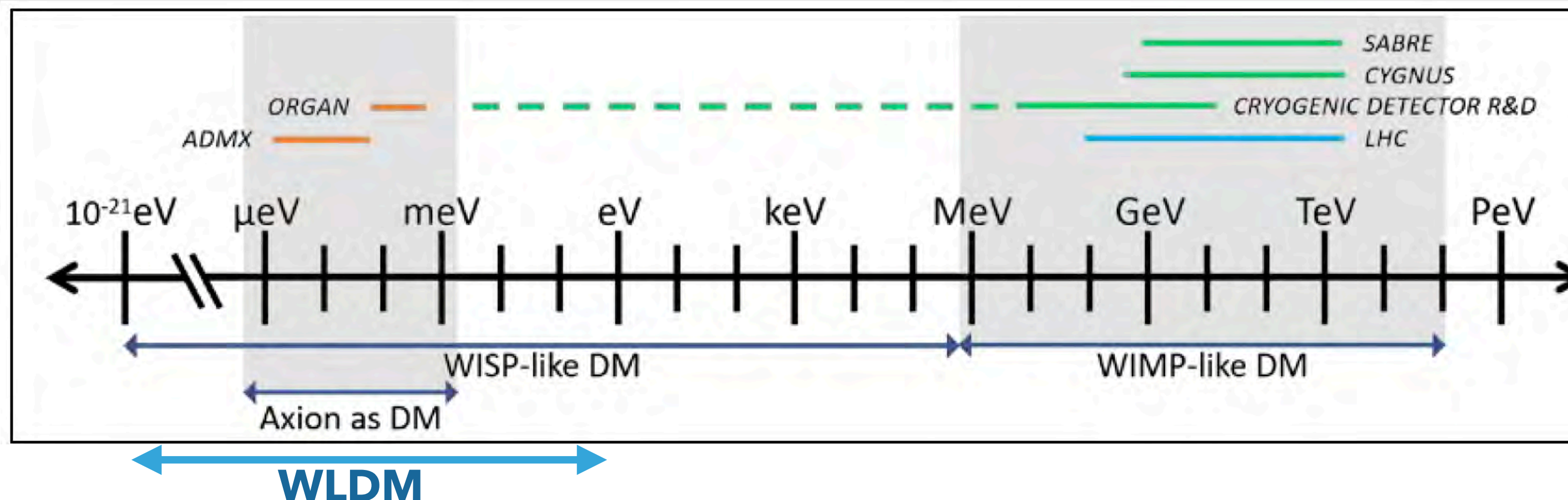


Figure 4: Dark matter mass ranges to be searched in Centre WIMP and WISP direct detection experiments and the LHC Program.

## SNOWMASS

### Cosmic Frontier: Wave-Like Dark Matter

**Joerg Jaeckel**  
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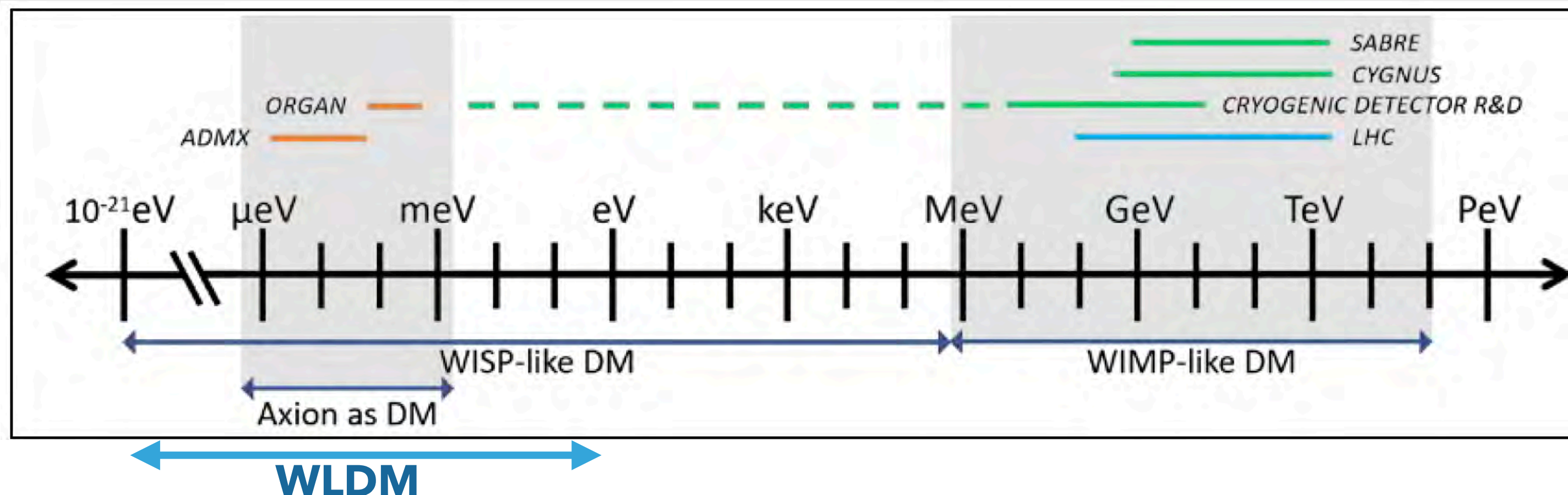


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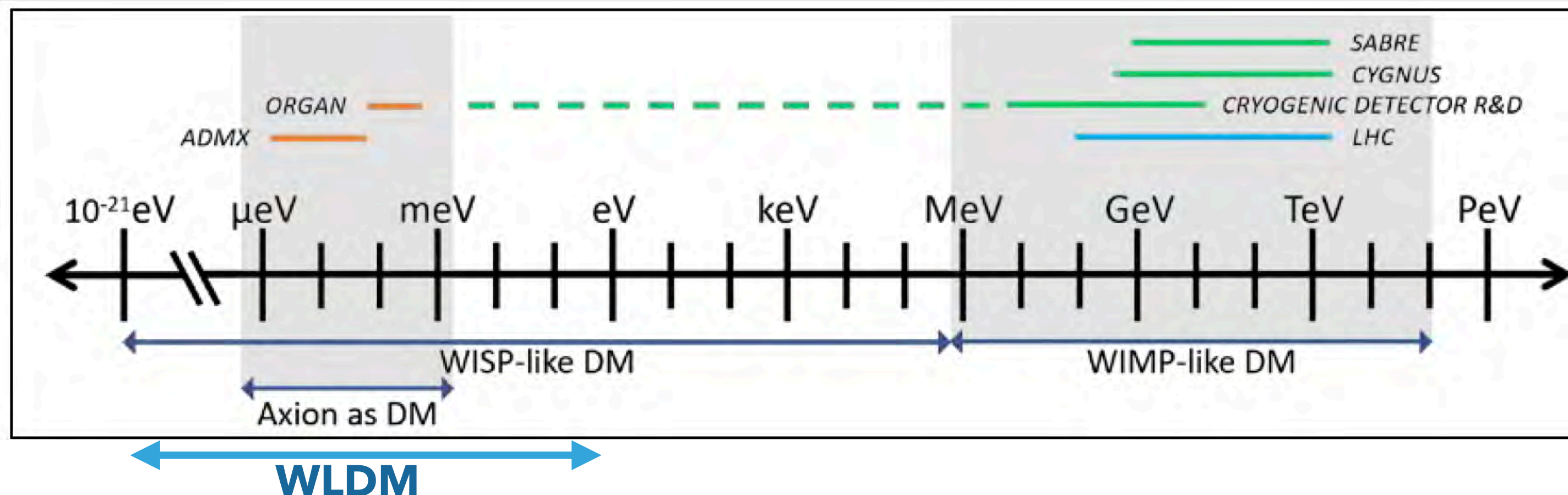


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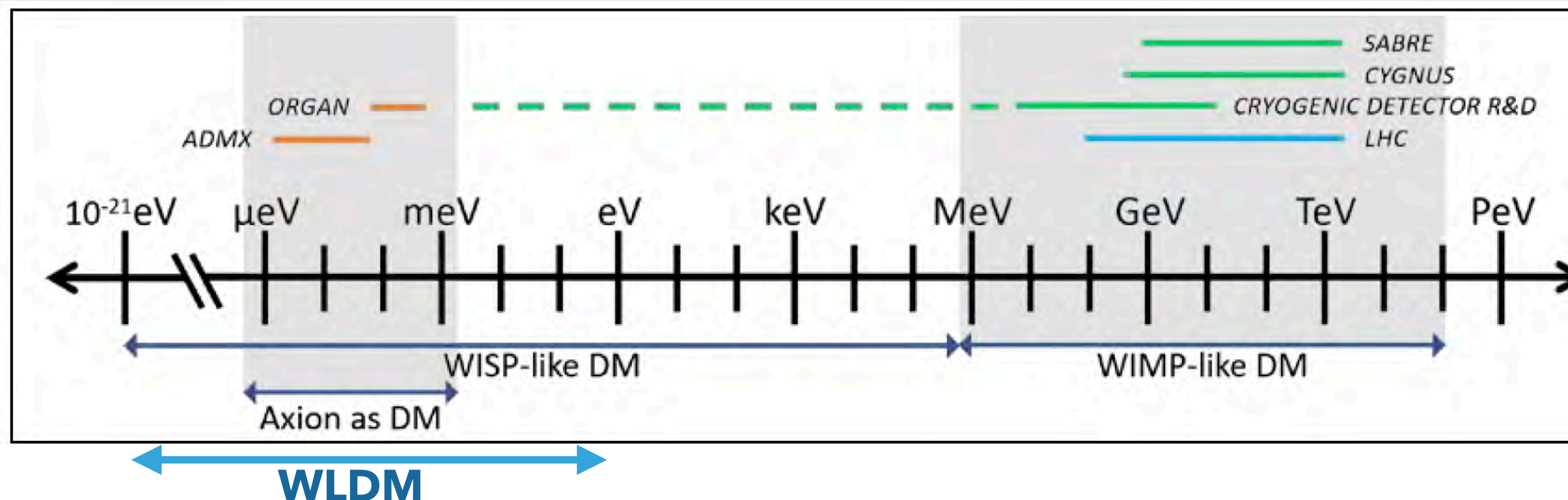


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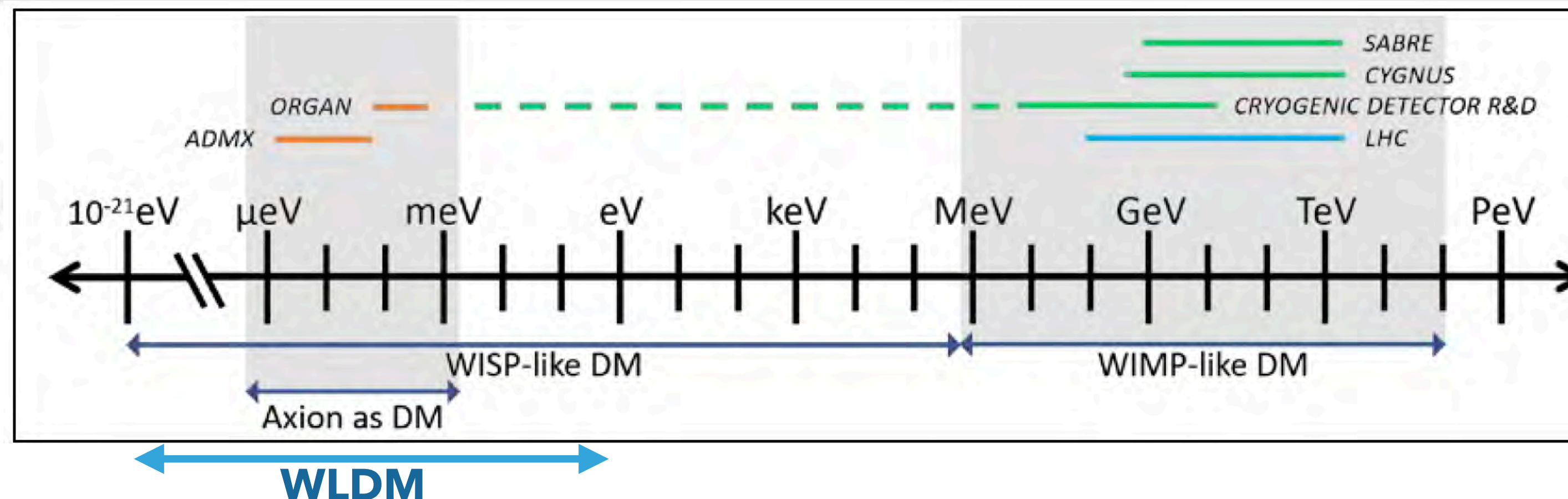


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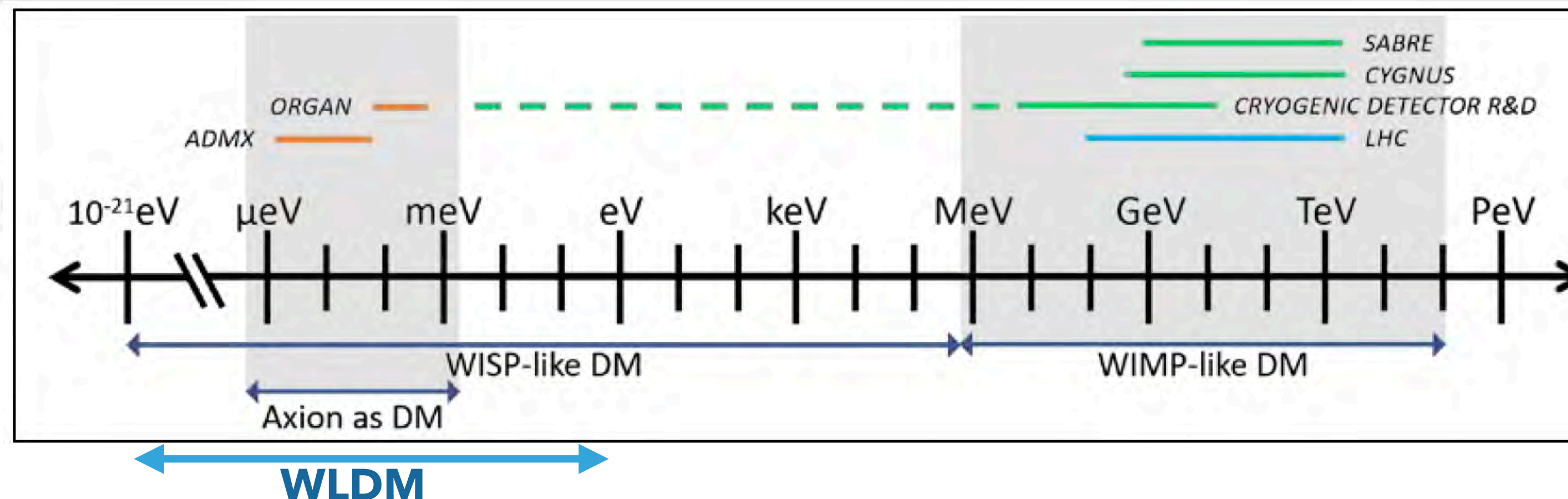


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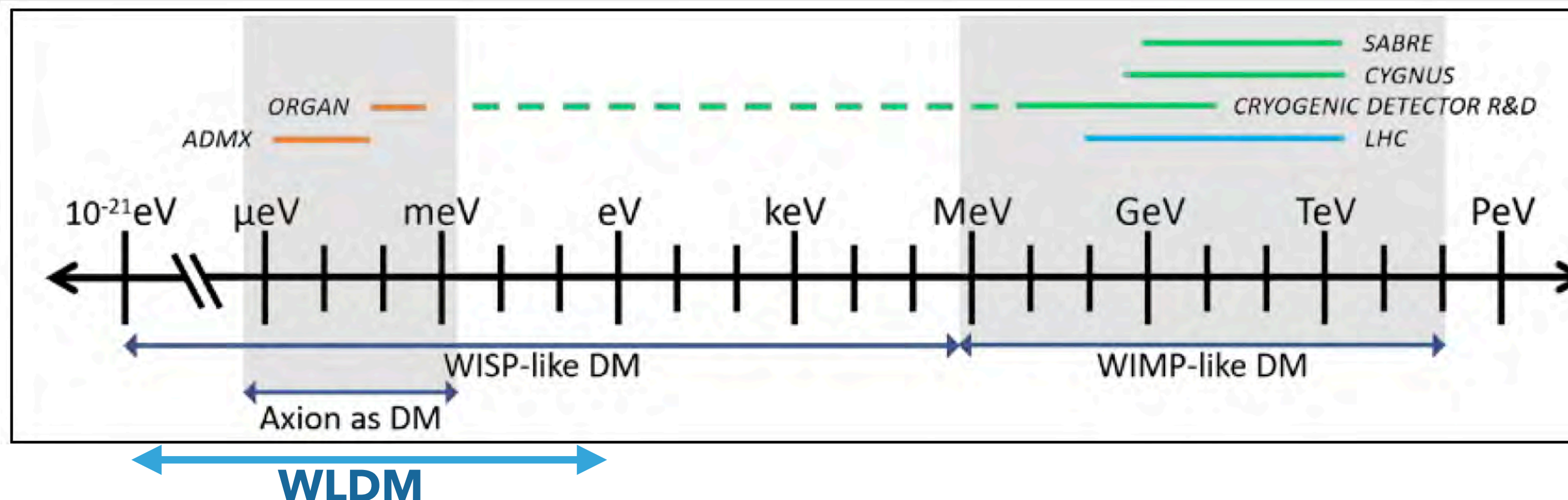


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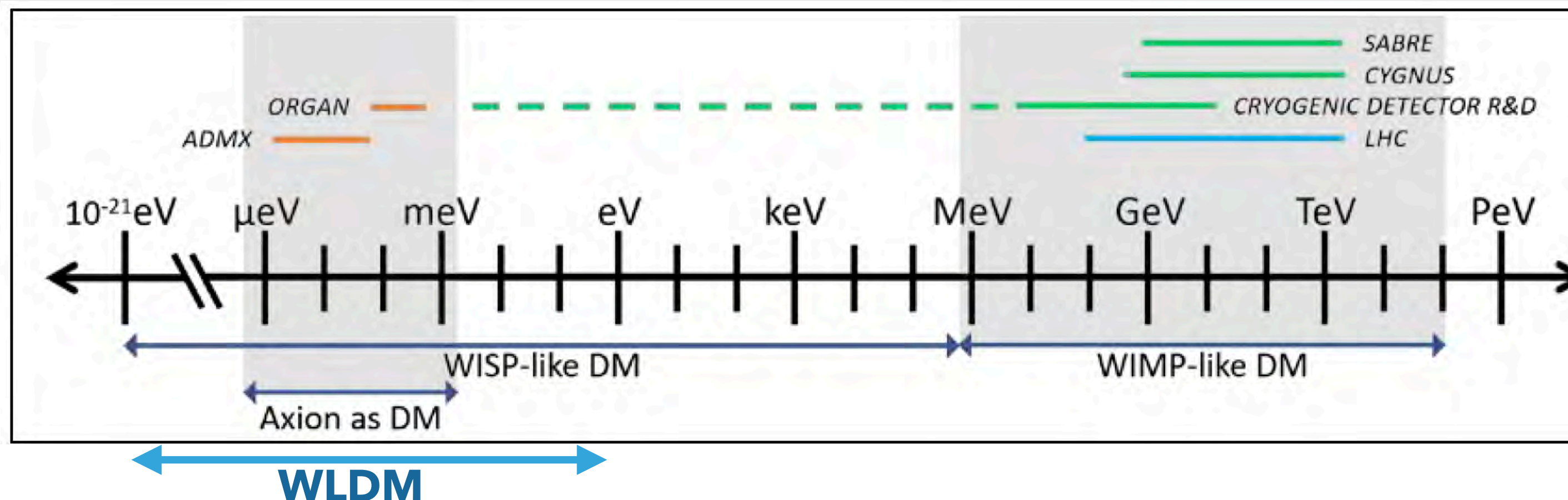


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- > Surpass Quantum Limit: Quantum Metrology

# STATUS AND PLANS

## CURRENT AXION DM PROGRAMS

ORGAN

UPLOAD

ADMX

Collaboration

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## NEW AXION DM PROGRAMS

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AXION-MONOPOLE  
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BULK ACOUSTIC WAVE:  
OSCILLATING  
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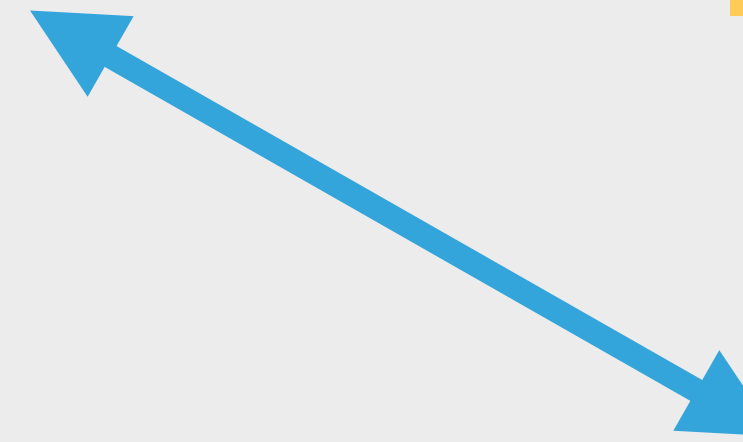
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MONOPOLE AXION COUPLINGS and SCALAR DARK MATTER

STATUS

SCALAR DM PROGRAM

BULK ACOUSTIC WAVE: OSCILLATING FUNDAMENTAL CONSTANTS



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2020 J. J. Sakurai Prize for Theoretical Particle Physics



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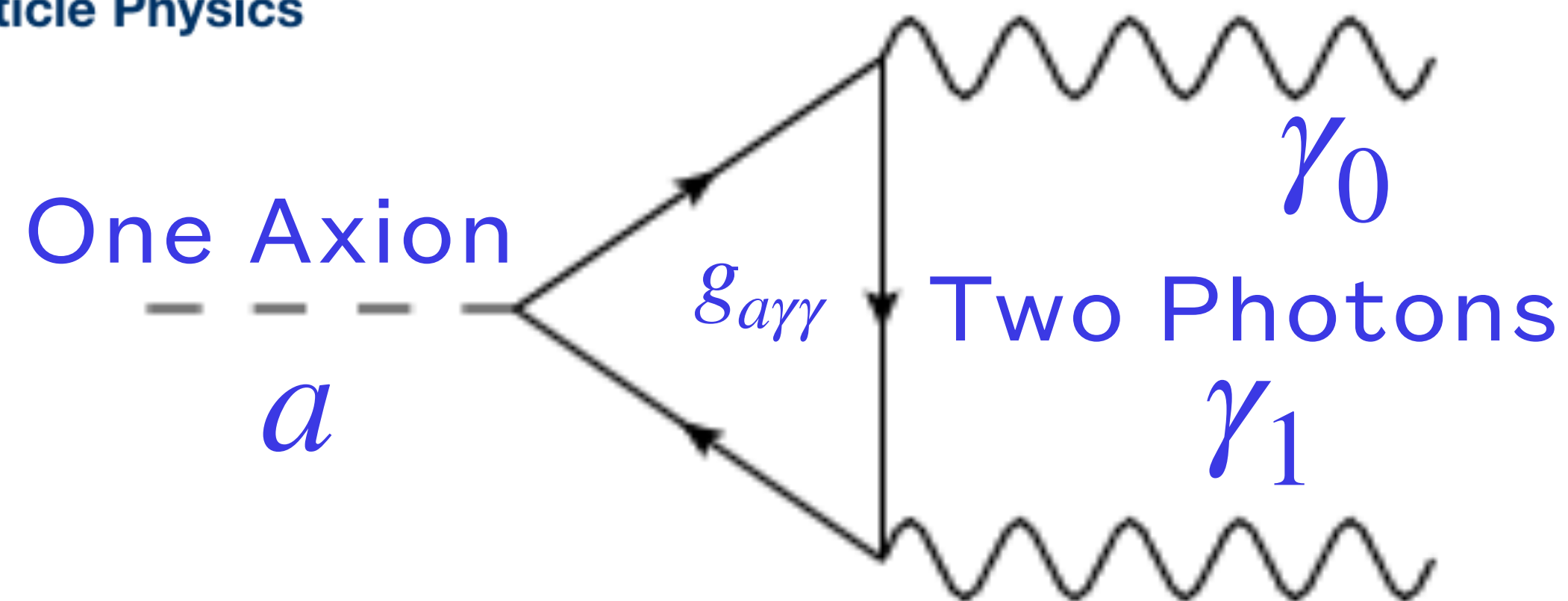
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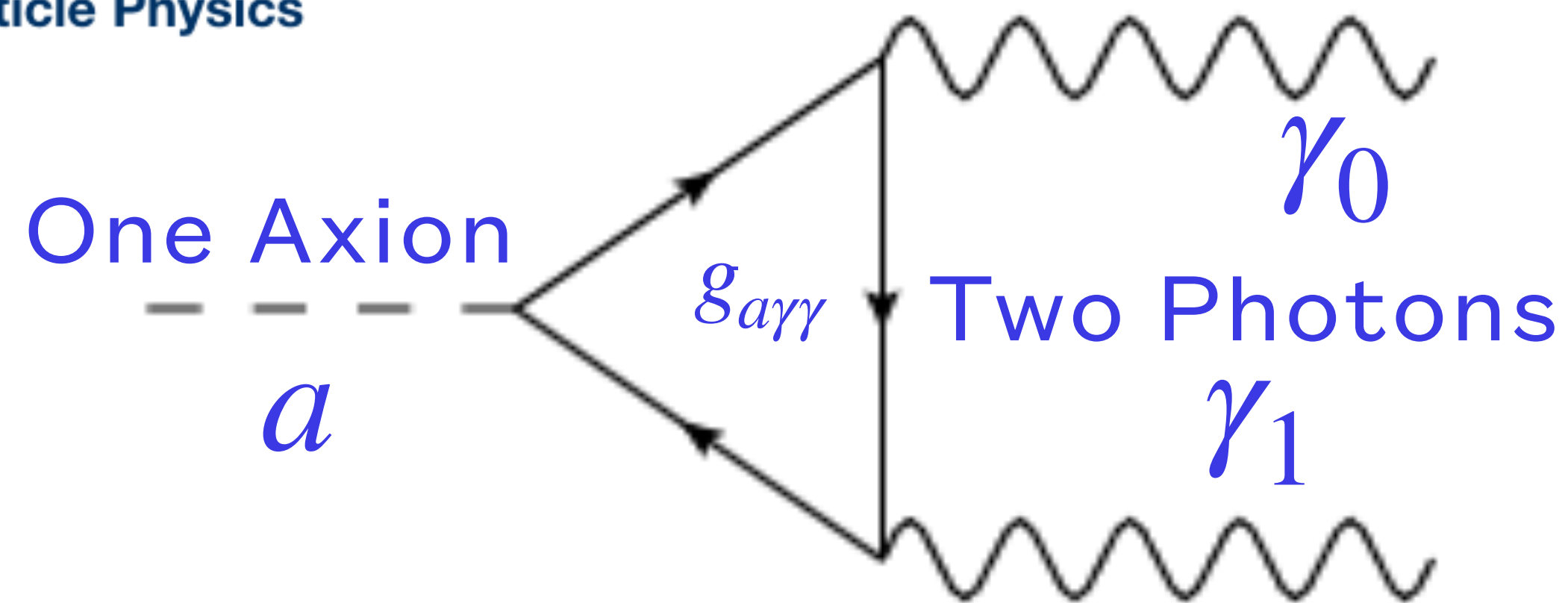
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axion-photon coupling  $g_{a\gamma\gamma}$   $\rightarrow$  chiral anomaly

2020 J. J. Sakurai Prize for Theoretical Particle Physics



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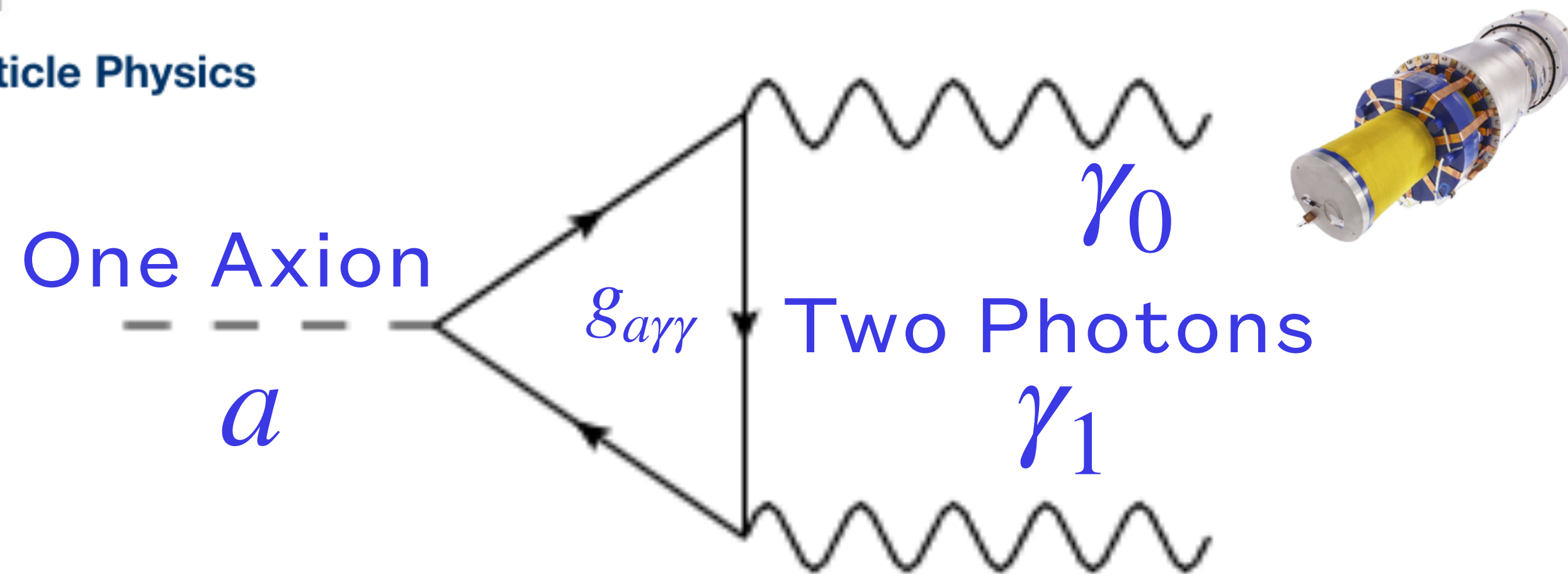


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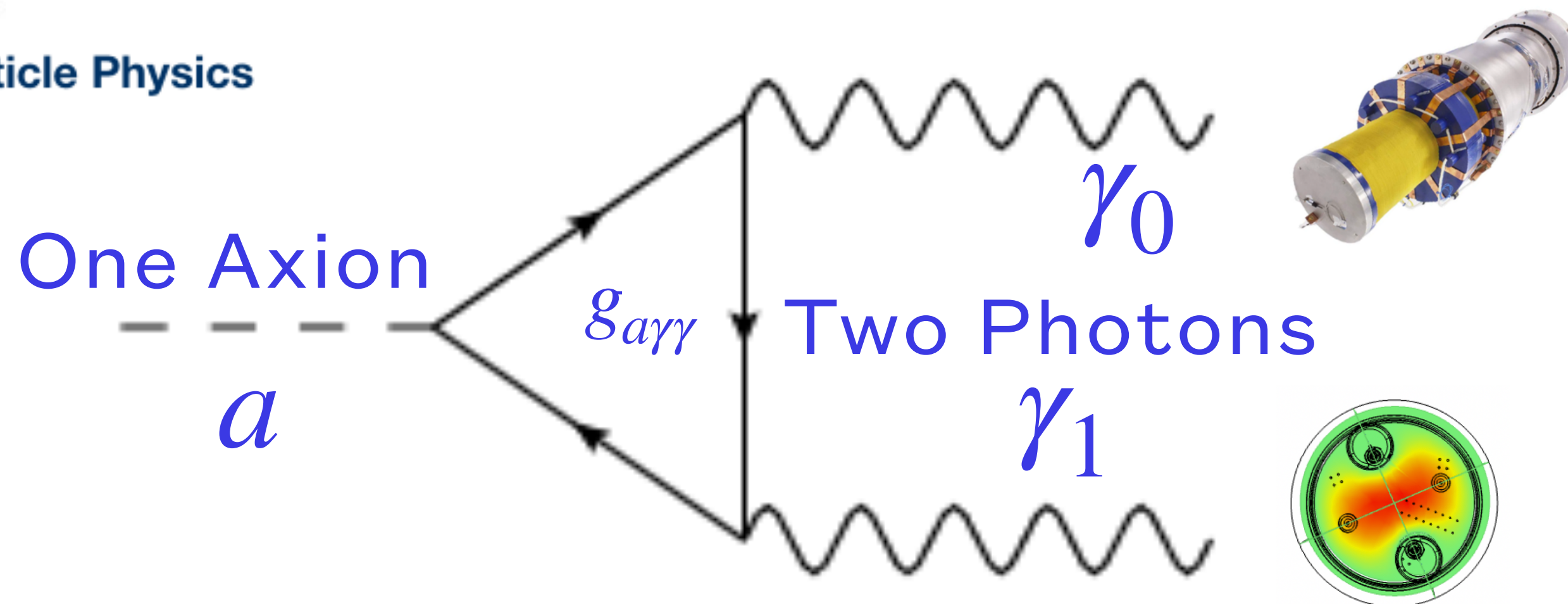


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Measure

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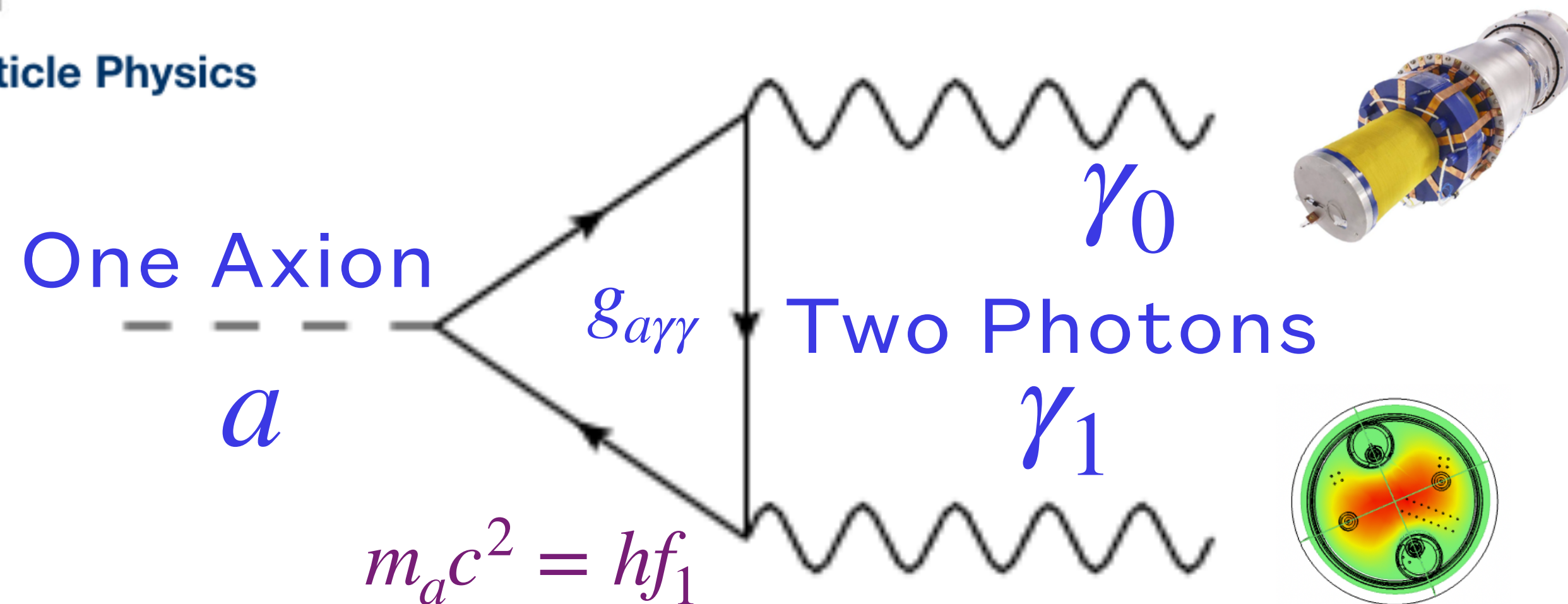


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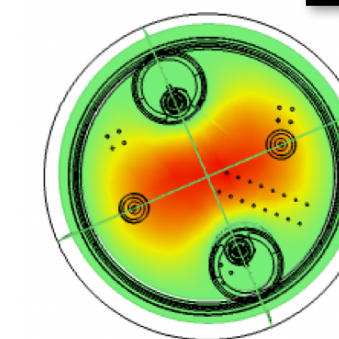
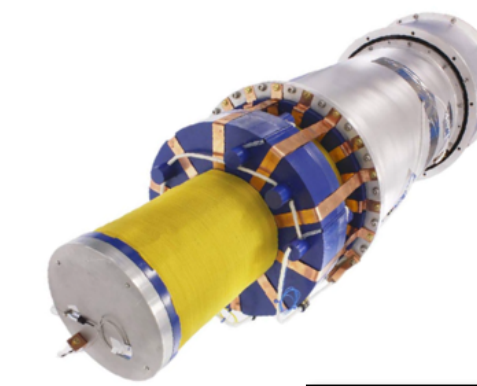
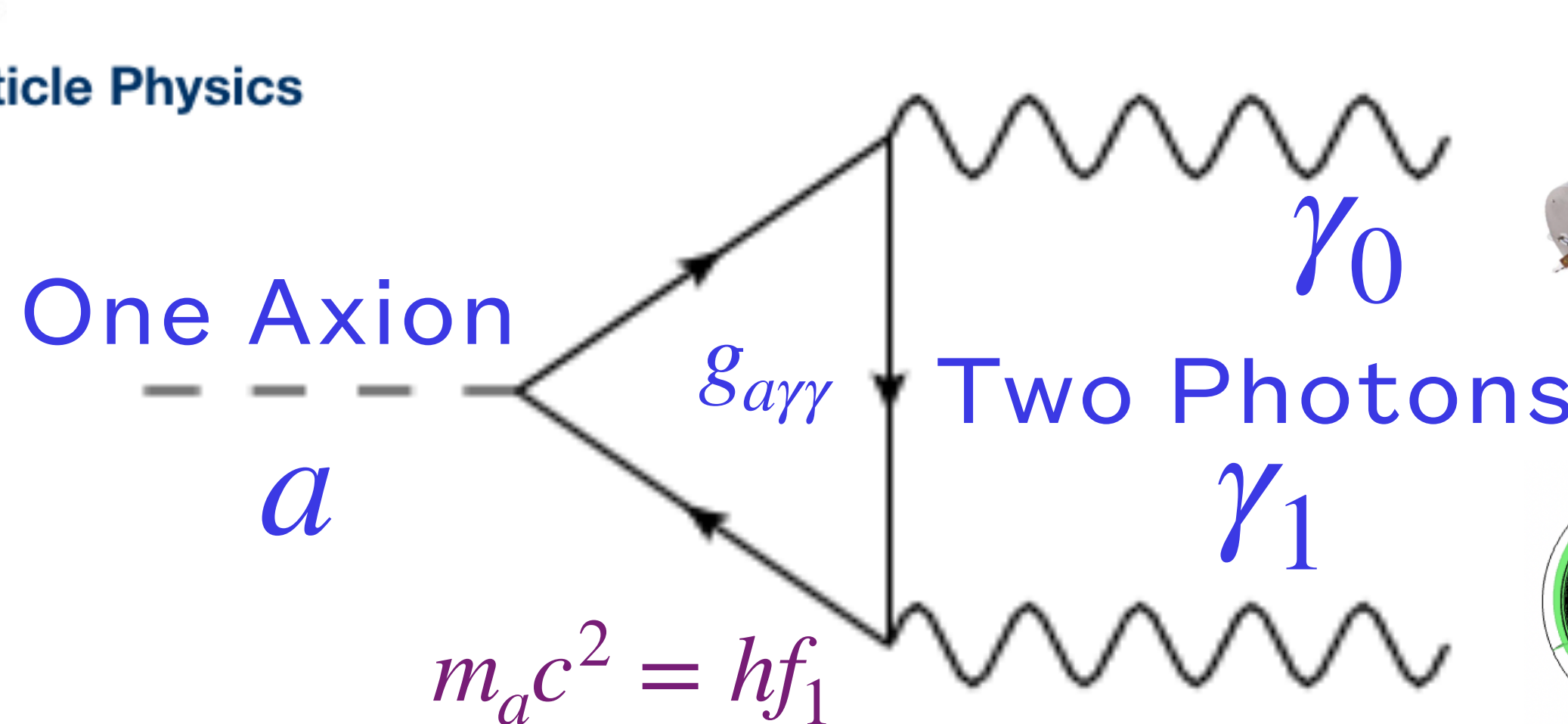


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$$\mathcal{H}_{int} = \epsilon_0 c g_{a\gamma\gamma} a \mathbf{E}_1 \cdot \mathbf{B}_0$$

Measure

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## Modified Axion Electrodynamics

(Represents two photons)

Axion Equation of Motion:

Klein-Gordon equation  
for massive spin 0  
particle

$$a(t) = \frac{1}{2} (\tilde{a}e^{-j\omega_a t} + \tilde{a}^*e^{j\omega_a t}) \\ = \text{Re} (\tilde{a}e^{-j\omega_a t})$$

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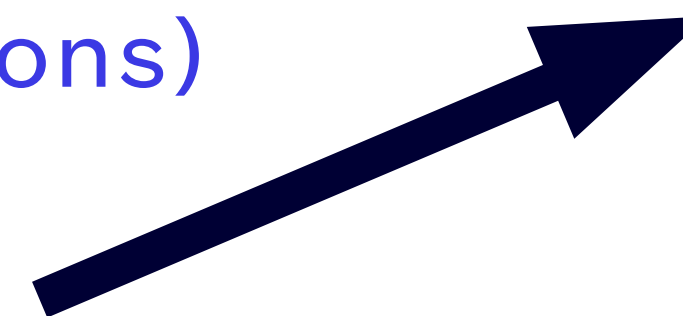
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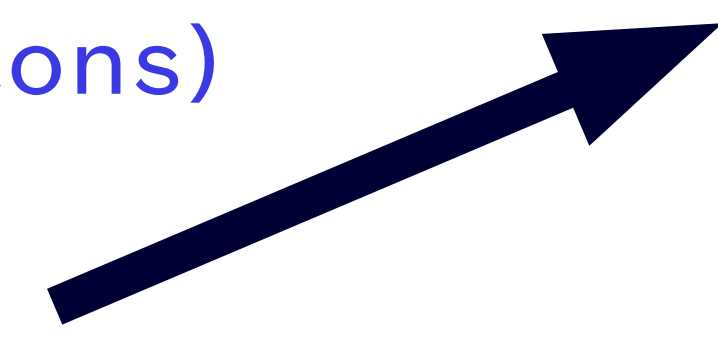
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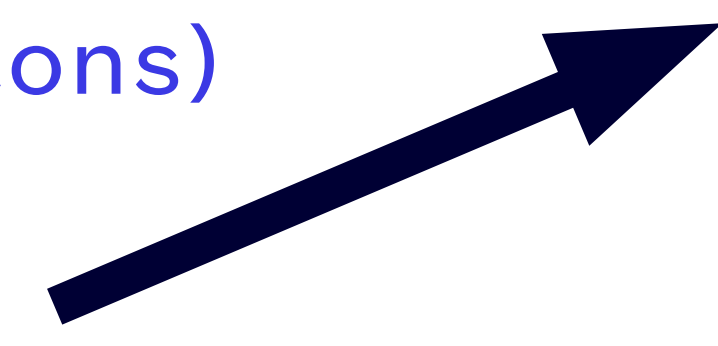
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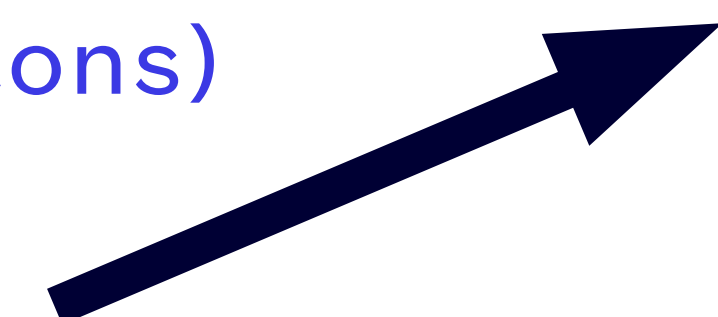
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**Source Terms Generate Photons->  
From Background Fields Mixing with Axion**

## Measure Created Photon

$$\nabla \cdot \left( \vec{E}_1(\vec{r}, t) - g_{a\gamma\gamma} a(t) c \vec{B}_0(\vec{r}, t) \right) = \frac{\rho_{e_1}}{\epsilon_0}$$

$$\nabla \times \left( \vec{B}_1(\vec{r}, t) + \frac{g_{a\gamma\gamma} a(t)}{c} \vec{E}_0(\vec{r}, t) \right)$$

$$- \frac{1}{c^2} \partial_t \left( \vec{E}_1(\vec{r}, t) - g_{a\gamma\gamma} a(\vec{r}, t) c \vec{B}_0(\vec{r}, t) \right) = \mu_0 \vec{J}_{e_1}$$

$$\nabla \cdot \vec{B}_1(\vec{r}, t) = 0$$

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## Applied Background Field

$$\nabla \times \vec{B}_0 = \mu_0 \epsilon_0 \partial_t \vec{E}_0 + \mu_0 \vec{J}_{e_0}$$

$$\nabla \times \vec{E}_0 = - \partial_t \vec{B}_0$$

$$\nabla \cdot \vec{B}_0 = 0$$

$$\nabla \cdot \vec{E}_0 = \epsilon_0^{-1} \rho_{e_0}$$

# Photonic Haloscope Equations in terms of Auxiliary Fields

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$$\nabla \times \vec{B}_0 = \mu_0 \epsilon_0 \partial_t \vec{E}_0 + \mu_0 \vec{J}_{e_0}$$

$$\nabla \times \vec{E}_0 = -\partial_t \vec{B}_0$$

$$\nabla \cdot \vec{B}_0 = 0$$

$$\nabla \cdot \vec{E}_0 = \epsilon_0^{-1} \rho_{e_0}$$

# Photonic Haloscope Equations in terms of Auxiliary Fields

## Measure Created Photon

$$\nabla \cdot \left( \vec{E}_1(\vec{r}, t) - g_{a\gamma\gamma} a(t) c \vec{B}_0(\vec{r}, t) \right) = \frac{\rho_{e_1}}{\epsilon_0}$$

$$\nabla \times \left( \vec{B}_1(\vec{r}, t) + \frac{g_{a\gamma\gamma} a(t)}{c} \vec{E}_0(\vec{r}, t) \right)$$

$$-\frac{1}{c^2} \partial_t \left( \vec{E}_1(\vec{r}, t) - g_{a\gamma\gamma} a(\vec{r}, t) c \vec{B}_0(\vec{r}, t) \right) = \mu_0 \vec{J}_{e_1}$$

$$\nabla \cdot \vec{B}_1(\vec{r}, t) = 0$$

$$\nabla \times \vec{E}_1(\vec{r}, t) + \partial_t \vec{B}_1(\vec{r}, t) = 0.$$



$$\nabla \cdot \vec{D}_1 = \rho_{e_1}$$

$$\nabla \times \vec{H}_1 - \partial_t \vec{D}_1 = \vec{J}_{e_1}$$

$$\nabla \cdot \vec{B}_1(\vec{r}, t) = 0$$

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**Constitutive Relations (Include Matter)  
Effective Magnetisation and Polarisation**

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Effective Magnetisation and Polarisation**

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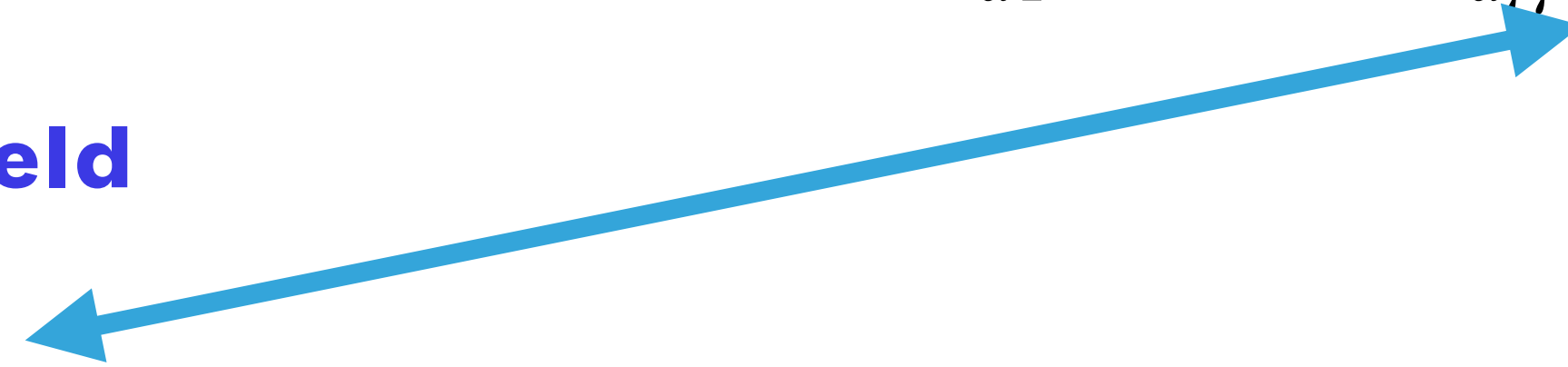
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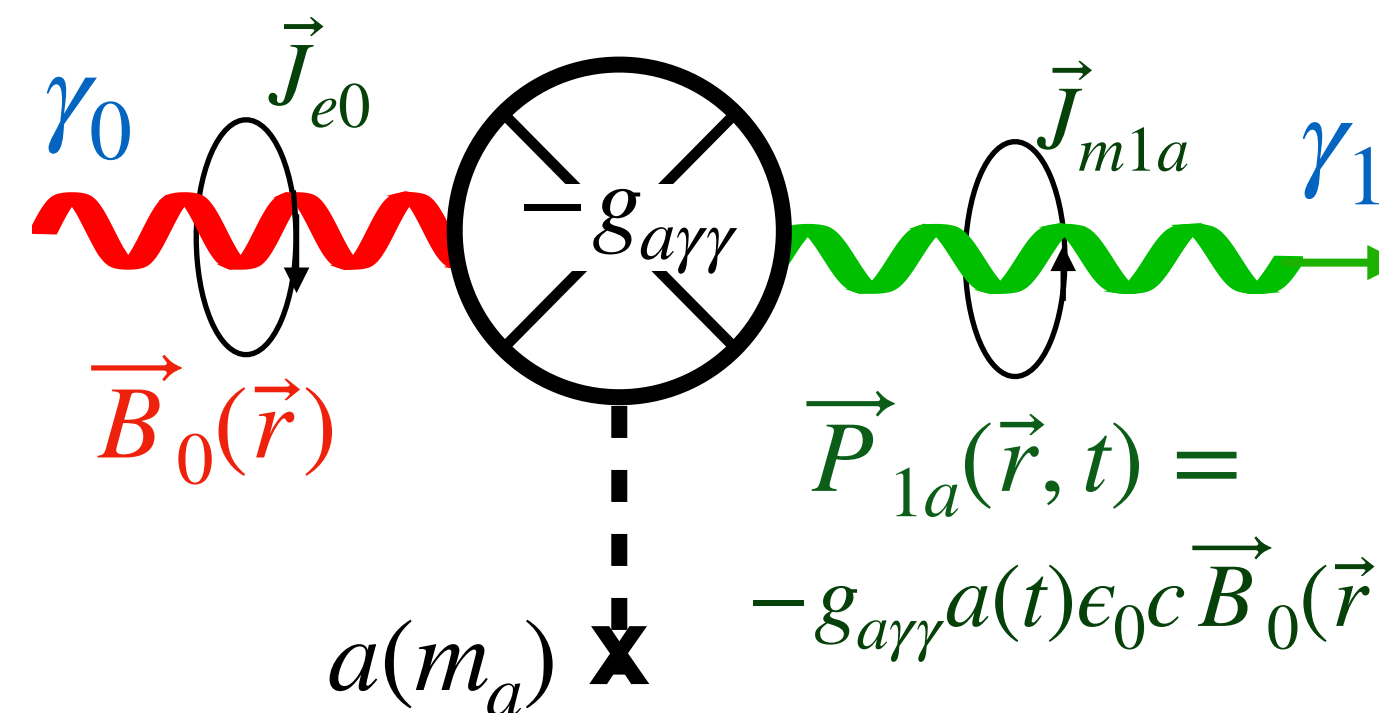
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$$\nabla \cdot \vec{E}_0 = \epsilon_0^{-1} \rho_{e_0}$$



$$\vec{J}_{ab}(\vec{r}, t) = \frac{\partial \vec{P}_{a1}(\vec{r}, t)}{\partial t}$$

$$\mathcal{E} = \oint_P \vec{P}_{a1} \cdot d\vec{l}$$



## Modified axion electrodynamics as impressed electromagnetic sources through oscillating background polarization and magnetization

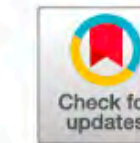


Michael E. Tobar\*, Ben T. McAllister, Maxim Goryachev

ARC Centre of Excellence For Engineered Quantum Systems, Department of Physics, School of Physics, Mathematics and Computing, University of Western Australia, 35 Stirling Highway, Crawley WA 6009, Australia



## Broadband electrical action sensing techniques with conducting wires for low-mass dark matter axion detection



Michael E. Tobar\*, Ben T. McAllister, Maxim Goryachev

ARC Centre of Excellence For Engineered Quantum Systems, Department of Physics, University of Western Australia, 35 Stirling Highway, Crawley WA 6009, Australia

## Few thoughts on $\theta$ and the electric dipole moments

Ariel Zhitnitsky\*

Department of Physics and Astronomy, University of British Columbia, Vancouver, British Columbia V6T 1Z1, Canada

## Electric polarization as a nonquantized topological response and boundary Luttinger theorem

Xue-Yang Song<sup>1,2</sup>, Yin-Chen He<sup>2</sup>, Ashvin Vishwanath<sup>1</sup> and Chong Wang<sup>2</sup>

<sup>1</sup>Department of Physics, Harvard University, Cambridge, Massachusetts 02138, USA

<sup>2</sup>Perimeter Institute for Theoretical Physics, Waterloo, Ontario N2L 2Y5, Canada

(Received 22 February 2021; accepted 5 March 2021; published 2 April 2021)

## Emergent electric field from magnetic resonances in a one-dimensional chiral magnet

Kotaro Shimizu<sup>1</sup>, Shun Okumura<sup>1</sup>, Yasuyuki Kato<sup>1</sup> and Yukitoshi Motome<sup>1</sup>

<sup>1</sup>Department of Applied Physics, The University of Tokyo, Tokyo 113-8656, Japan

(Dated: July 18, 2023)

The emergent electric field (EEF) is a fictitious electric field acting on conduction electrons through the Berry phase mechanism.



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# DC Magnetic Haloscopes

- Axions convert into photons in presence of strong magnetic field: Mass is unknown

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- So: narrowband photon signal of an unknown frequency is generated (need to scan frequency)

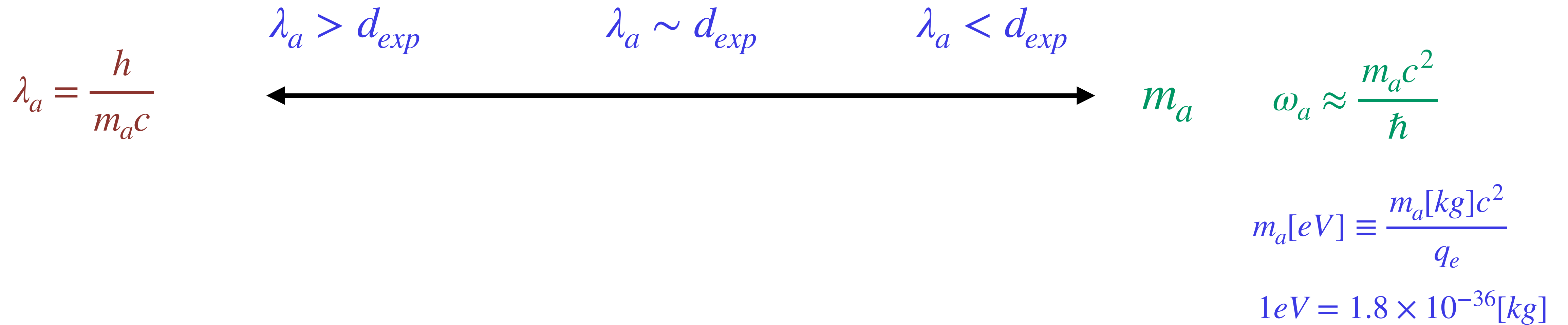
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- Axions convert into photons in presence of strong magnetic field: Mass is unknown
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- Three regimes of haloscope detector

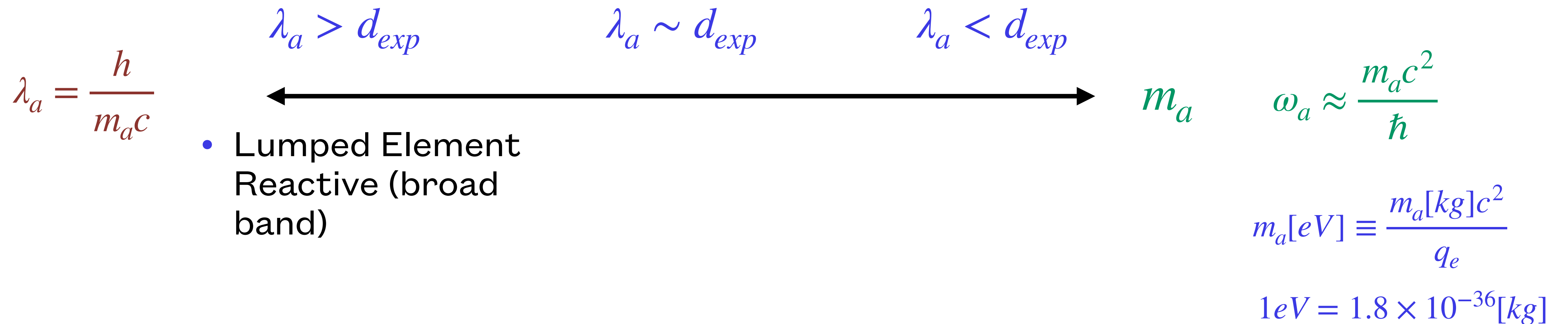
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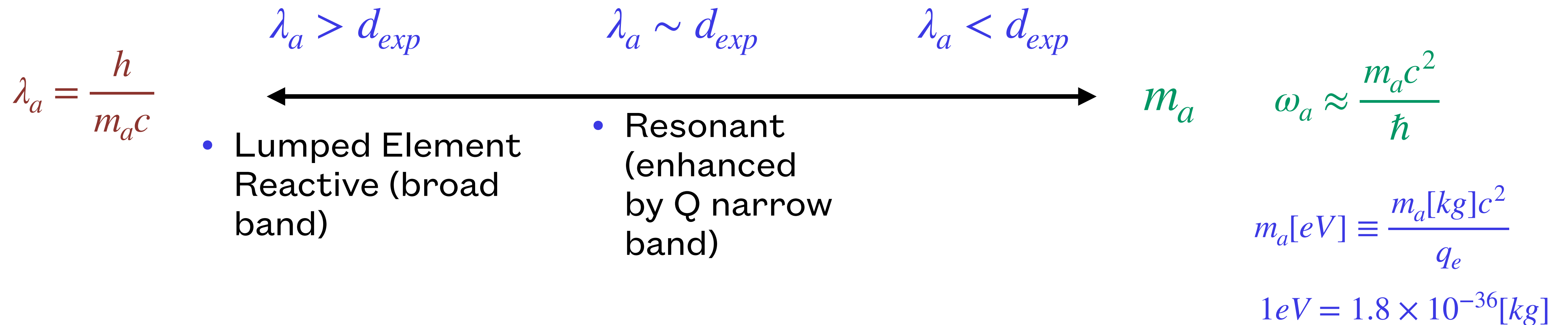
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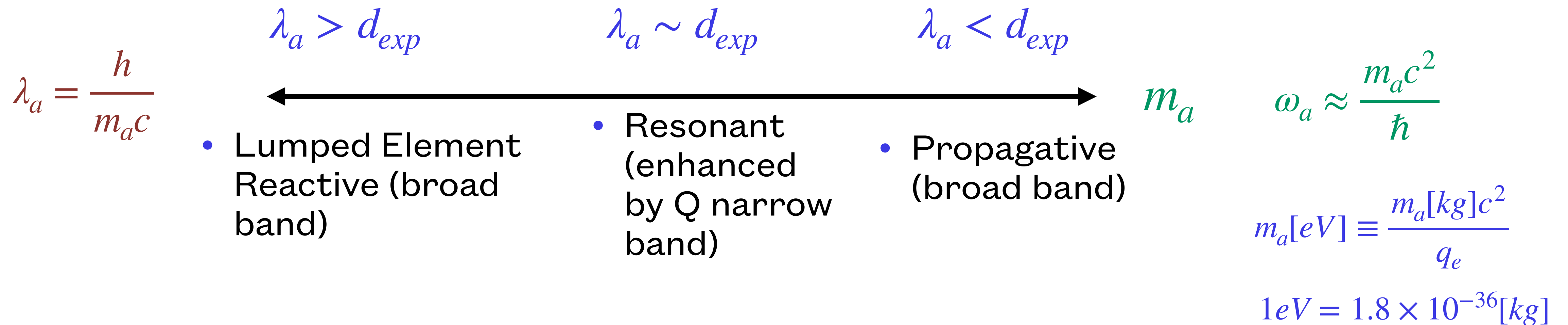
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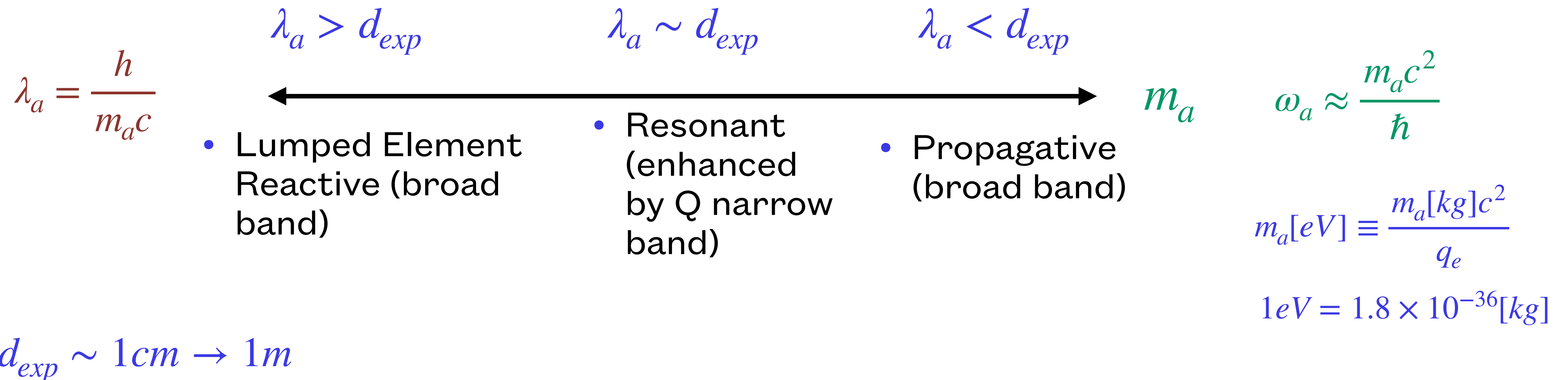
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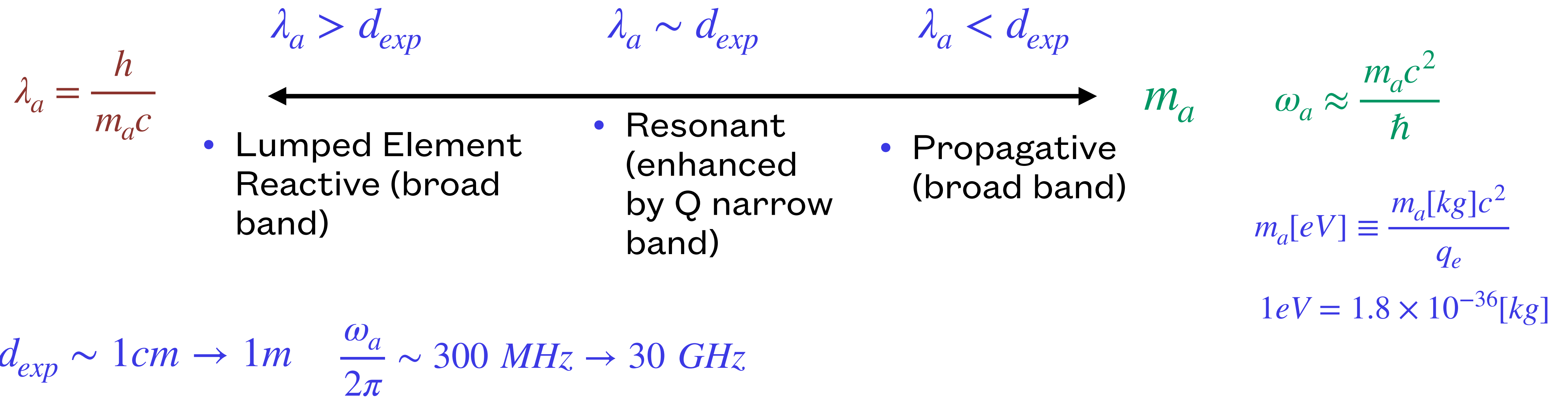
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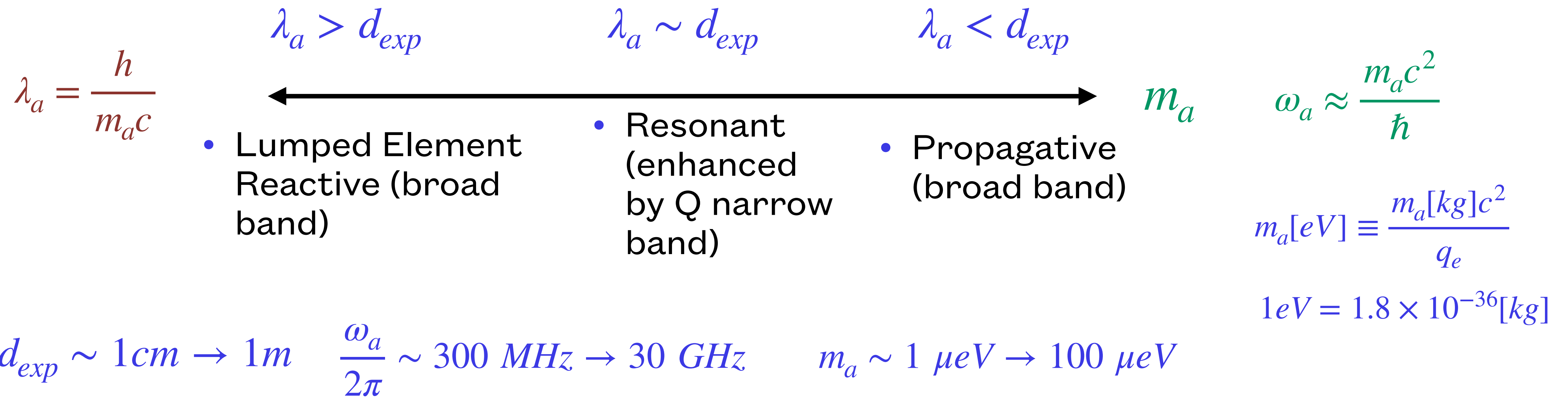
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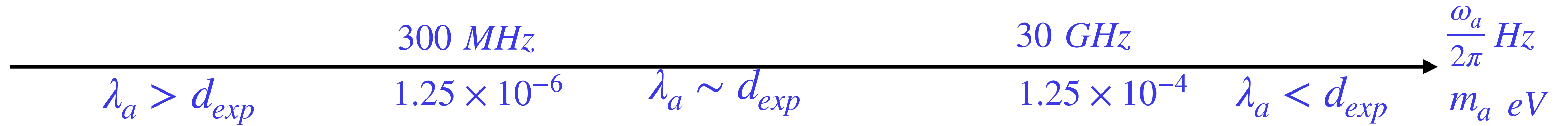
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# DC Magnetic Haloscopes

Type Depends on Axion Compton Wavelength

$$\lambda_a = \frac{h}{cm_a}$$



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Type Depends on Axion Compton Wavelength

$$\lambda_a = \frac{h}{cm_a}$$

Low Mass: Lumped Element

Reactive

300 MHz

30 GHz

$\frac{\omega_a}{2\pi}$  Hz

$$\lambda_a > d_{exp}$$

$$1.25 \times 10^{-6}$$

$$\lambda_a \sim d_{exp}$$

$$1.25 \times 10^{-4}$$

$$\lambda_a < d_{exp}$$

$$m_a \text{ eV}$$

ADMX SLIC  
RE-ENTRANT CAVITY  
ABRACADABRA  
SHAFT  
DM RADIO

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$\frac{\omega_a}{2\pi}$  Hz

$$\lambda_a > d_{exp}$$

$$1.25 \times 10^{-6}$$

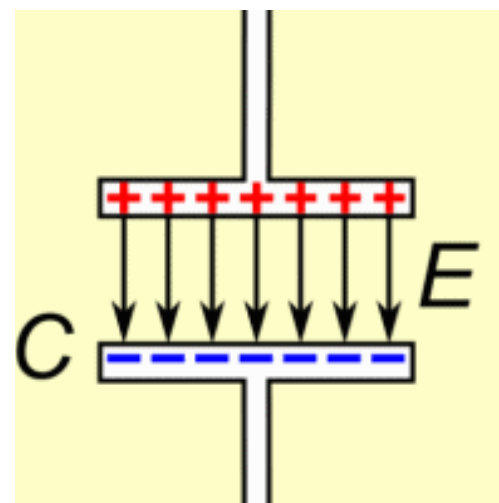
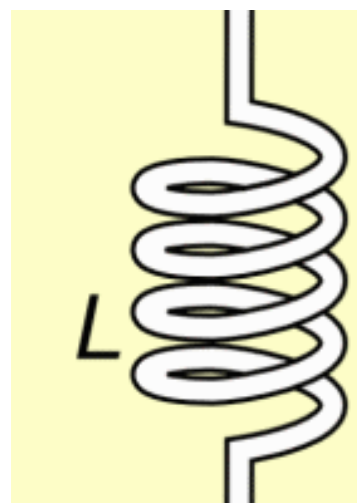
$$\lambda_a \sim d_{exp}$$

$$1.25 \times 10^{-4}$$

$$\lambda_a < d_{exp}$$

$$m_a \text{ eV}$$

ADMX SLIC  
RE-ENTRANT CAVITY  
ABRACADABRA  
SHAFT  
DM RADIO



# DC Magnetic Haloscopes

Type Depends on Axion Compton Wavelength

$$\lambda_a = \frac{h}{cm_a}$$

Low Mass: Lumped Element

Reactive

300 MHz

30 GHz

$\frac{\omega_a}{2\pi}$  Hz

$$\lambda_a > d_{exp}$$

$$1.25 \times 10^{-6}$$

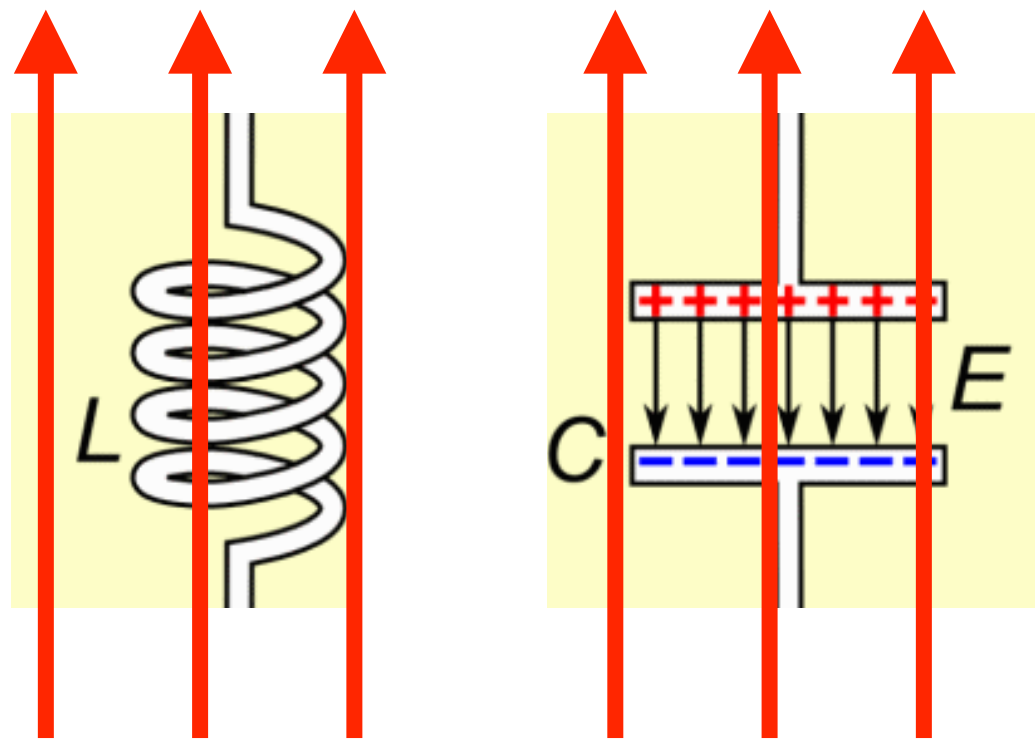
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ADMX SLIC  
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ABRACADABRA  
SHAFT  
DM RADIO



$$\vec{B} = B_{DC} \hat{z}$$

# DC Magnetic Haloscopes

Type Depends on Axion Compton Wavelength

$$\lambda_a = \frac{h}{cm_a}$$

Middle Mass: Resonant Cavity  
Reactive and Dissipative

Low Mass: Lumped Element  
Reactive

30 GHz

300 MHz

$\frac{\omega_a}{2\pi}$  Hz

Reactive

Reactive and Dissipative

$1.25 \times 10^{-4}$

$1.25 \times 10^{-6}$

$\lambda_a < d_{exp}$

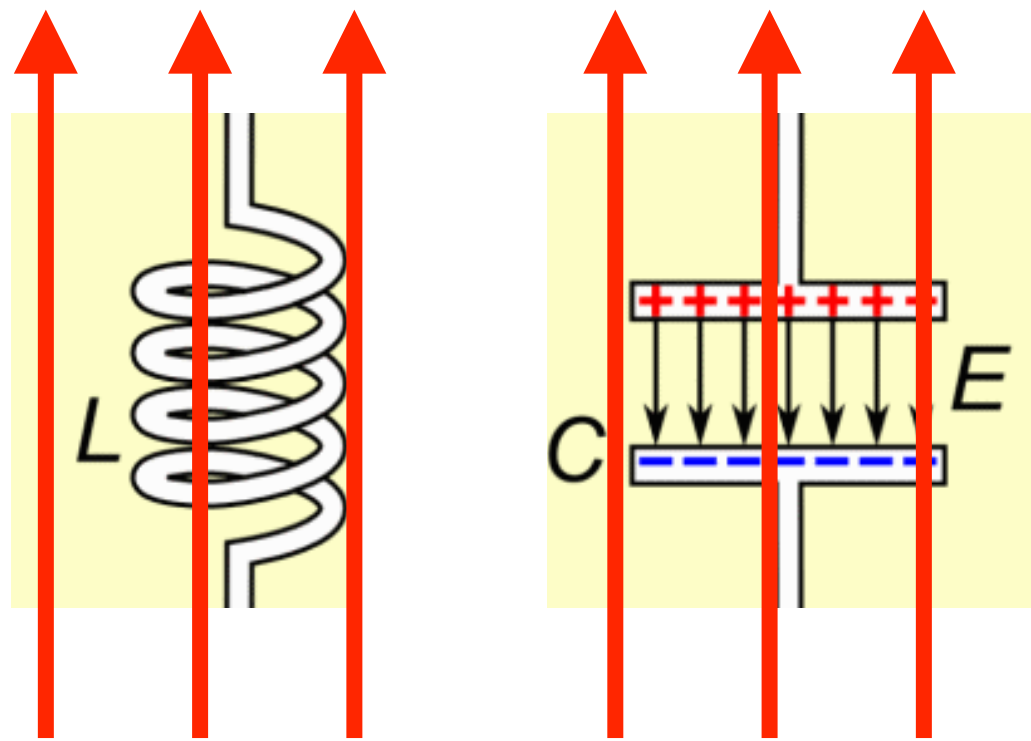
$\lambda_a \sim d_{exp}$

$\lambda_a > d_{exp}$

$m_a$  eV

ADMX SLIC  
RE-ENTRANT CAVITY  
ABRACADABRA  
SHAFT  
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CULTASK  
ORGAN  
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Reactive

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ADMX SLIC  
RE-ENTRANT CAVITY  
ABRACADABRA  
SHAFT  
DM RADIO

300 MHz

$$1.25 \times 10^{-6}$$

ADMX  
CULTASK  
ORGAN  
QUAX  
RADES

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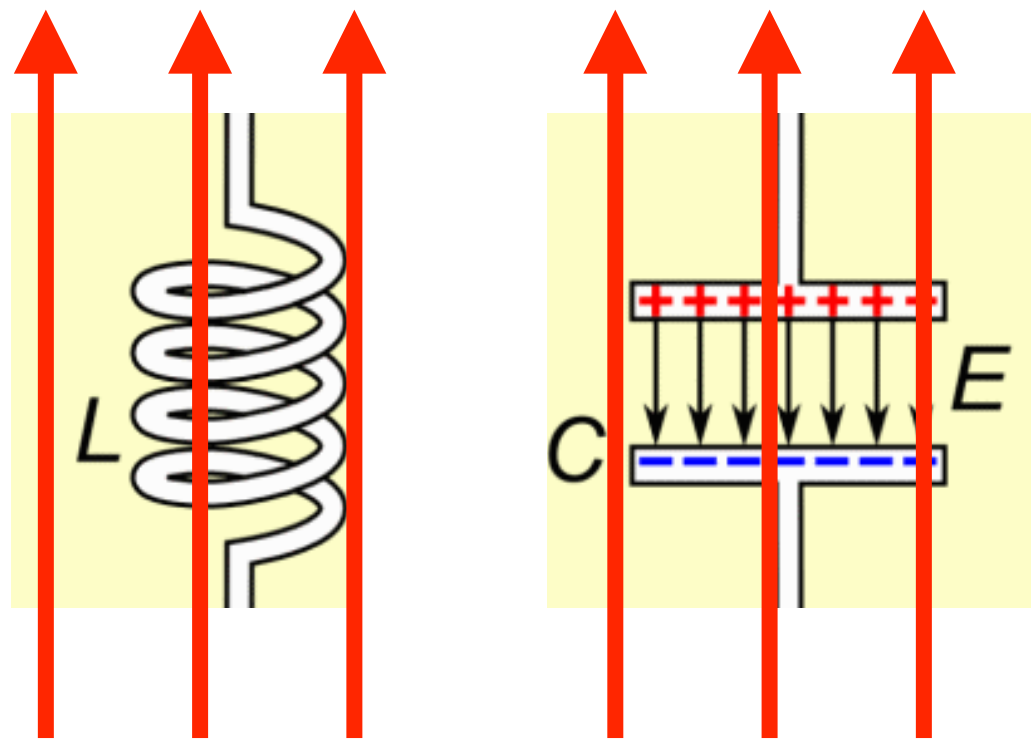
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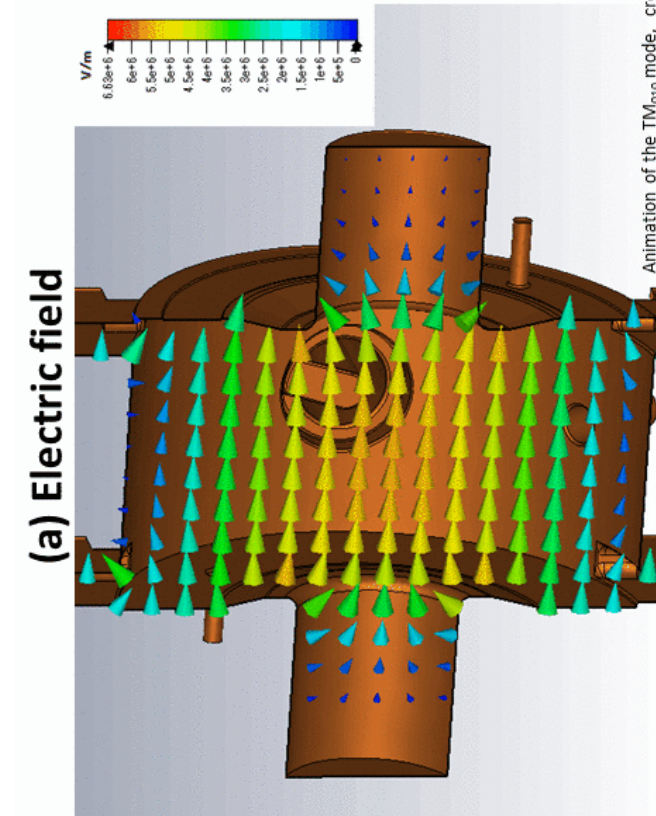
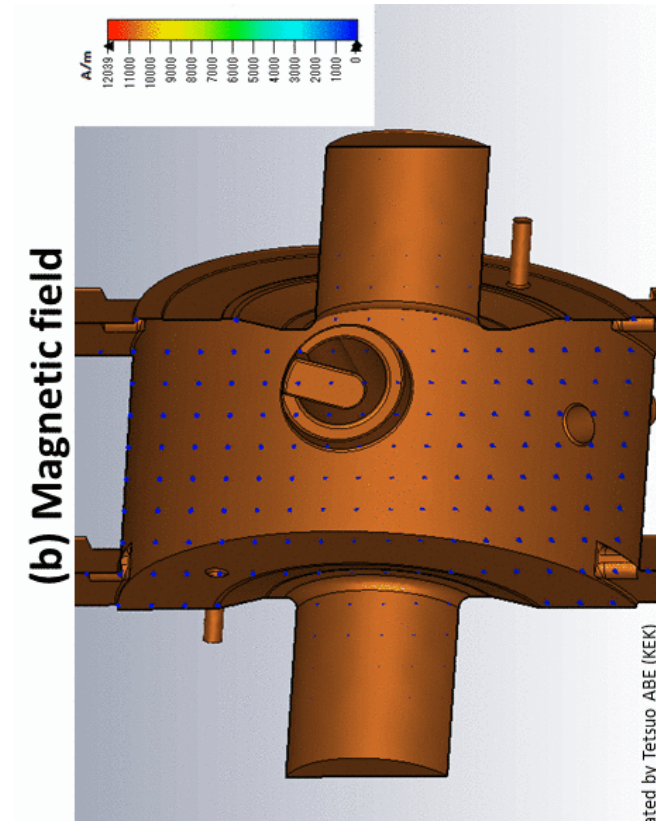
$$\lambda_a < d_{exp}$$

$$\frac{\omega_a}{2\pi} \text{ Hz}$$

$$m_a \text{ eV}$$



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Animation of the TM<sub>100</sub> mode, created by Tatsuo ABE (KEK)



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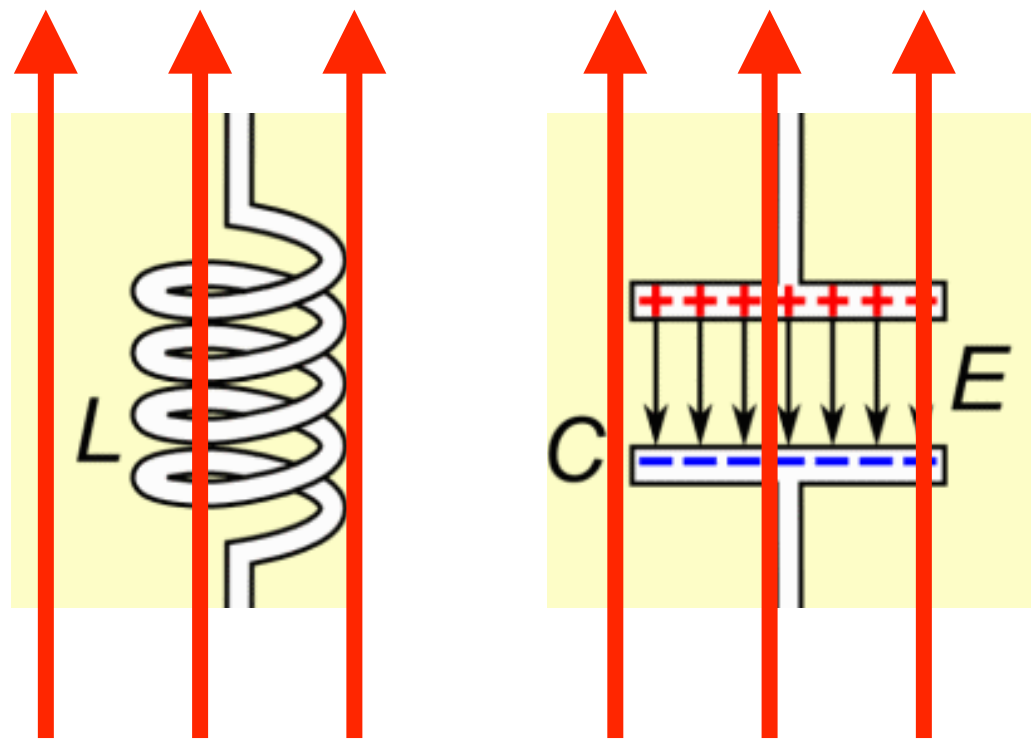
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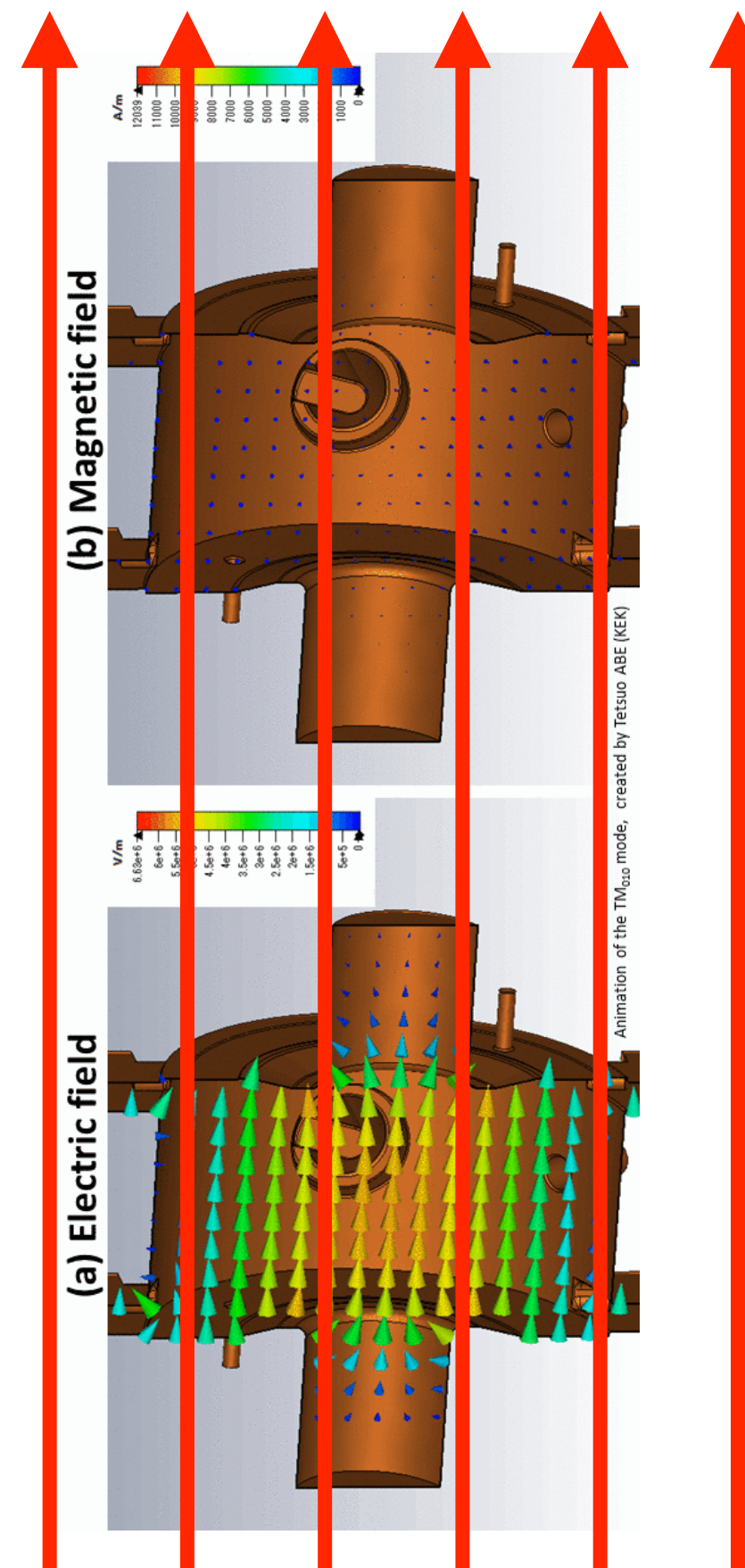
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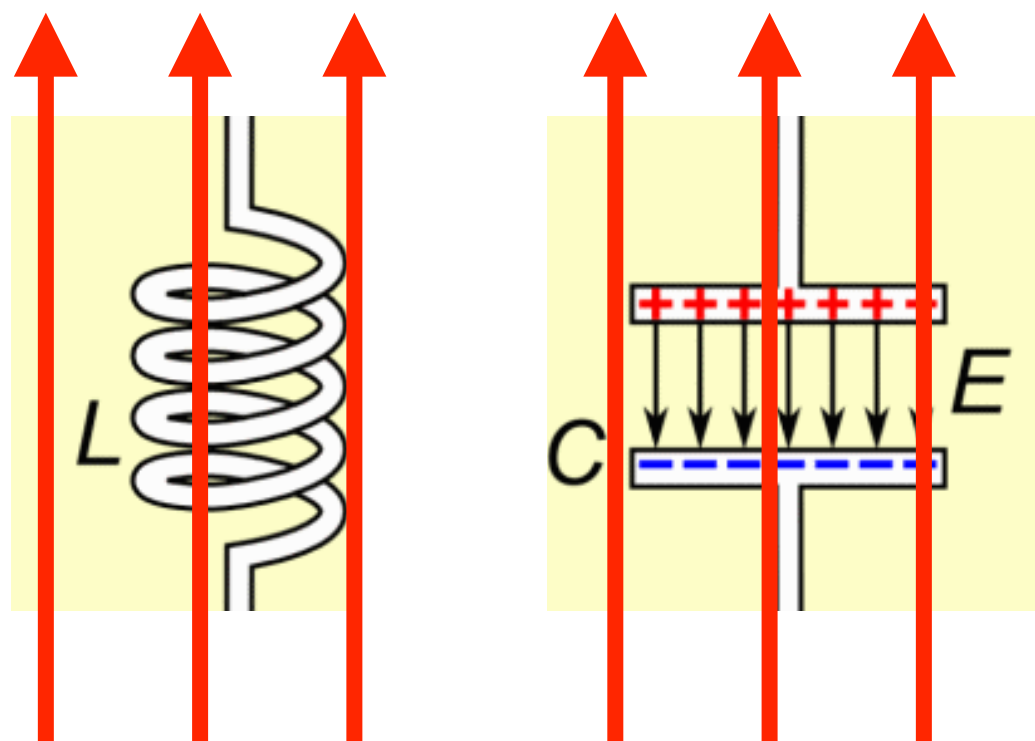
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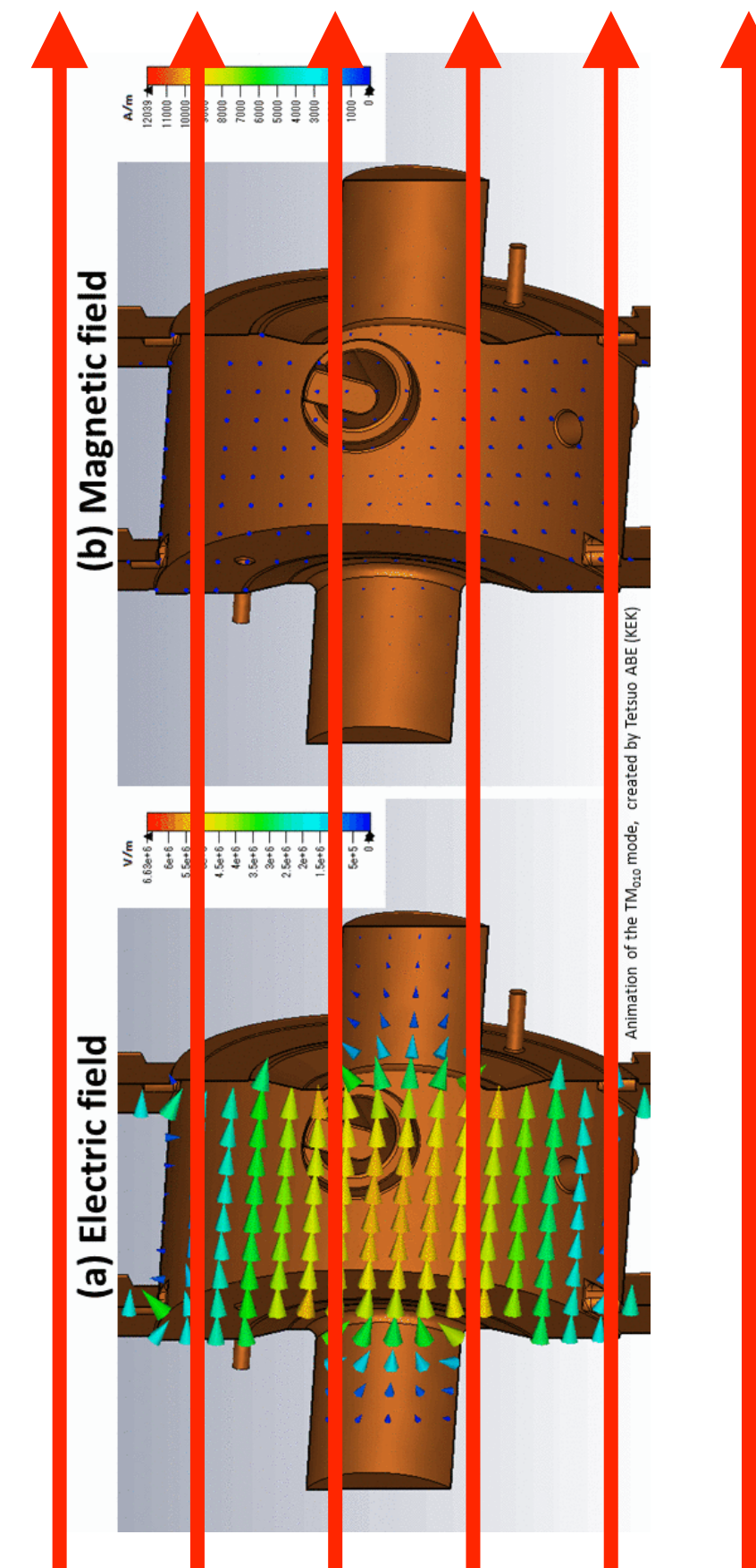
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ADMX  
CULTASK  
ORGAN  
QUAX  
RADES

Middle Mass: Resonant Cavity  
Reactive and Dissipative

$$\lambda_a \sim d_{exp}$$



30 GHz

$$1.25 \times 10^{-4}$$

MADMAX  
BREAD

High Mass: Propagating

$$\lambda_a < d_{exp}$$

$$\frac{\omega_a}{2\pi} \text{ Hz}$$

$$m_a \text{ eV}$$

# DC Magnetic Haloscopes

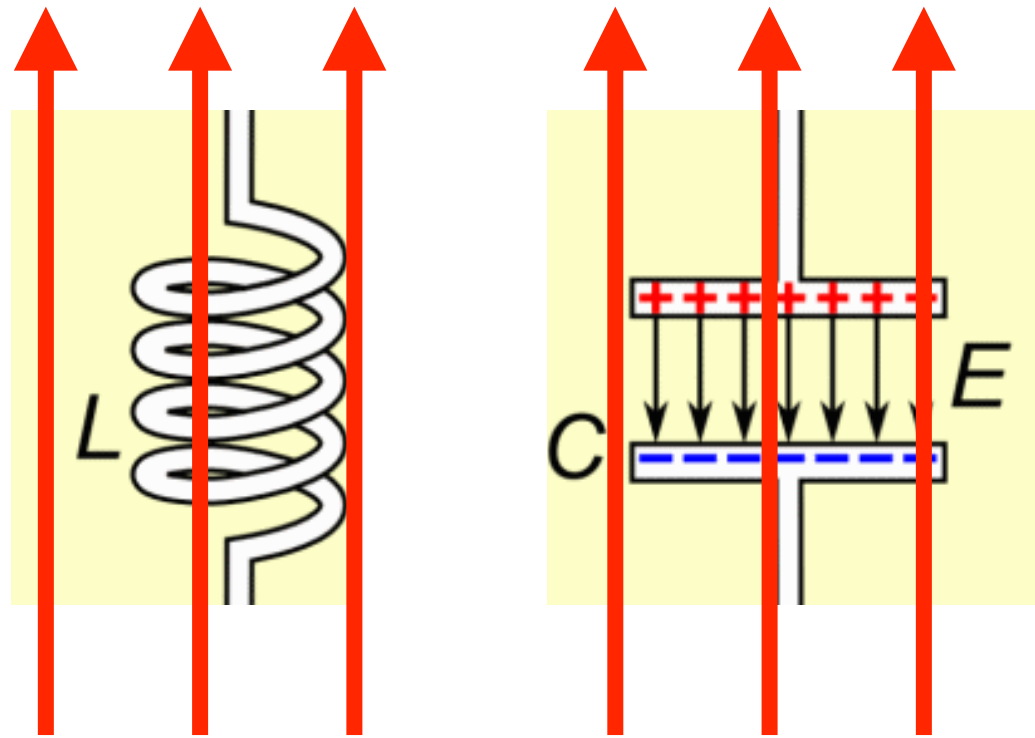
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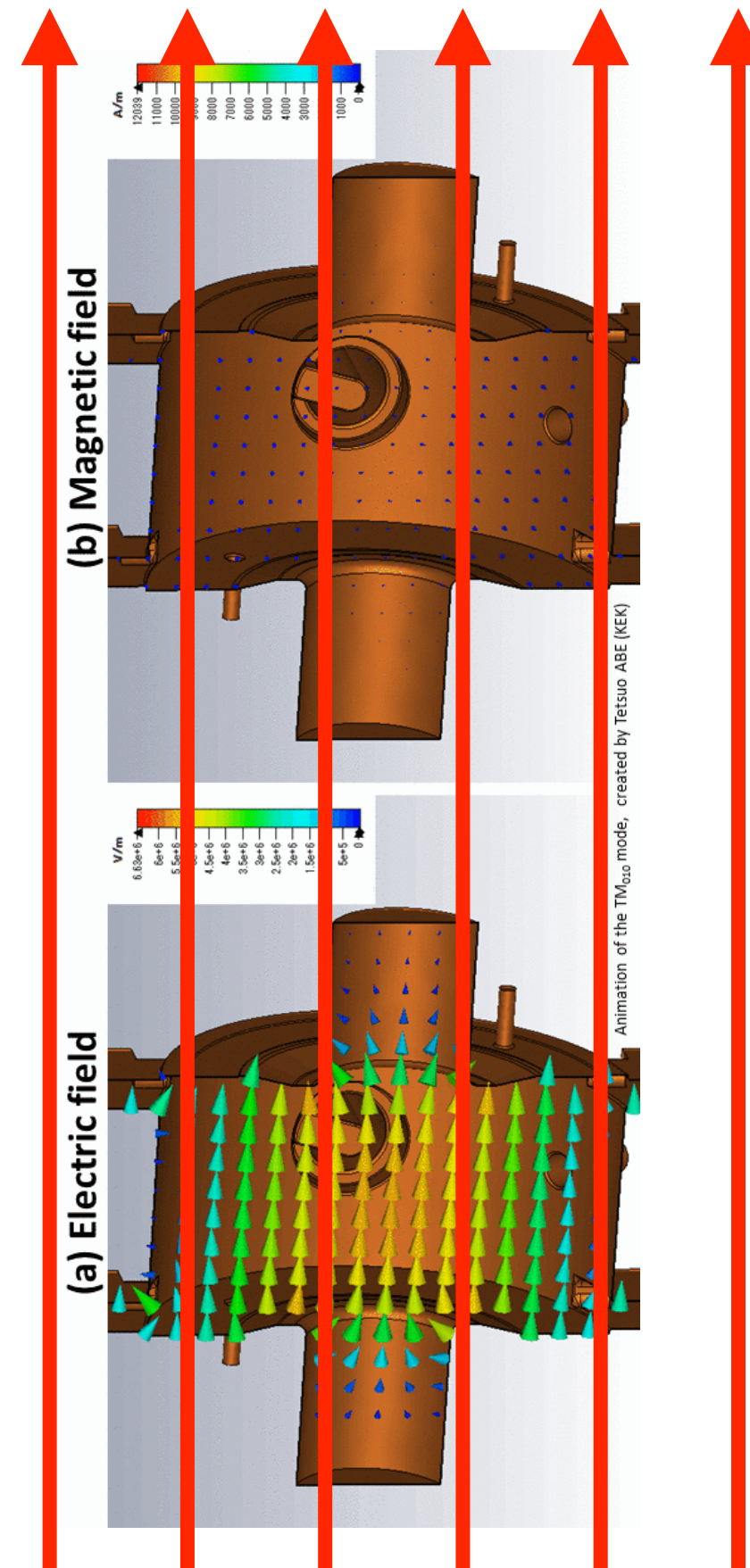
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CULTASK  
ORGAN  
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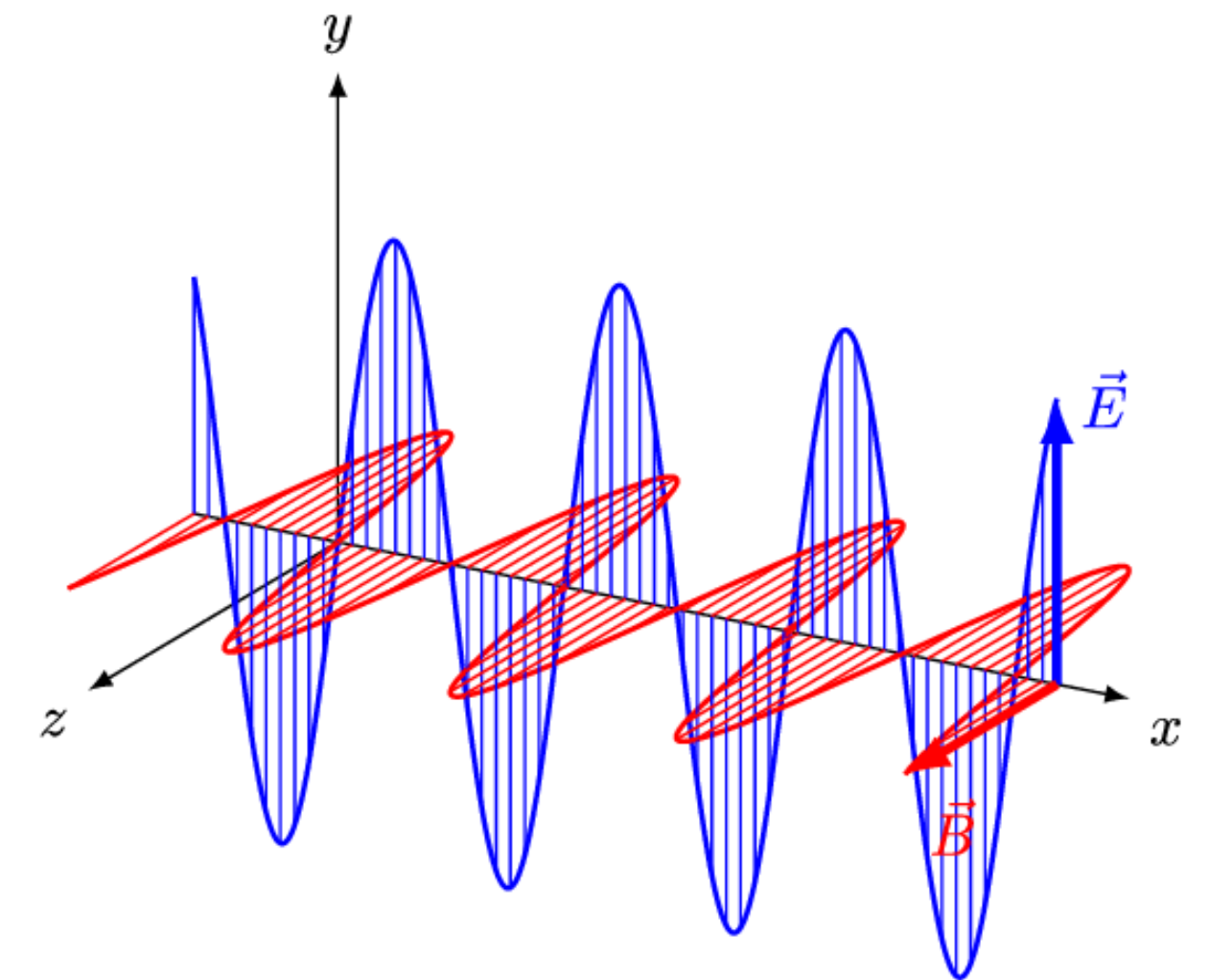
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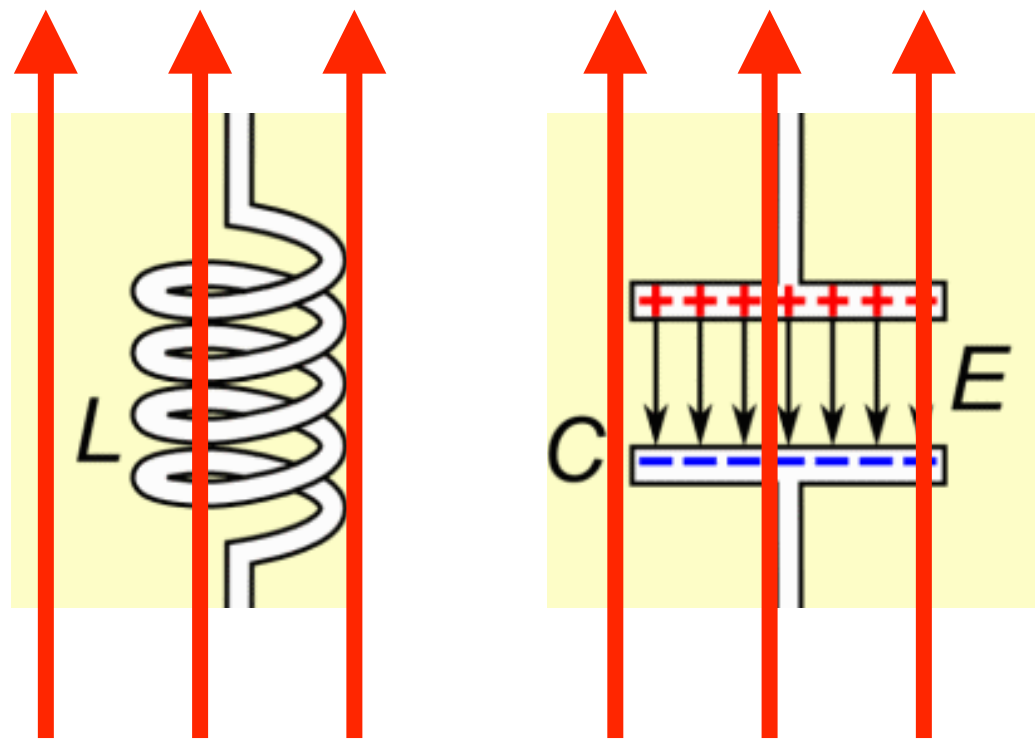
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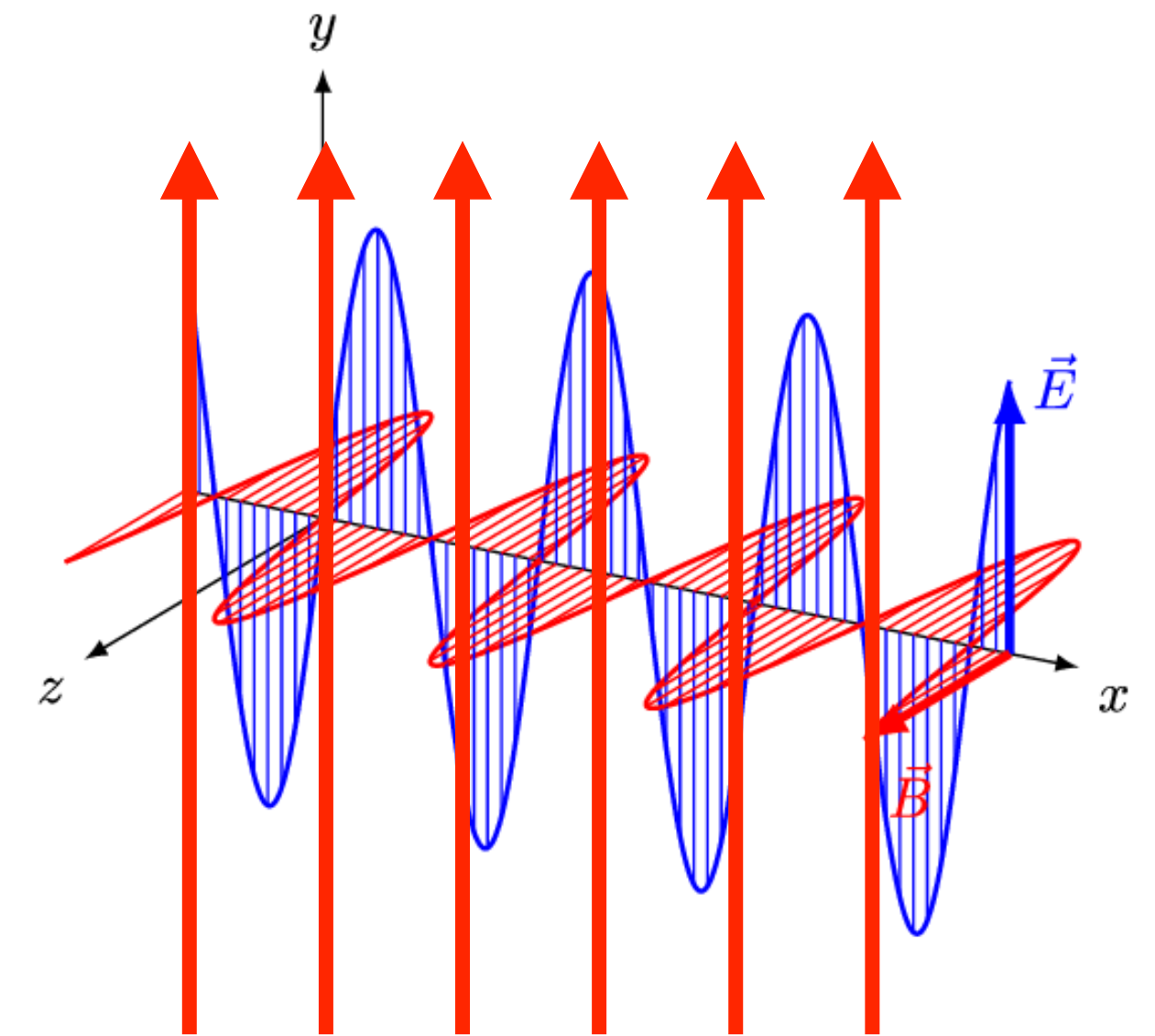
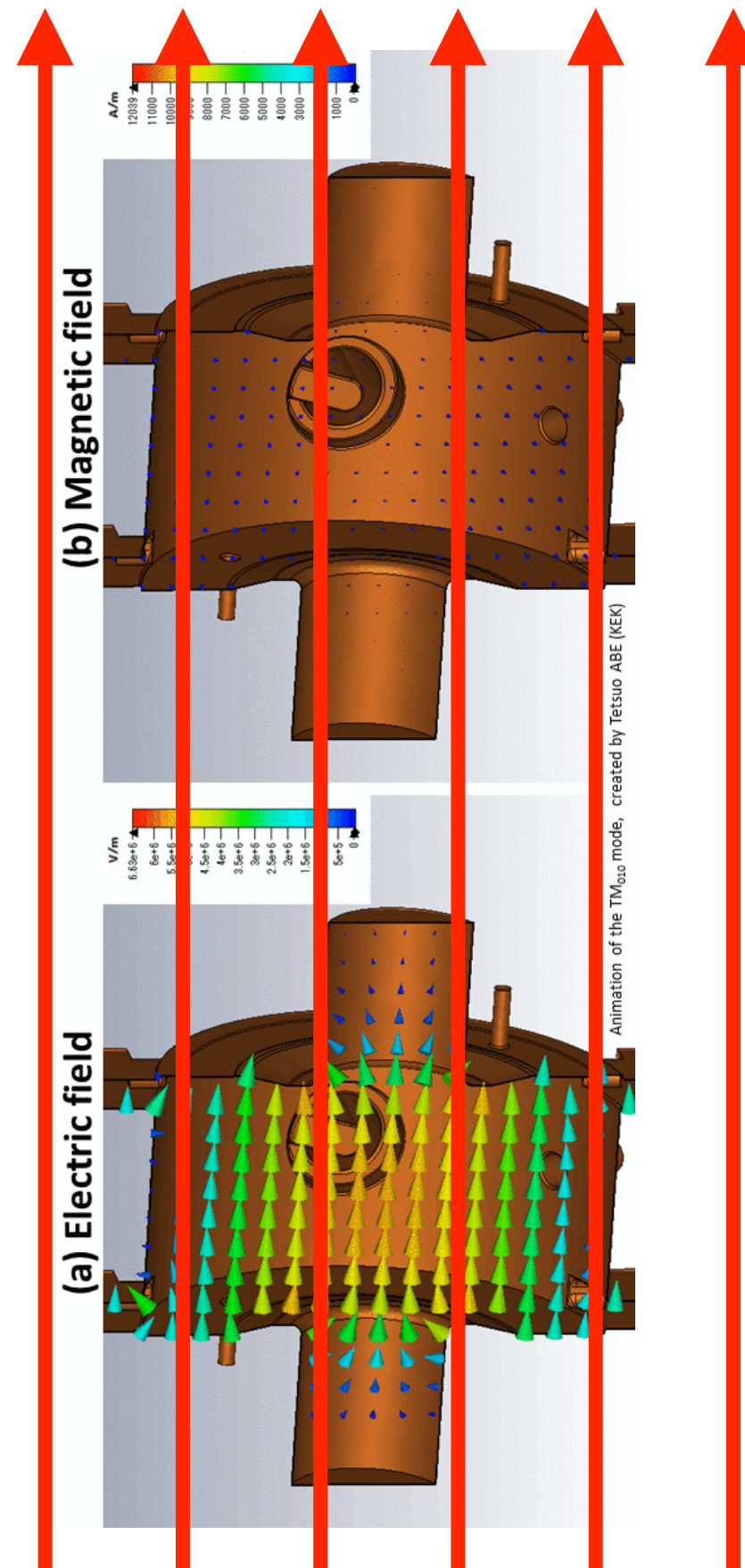
ADMX SLIC  
RE-ENTRANT CAVITY  
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SHAFT  
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$$\vec{B} = B_{DC} \hat{z}$$



# POYNTING THEOREM

- The basic conservation law for electromagnetic energy (EM)

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## Instantaneous Poynting vector

$$\begin{aligned}\vec{S}_1(t) &= \frac{1}{\mu_0} \vec{E}_1(t) \times \vec{B}_1(t) = \frac{1}{2} \left( \mathbf{E}_1 e^{-j\omega_1 t} + \mathbf{E}_1^* e^{j\omega_1 t} \right) \times \frac{1}{2\mu_0} \left( \mathbf{B}_1 e^{-j\omega_1 t} + \mathbf{B}_1^* e^{j\omega_1 t} \right) \\ &= \frac{1}{2\mu_0} \operatorname{Re} \left( \mathbf{E}_1 \times \mathbf{B}_1^* \right) + \frac{1}{2\mu_0} \operatorname{Re} \left( \mathbf{E}_1 \times \mathbf{B}_1 e^{-j2\omega_1 t} \right),\end{aligned}$$

$$\langle \vec{S}_1 \rangle = \frac{1}{T} \int_0^T \vec{S}_1(t) dt = \frac{1}{T} \int_0^T \left[ \frac{1}{2} \operatorname{Re} \left( \mathbf{E}_1 \times \mathbf{B}_1^* \right) + \frac{1}{2} \operatorname{Re} \left( \mathbf{E}_1 \times \mathbf{B}_1 e^{-2j\omega t} \right) \right] dt = \frac{1}{2} \operatorname{Re} \left( \mathbf{E}_1 \times \mathbf{B}_1^* \right)$$



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## Complex Poynting vector

- The corresponding phasor form of the Poynting vector

$$\mathbf{S}_1 = \frac{1}{2\mu_0} \mathbf{E}_1 \times \mathbf{B}_1^* \quad \text{and} \quad \mathbf{S}_1^* = \frac{1}{2\mu_0} \mathbf{E}_1^* \times \mathbf{B}_1,$$

$$\operatorname{Re}(\mathbf{S}_1) = \frac{1}{2}(\mathbf{S}_1 + \mathbf{S}_1^*) \quad \text{and} \quad j \operatorname{Im}(\mathbf{S}_1) = \frac{1}{2}(\mathbf{S}_1 - \mathbf{S}_1^*).$$

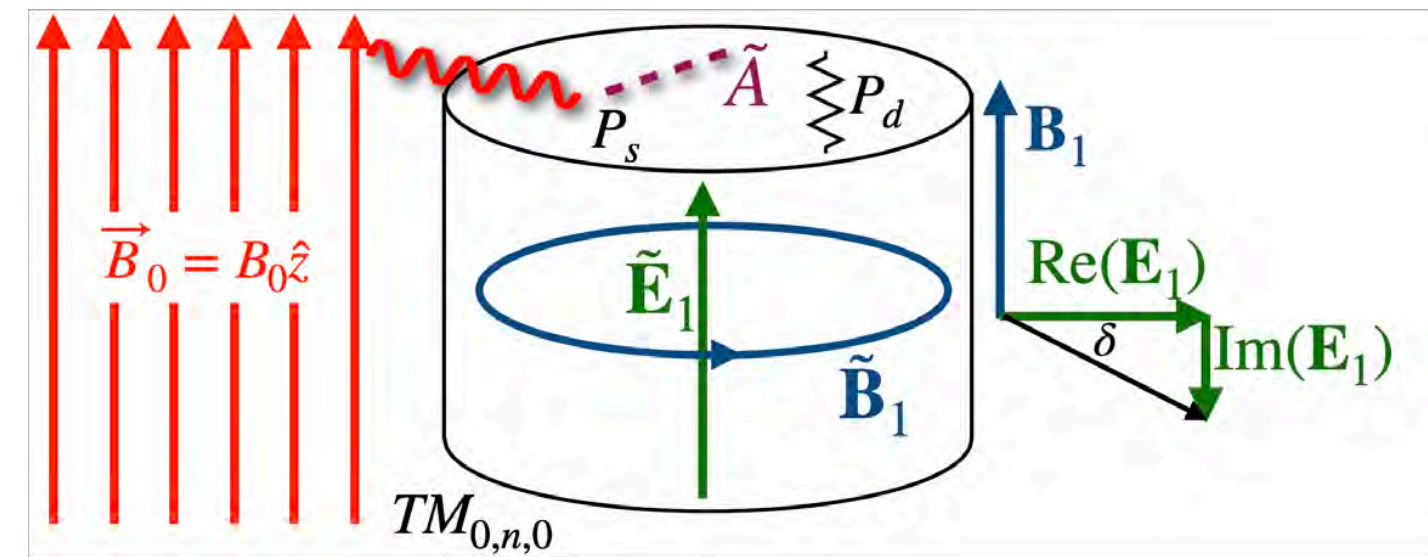
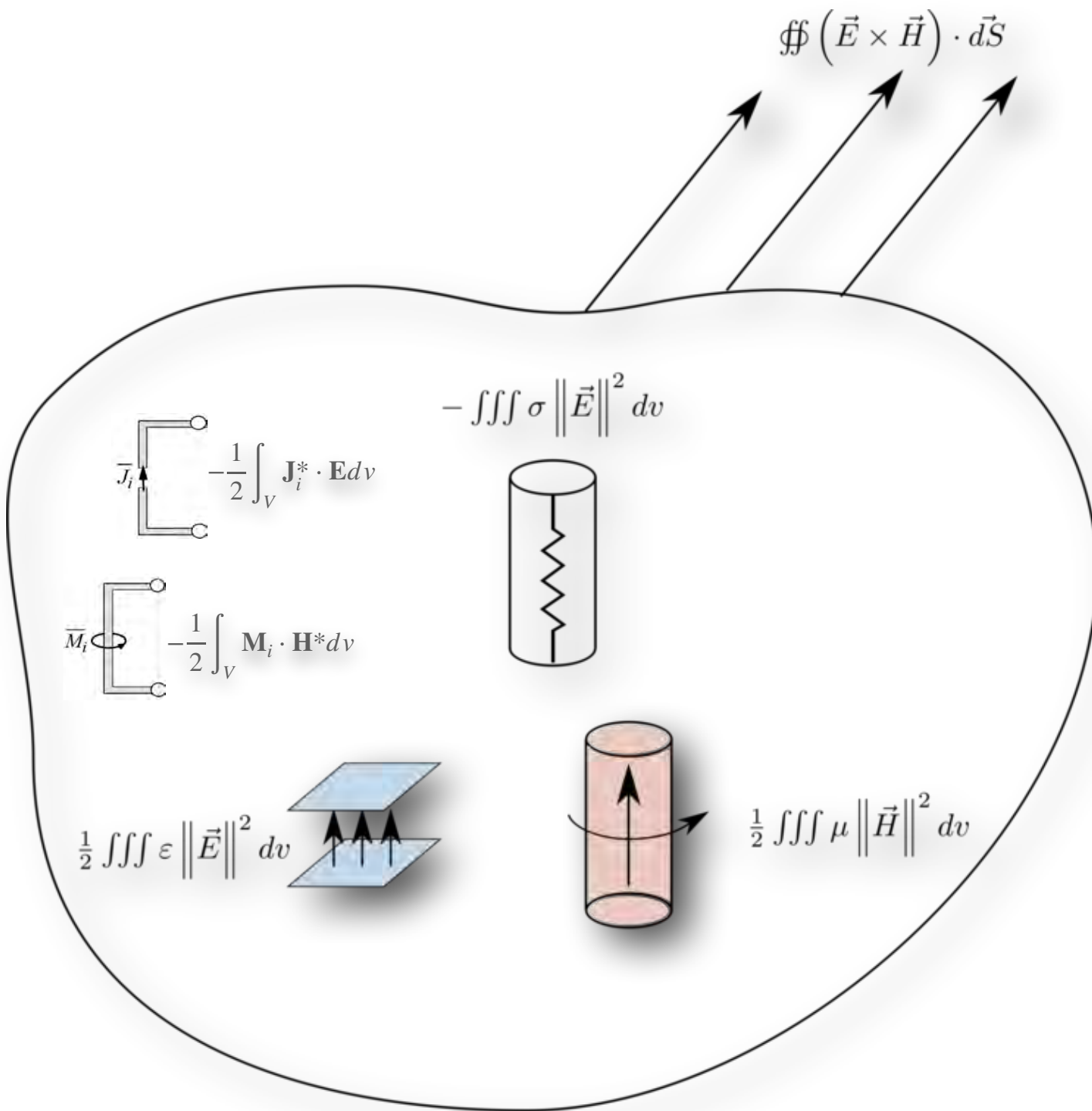
Time Average Power

Reactive Power

# Sensitivity of a Resonant Haloscope

$$P_{av} = \frac{1}{2} \operatorname{Re} \oint_{S_c} (\mathbf{E} \times \mathbf{H}^*) \cdot d\mathbf{s}$$

Average radiated power outside volume



## Poynting vector controversy in axion modified electrodynamics

Michael E. Tobar<sup>✉,\*</sup>, Ben T. McAllister, and Maxim Goryachev

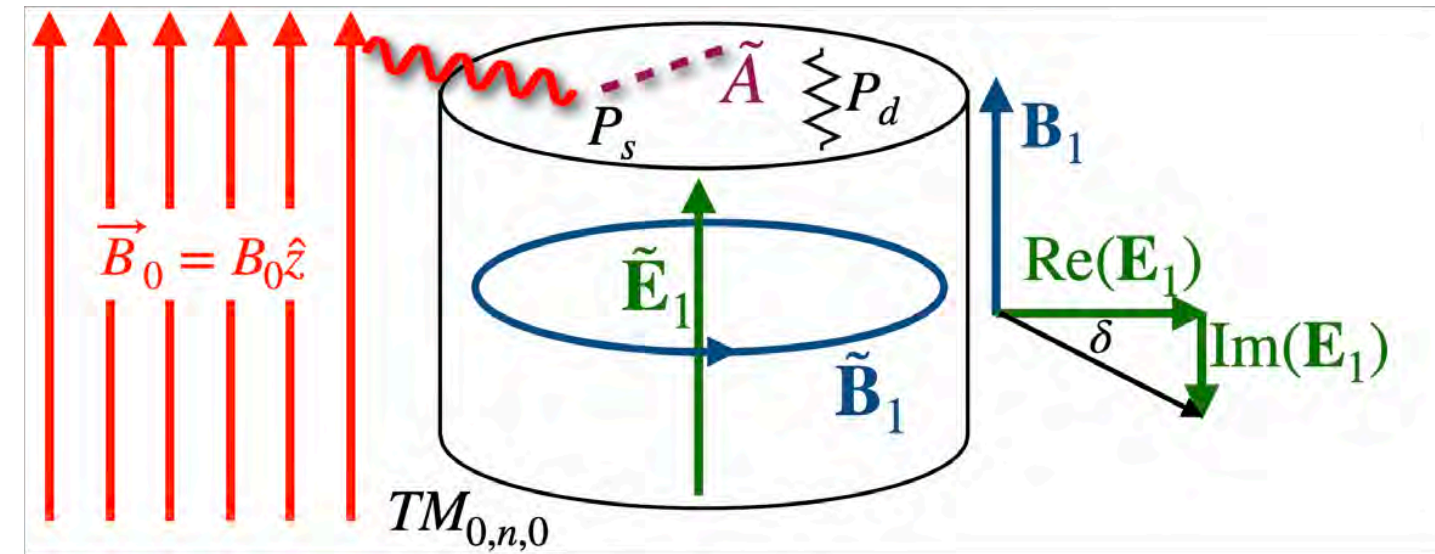
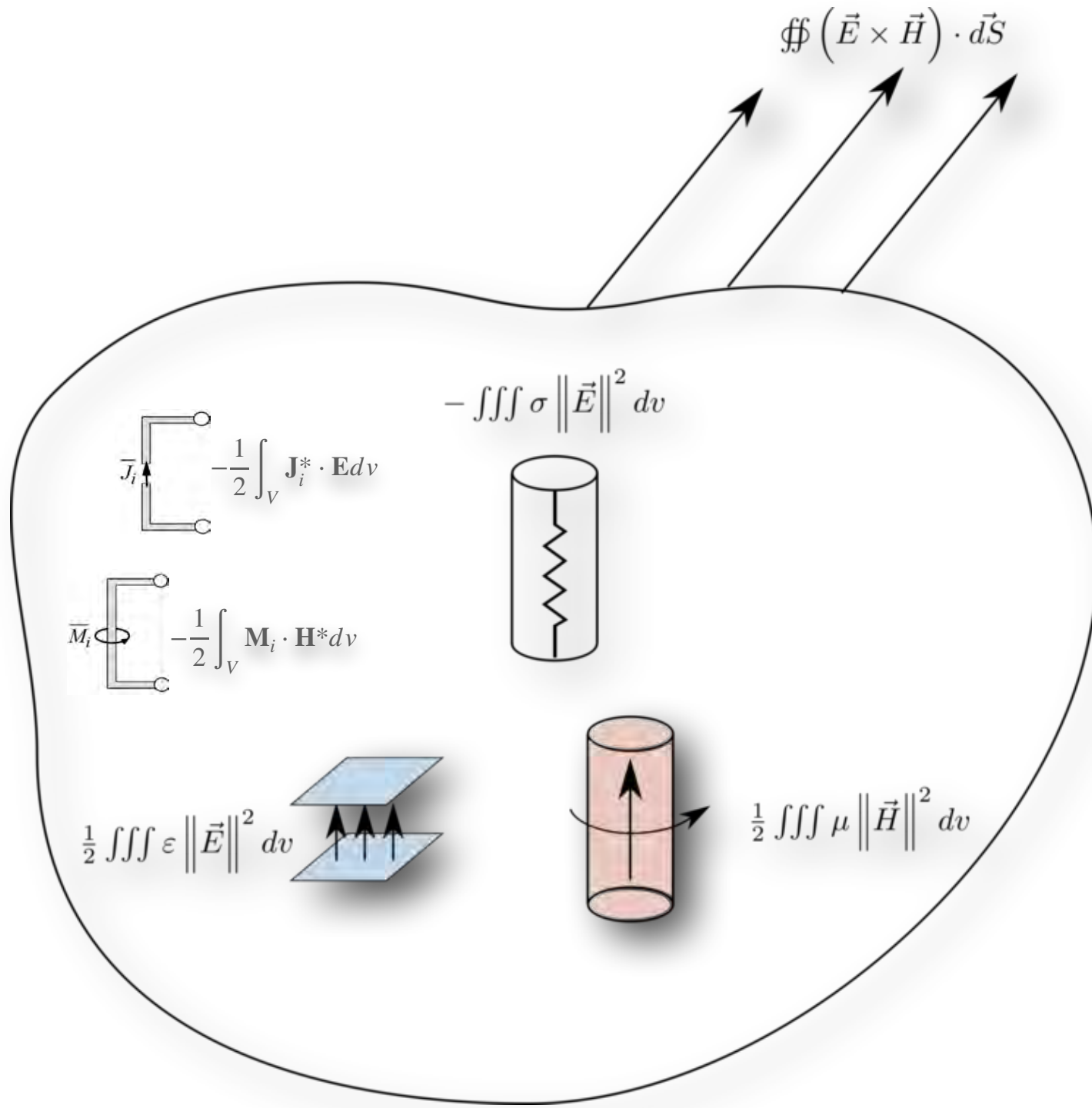
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$$\nabla \cdot \mathbf{S} = \frac{1}{2\mu_0} \nabla \cdot (\mathbf{E}_1 \times \mathbf{B}_1^*) = \frac{1}{2\mu_0} \mathbf{B}_1^* \cdot (\nabla \times \mathbf{E}_1) - \frac{1}{2\mu_0} \mathbf{E}_1 \cdot (\nabla \times \mathbf{B}_1^*)$$

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On resonance: Real part of Complex Poynting Theorem = 0 for closed system

$$\oint \operatorname{Re}(\mathbf{S}) \cdot \hat{n} ds = \frac{j\omega_a g_{a\gamma\gamma} \epsilon_0 c}{4} \int (\mathbf{E}_1 \cdot \tilde{a}^* \mathbf{B}_0^* - \mathbf{E}_1^* \cdot \tilde{a} \mathbf{B}_0) d\tau - \frac{1}{4} \int (\mathbf{E}_1 \cdot \mathbf{J}_{e1}^* + \mathbf{E}_1^* \cdot \mathbf{J}_{e1}) d\tau$$

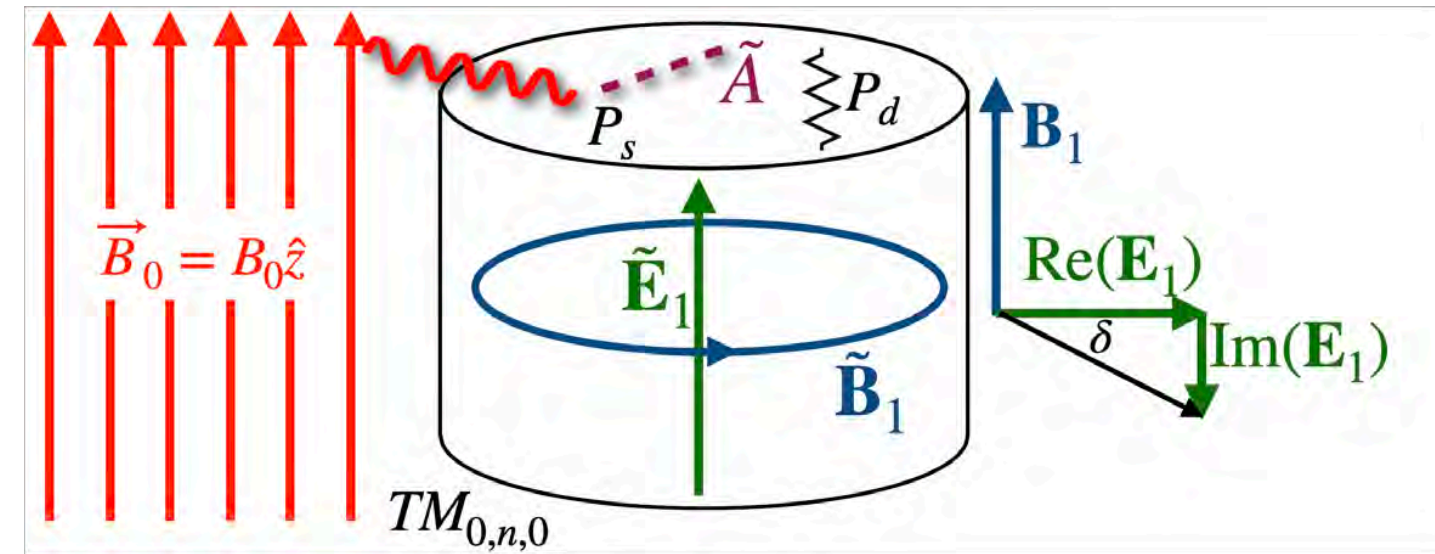
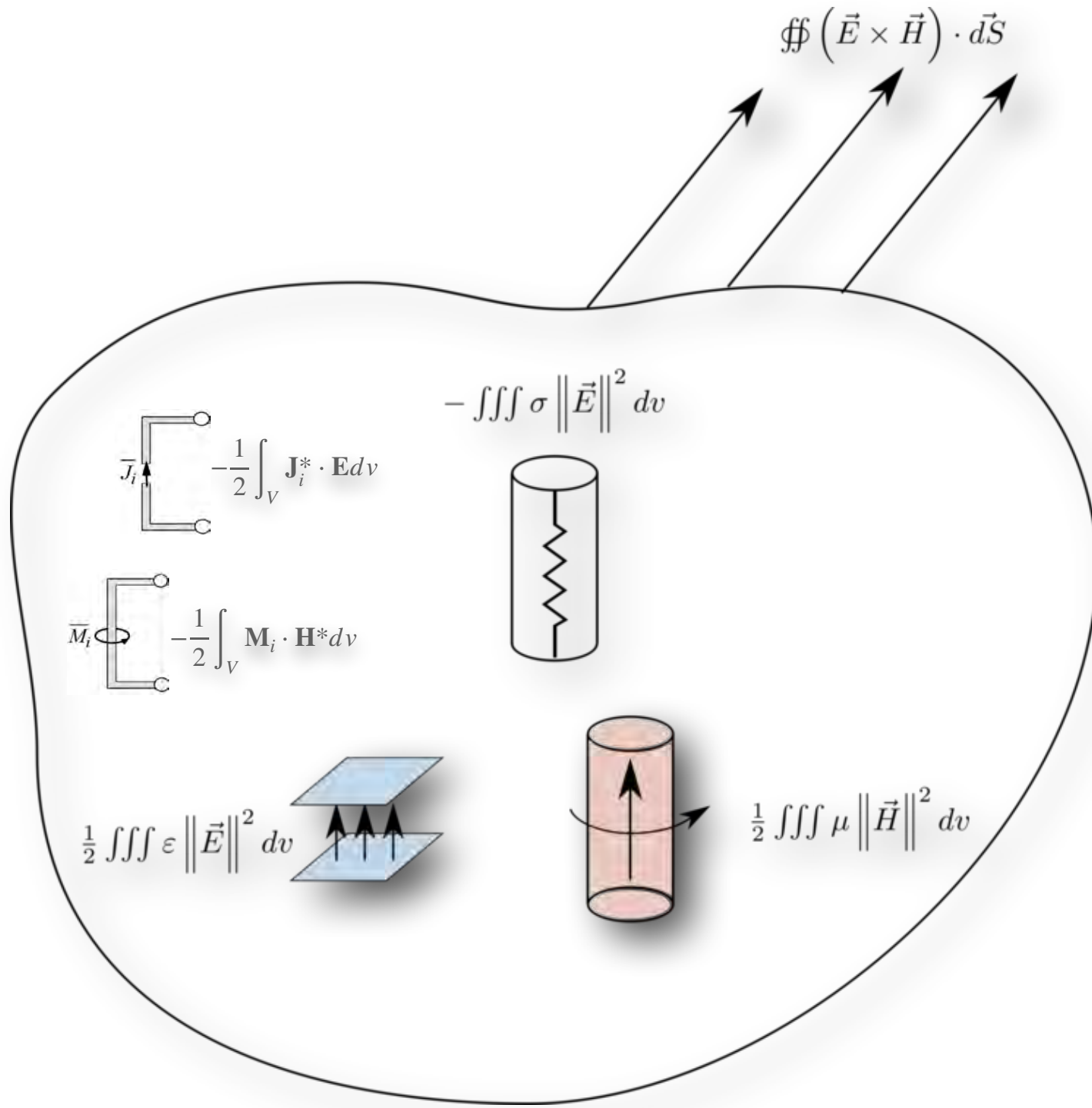
$P_s$  Axion power input

$P_d$  Cavity power distribution

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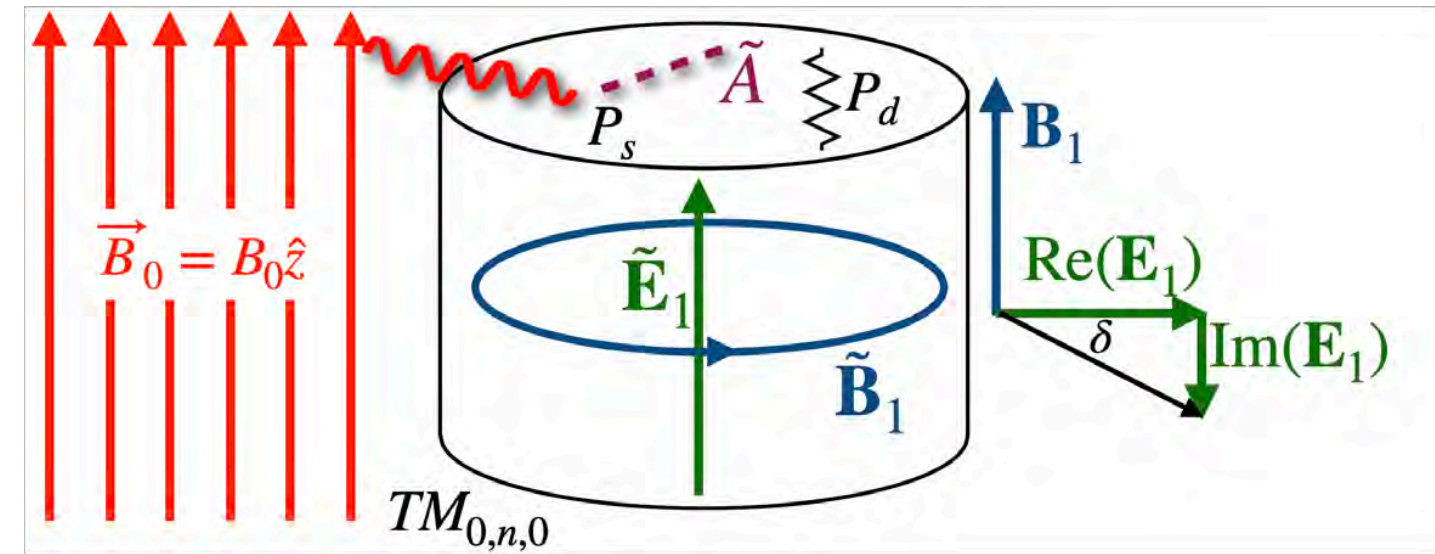
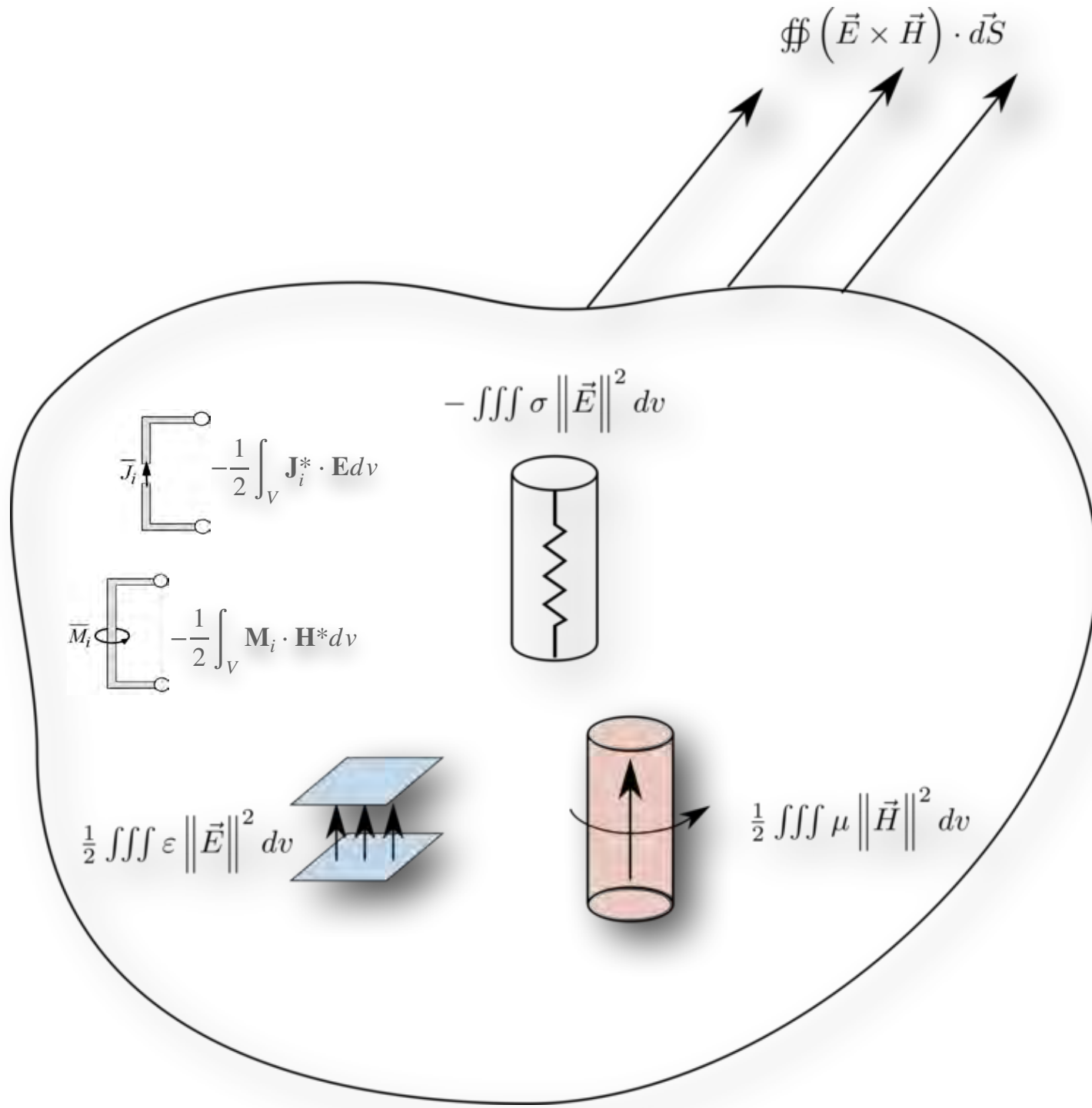
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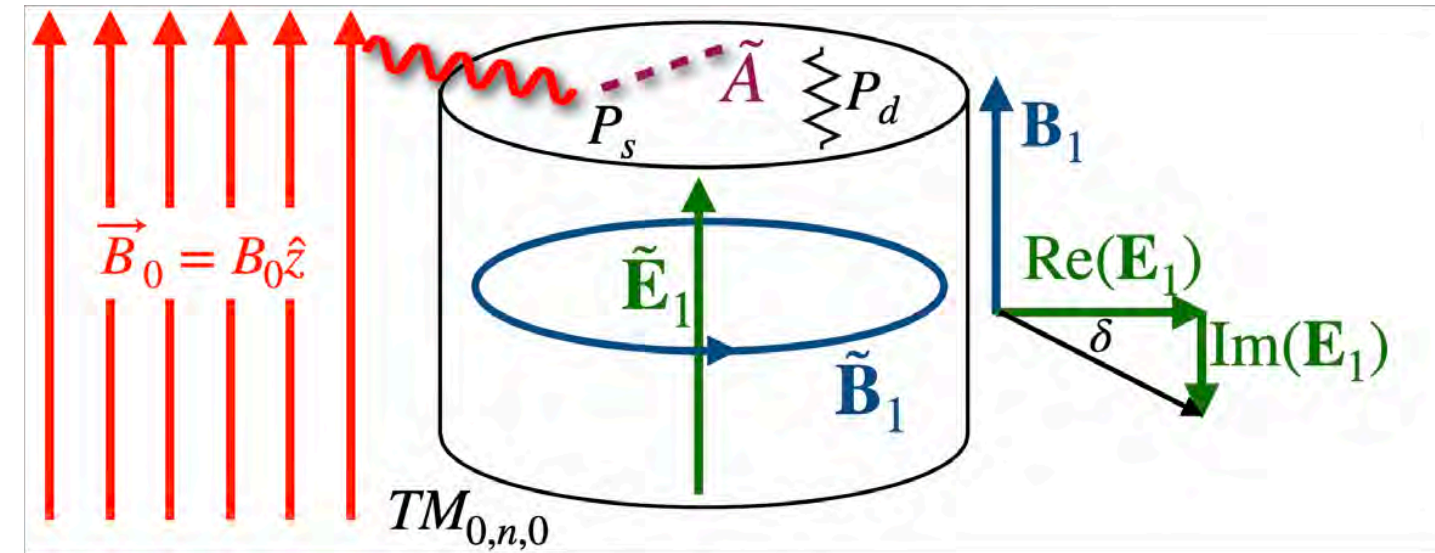
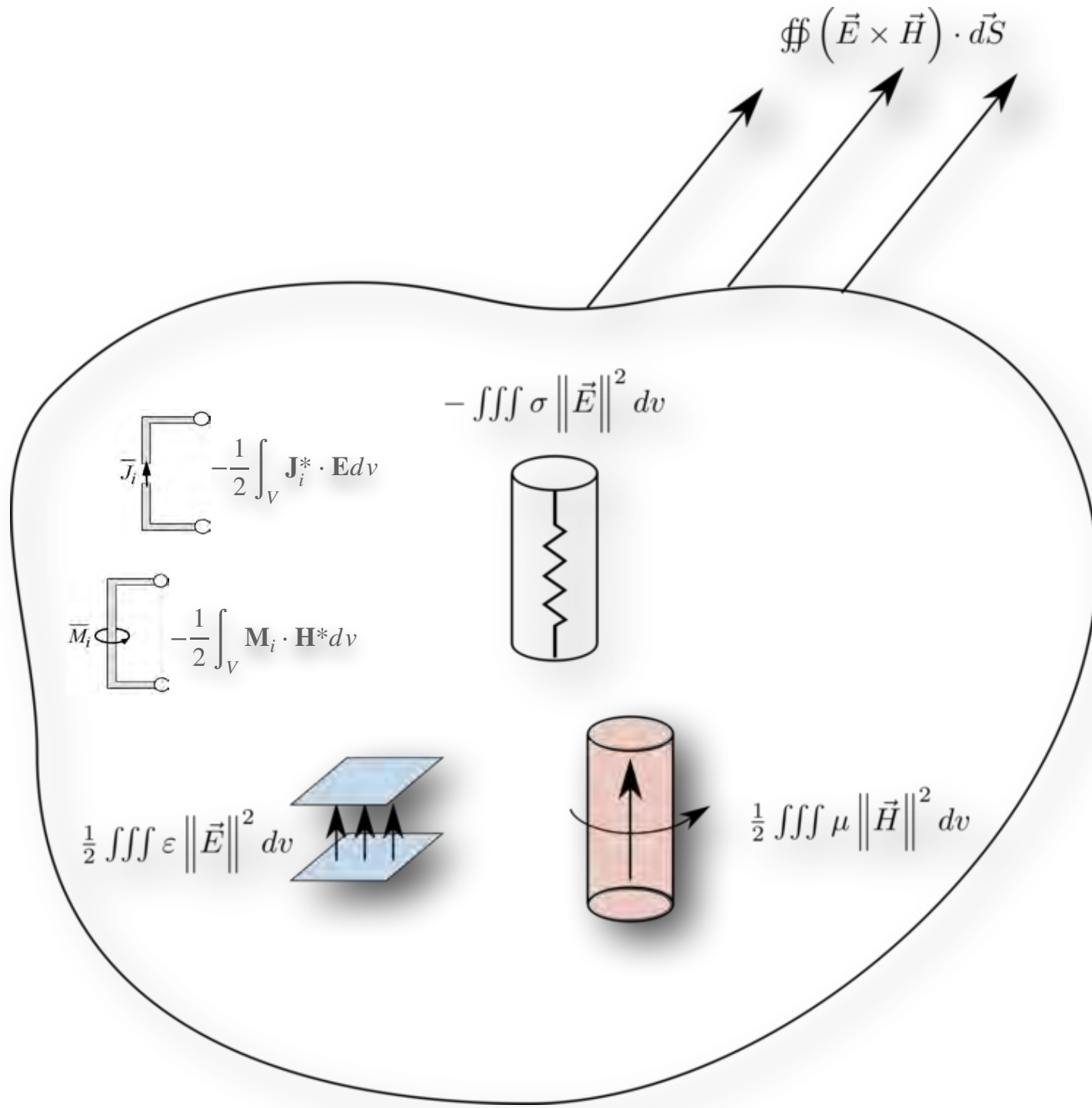
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$$P_{a1} = \frac{\omega_a g_{a\gamma\gamma} a_0 \epsilon_0 c}{2Q_1} \int (\operatorname{Re}(\mathbf{E}_1) \cdot \operatorname{Re}(\mathbf{B}_0)) d\tau = P_d = \frac{\omega_1 U_1}{Q_1}$$

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$$\nabla \cdot \mathbf{S} = \frac{1}{2\mu_0} \nabla \cdot (\mathbf{E}_1 \times \mathbf{B}_1^*) = \frac{1}{2\mu_0} \mathbf{B}_1^* \cdot (\nabla \times \mathbf{E}_1) - \frac{1}{2\mu_0} \mathbf{E}_1 \cdot (\nabla \times \mathbf{B}_1^*)$$

$$\nabla \cdot \mathbf{S}^* = \frac{1}{2\mu_0} \nabla \cdot (\mathbf{E}_1^* \times \mathbf{B}_1) = \frac{1}{2\mu_0} \mathbf{B}_1 \cdot (\nabla \times \mathbf{E}_1^*) - \frac{1}{2\mu_0} \mathbf{E}_1^* \cdot (\nabla \times \mathbf{B}_1)$$

On resonance: Real part of Complex Poynting Theorem = 0 for closed system

$$\oint \operatorname{Re}(\mathbf{S}) \cdot \hat{n} ds = \frac{j\omega_a g_{a\gamma\gamma} \epsilon_0 c}{4} \int (\mathbf{E}_1 \cdot \tilde{a}^* \mathbf{B}_0^* - \mathbf{E}_1^* \cdot \tilde{a} \mathbf{B}_0) d\tau - \frac{1}{4} \int (\mathbf{E}_1 \cdot \mathbf{J}_{e1}^* + \mathbf{E}_1^* \cdot \mathbf{J}_{e1}) d\tau$$

$P_s$  Axion power input

$P_d$  Cavity power distribution

$$P_d = \frac{1}{4} \int (\mathbf{E}_1 \cdot \mathbf{J}_{e1}^* + \mathbf{E}_1^* \cdot \mathbf{J}_{e1}) d\tau = \frac{\omega_1 \epsilon_0}{2Q_1} \int \mathbf{E}_1 \cdot \mathbf{E}_1^* dV = \frac{\omega_1 U_1}{Q_1}$$

$$P_{a1} = \frac{\omega_a g_{a\gamma\gamma} a_0 \epsilon_0 c}{2Q_1} \int (\operatorname{Re}(\mathbf{E}_1) \cdot \operatorname{Re}(\mathbf{B}_0)) d\tau = P_d = \frac{\omega_1 U_1}{Q_1}$$

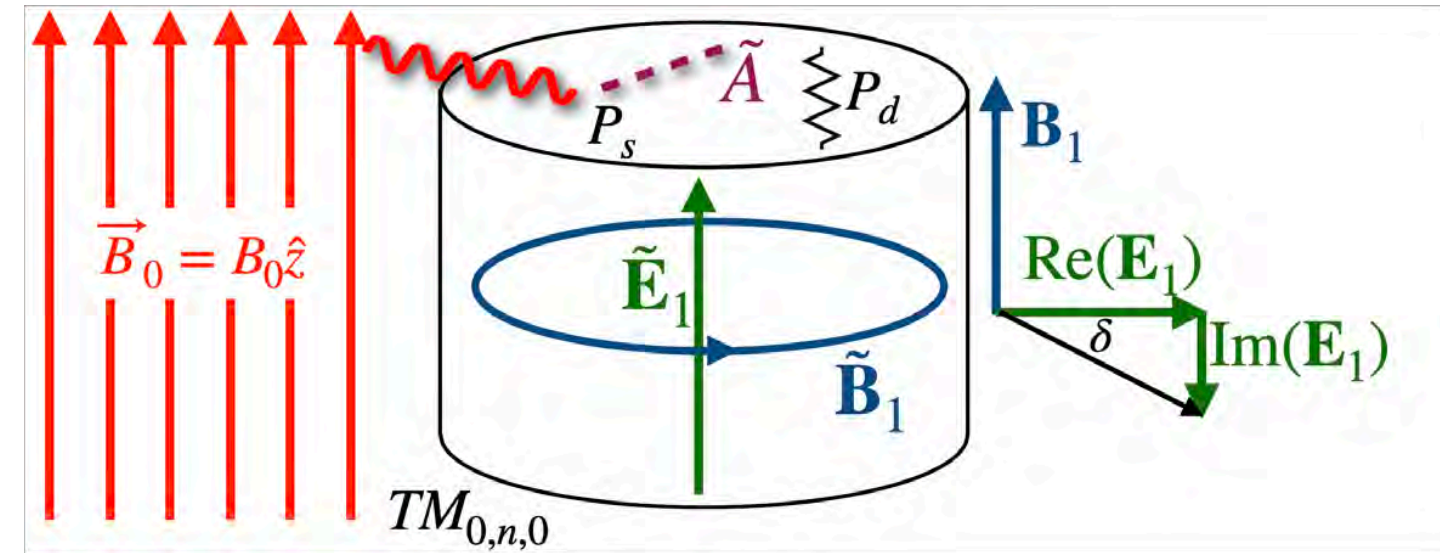
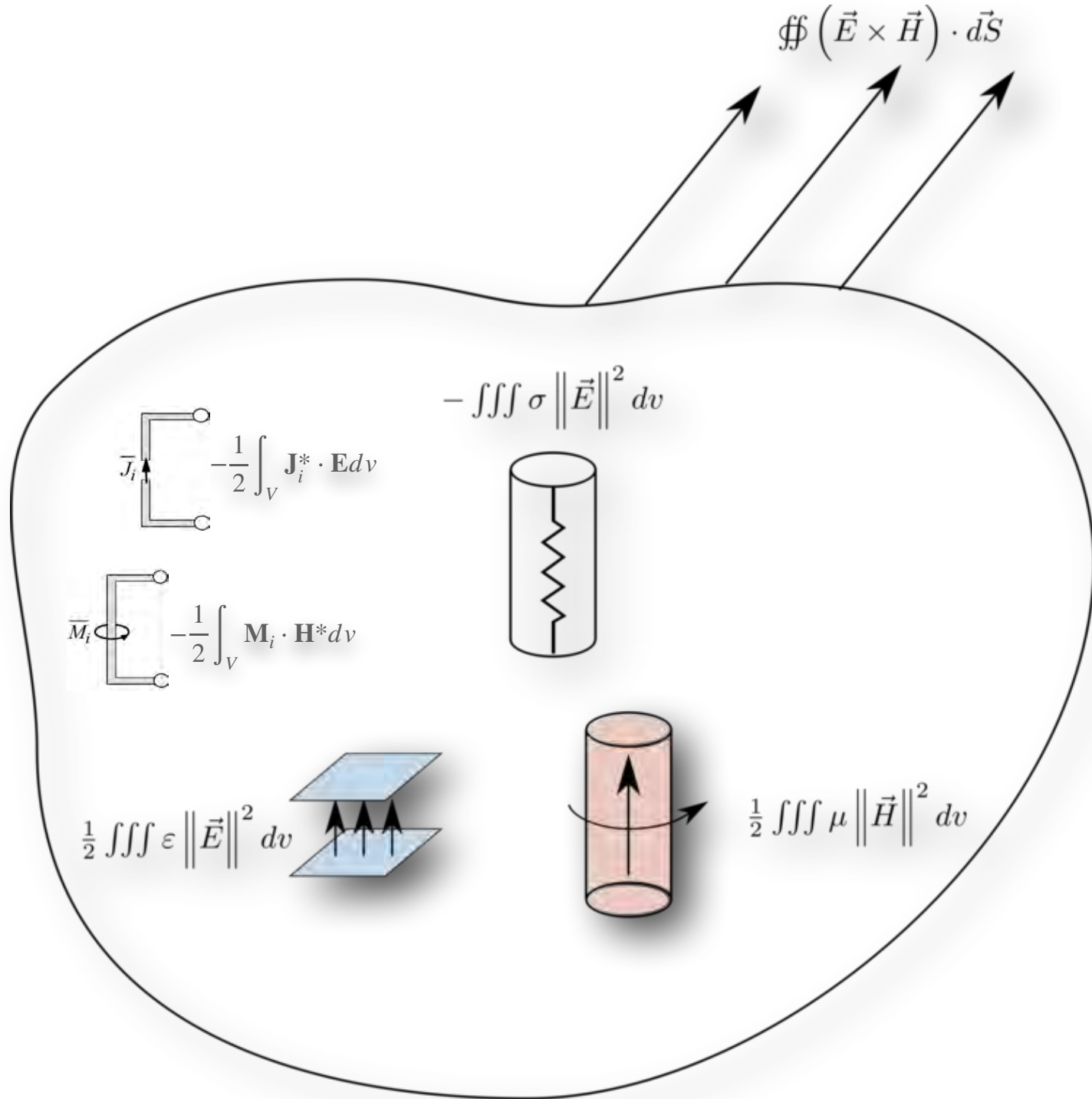
$$P_{a1} = \omega_a Q U_1 = g_{a\gamma\gamma}^2 \langle a_0 \rangle^2 \omega_a Q_1 \epsilon_0 c^2 B_0^2 V_1 C_1,$$

$$C_1 = \frac{\left( \int \vec{B}_0 \cdot \operatorname{Re}(\mathbf{E}_1) d\tau \right)^2}{B_0^2 V_1 \int \mathbf{E}_1 \cdot \mathbf{E}_1^* d\tau},$$

# Sensitivity of a Resonant Haloscope

$$P_{av} = \frac{1}{2} \operatorname{Re} \oint_{S_c} (\mathbf{E} \times \mathbf{H}^*) \cdot d\mathbf{s}$$

Average radiated power outside volume



## Poynting vector controversy in axion modified electrodynamics

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 ARC Centre of Excellence for Engineered Quantum Systems and ARC Centre of Excellence for Dark Matter Particle Physics, Department of Physics, University of Western Australia, 35 Stirling Highway, Crawley, Western Australia 6009, Australia

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$$\mathbf{S} = \frac{1}{2\mu_0} \mathbf{E}_1 \times \mathbf{B}_1^* \quad \text{and} \quad \mathbf{S}^* = \frac{1}{2\mu_0} \mathbf{E}_1^* \times \mathbf{B}_1$$

$$\nabla \cdot \mathbf{S} = \frac{1}{2\mu_0} \nabla \cdot (\mathbf{E}_1 \times \mathbf{B}_1^*) = \frac{1}{2\mu_0} \mathbf{B}_1^* \cdot (\nabla \times \mathbf{E}_1) - \frac{1}{2\mu_0} \mathbf{E}_1 \cdot (\nabla \times \mathbf{B}_1^*)$$

$$\nabla \cdot \mathbf{S}^* = \frac{1}{2\mu_0} \nabla \cdot (\mathbf{E}_1^* \times \mathbf{B}_1) = \frac{1}{2\mu_0} \mathbf{B}_1 \cdot (\nabla \times \mathbf{E}_1^*) - \frac{1}{2\mu_0} \mathbf{E}_1^* \cdot (\nabla \times \mathbf{B}_1)$$

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$P_s$  Axion power input

$P_d$  Cavity power distribution

$$P_d = \frac{1}{4} \int (\mathbf{E}_1 \cdot \mathbf{J}_{e1}^* + \mathbf{E}_1^* \cdot \mathbf{J}_{e1}) d\tau = \frac{\omega_1 \epsilon_0}{2Q_1} \int \mathbf{E}_1 \cdot \mathbf{E}_1^* dV = \frac{\omega_1 U_1}{Q_1}$$

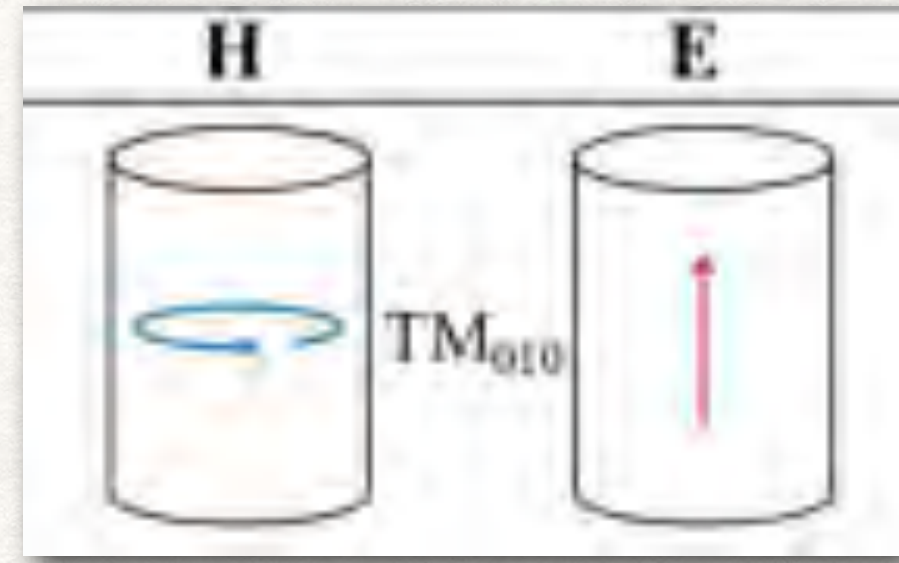
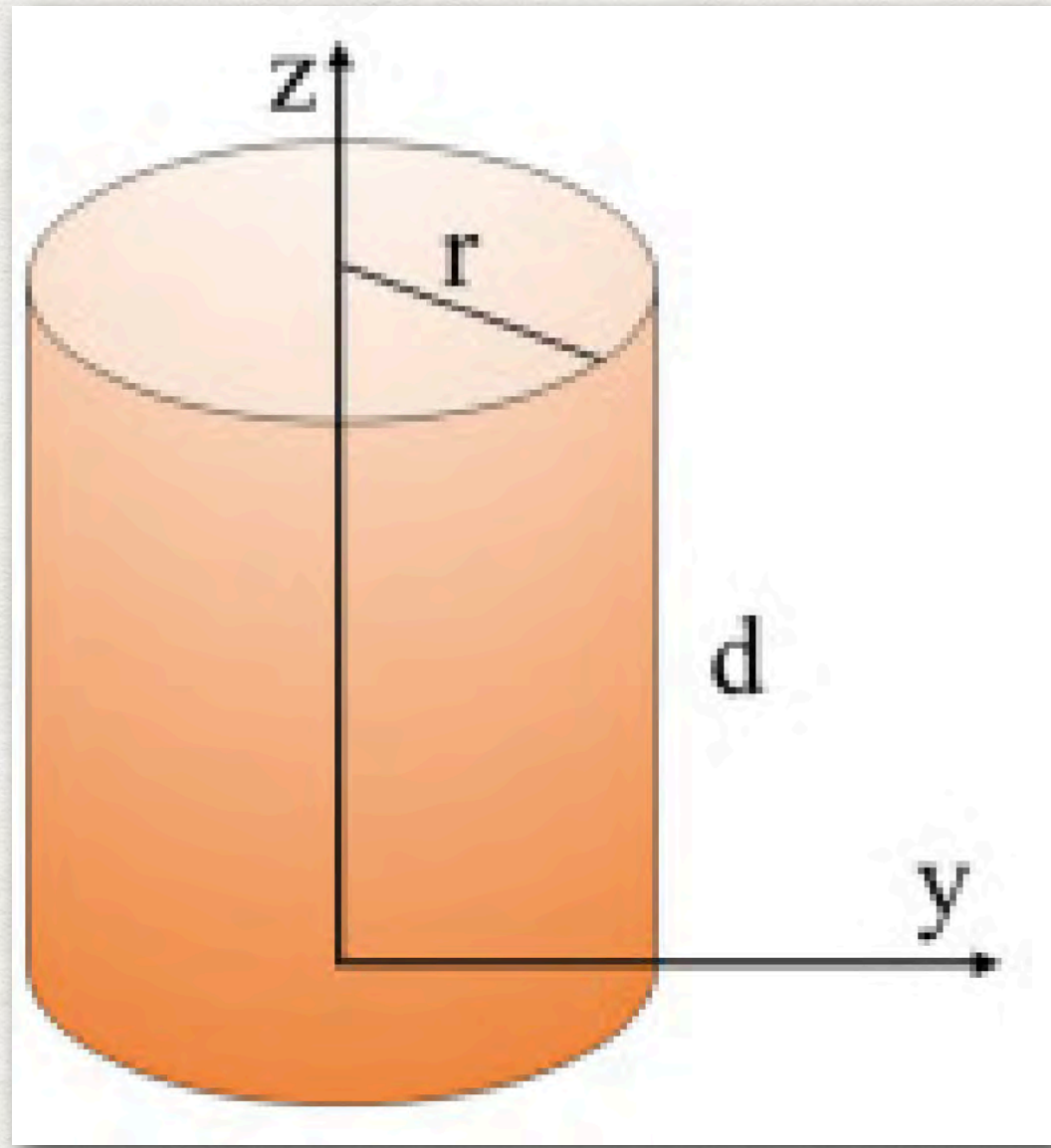
$$P_{a1} = \frac{\omega_a g_{a\gamma\gamma} a_0 \epsilon_0 c}{2Q_1} \int (\operatorname{Re}(\mathbf{E}_1) \cdot \operatorname{Re}(\mathbf{B}_0)) d\tau = P_d = \frac{\omega_1 U_1}{Q_1}$$

$$P_{a1} = \omega_a Q U_1 = g_{a\gamma\gamma}^2 \langle a_0 \rangle^2 \omega_a Q_1 \epsilon_0 c^2 B_0^2 V_1 C_1,$$

$$C_1 = \frac{\left( \int \vec{B}_0 \cdot \operatorname{Re}(\mathbf{E}_1) d\tau \right)^2}{B_0^2 V_1 \int \mathbf{E}_1 \cdot \mathbf{E}_1^* d\tau},$$

Resonant Haloscope, on resonance,  
 Reactive Power = 0

# IMAGINARY POYNTING VECTOR INSIDE CAVITY

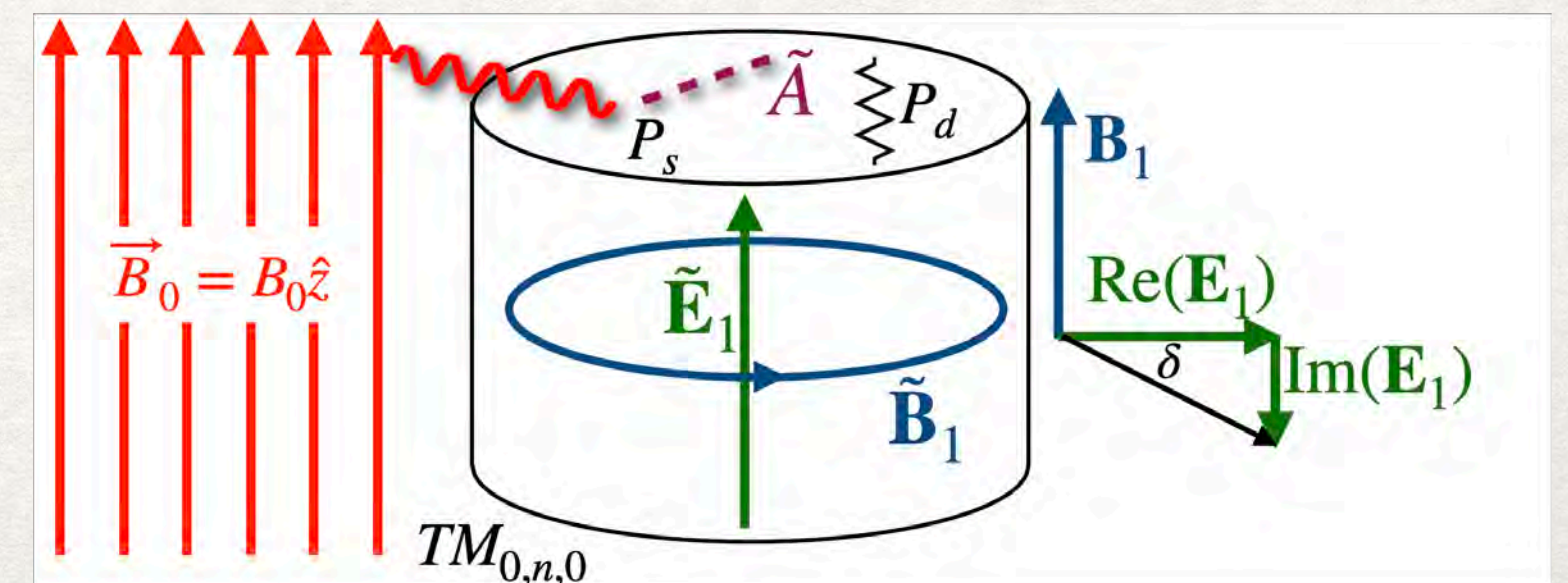
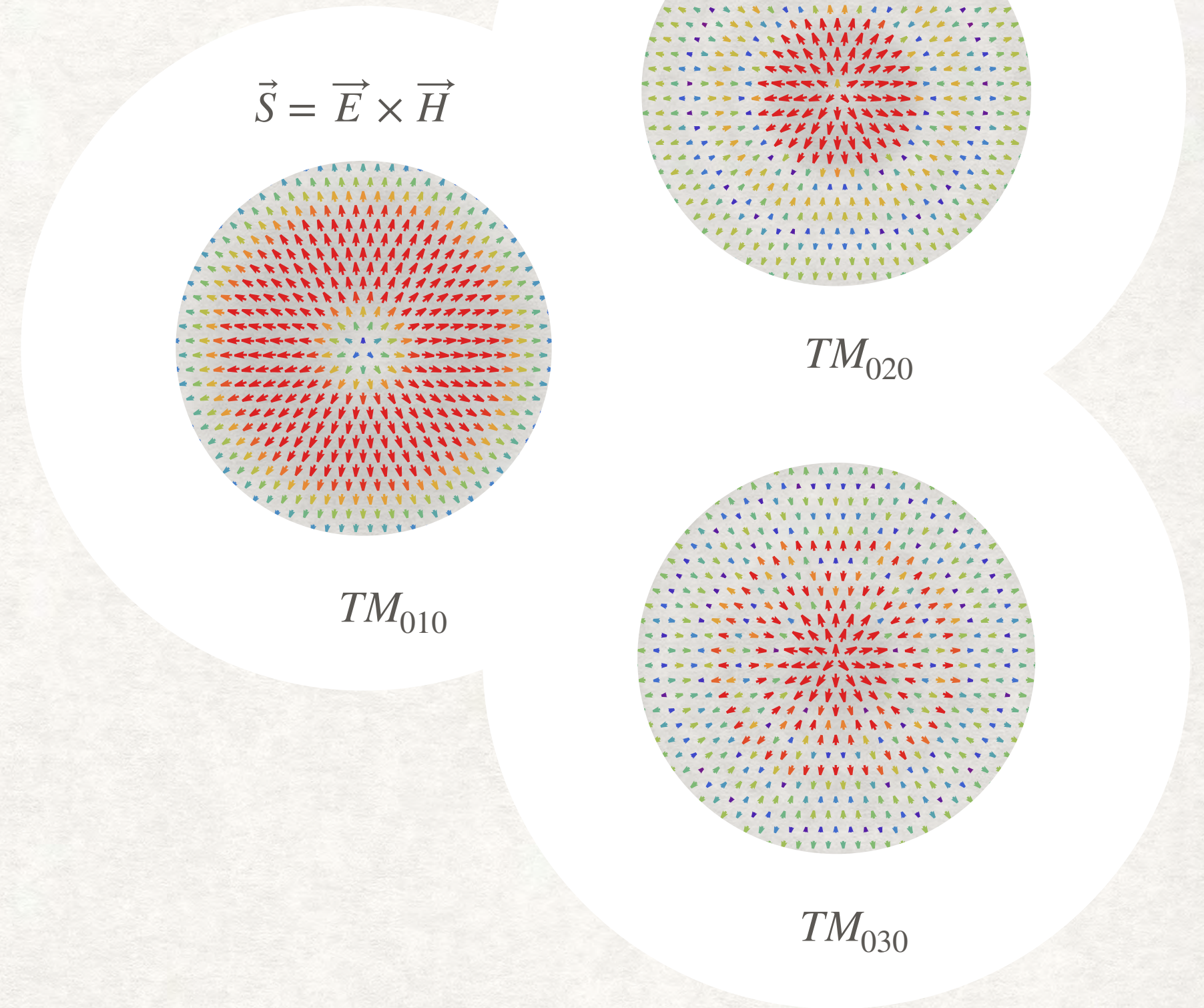
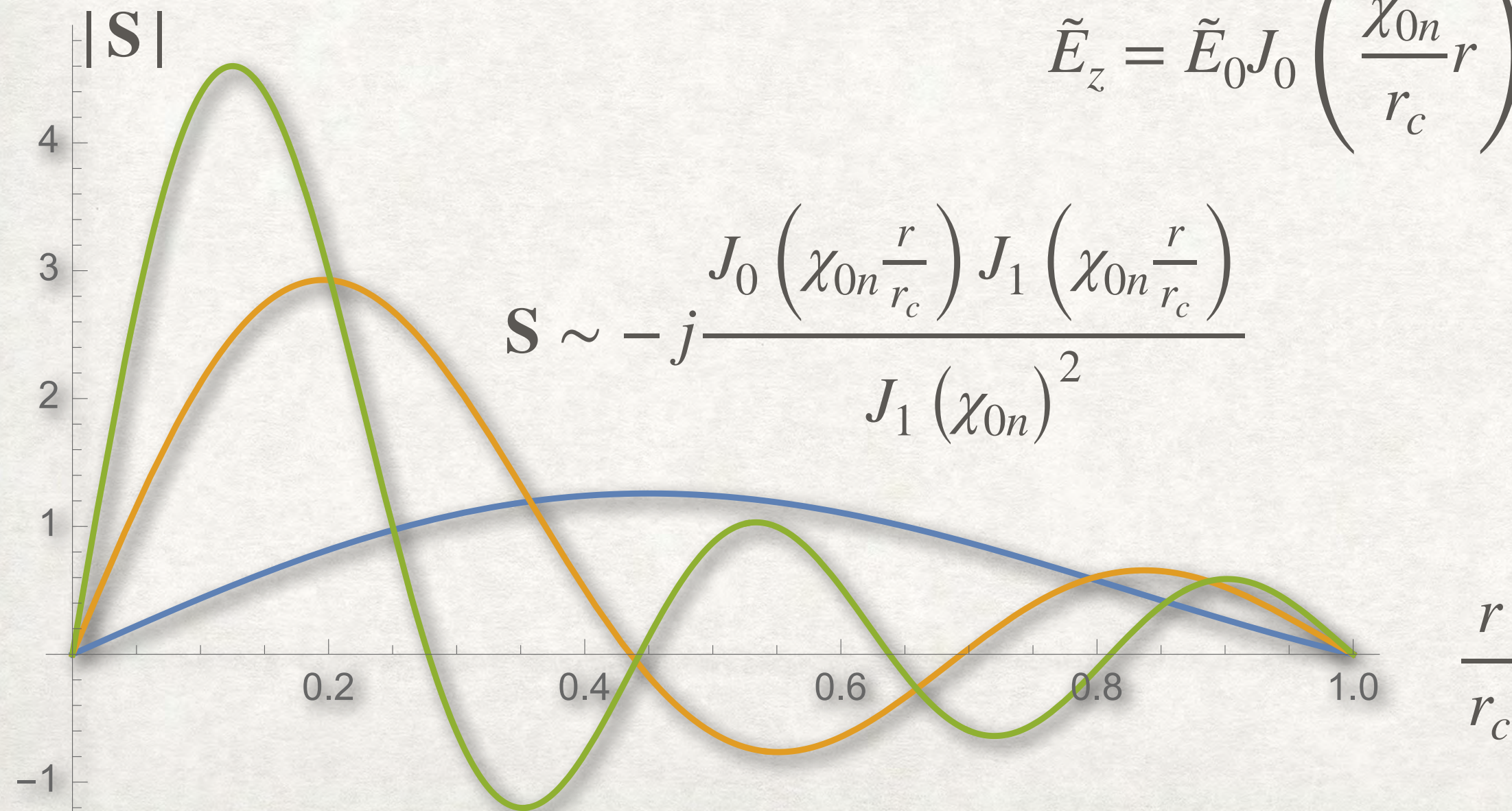


$TM_{0n0}$

$$\tilde{H}_\phi = -j\tilde{E}_0(\omega\epsilon)\frac{r_c}{\chi_{0n}}J'_0\left(\frac{\chi_{0n}r}{r_c}\right)$$

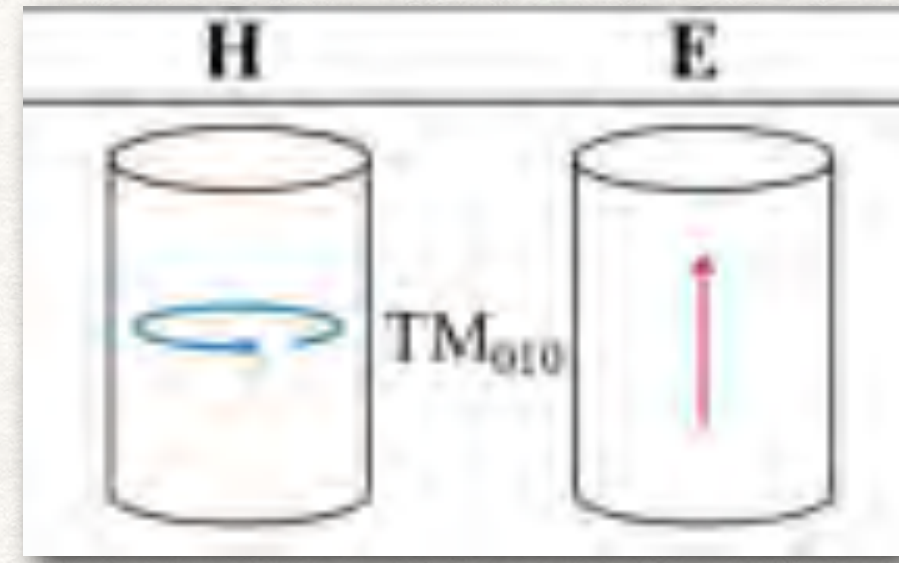
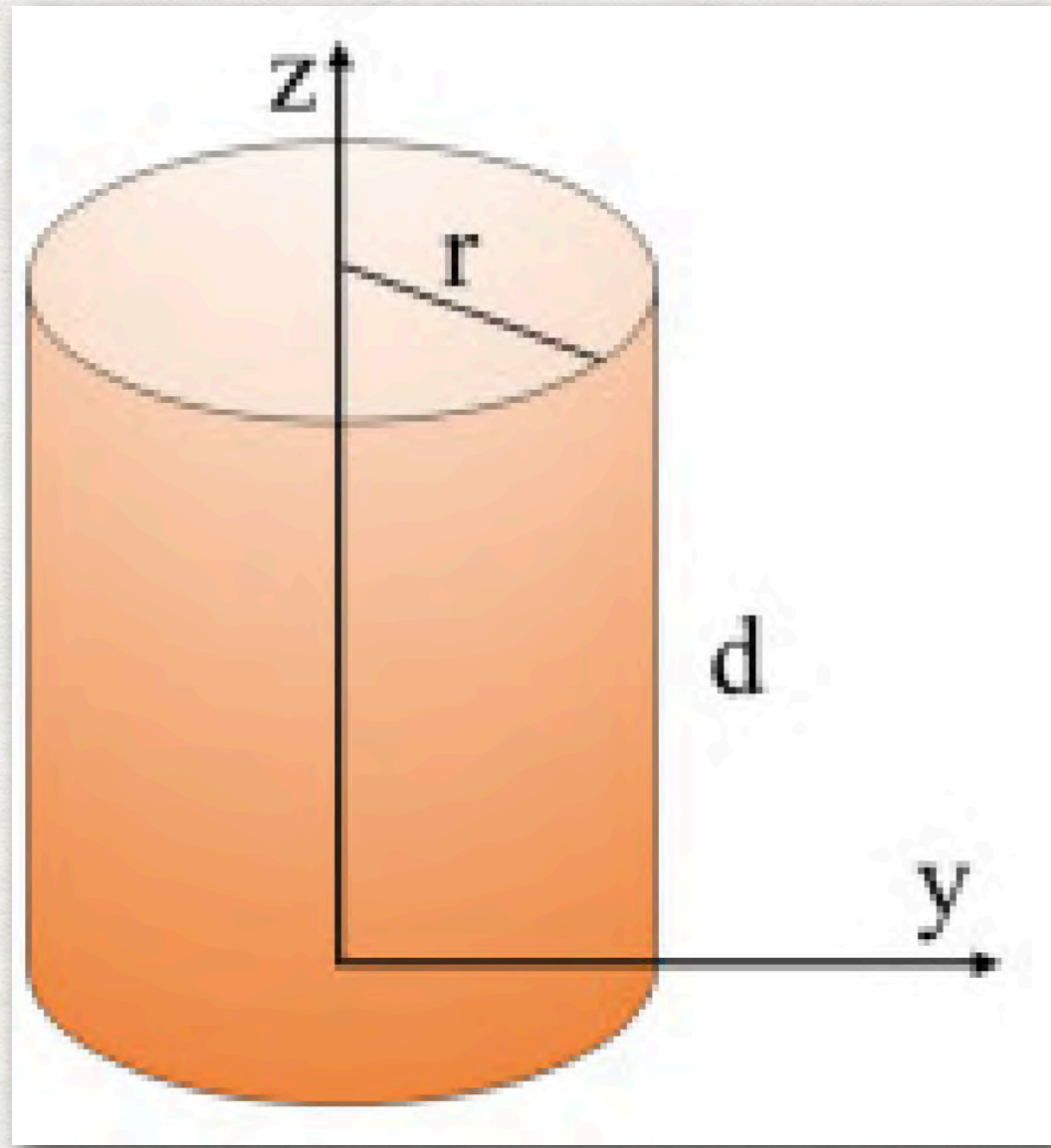
$$\tilde{E}_z = \tilde{E}_0J_0\left(\frac{\chi_{0n}r}{r_c}\right)$$

$$\mathbf{S} \sim -j\frac{J_0\left(\chi_{0n}\frac{r}{r_c}\right)J_1\left(\chi_{0n}\frac{r}{r_c}\right)}{J_1(\chi_{0n})^2}$$





# IMAGINARY POYNTING VECTOR INSIDE CAVITY



$TM_{0n0}$

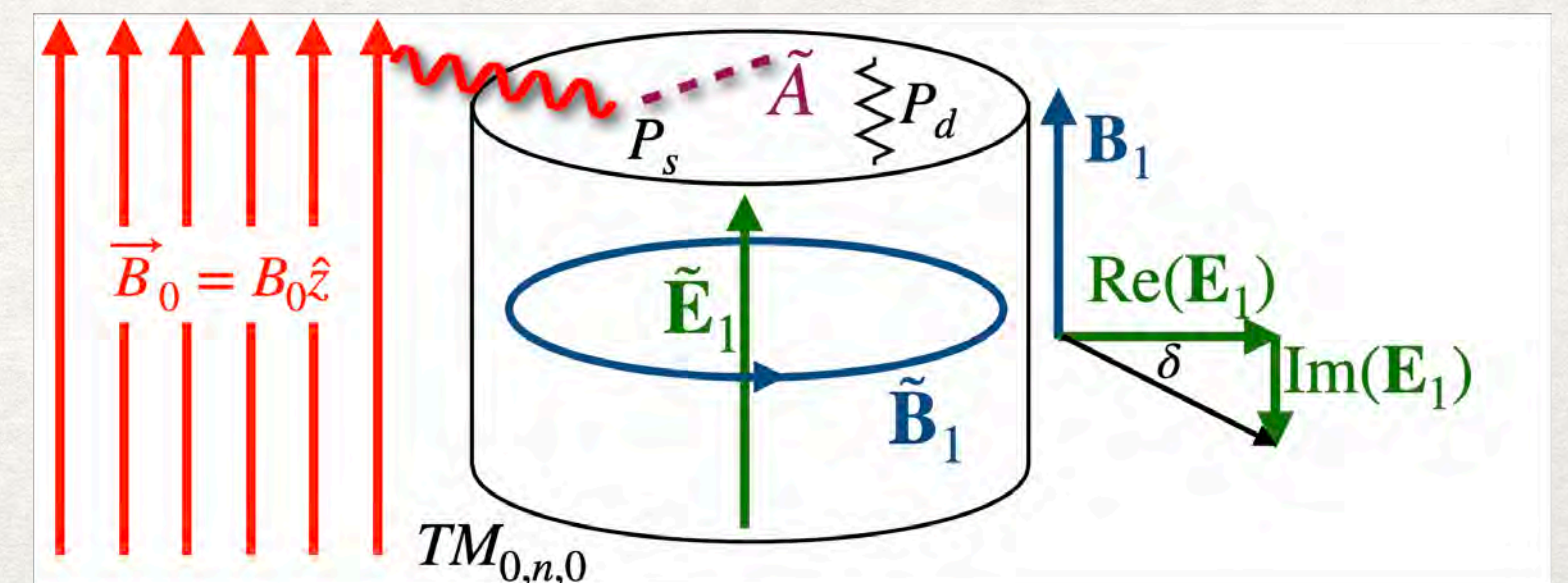
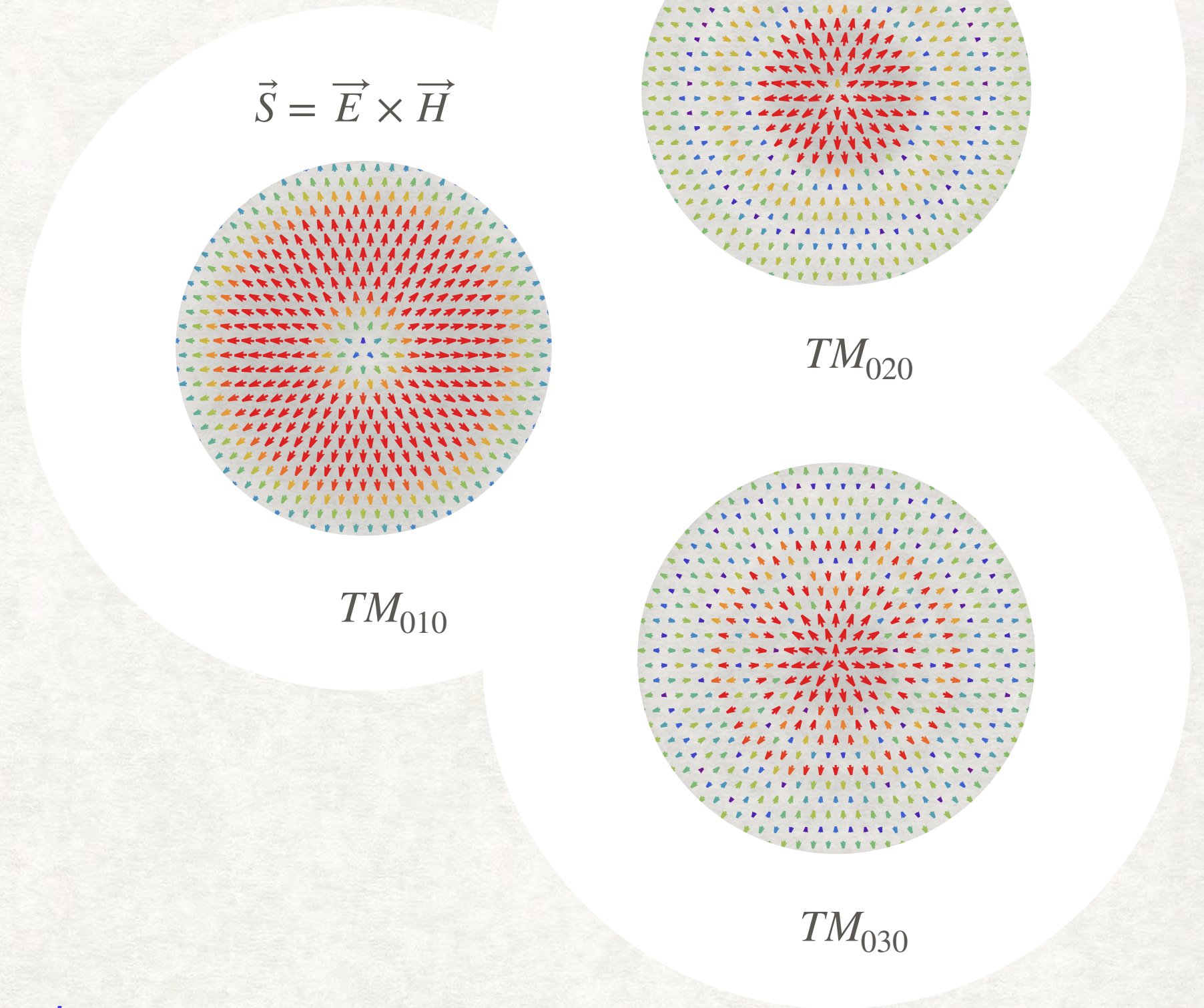
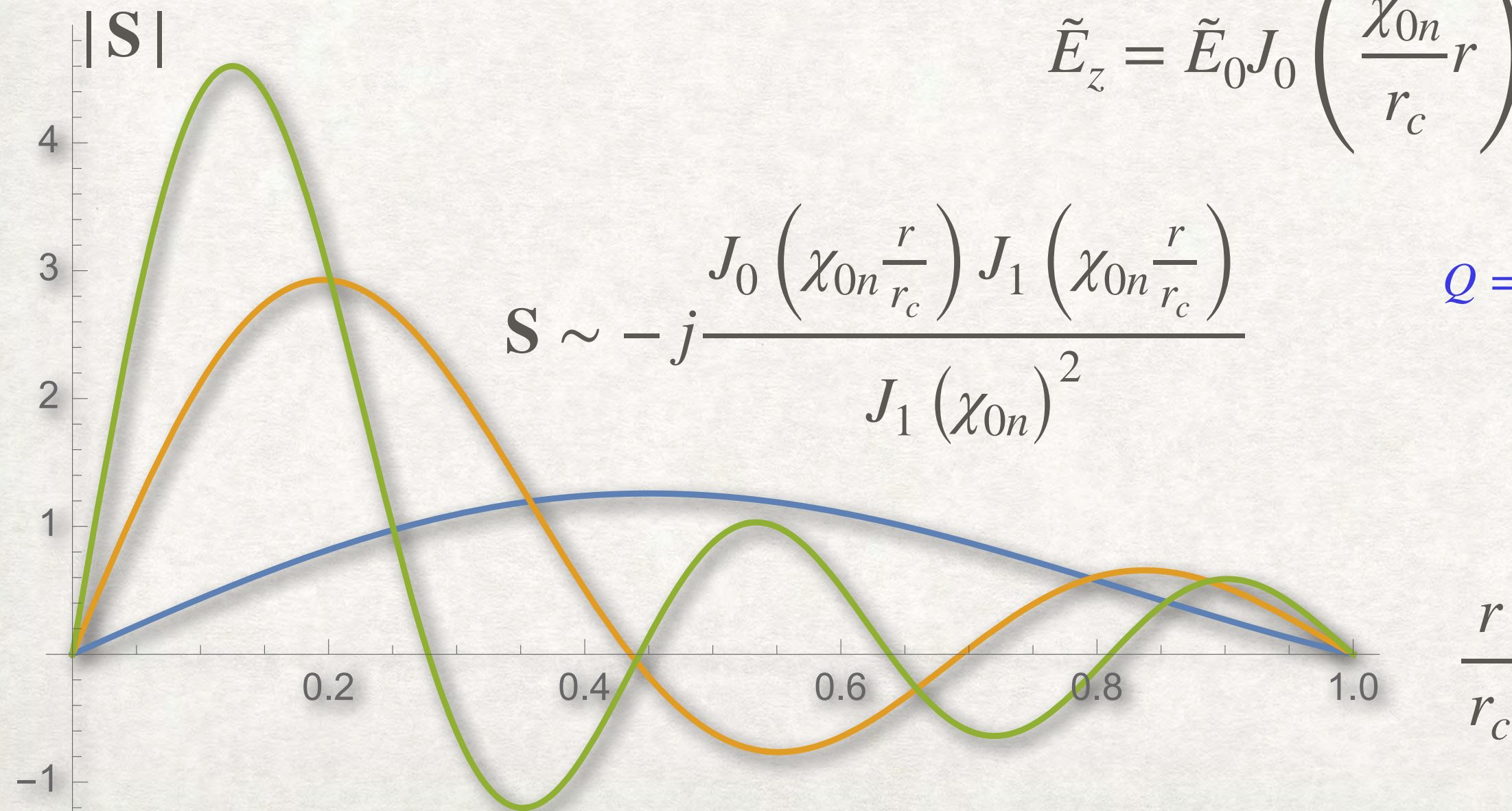
$$\tilde{H}_\phi = -j\tilde{E}_0(\omega\epsilon)\frac{r_c}{\chi_{0n}}J'_0\left(\frac{\chi_{0n}r}{r_c}\right)$$

$$\tilde{E}_z = \tilde{E}_0J_0\left(\frac{\chi_{0n}r}{r_c}\right)$$

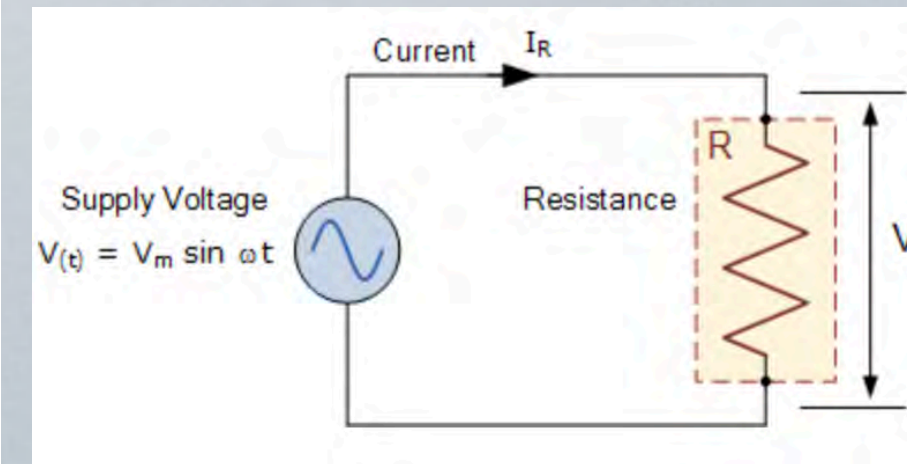
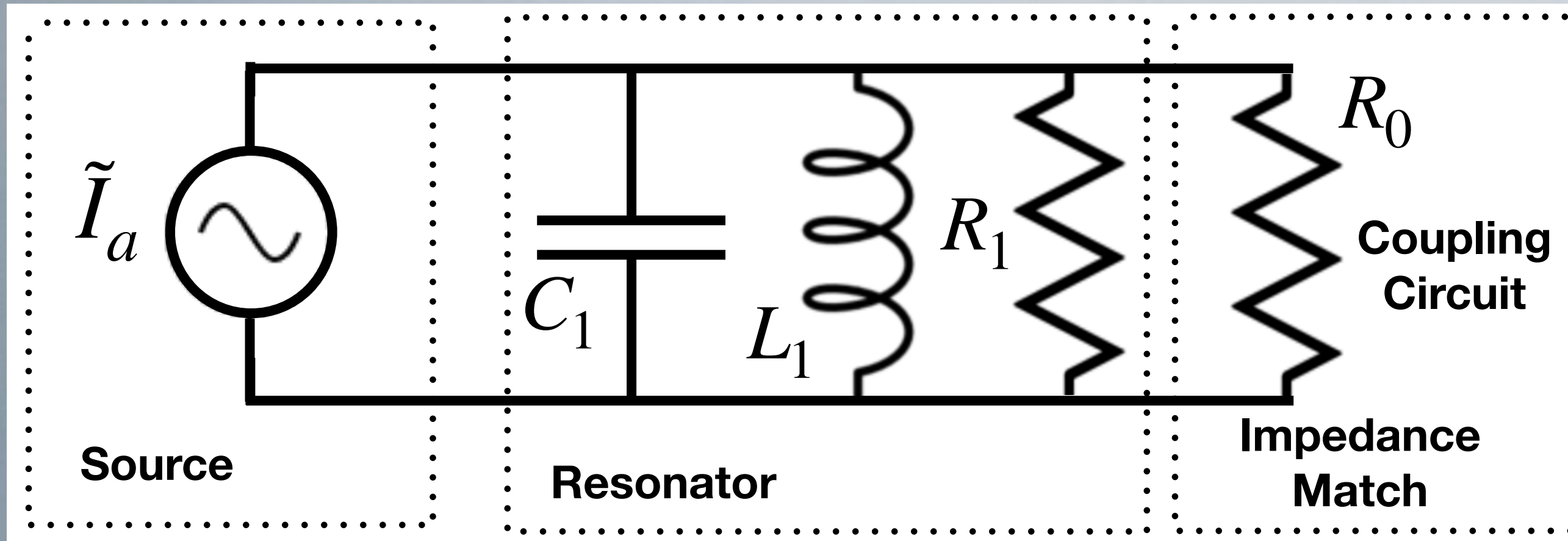
$$\mathbf{S} \sim -j\frac{J_0\left(\chi_{0n}\frac{r}{r_c}\right)J_1\left(\chi_{0n}\frac{r}{r_c}\right)}{J_1(\chi_{0n})^2}$$

$$Q = \omega_1 \frac{U_{tot}}{P_d} = 2\pi \frac{\text{stored energy}}{\text{energy dissipated during one period}}$$

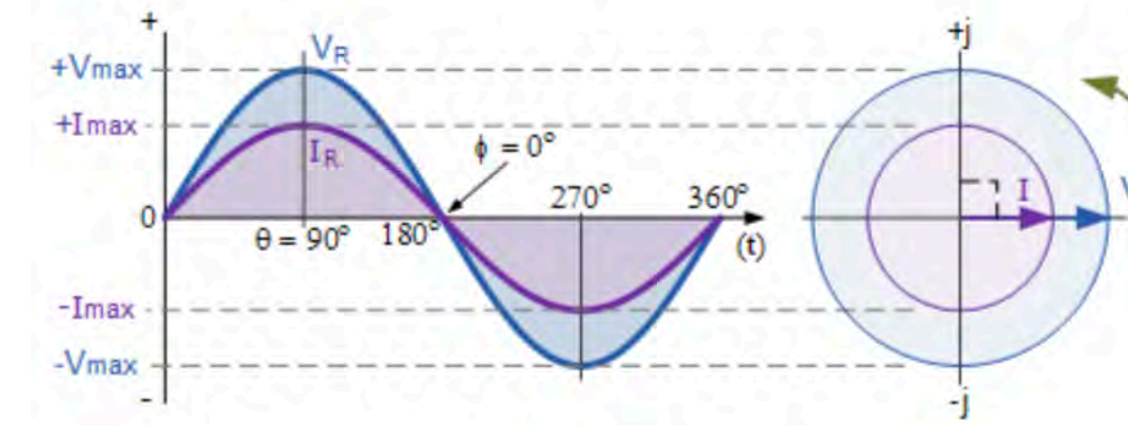
$$P_d = \frac{\omega_1 U_{tot}}{Q}$$



# Resonator Measurement: Impedance match; set coupling =1; Take Photons from Source

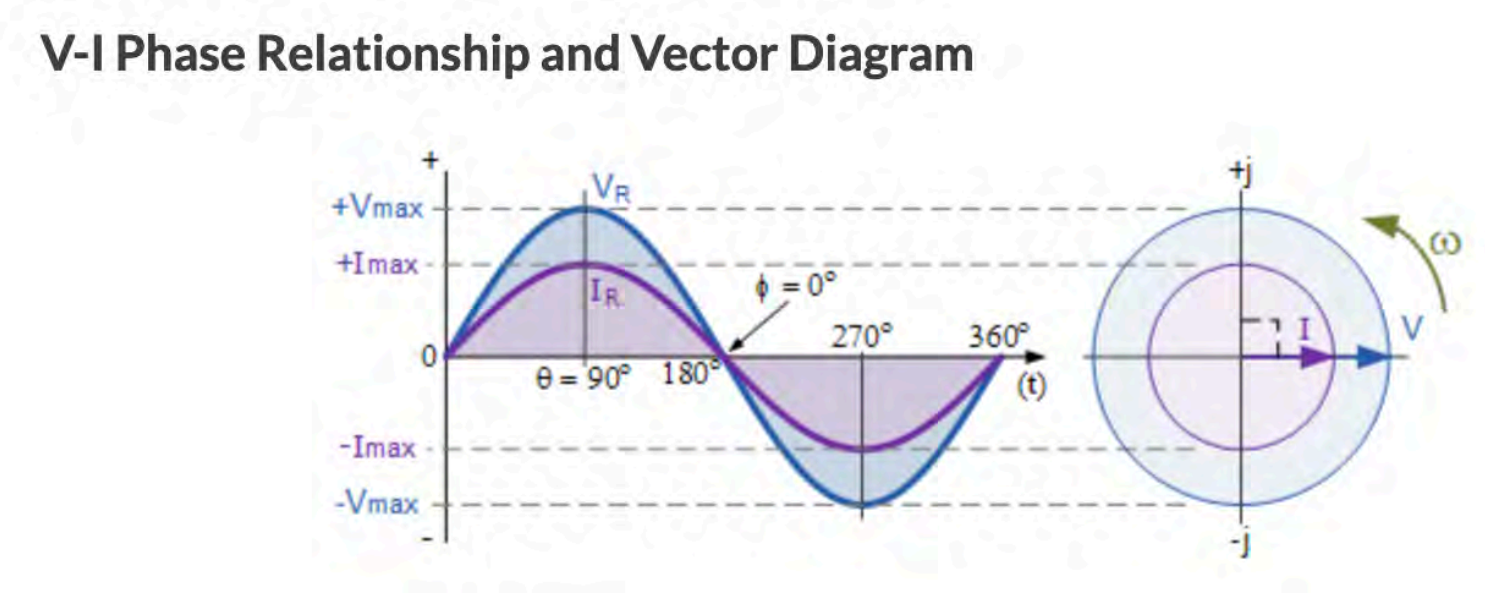
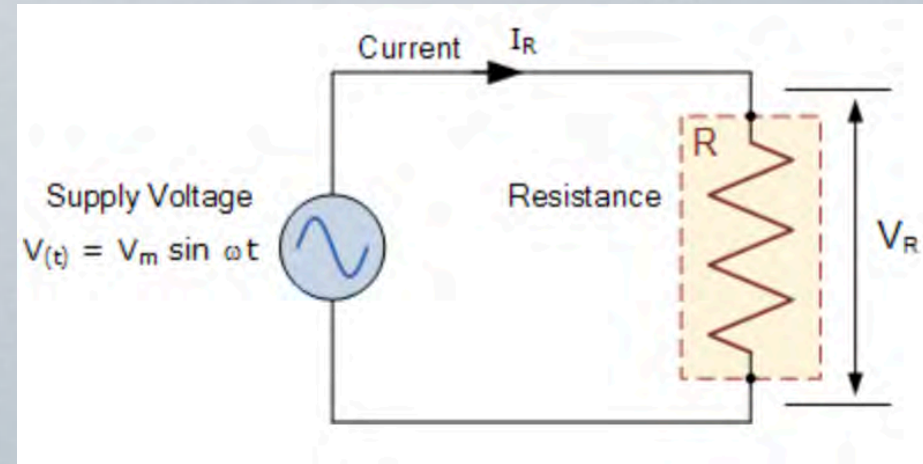
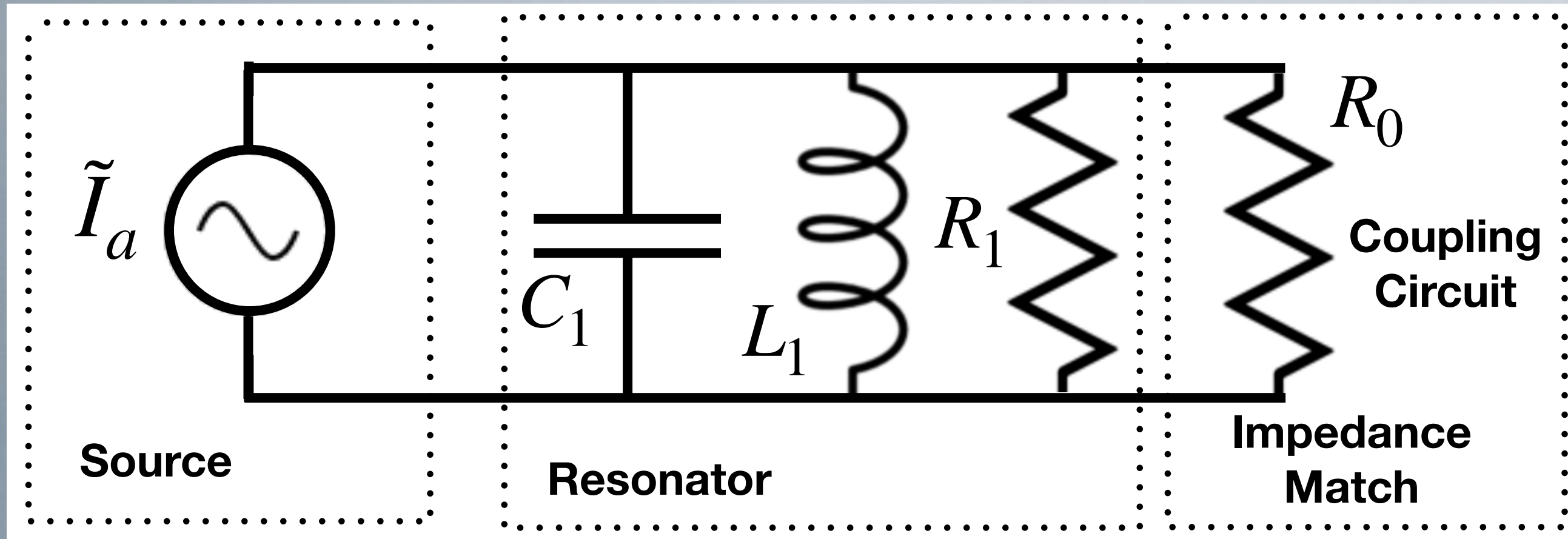


V-I Phase Relationship and Vector Diagram

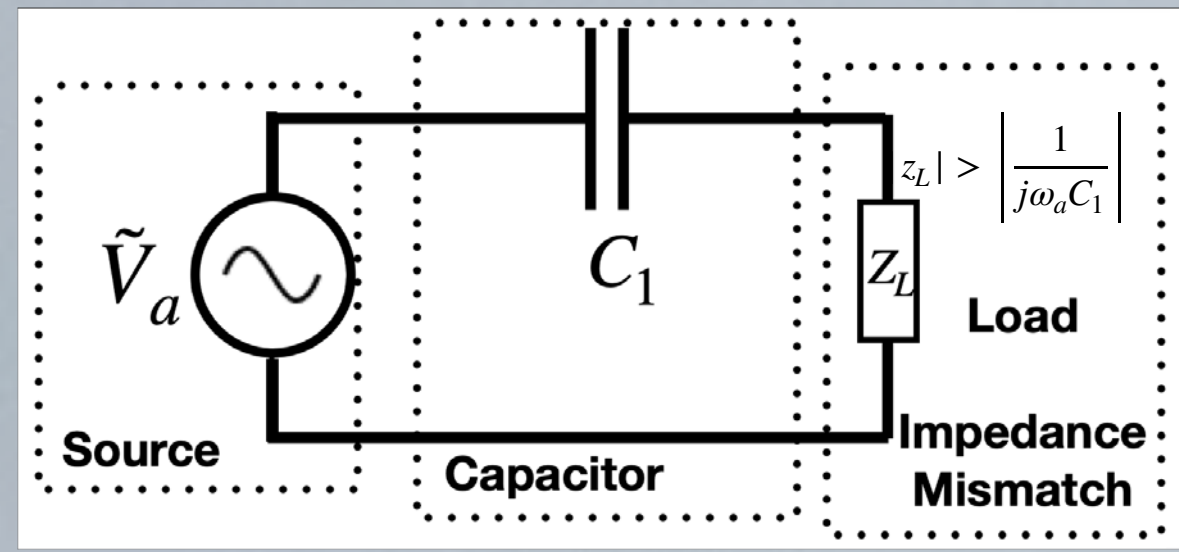
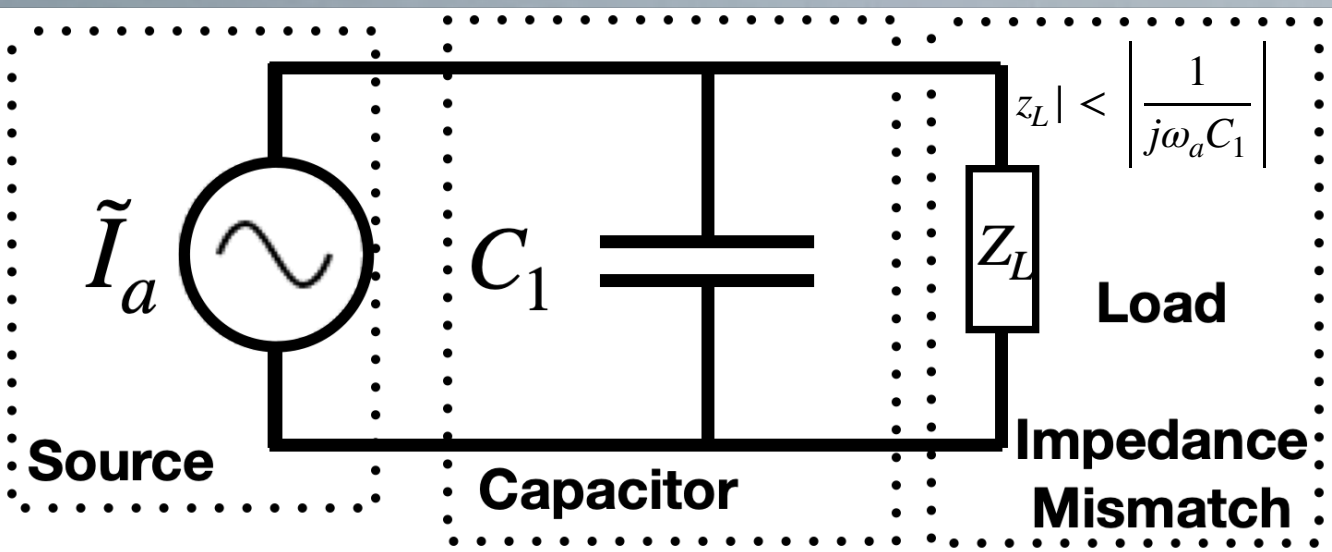


Real Power Measurement, Absorbs Energy:  $P_a = I_0^2 R_o = \frac{V_0^2}{R_0}$

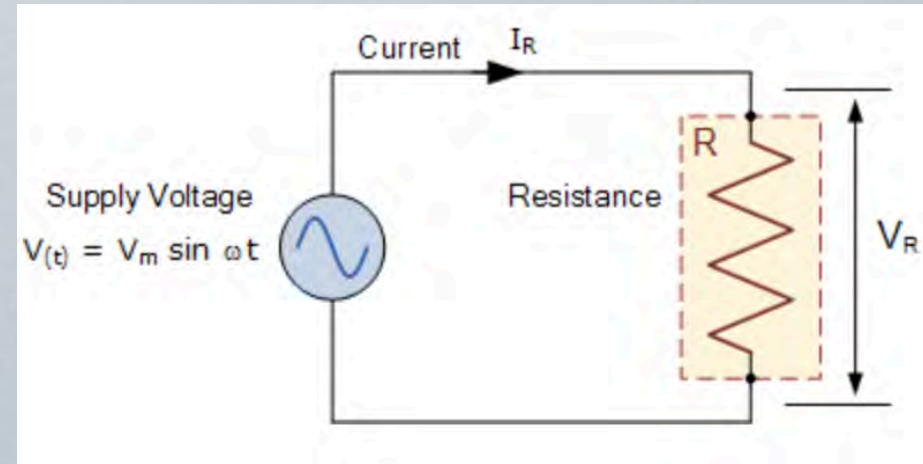
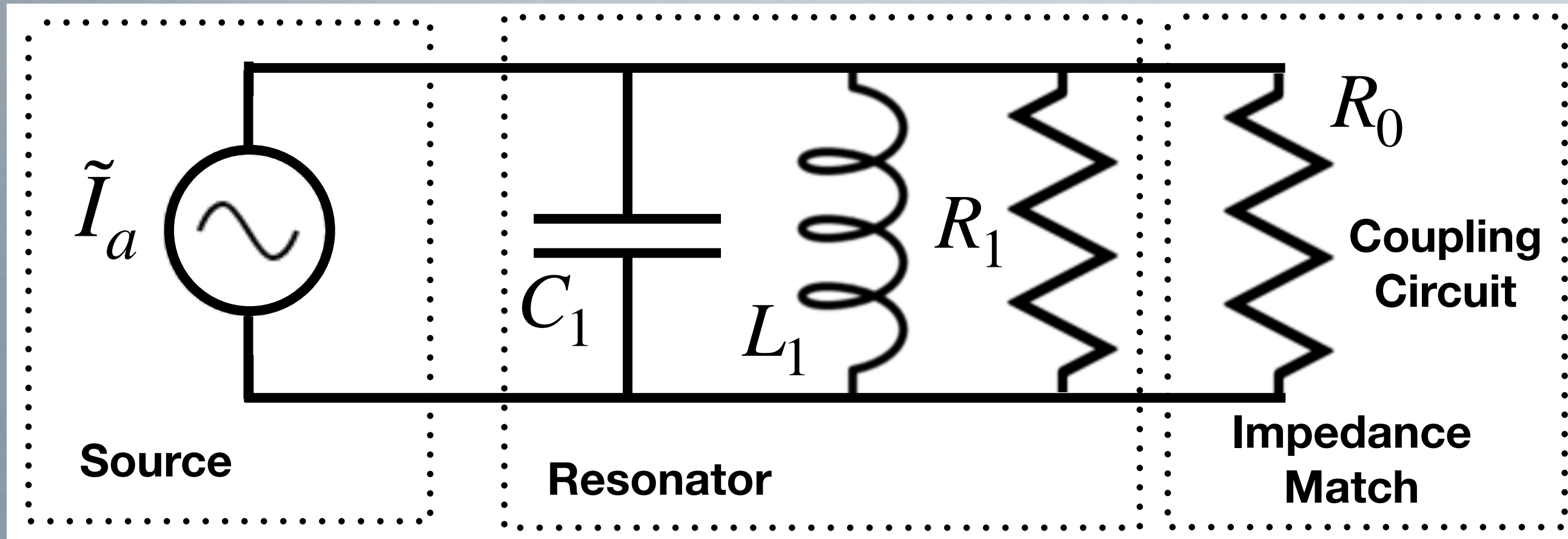
# Resonator Measurement: Impedance match; set coupling = 1; Take Photons from Source



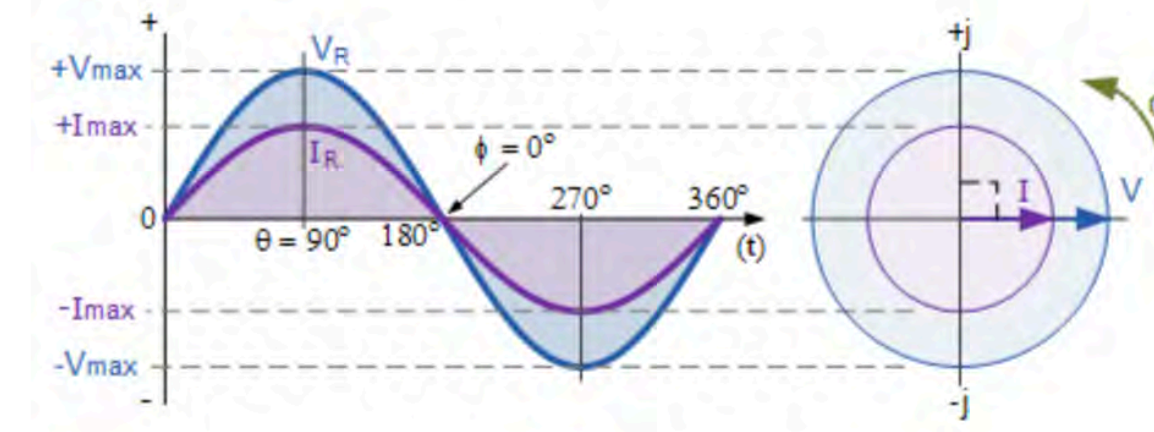
**Real Power Measurement, Absorbs Energy:**  $P_a = I_0^2 R_o = \frac{V_0^2}{R_0}$



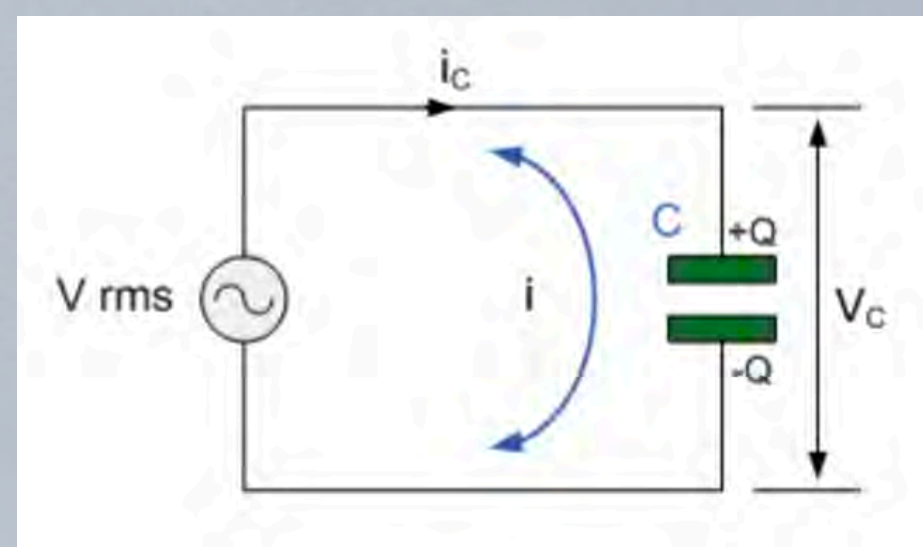
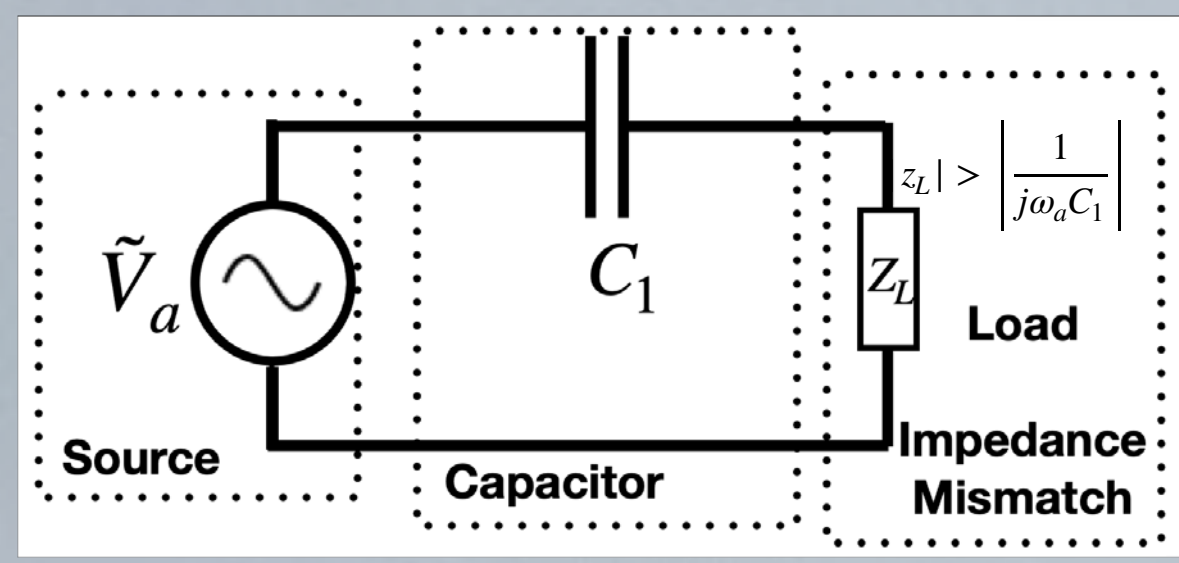
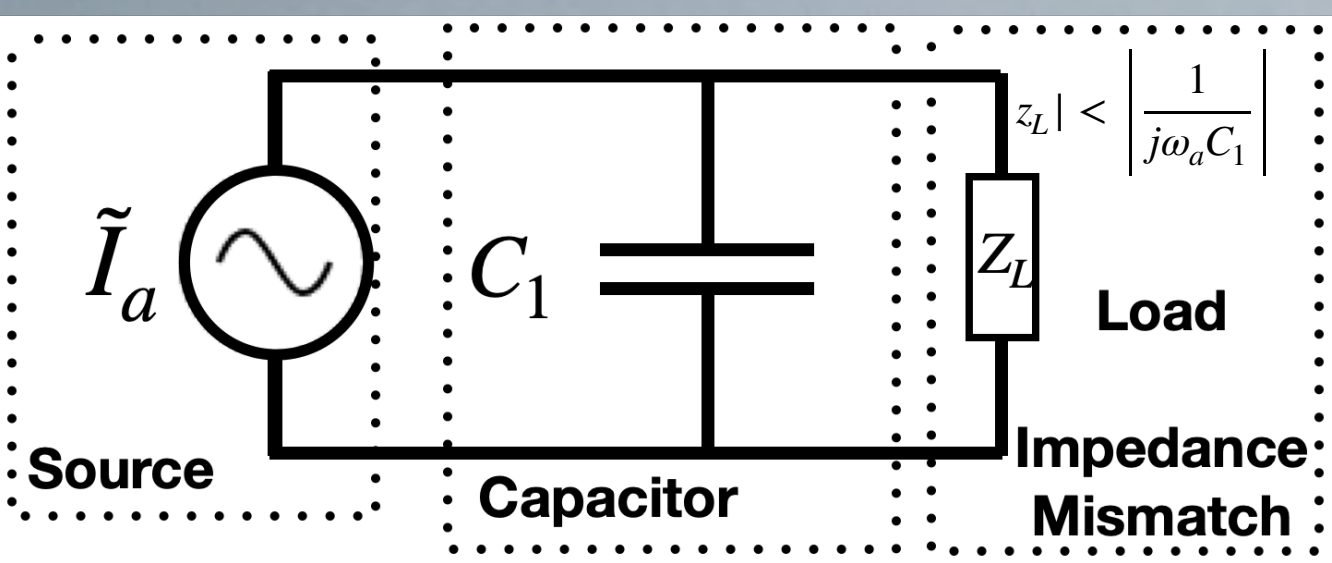
# Resonator Measurement: Impedance match; set coupling =1; Take Photons from Source



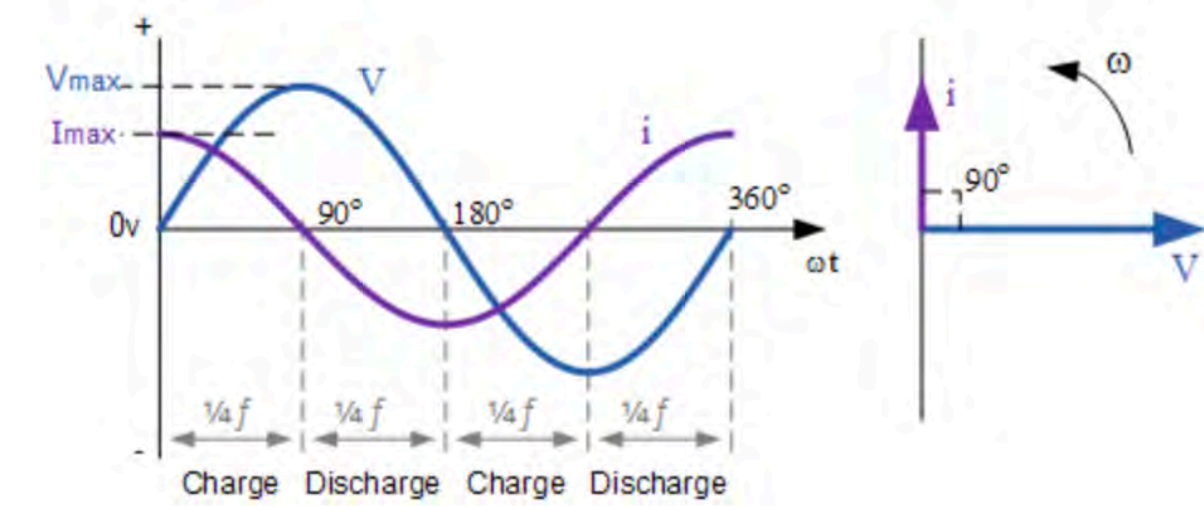
V-I Phase Relationship and Vector Diagram



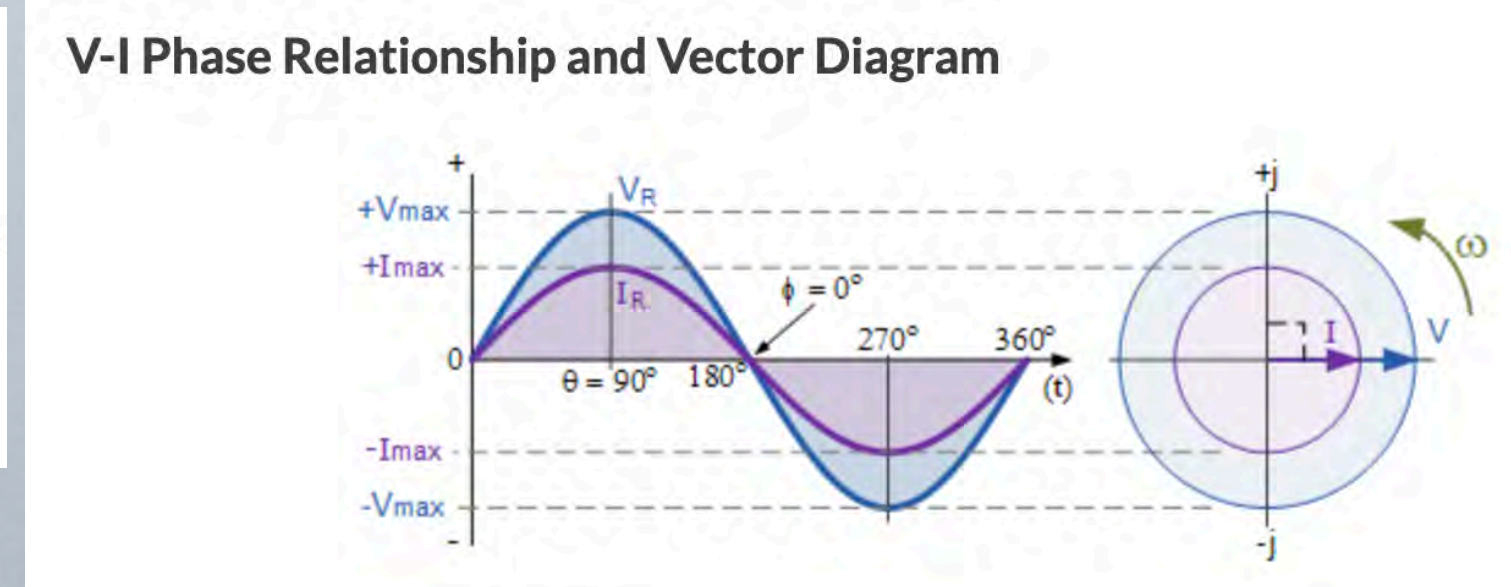
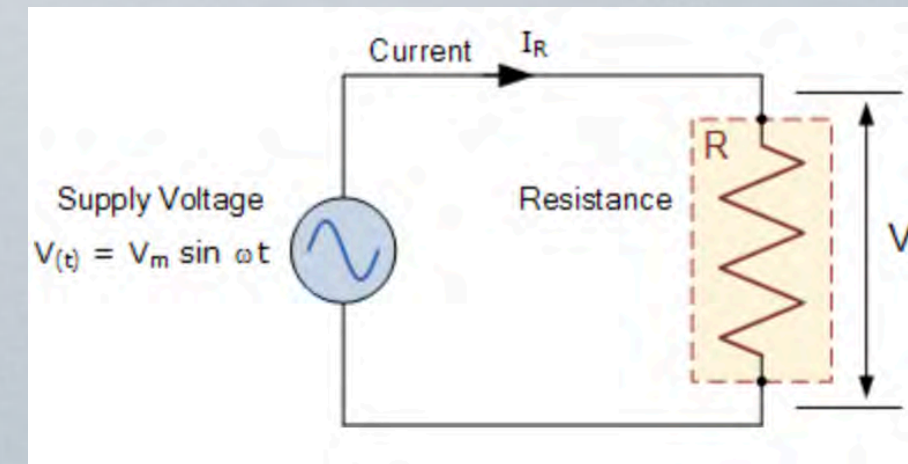
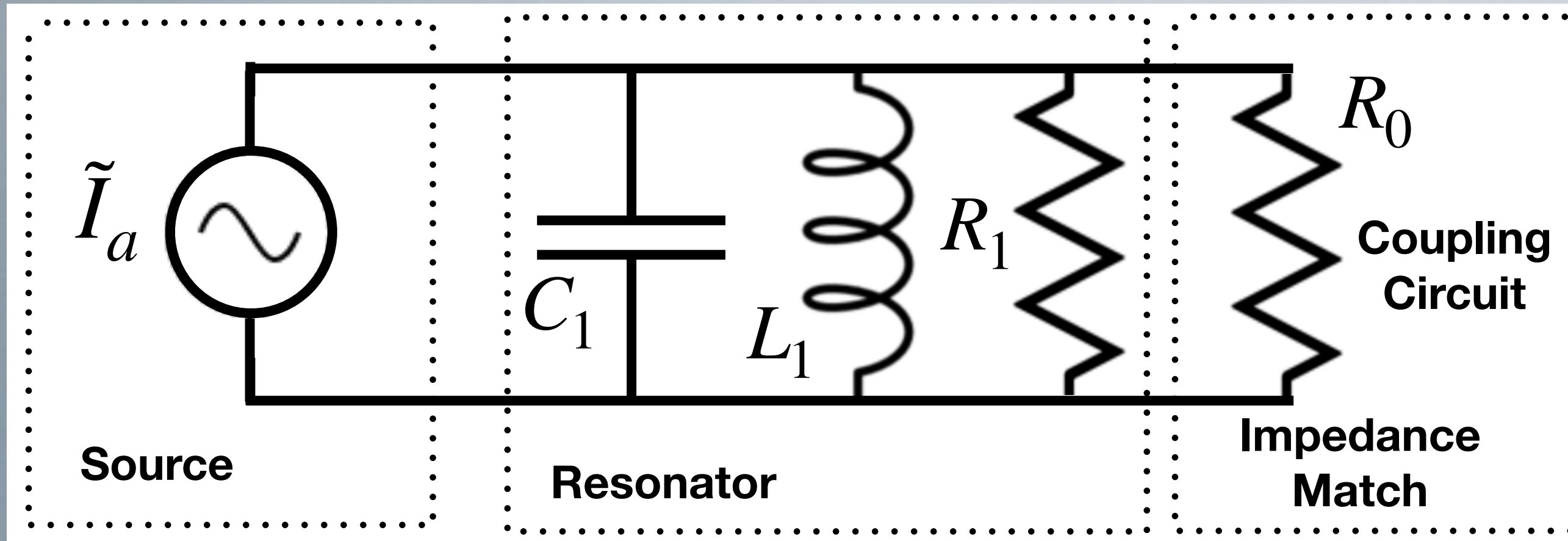
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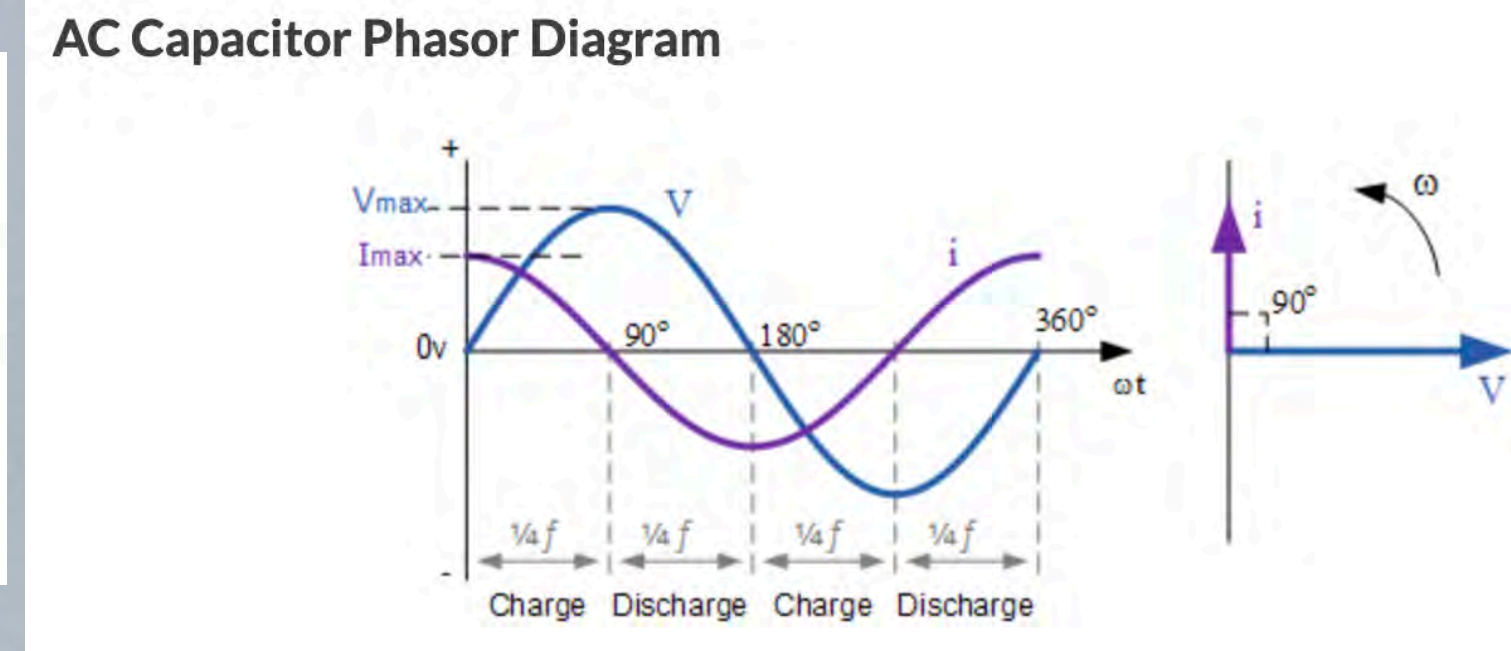
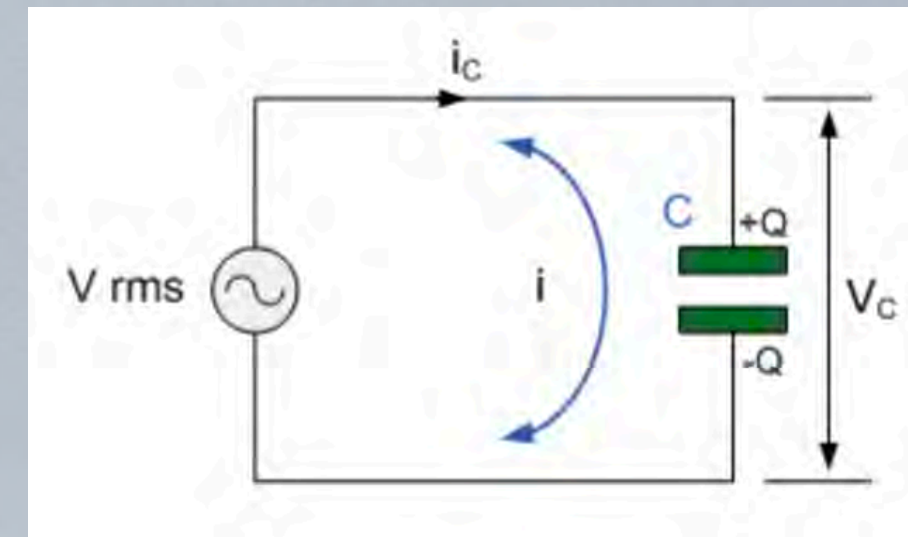
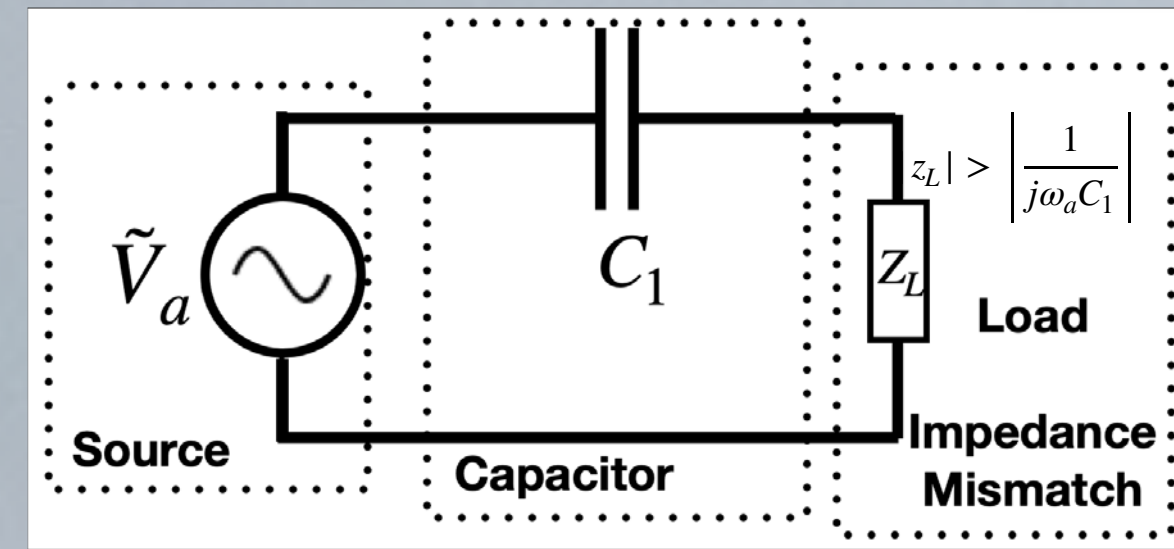
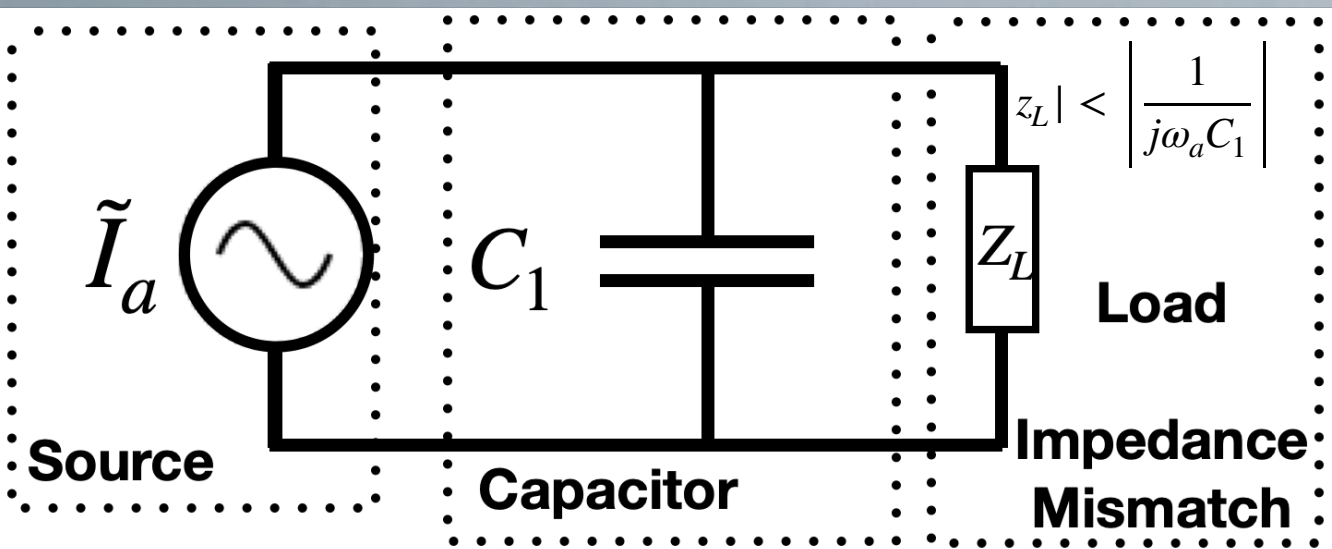
AC Capacitor Phasor Diagram



# Resonator Measurement: Impedance match; set coupling =1; Take Photons from Source

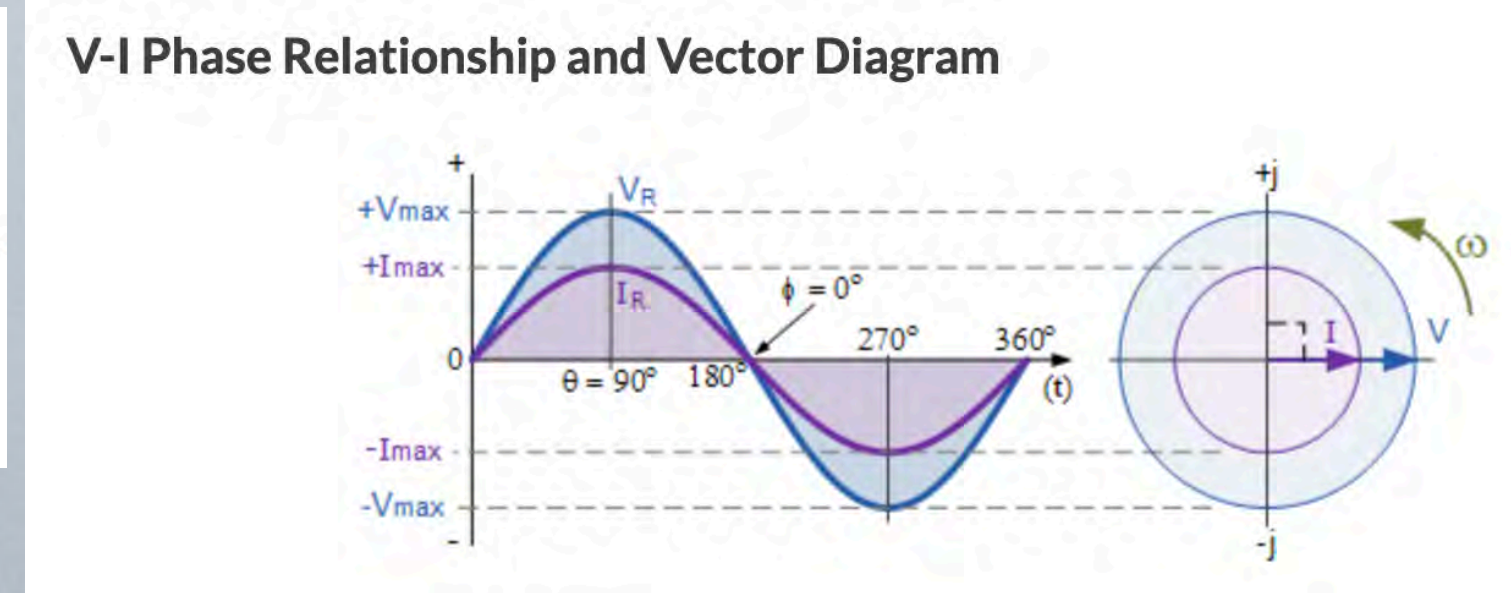
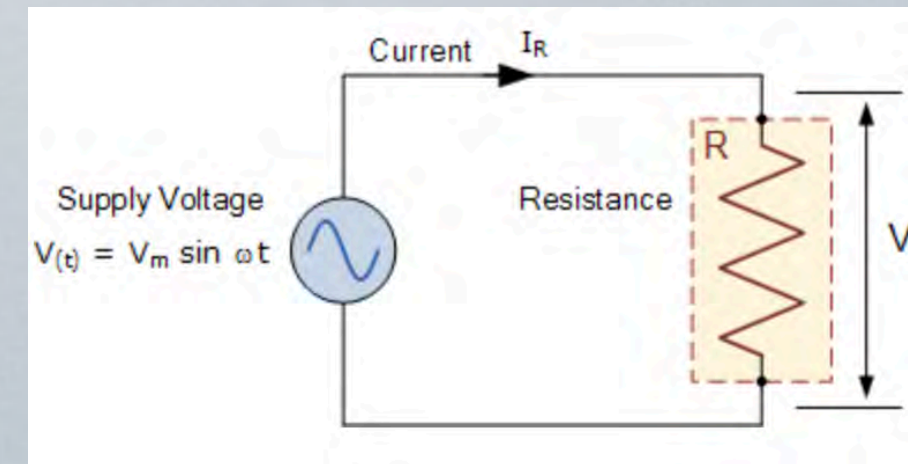
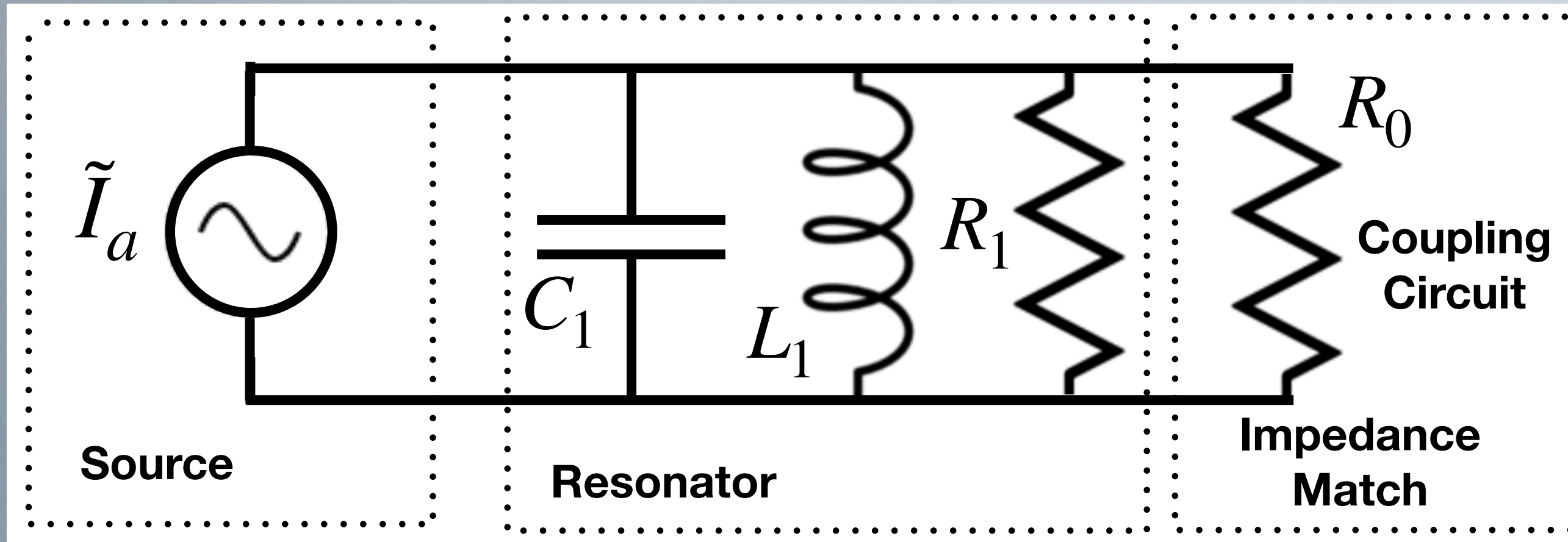


**Real Power Measurement, Absorbs Energy:**  $P_a = I_0^2 R_o = \frac{V_0^2}{R_0}$

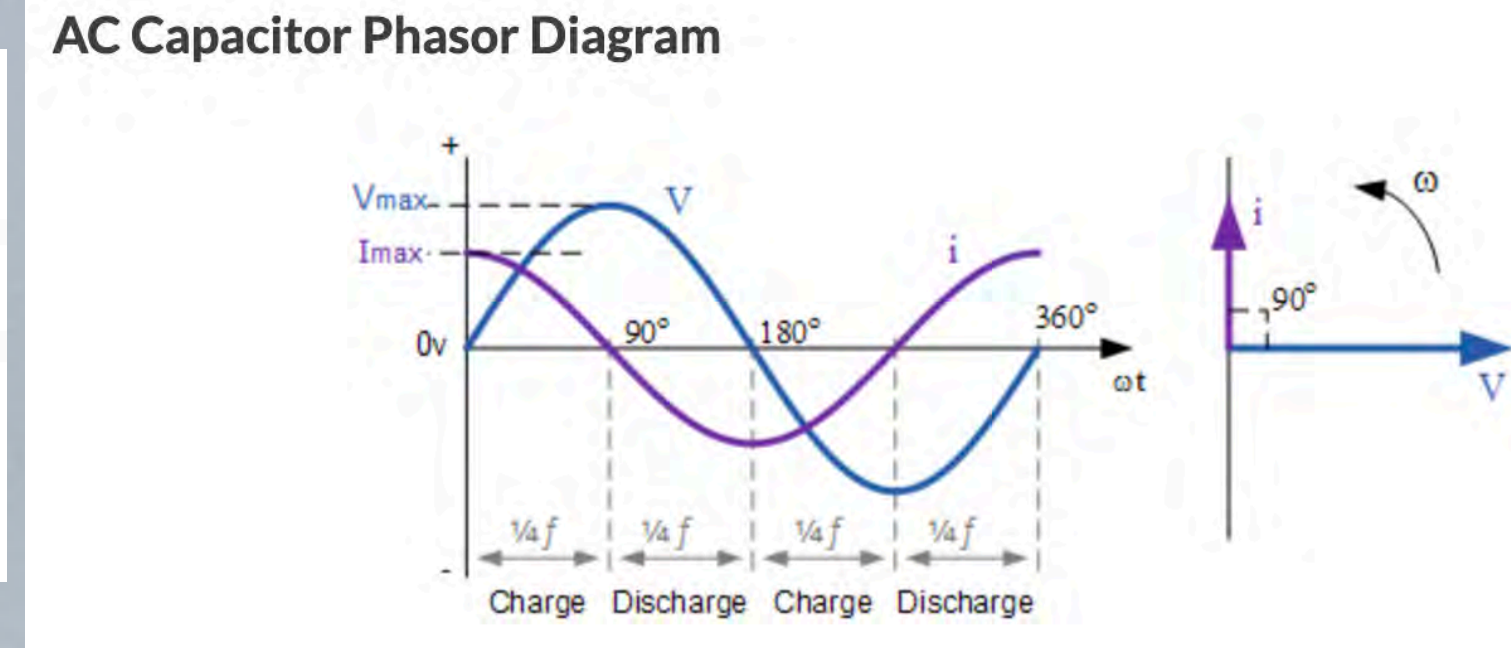
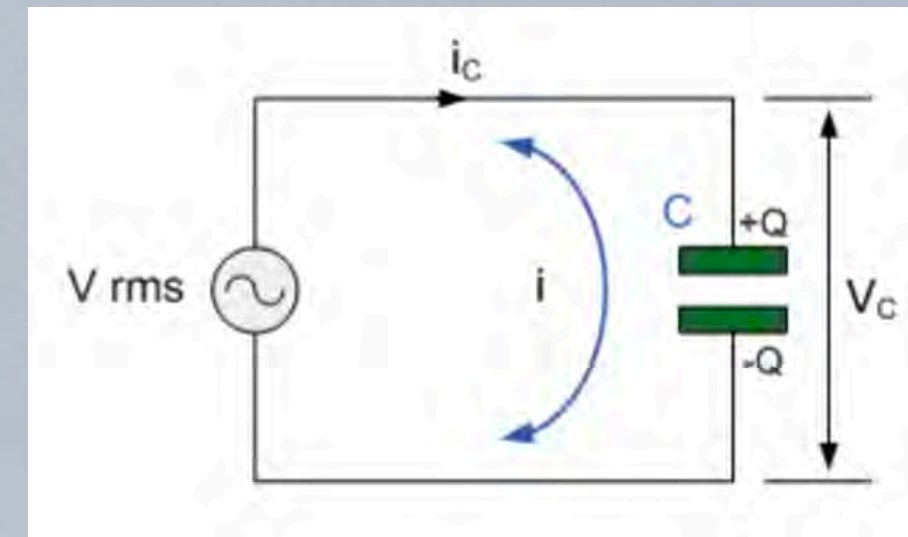
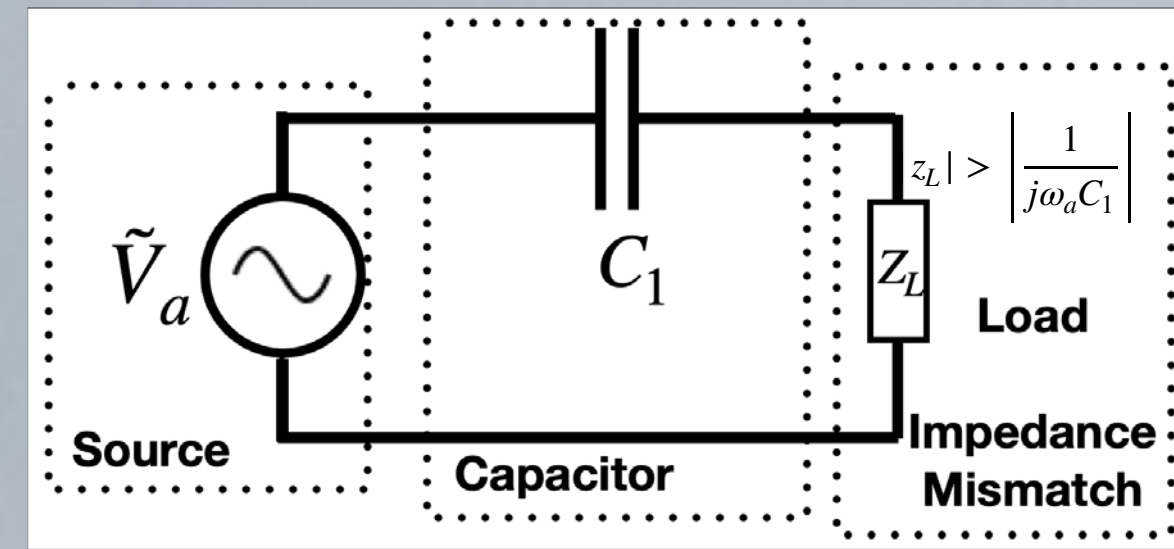
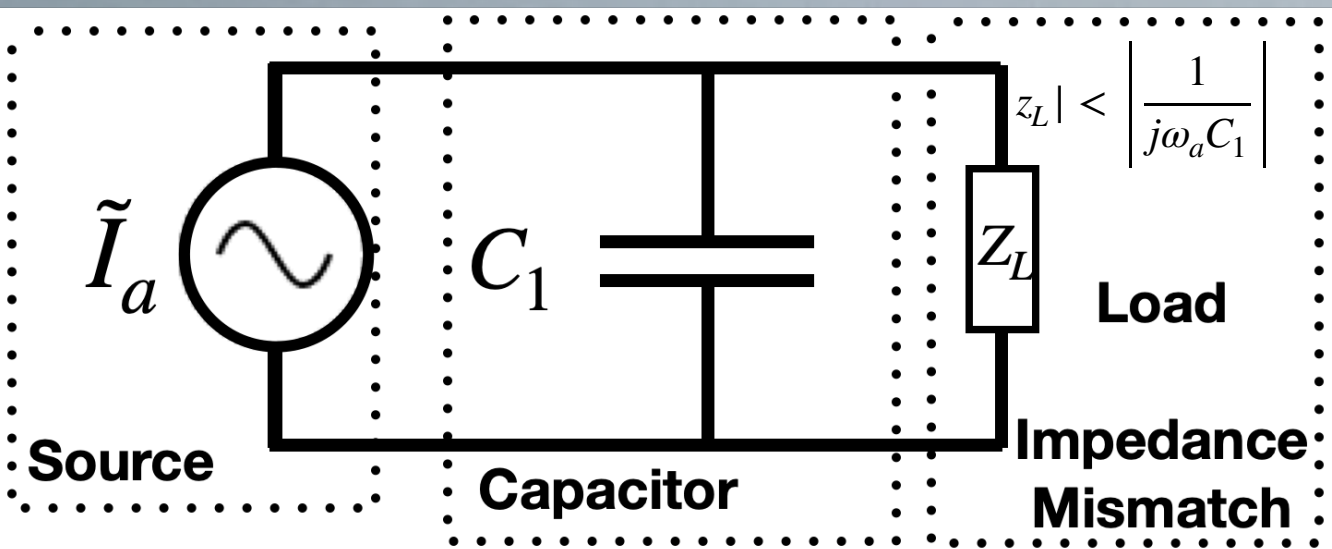


**Reactive Power Measurement, Does Not Absorb Energy:**

# Resonator Measurement: Impedance match; set coupling =1; Take Photons from Source



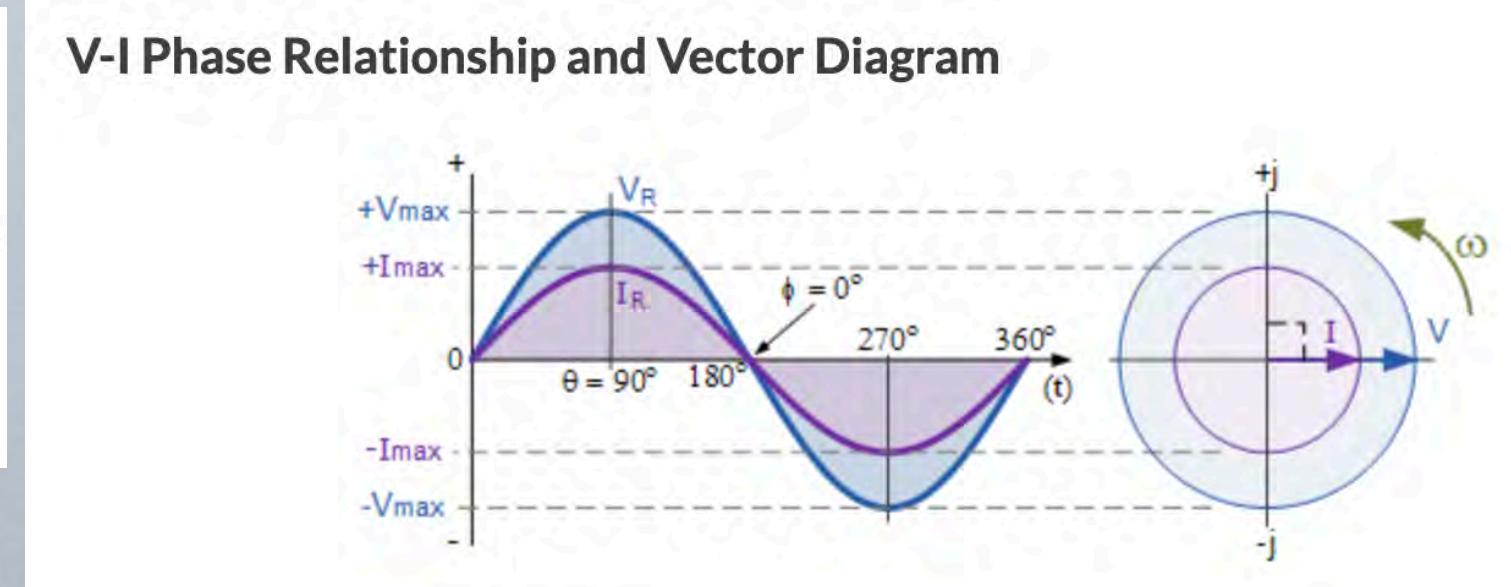
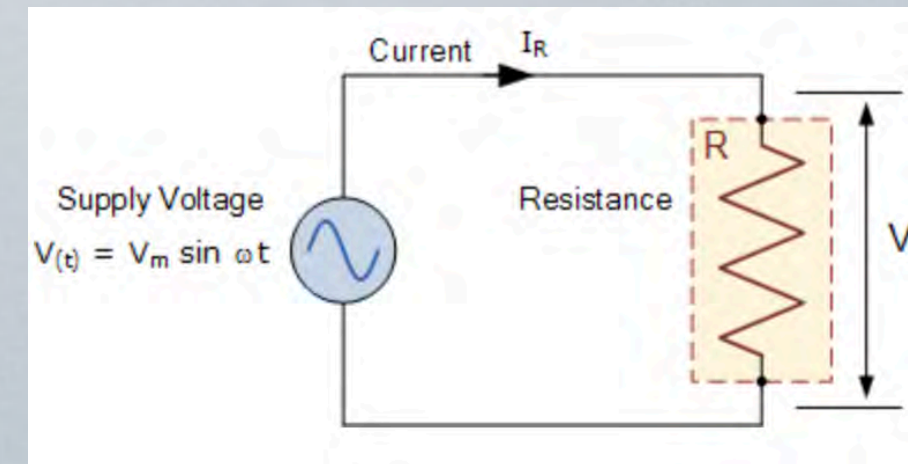
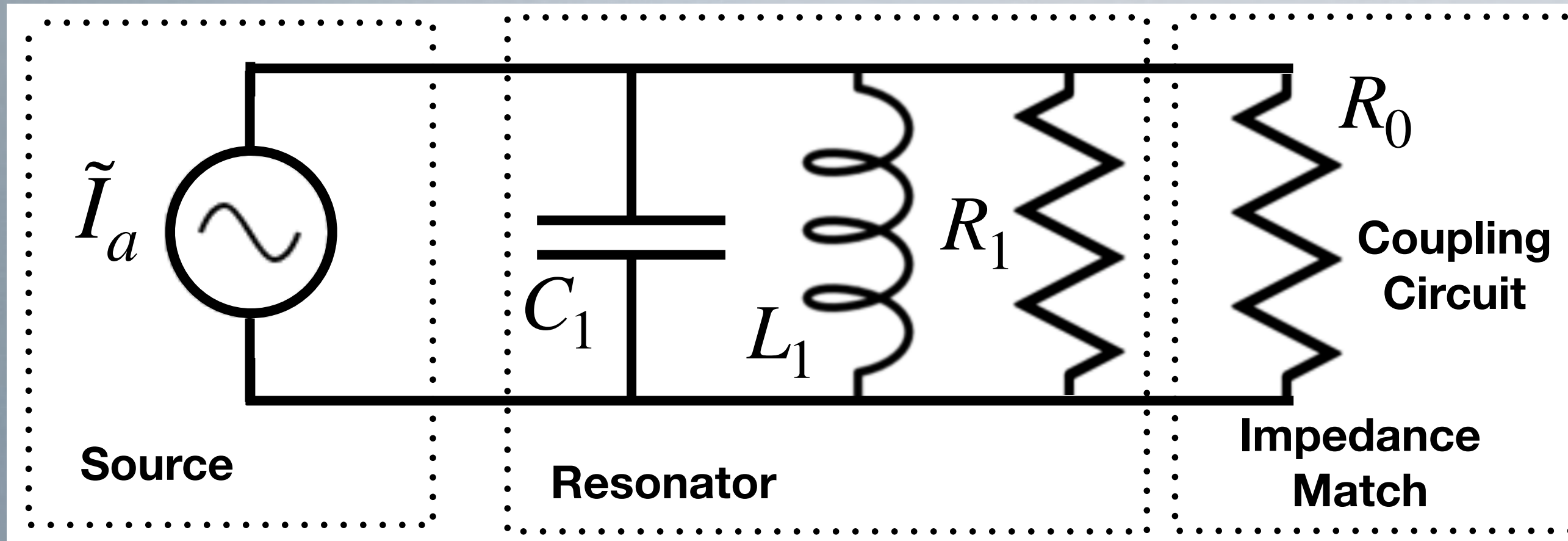
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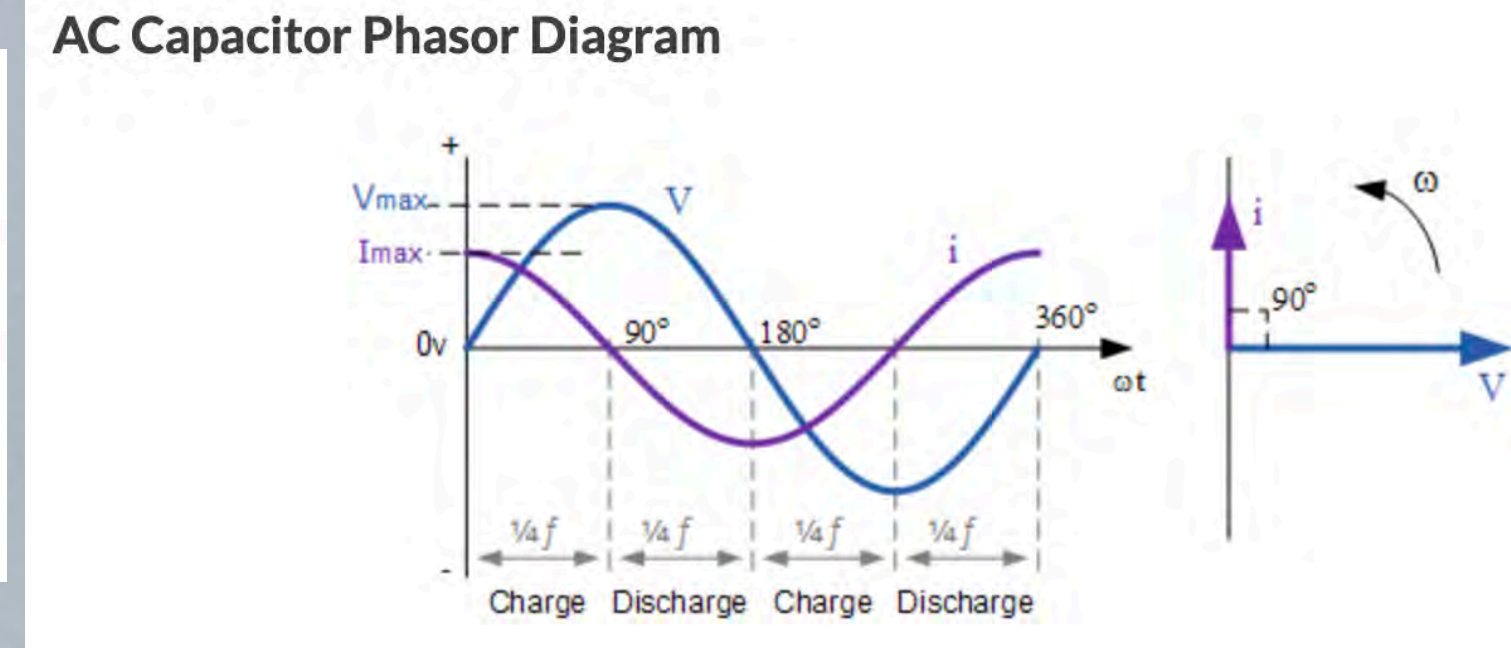
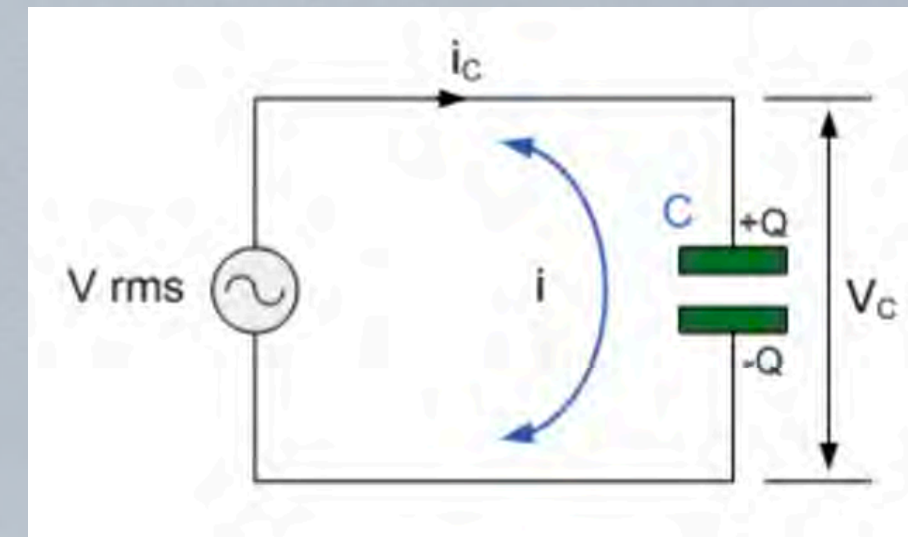
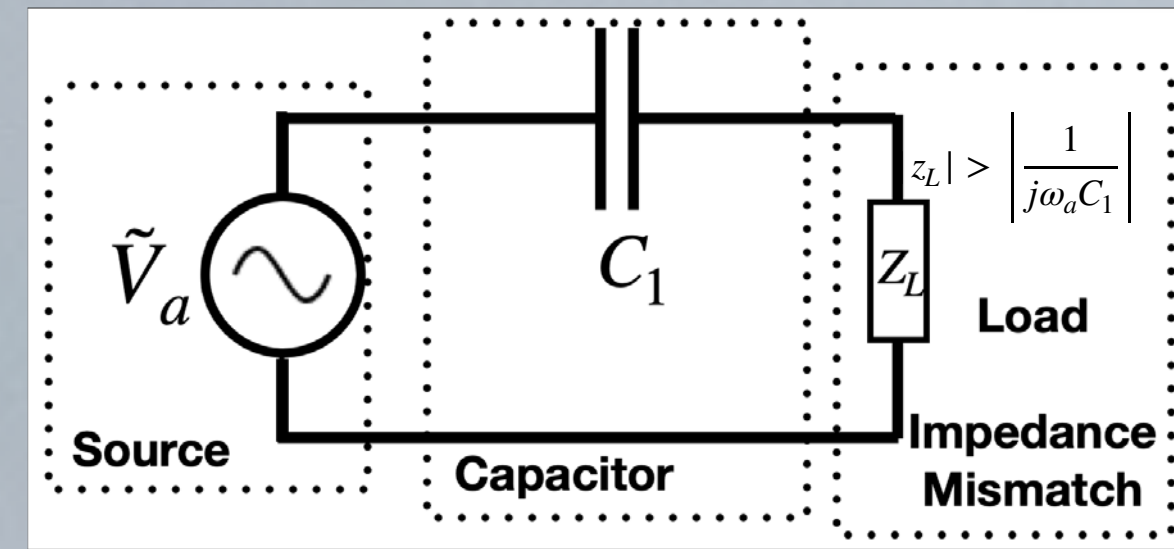
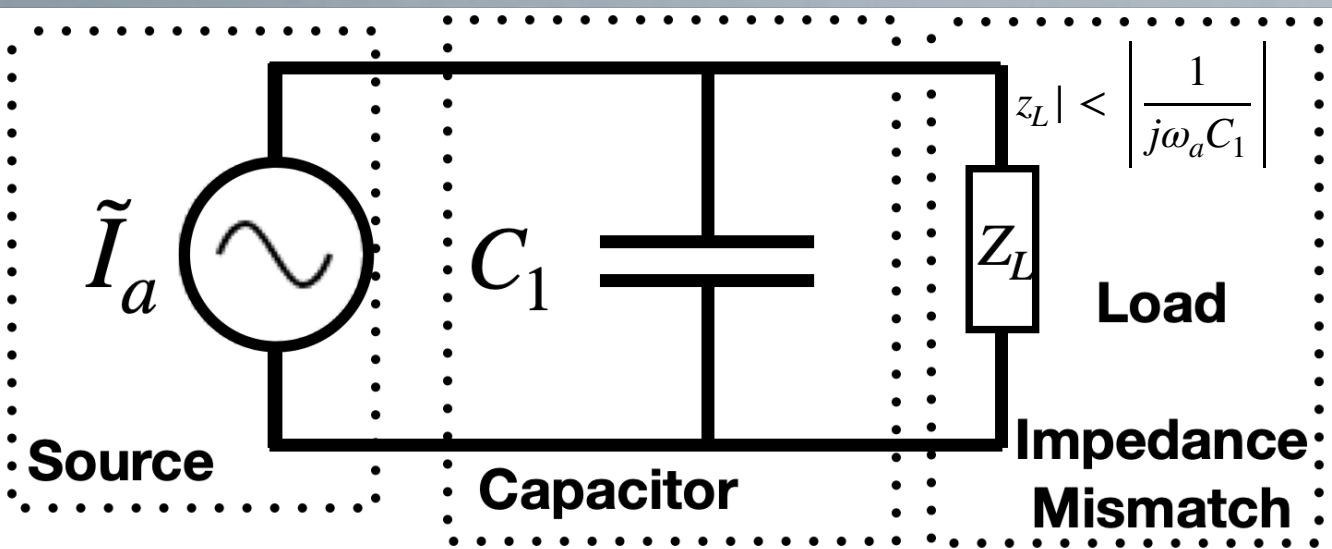
**Reactive Power Measurement, Does Not Absorb Energy:**

Left eg. Inductive couple SQUID Amplifier (Current of Mag Flux)

# Resonator Measurement: Impedance match; set coupling =1; Take Photons from Source



**Real Power Measurement, Absorbs Energy:**  $P_a = I_0^2 R_o = \frac{V_0^2}{R_0}$

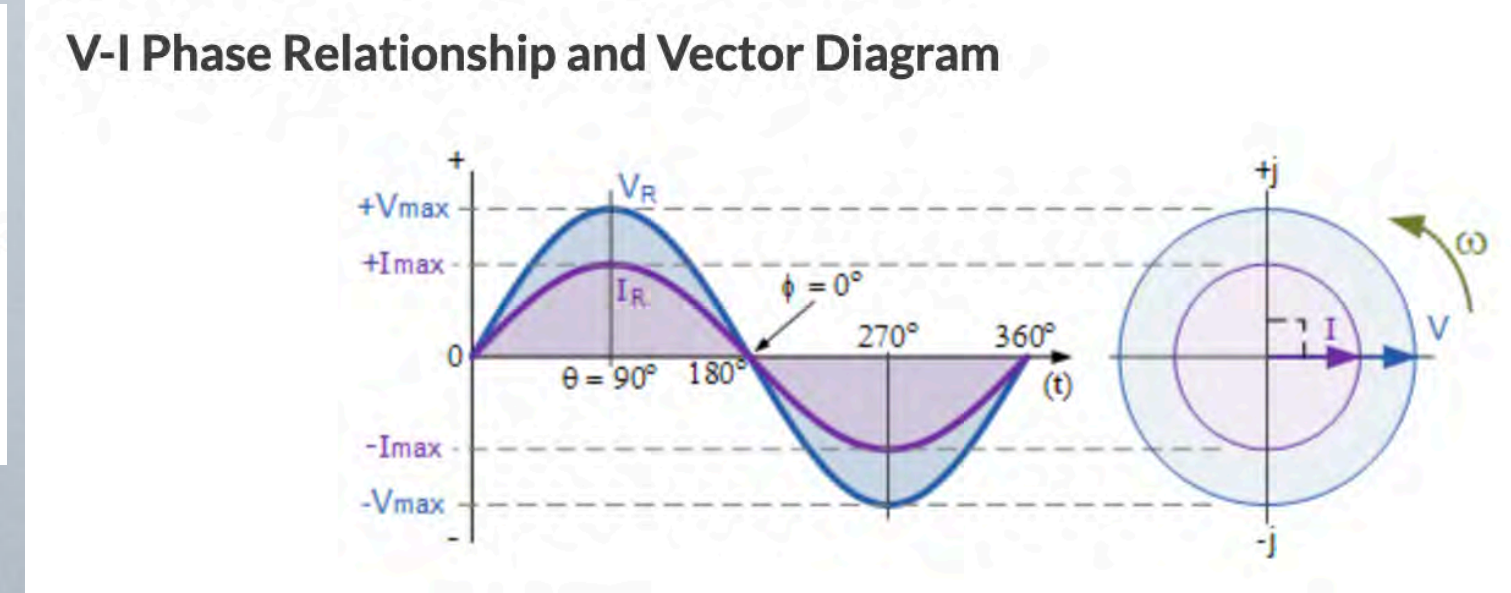
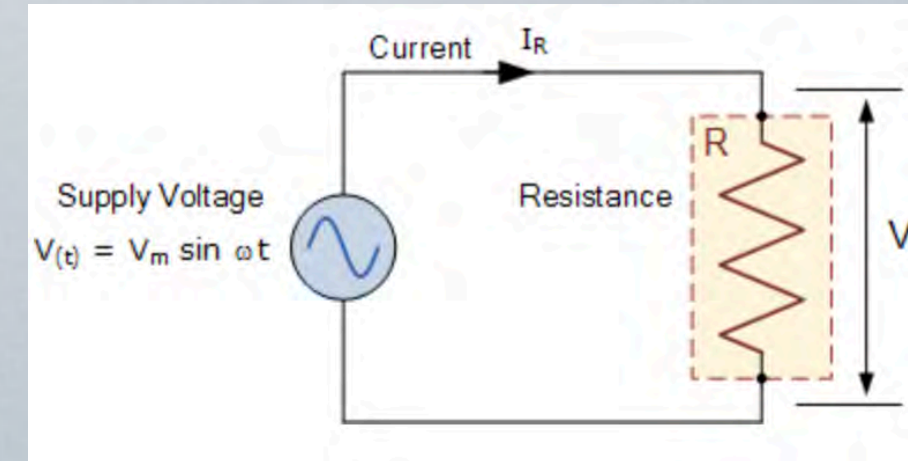
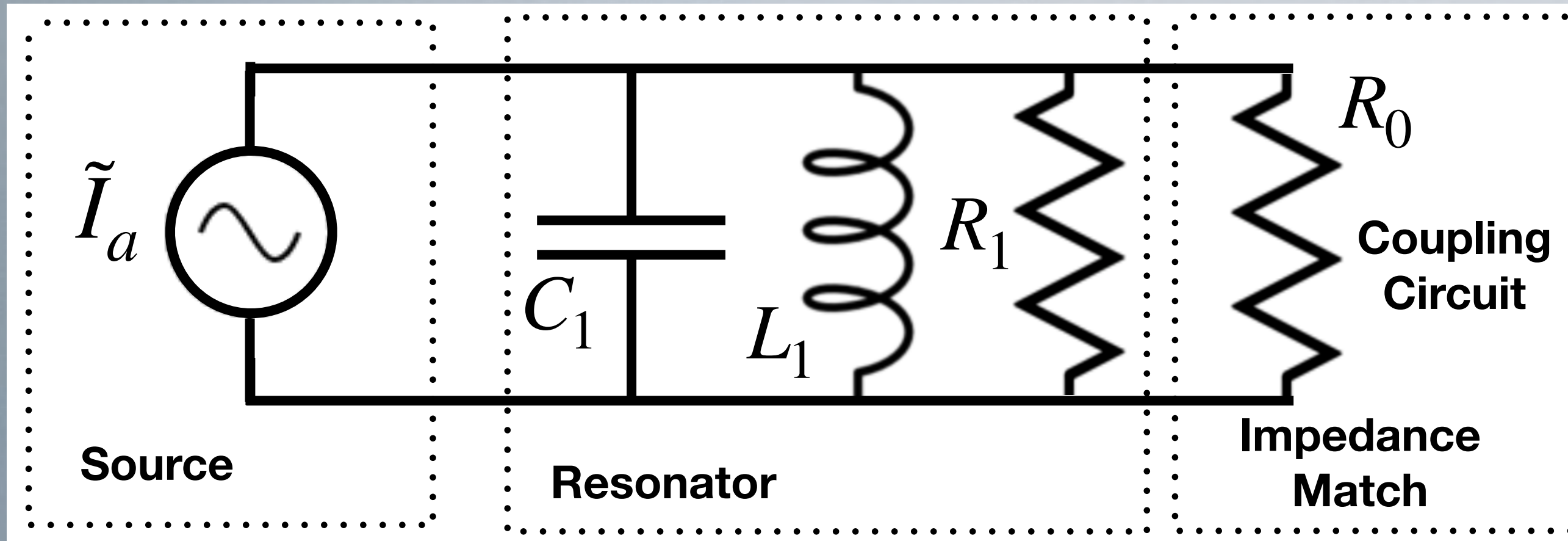


**Reactive Power Measurement, Does Not Absorb Energy:**

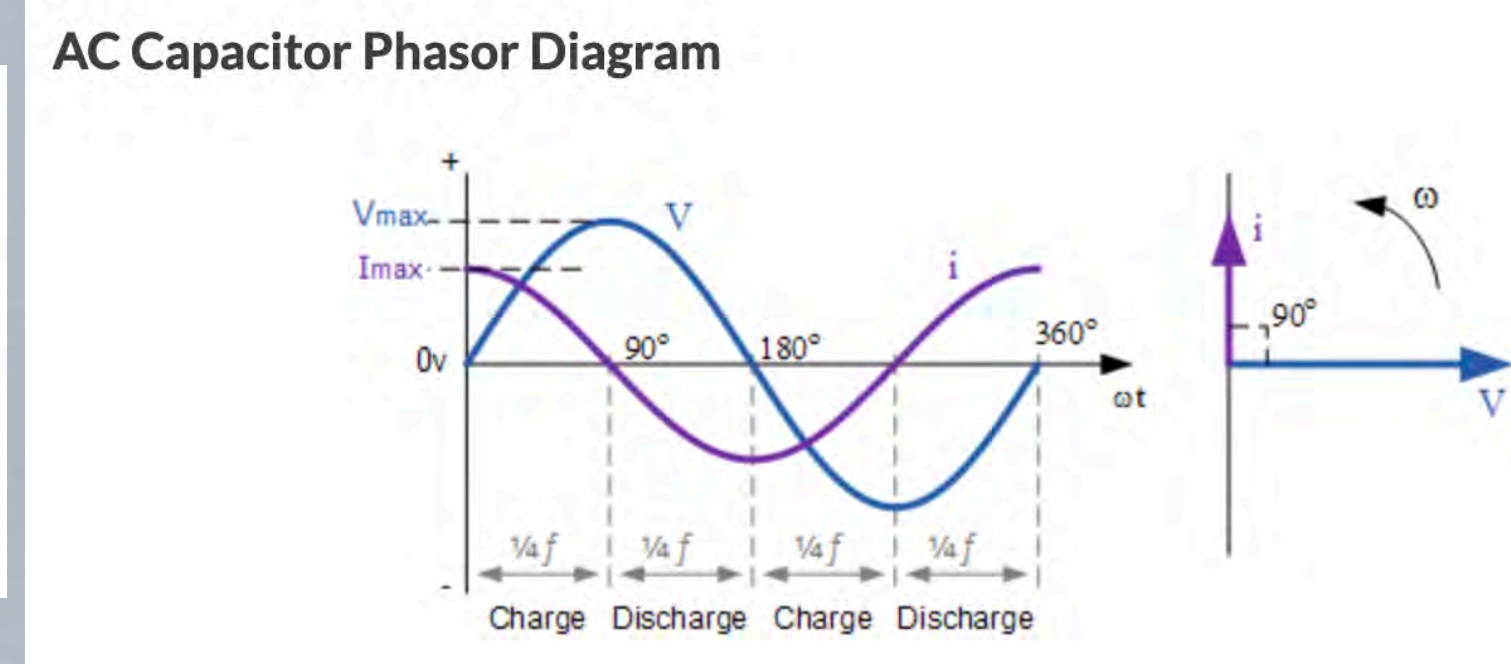
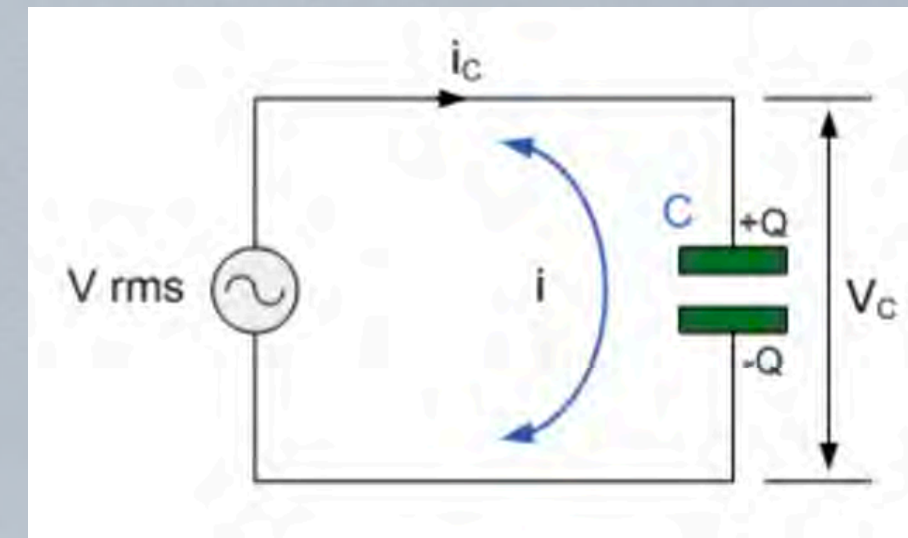
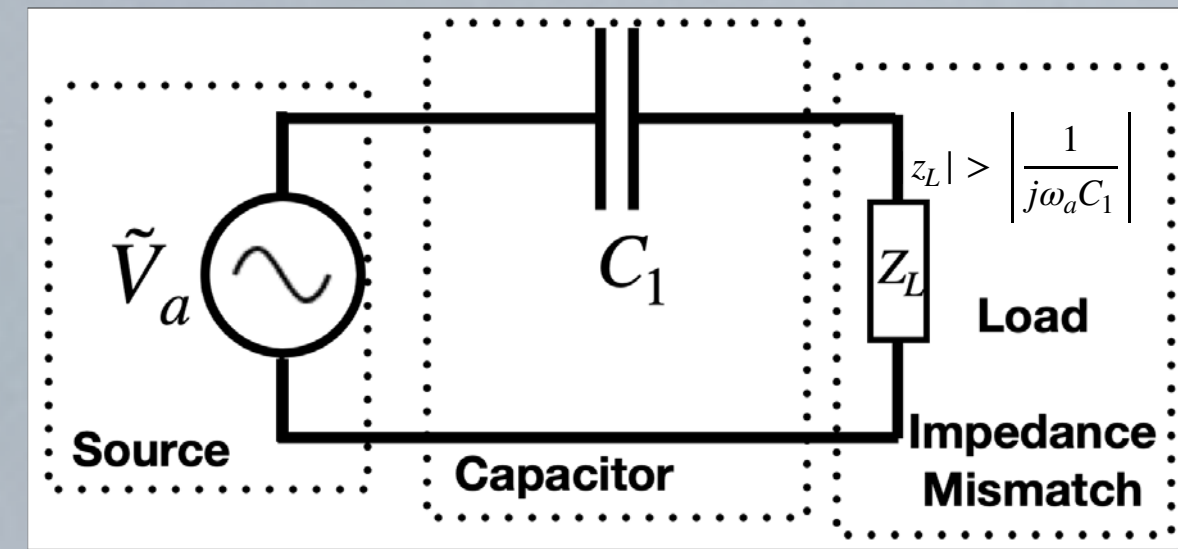
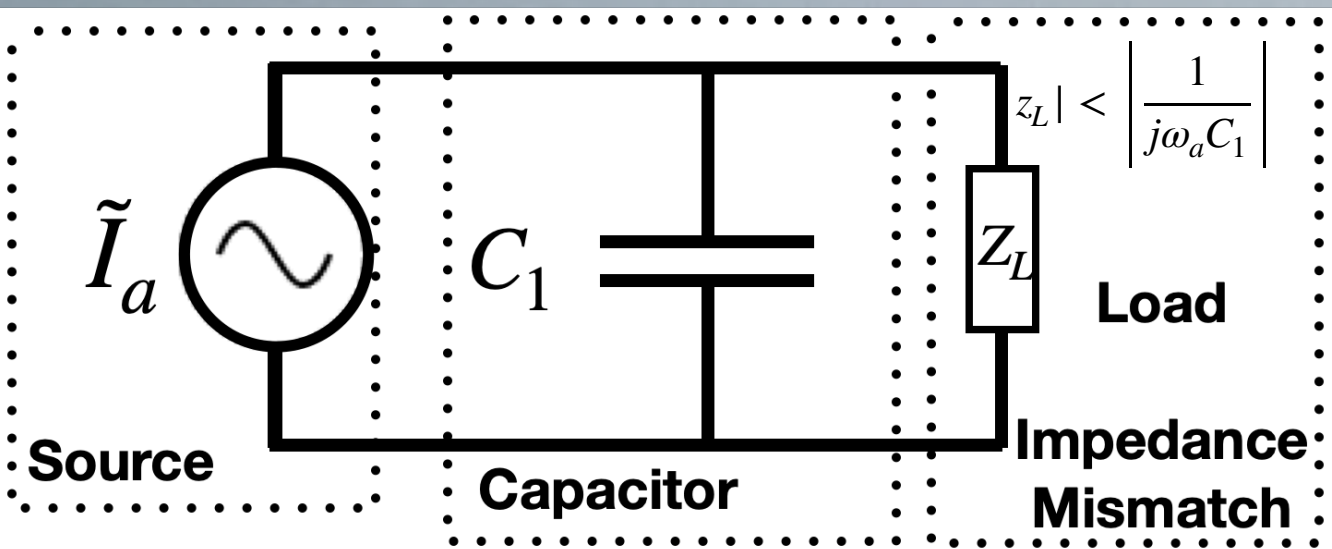
Left eg. Inductive couple SQUID Amplifier (Current of Mag Flux)

Right eg. Capacitive coupled High Impedance Amplifier (Voltage)

# Resonator Measurement: Impedance match; set coupling =1; Take Photons from Source



**Real Power Measurement, Absorbs Energy:**  $P_a = I_0^2 R_o = \frac{V_0^2}{R_0}$



**Reactive Power Measurement, Does Not Absorb Energy:**

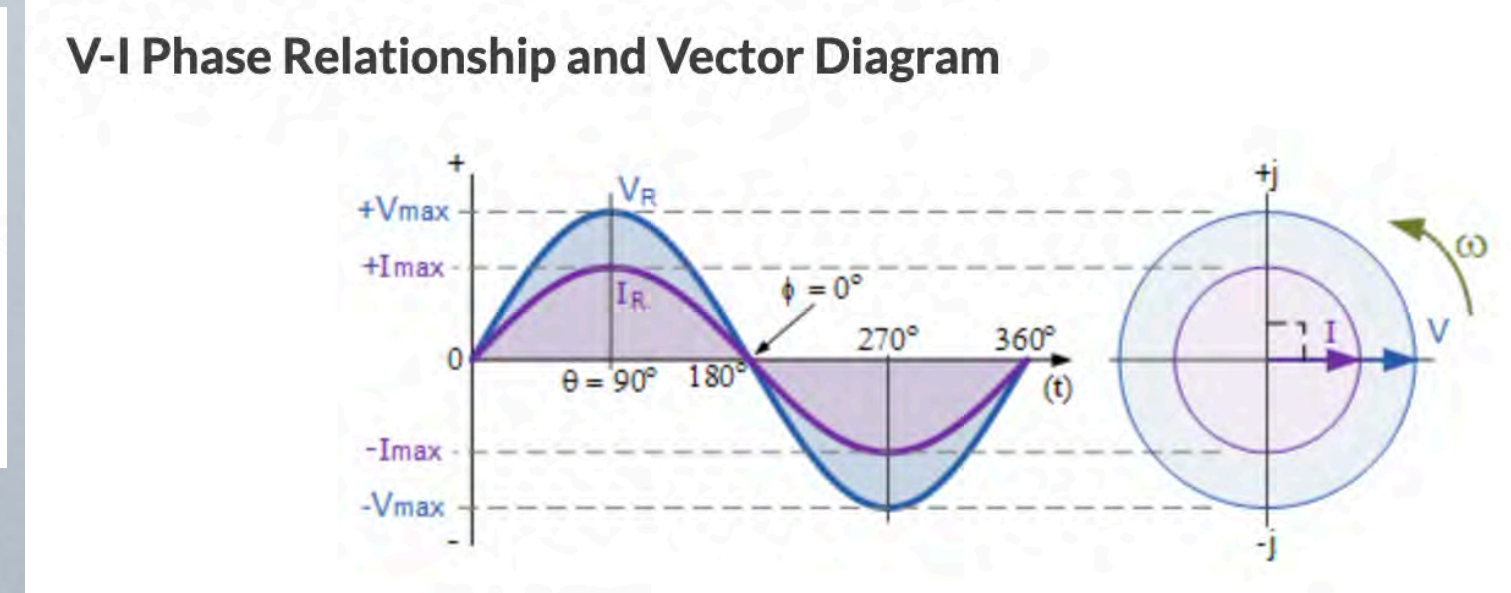
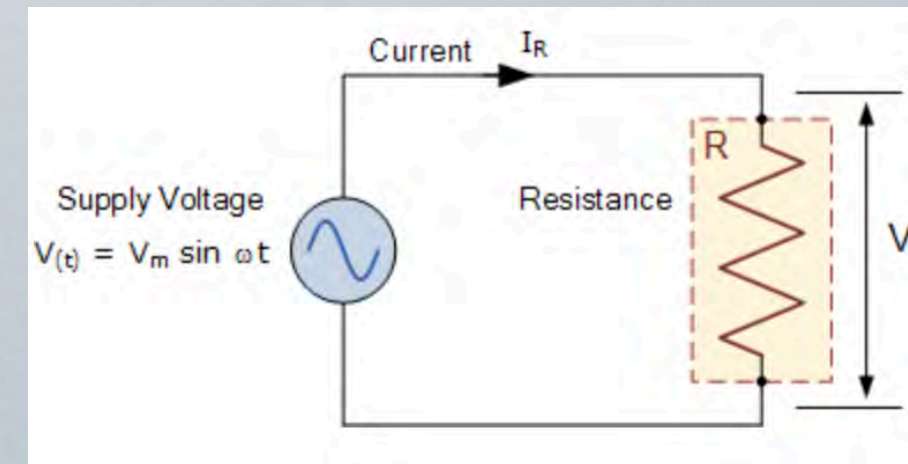
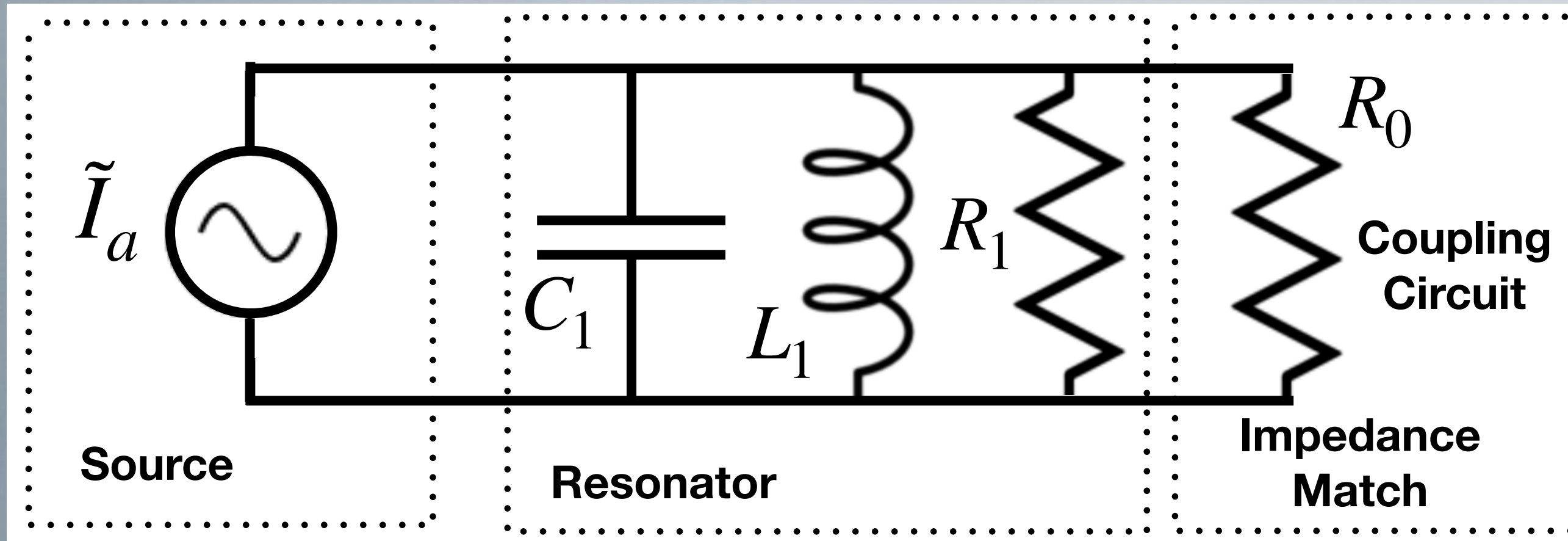
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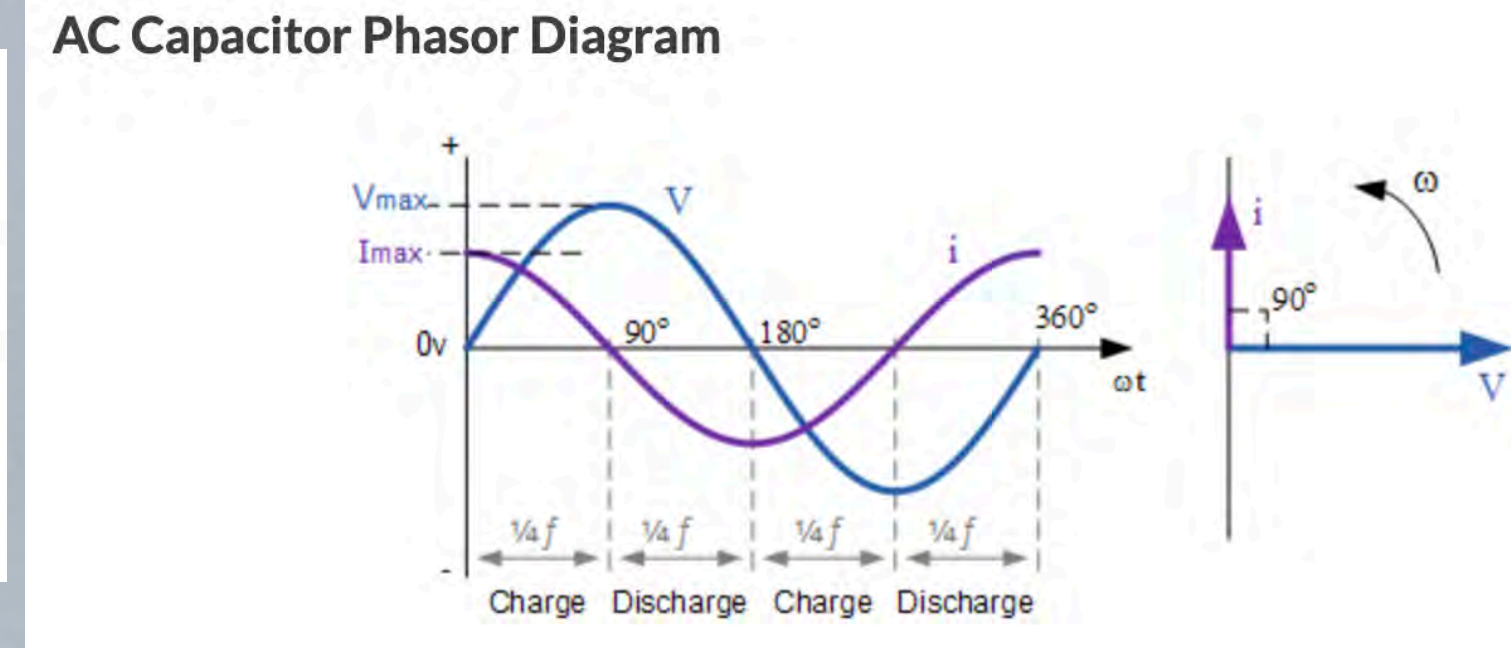
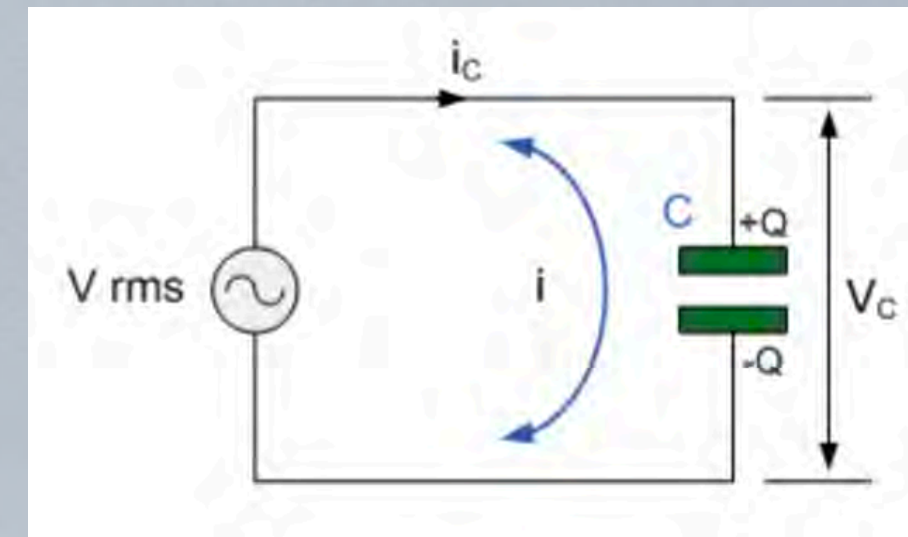
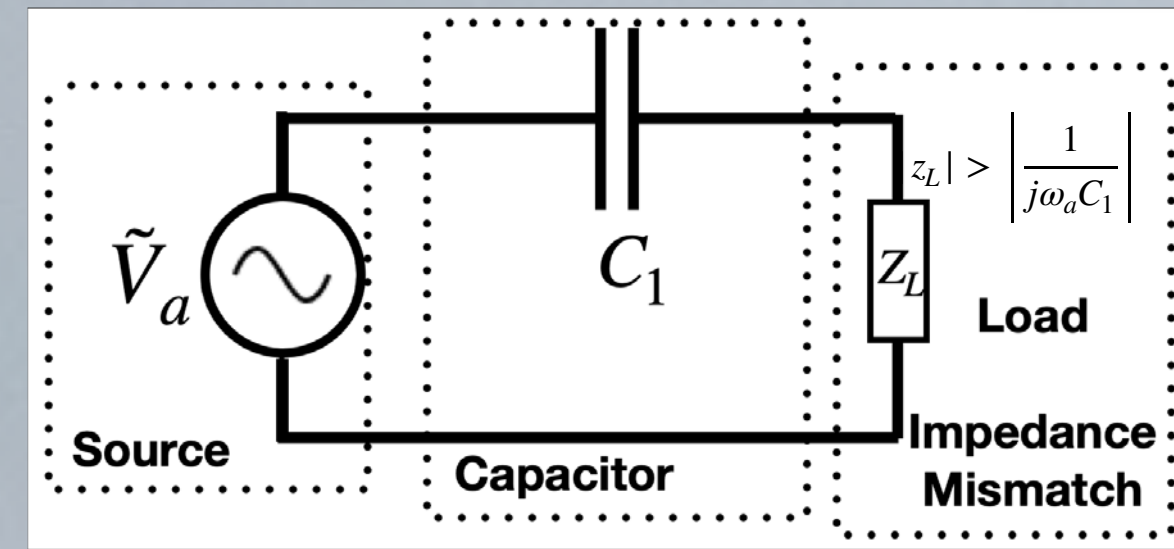
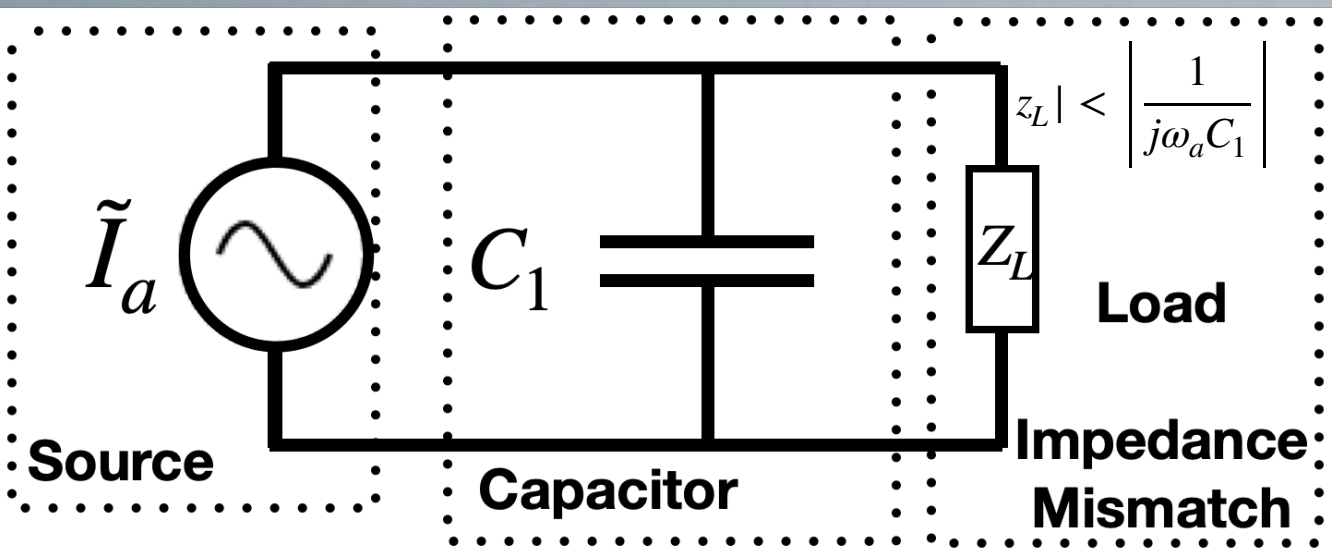
**Energy oscillates between Source and Capacitor**



# Resonator Measurement: Impedance match; set coupling =1; Take Photons from Source



**Real Power Measurement, Absorbs Energy:**  $P_a = I_0^2 R_o = \frac{V_0^2}{R_0}$



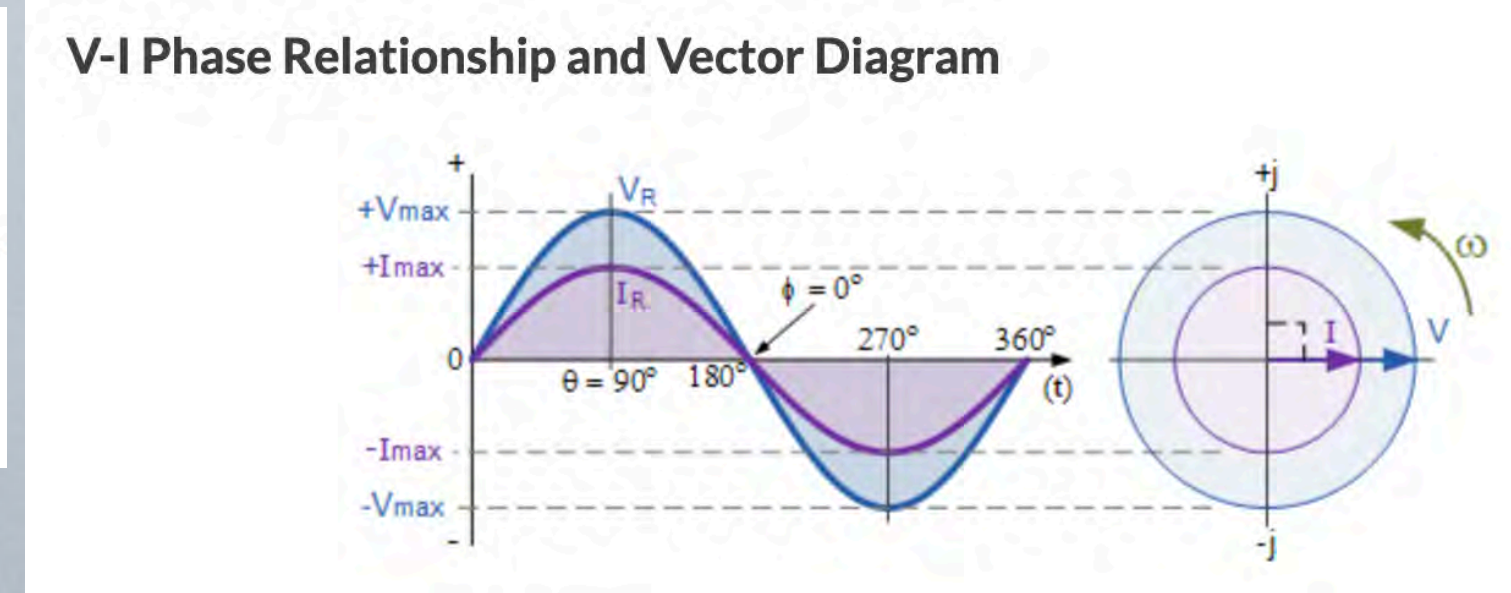
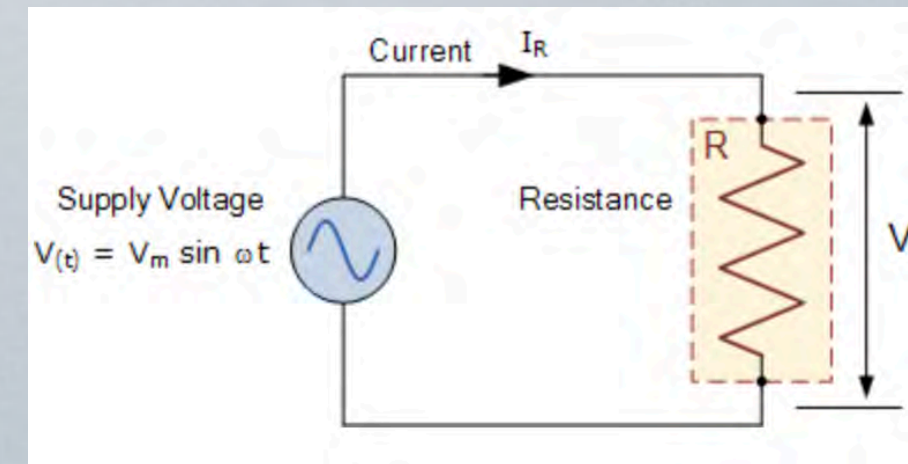
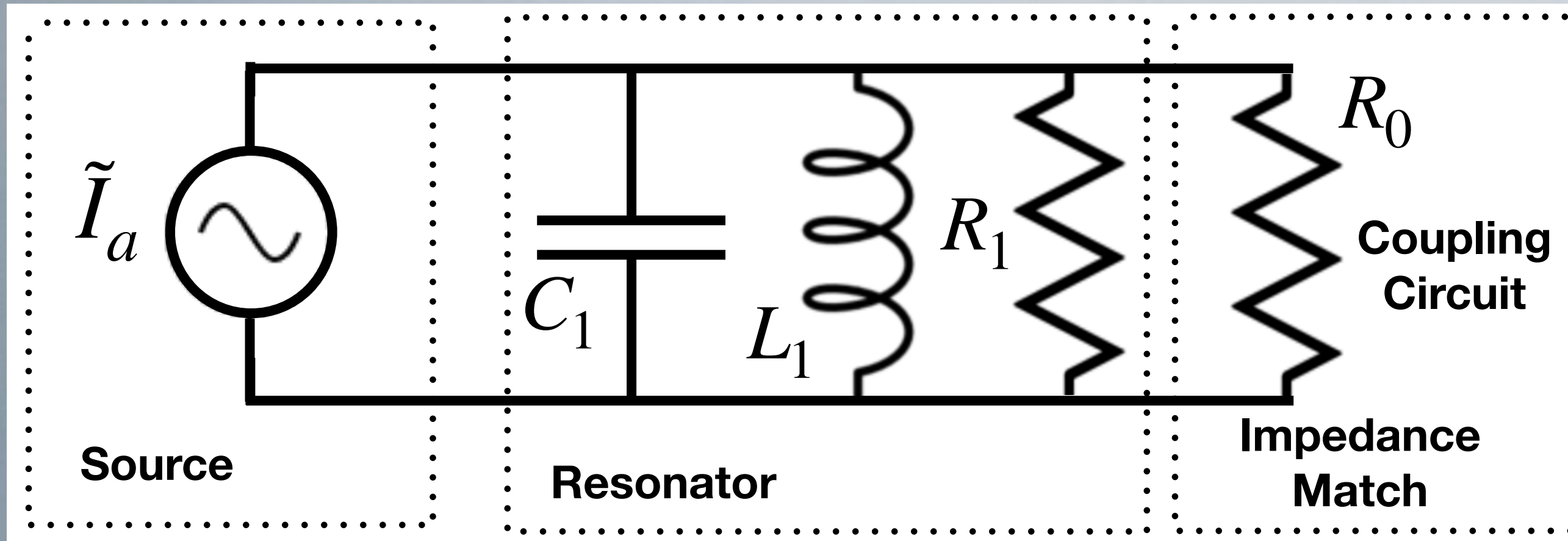
**Reactive Power Measurement, Does Not Absorb Energy:**

Left eg. Inductive couple SQUID Amplifier (Current of Mag Flux)

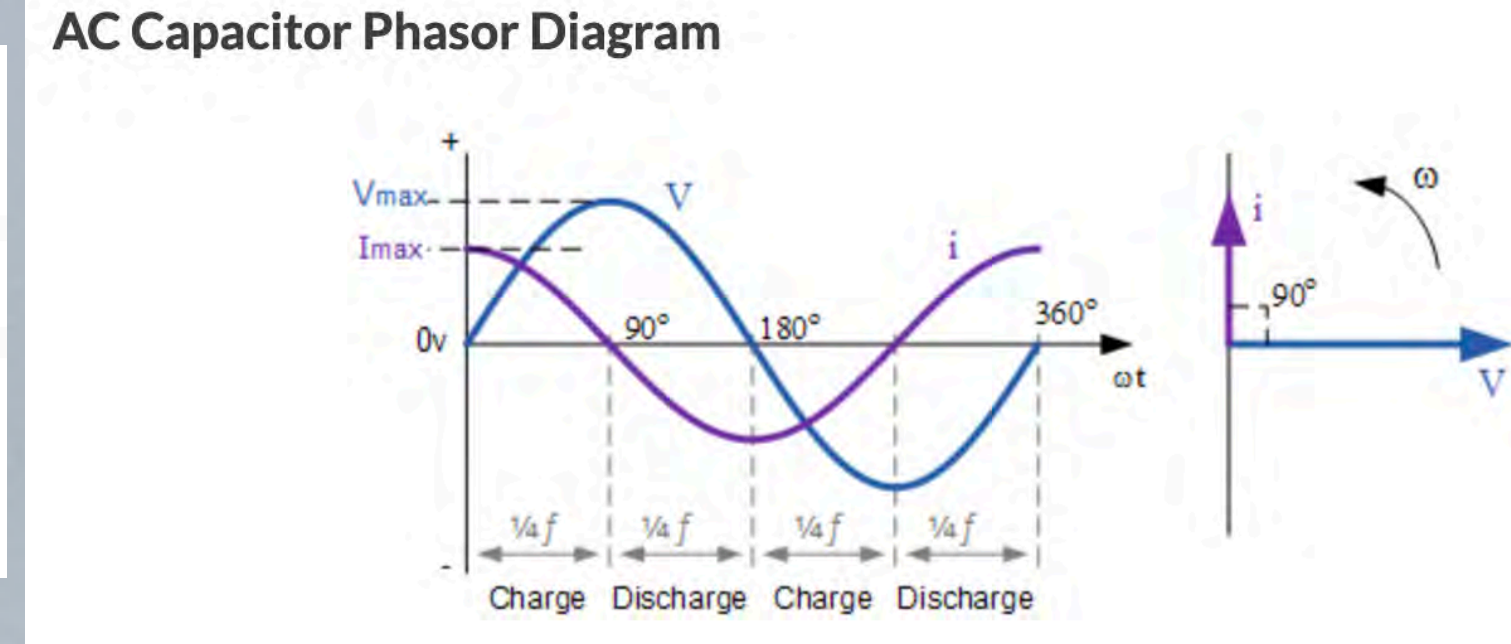
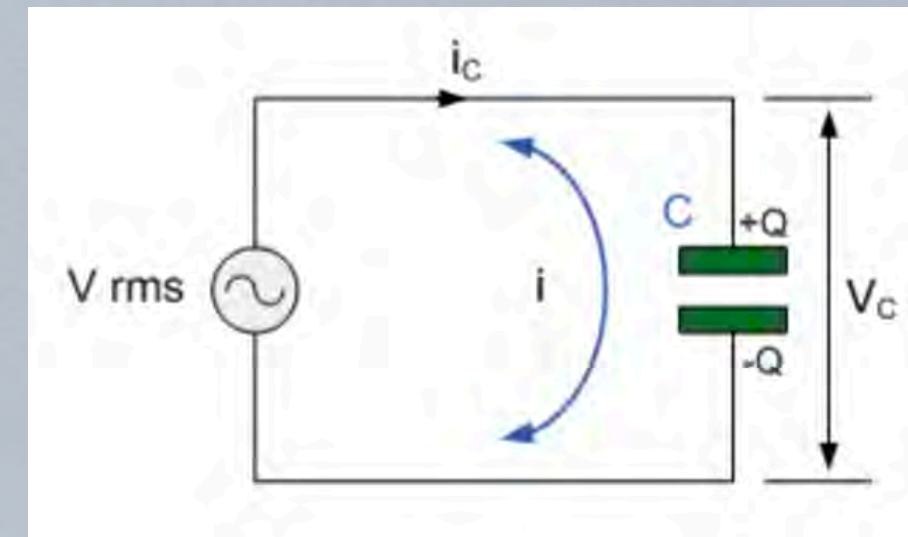
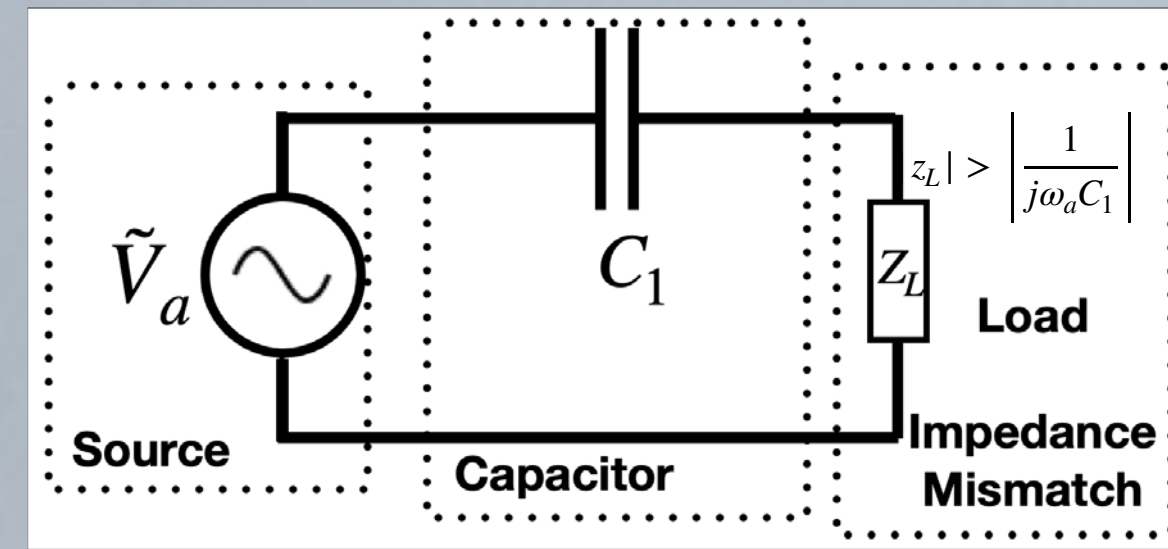
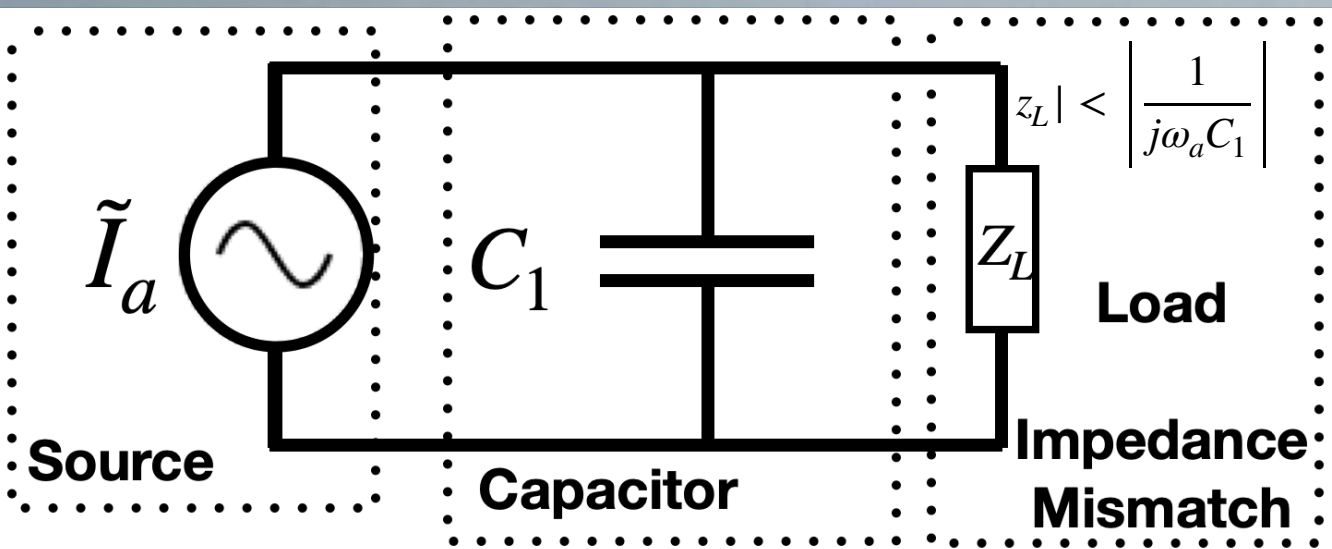
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**Energy oscillates between Source and Capacitor  
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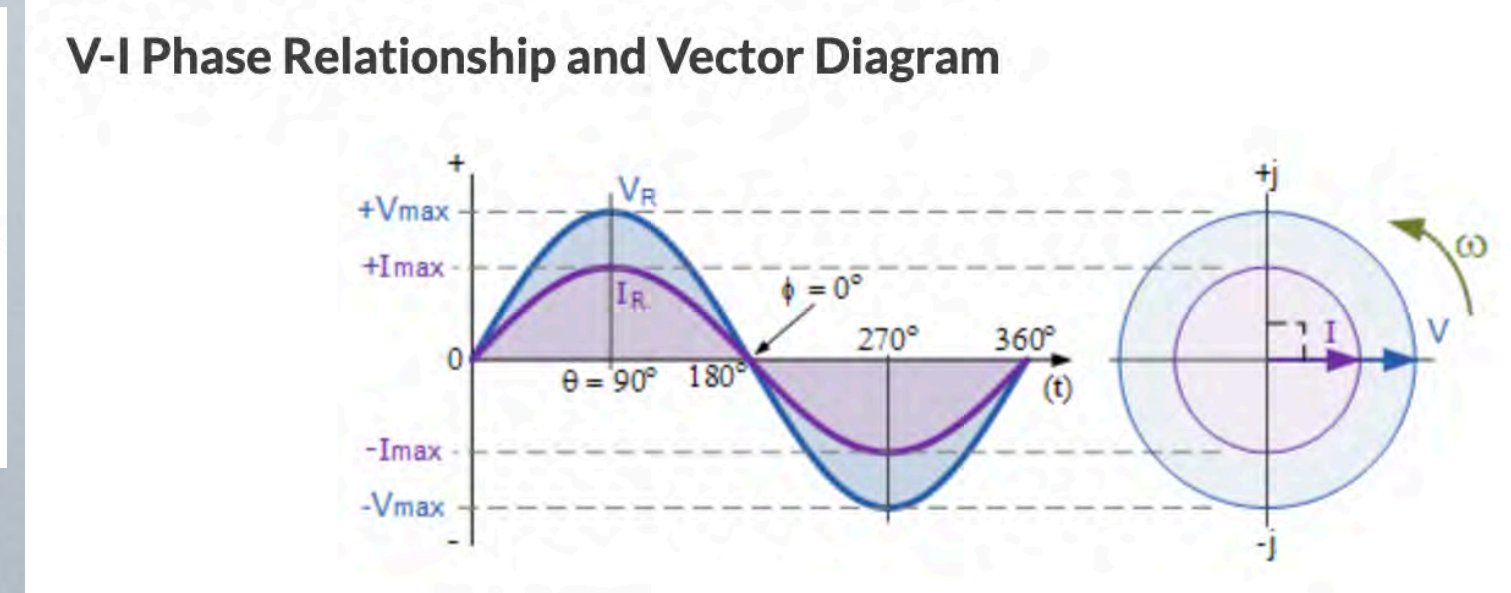
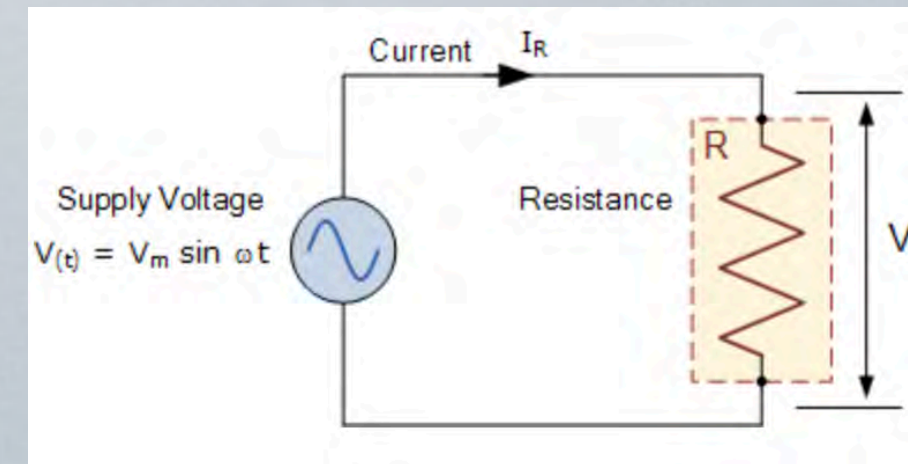
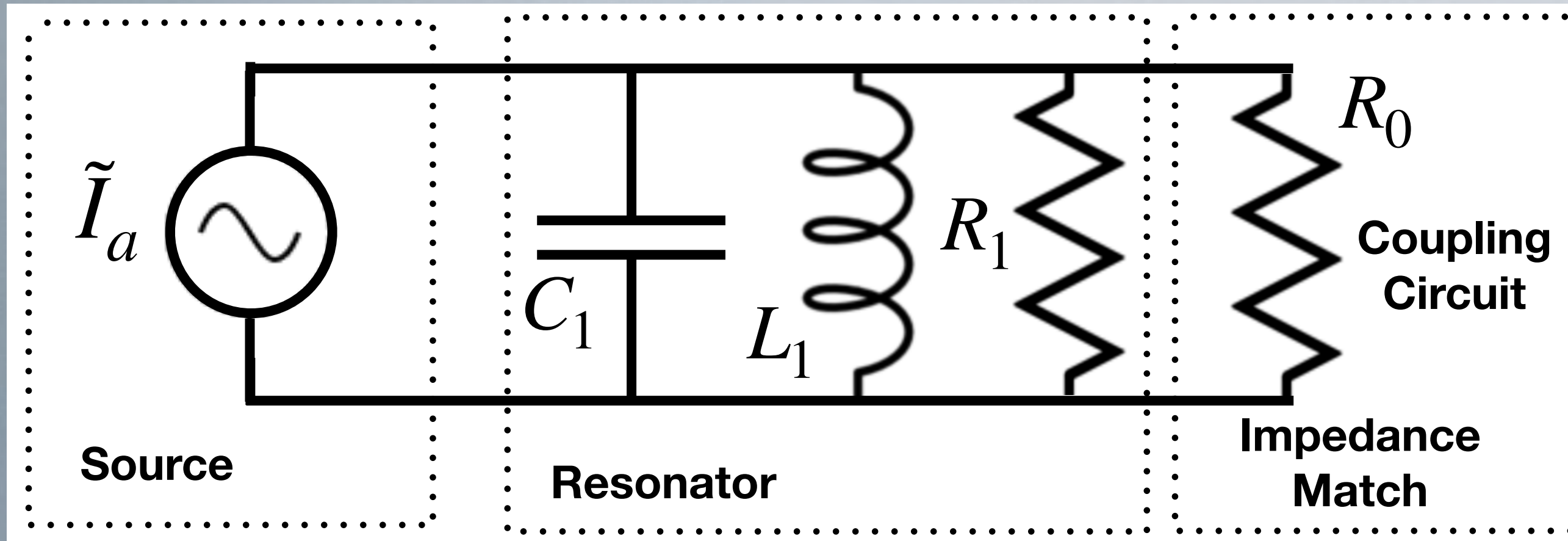
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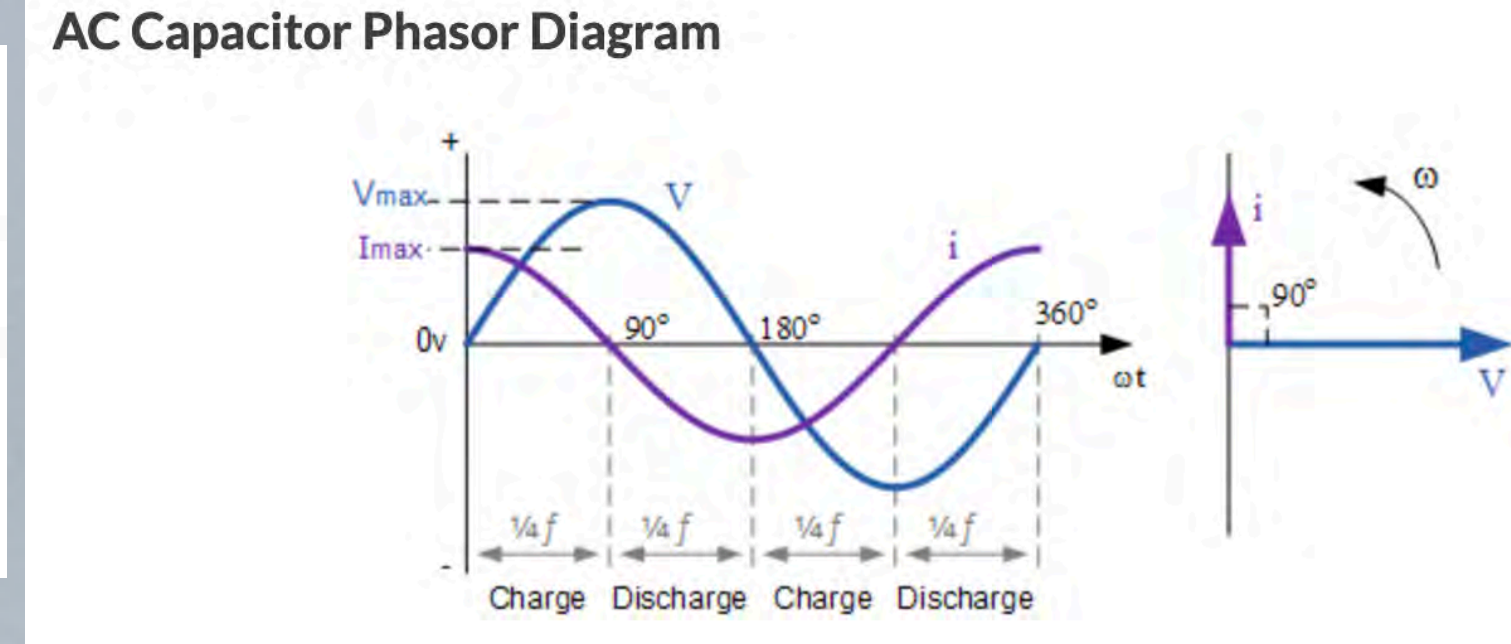
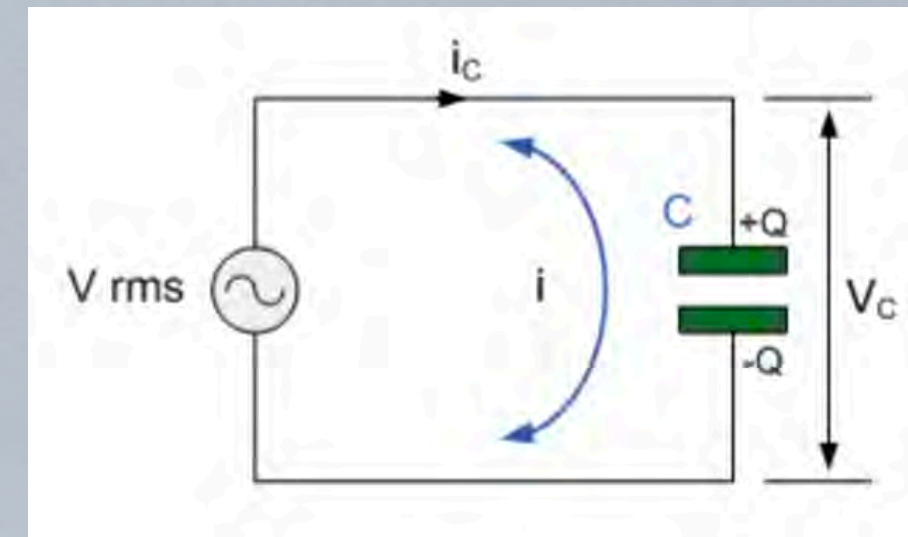
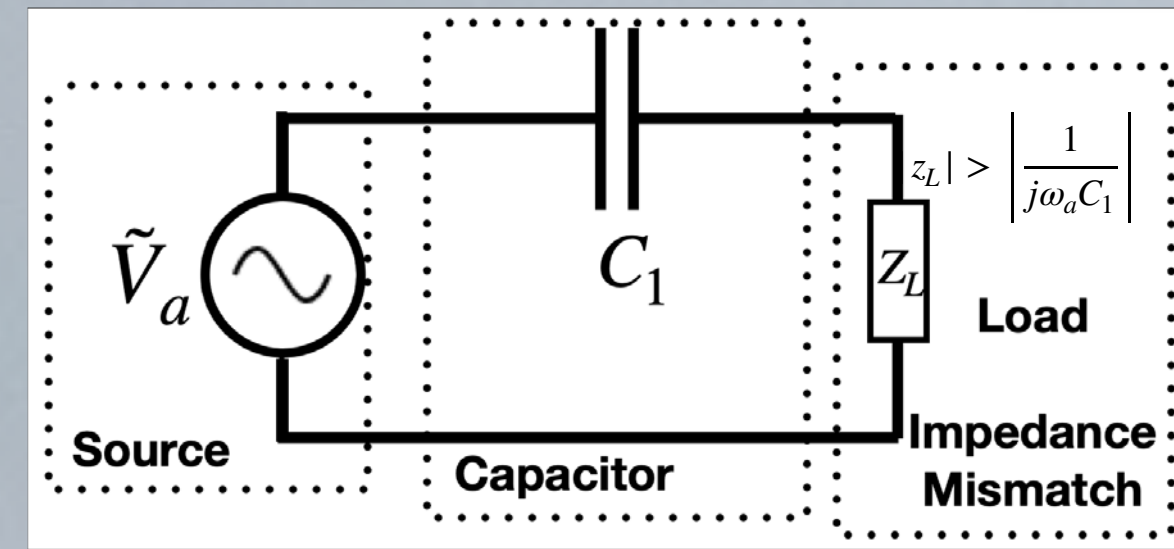
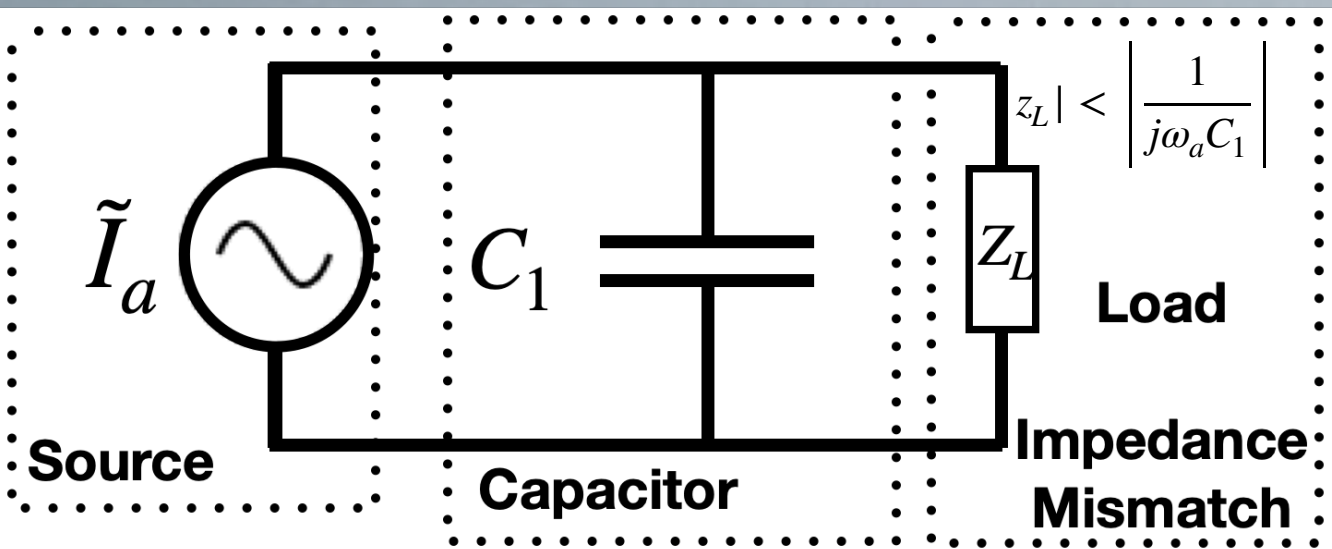
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Reactive power does not propagate or dissipate out of the volume of the detector (ie. no loss): Oscillates in and out of volume

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Does not need to be the order of the Compton wavelength in size (sub wavelength phenomena)

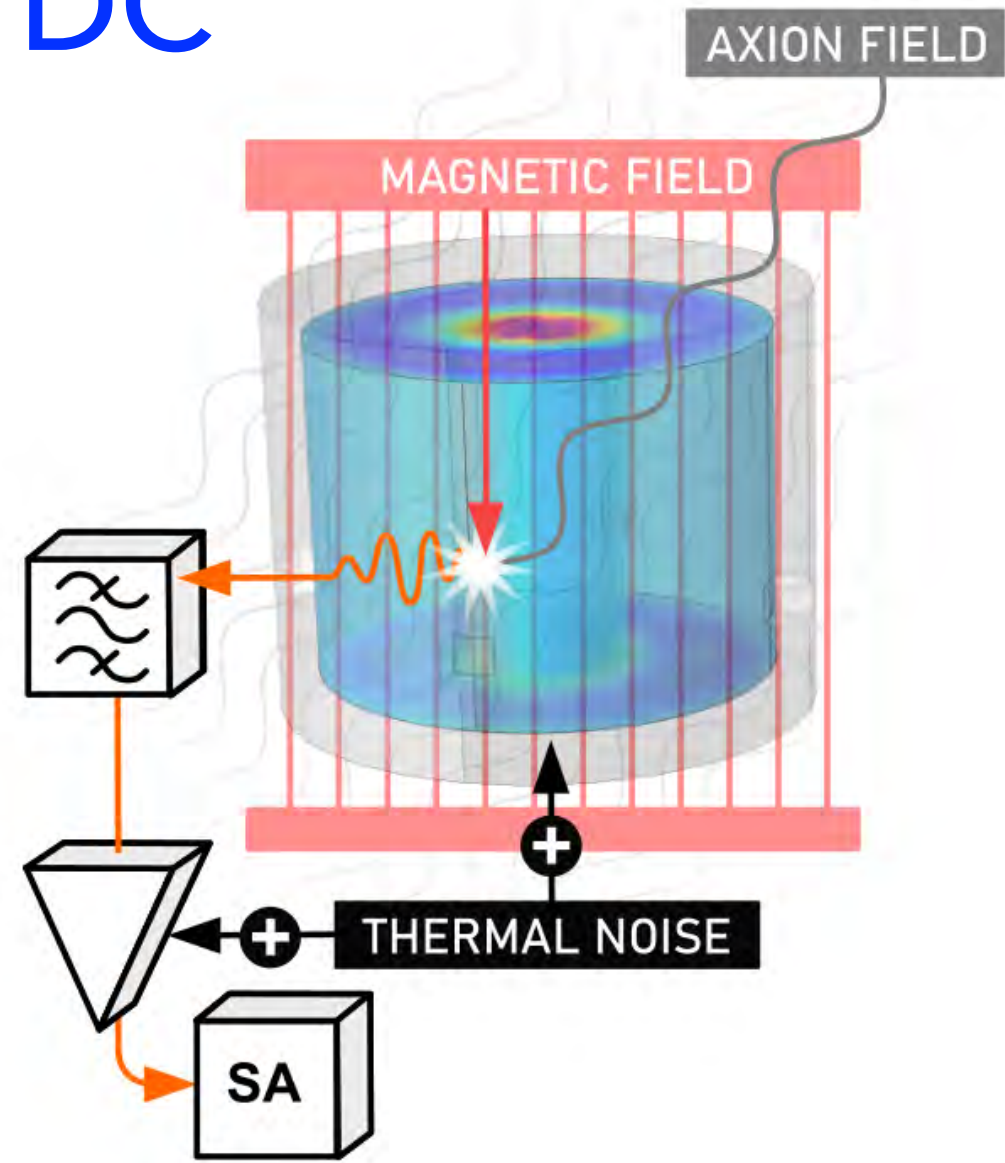
# Resonant Axion Haloscopes @ UWA

$$\mathcal{H}_{int} = \epsilon_0 c g_{a\gamma\gamma} a \mathbf{E} \cdot \mathbf{B}$$

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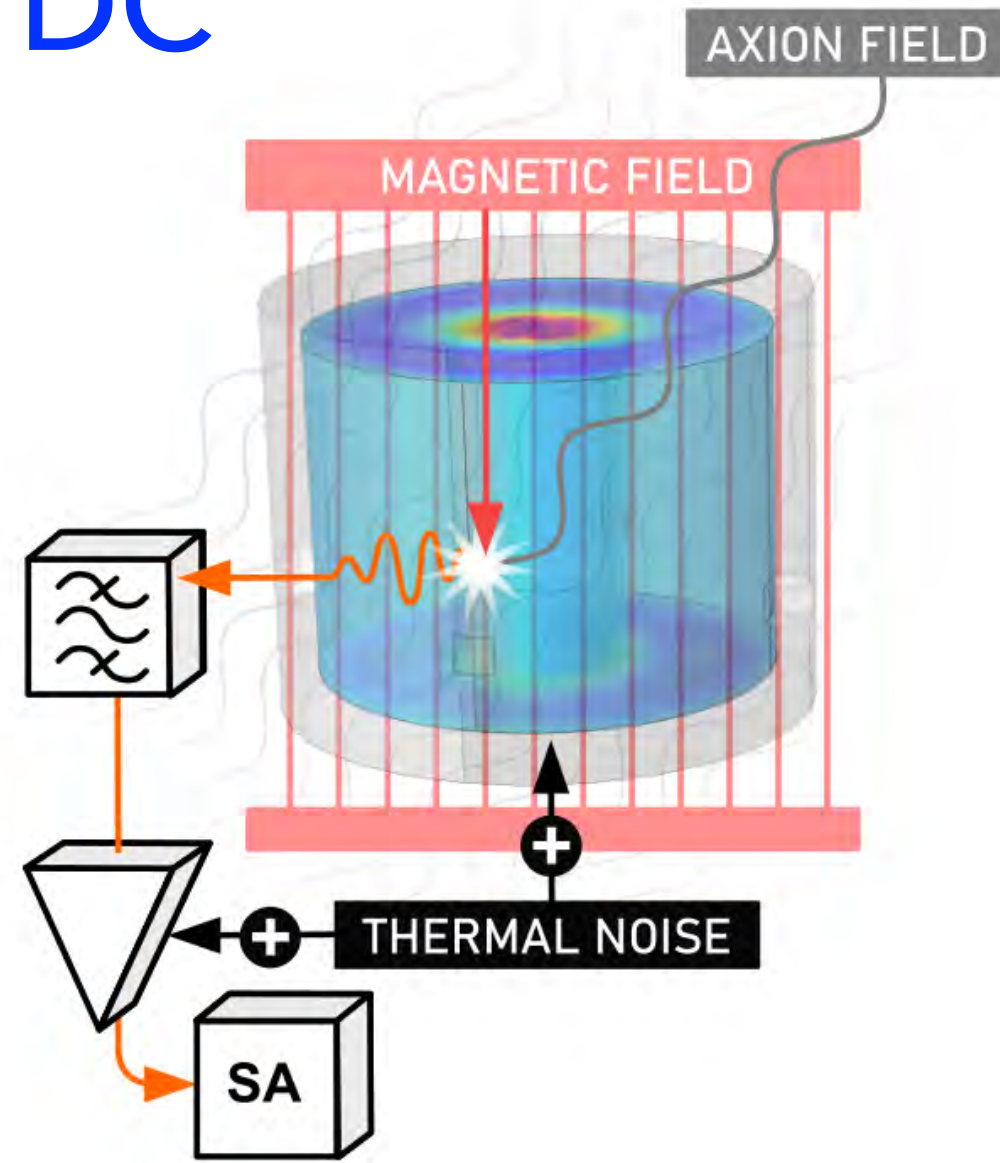
DC



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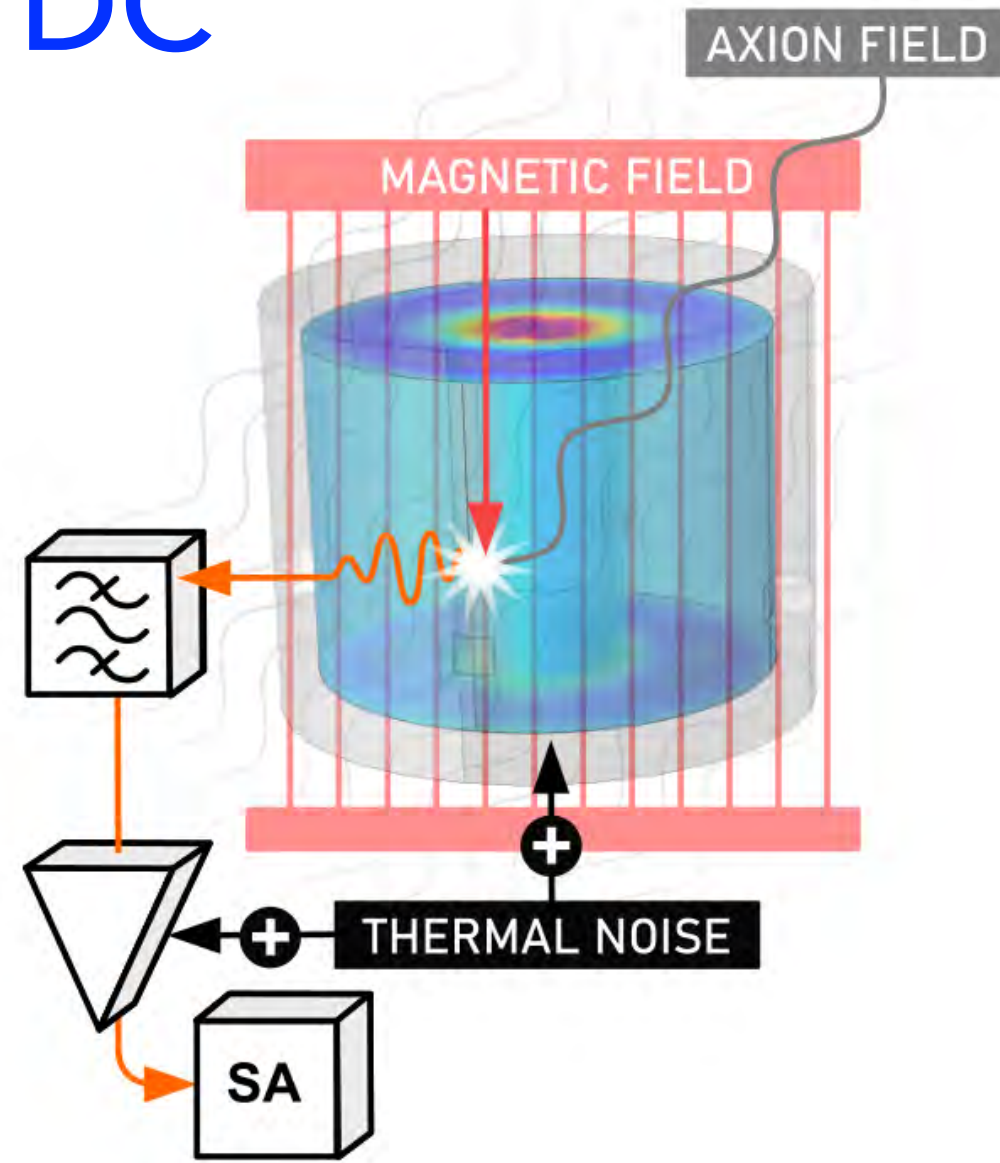


**Photon 1:** E field of cavity's resonant transverse magnetic mode,  $m_a = f_1 + \delta f$

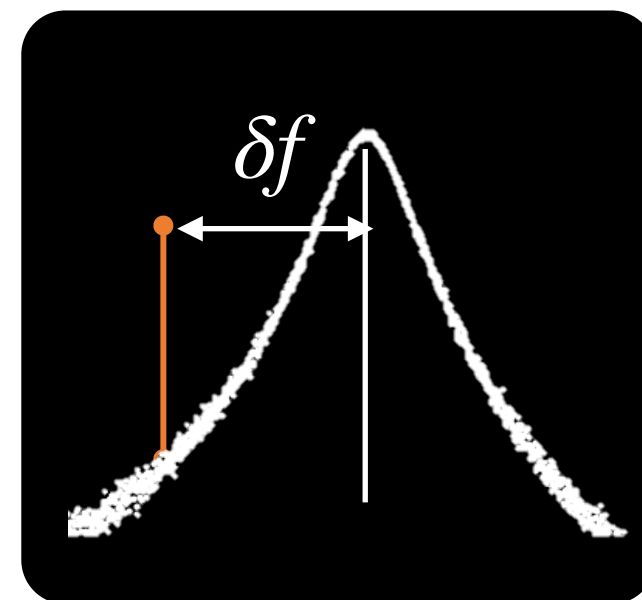
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DC



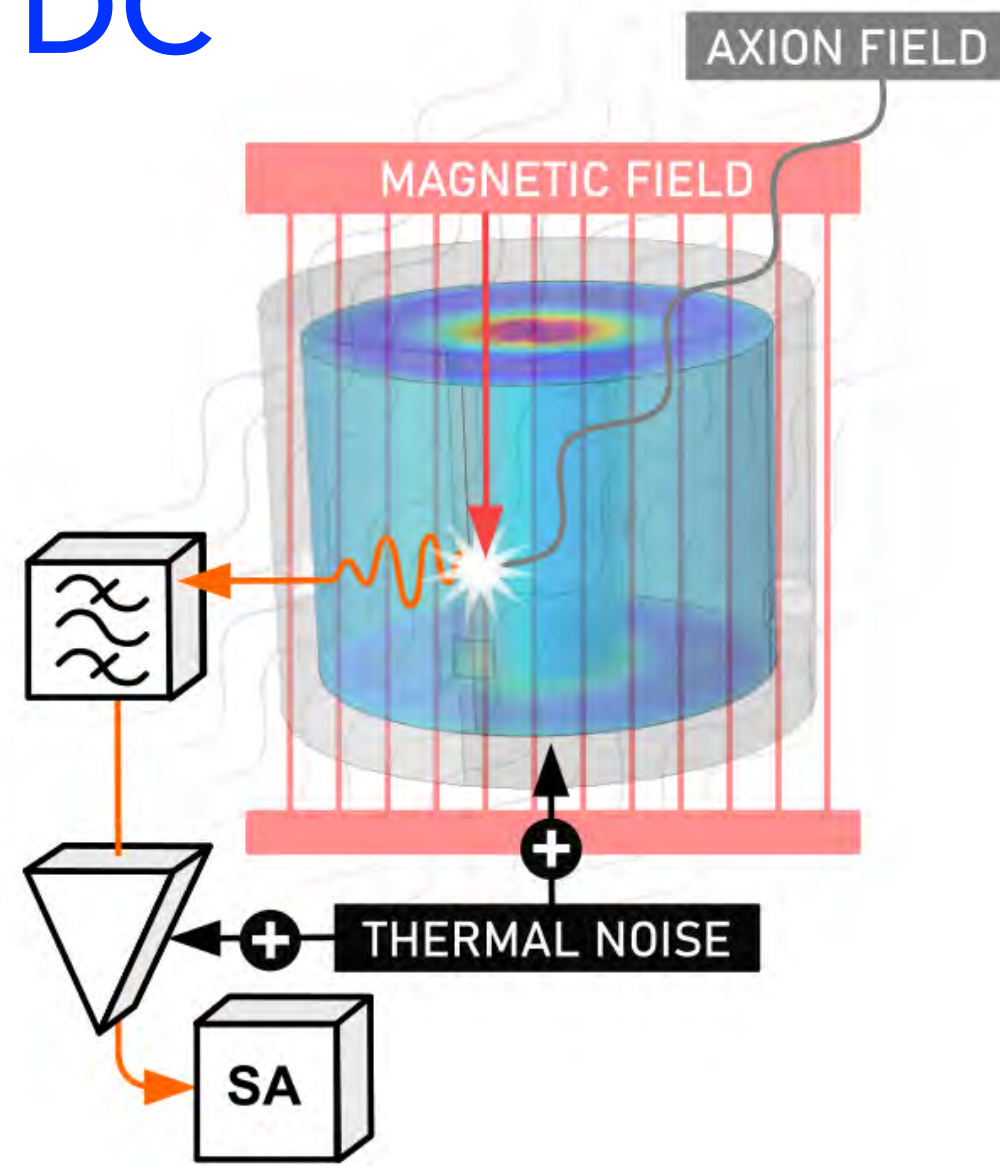
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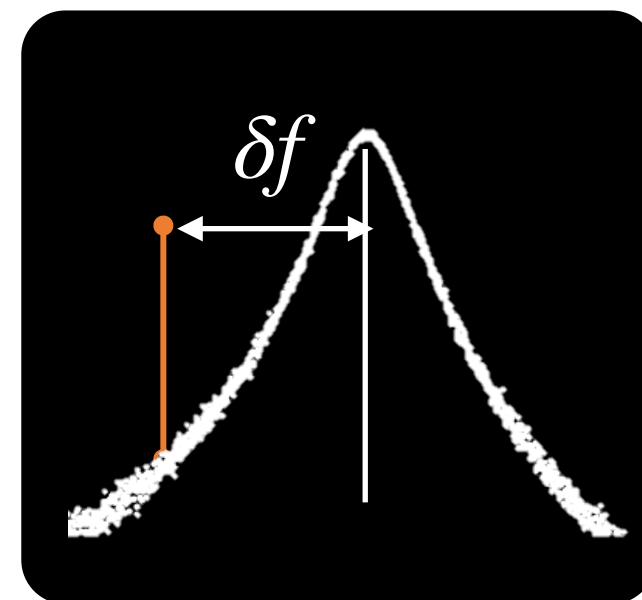
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DC



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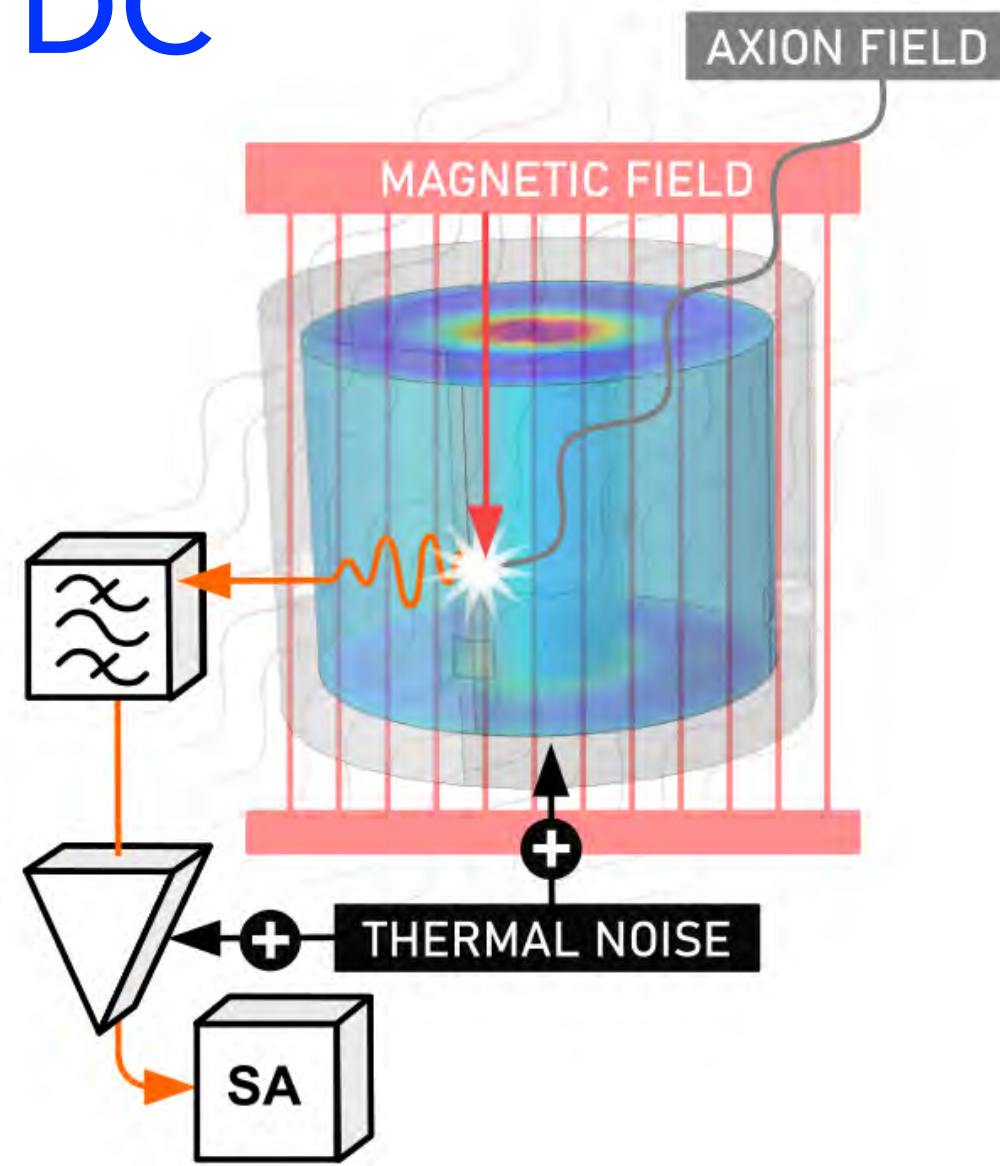




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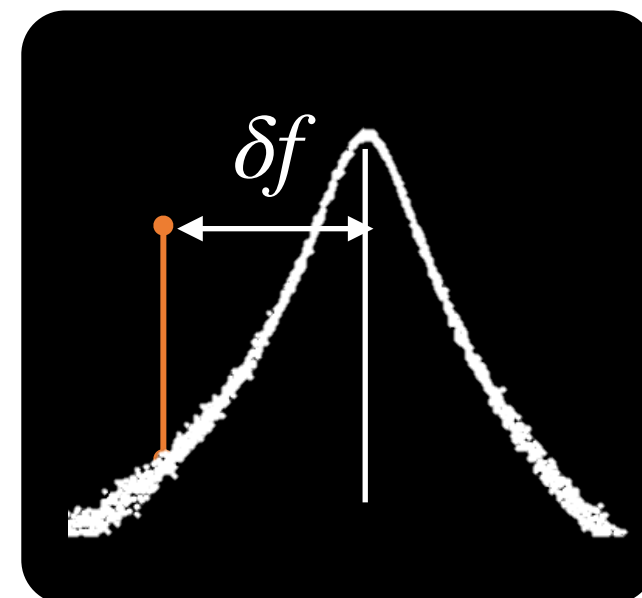


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eg.

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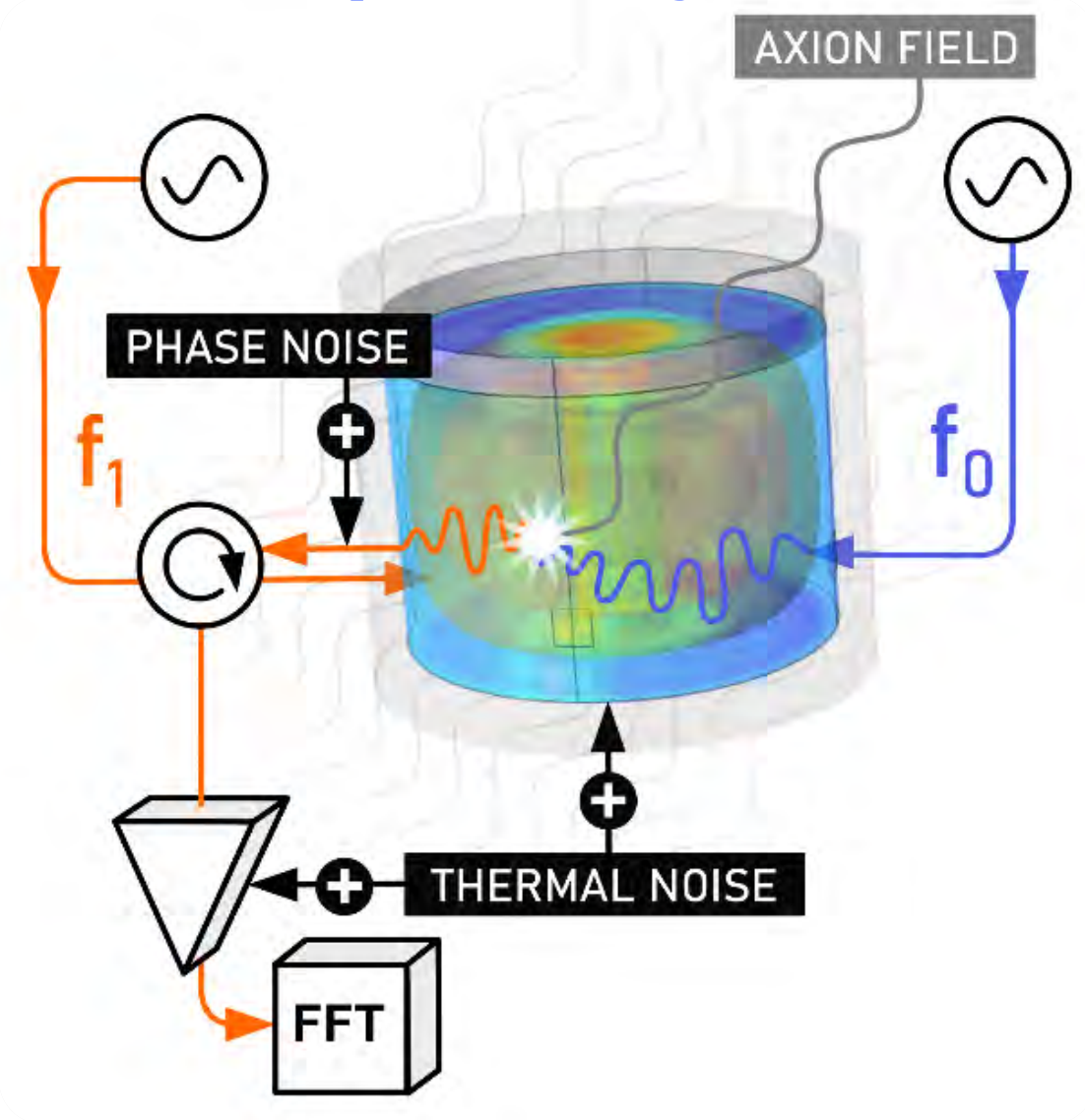
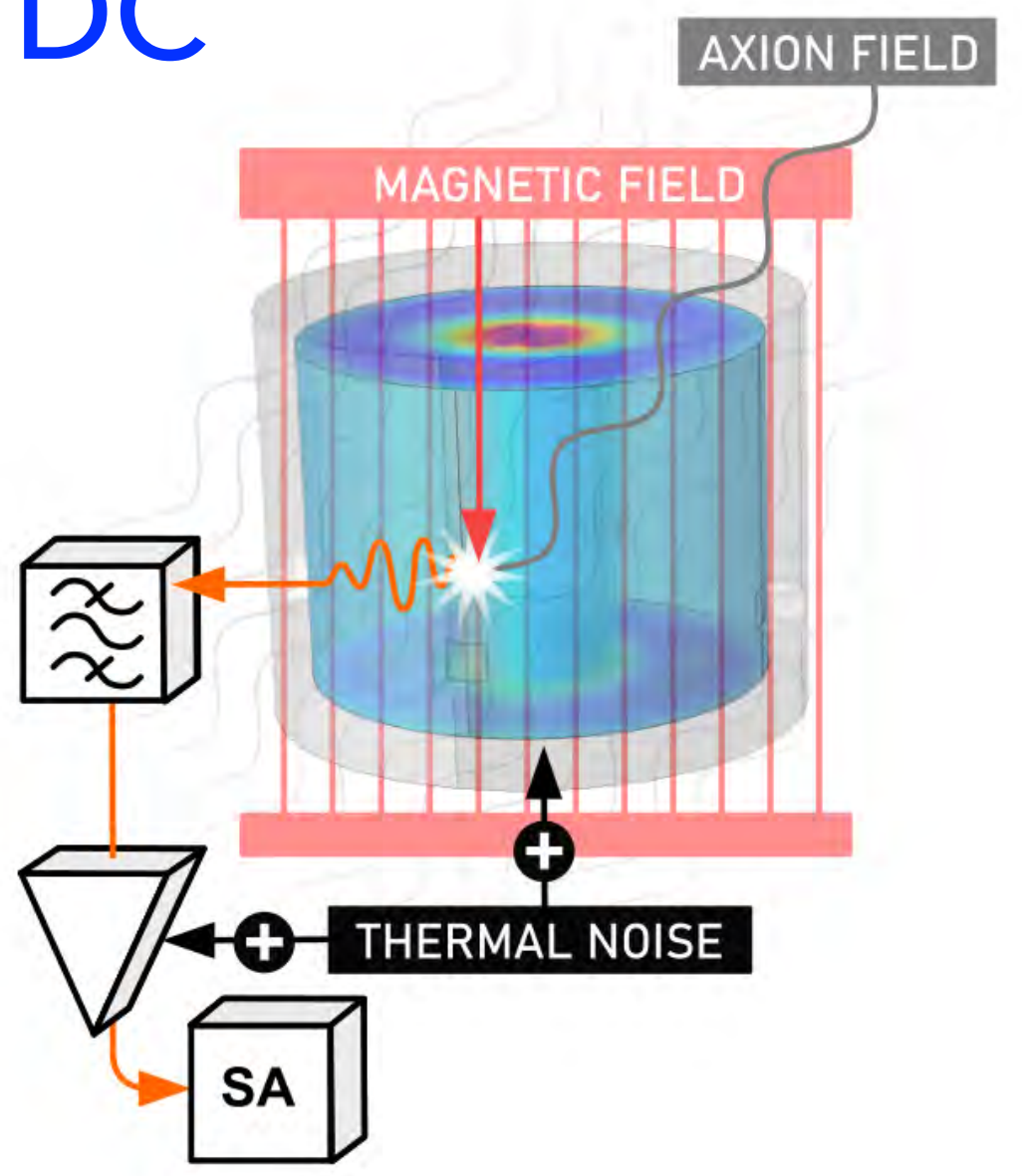


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AC Frequency

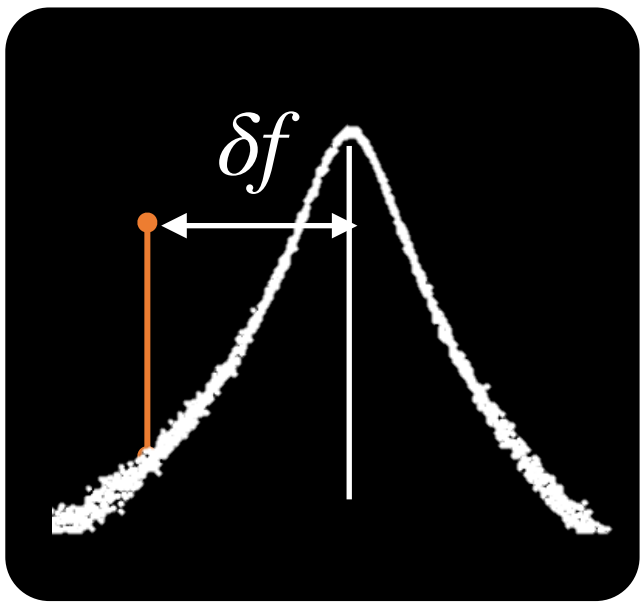
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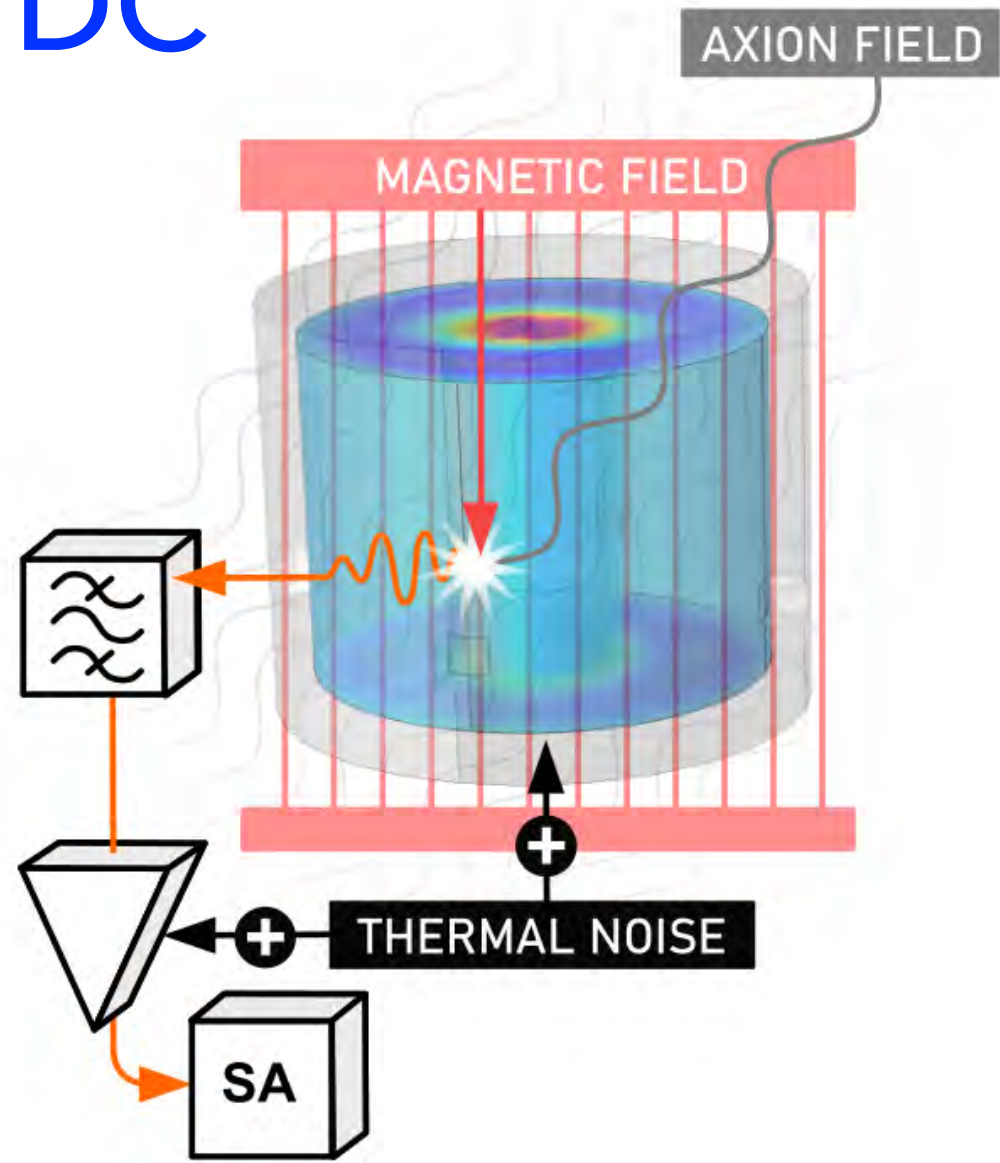
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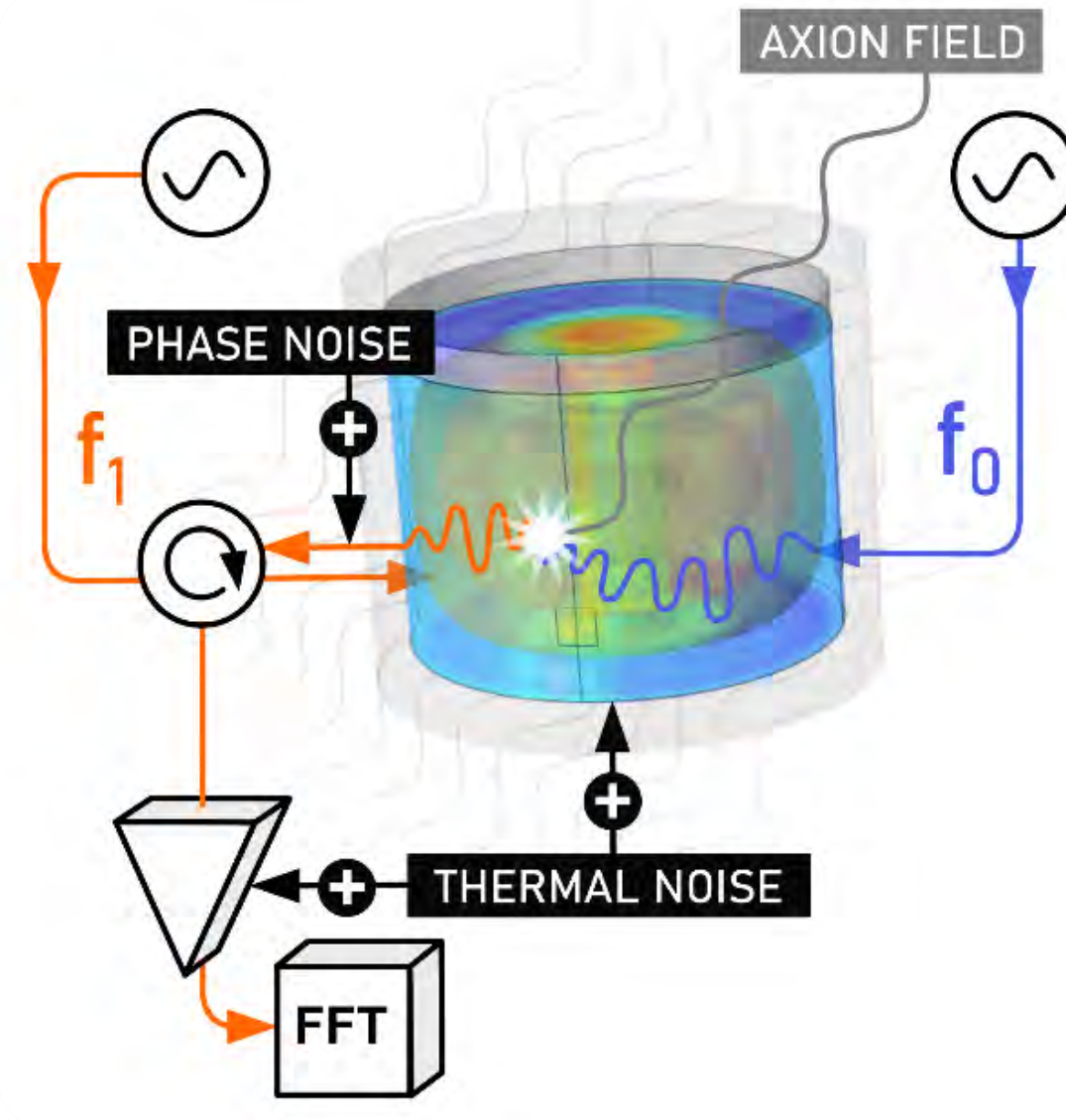
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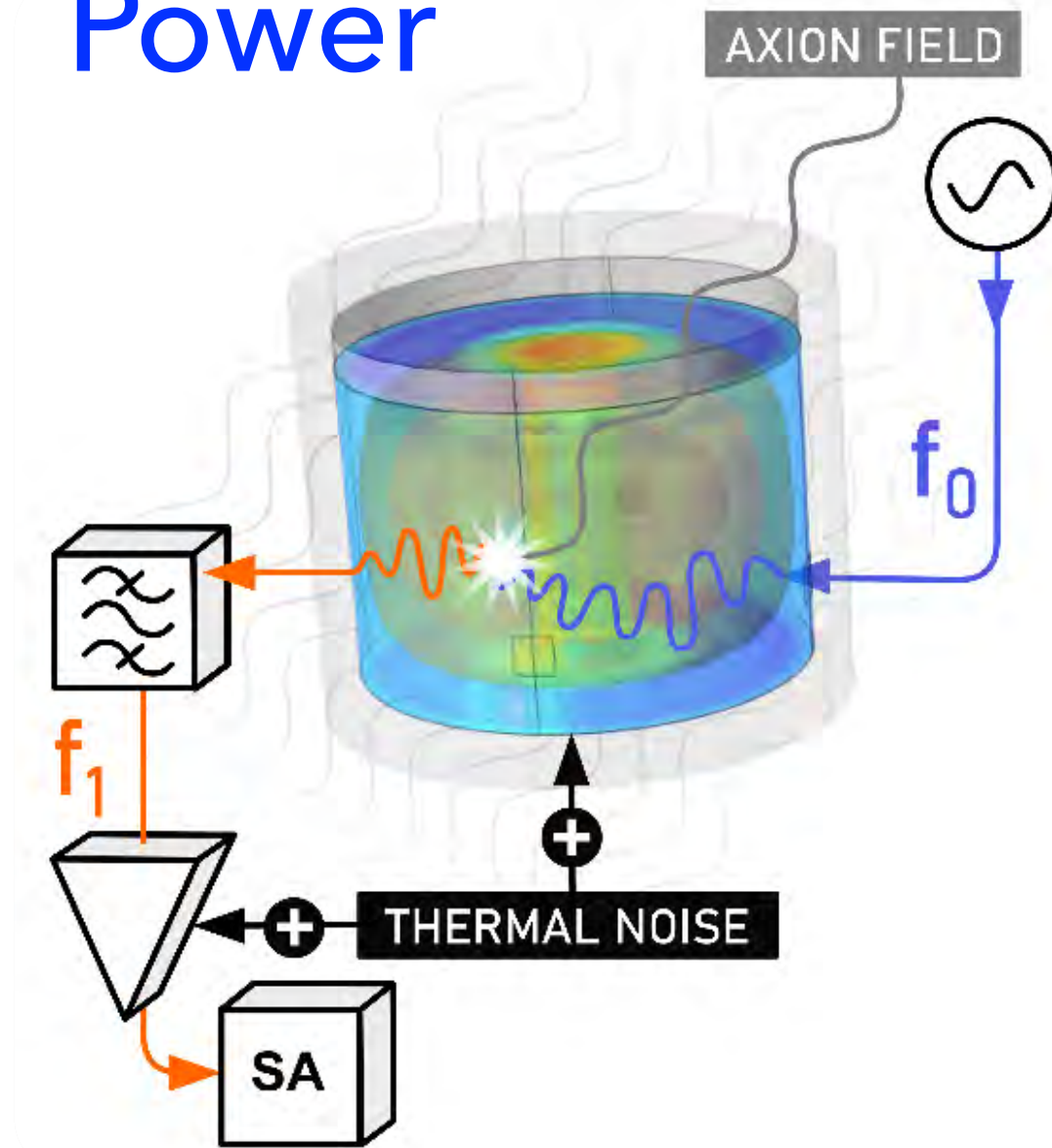
DC



AC Frequency



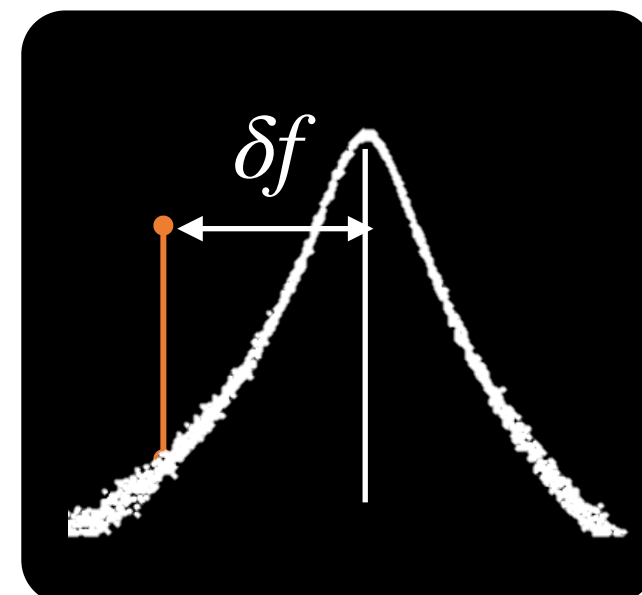
AC Power



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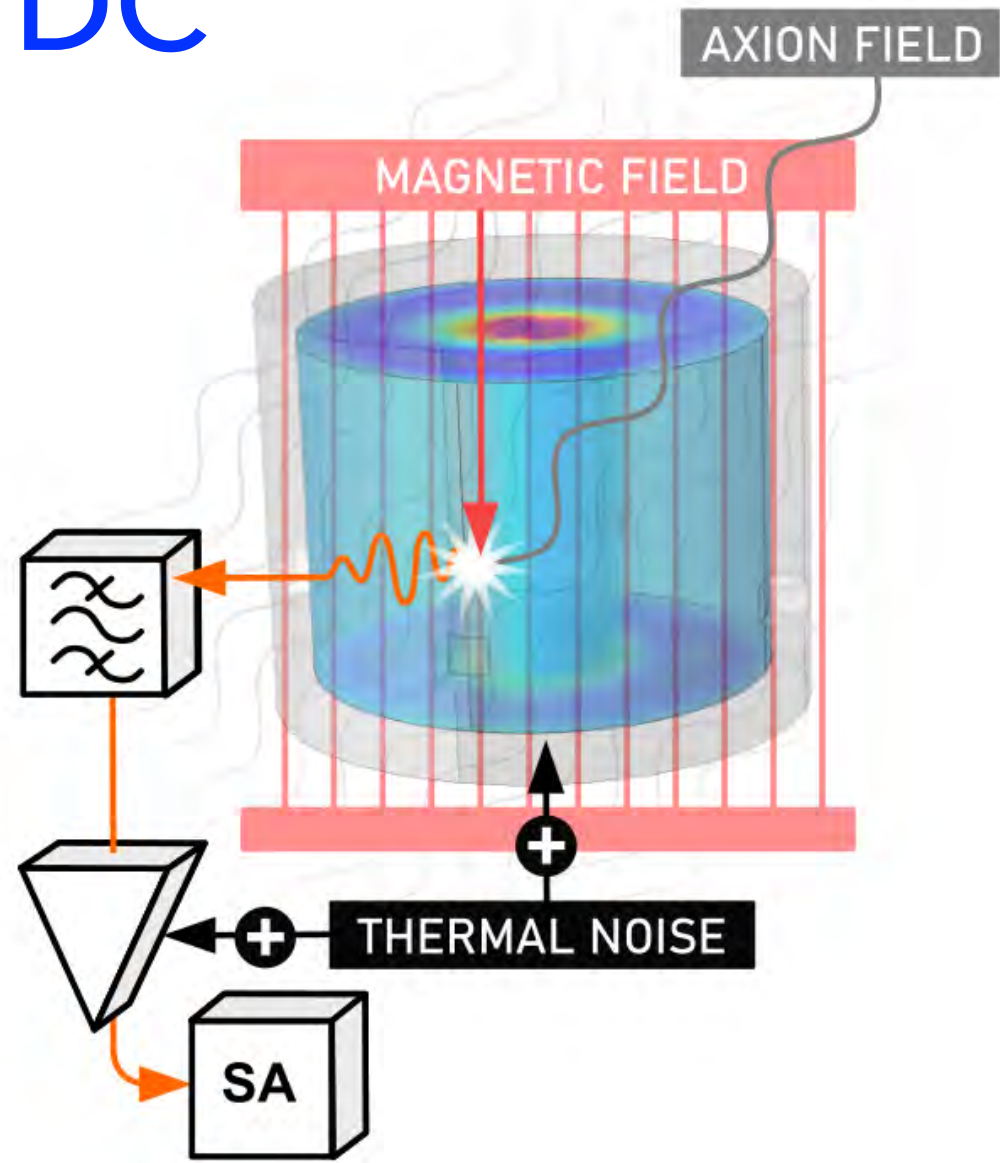
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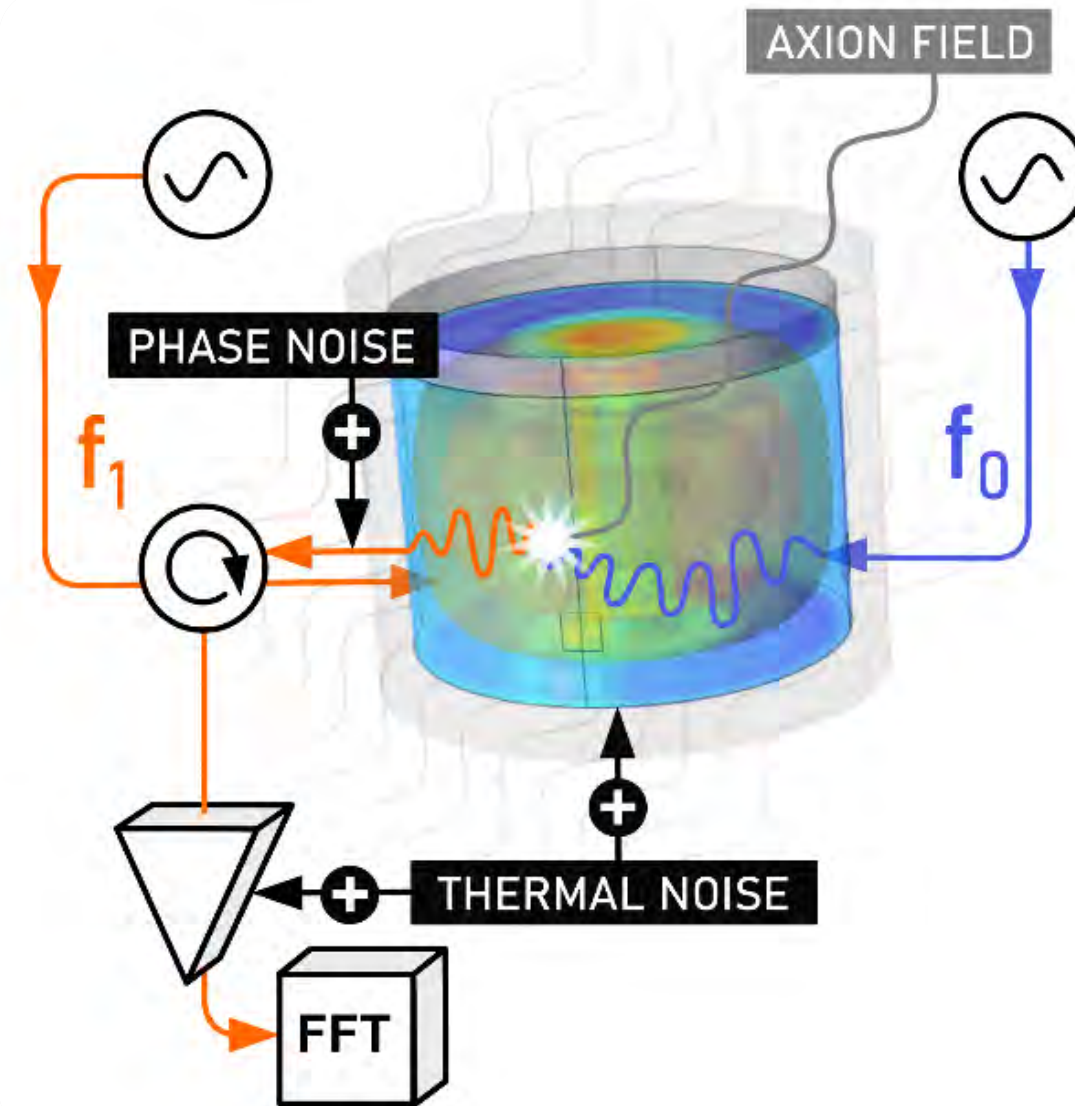
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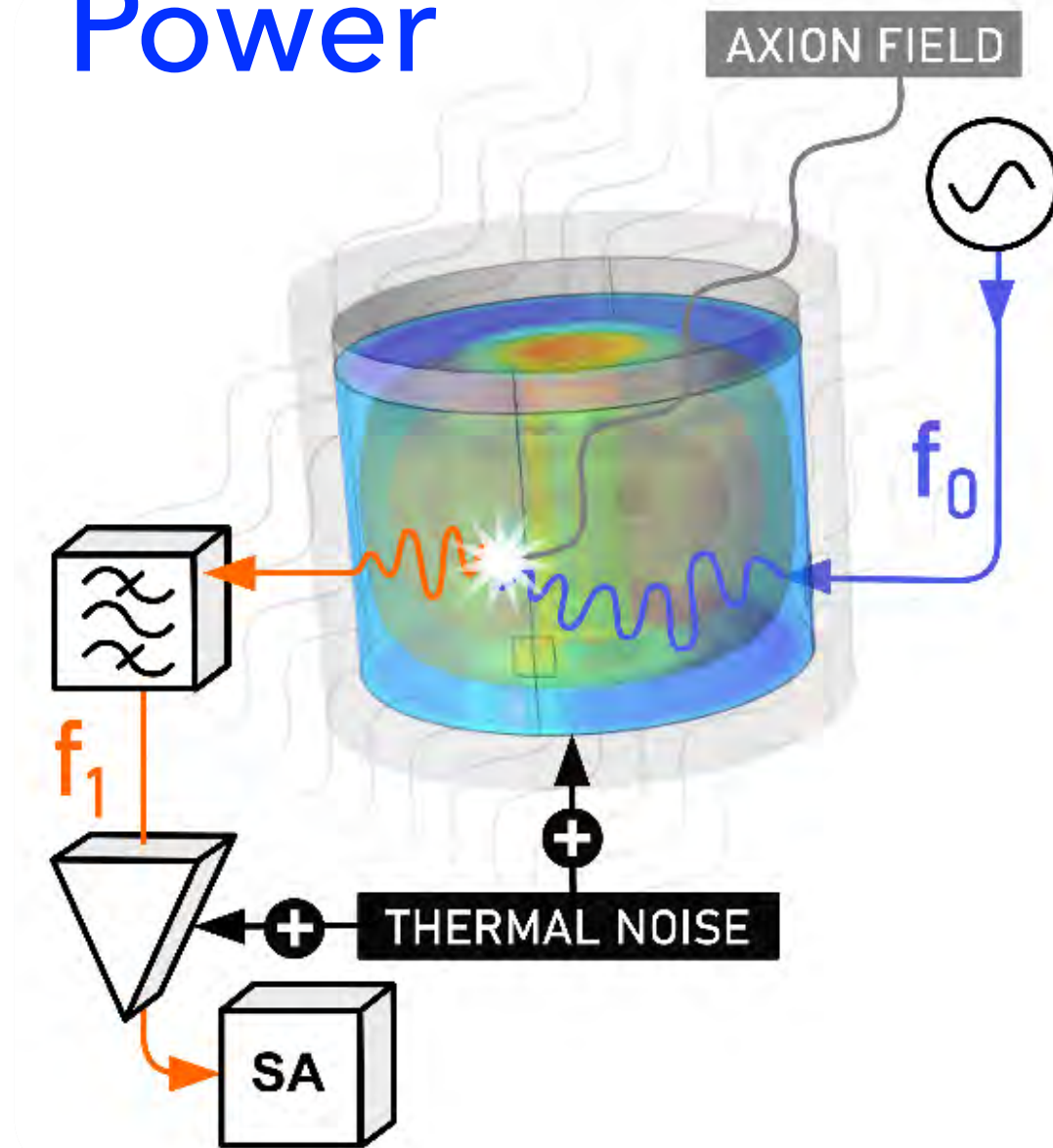
DC



AC Frequency



AC Power



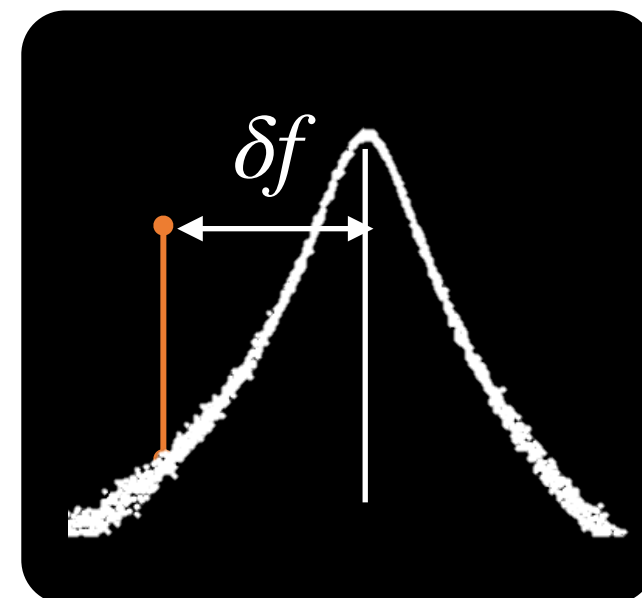
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eg.

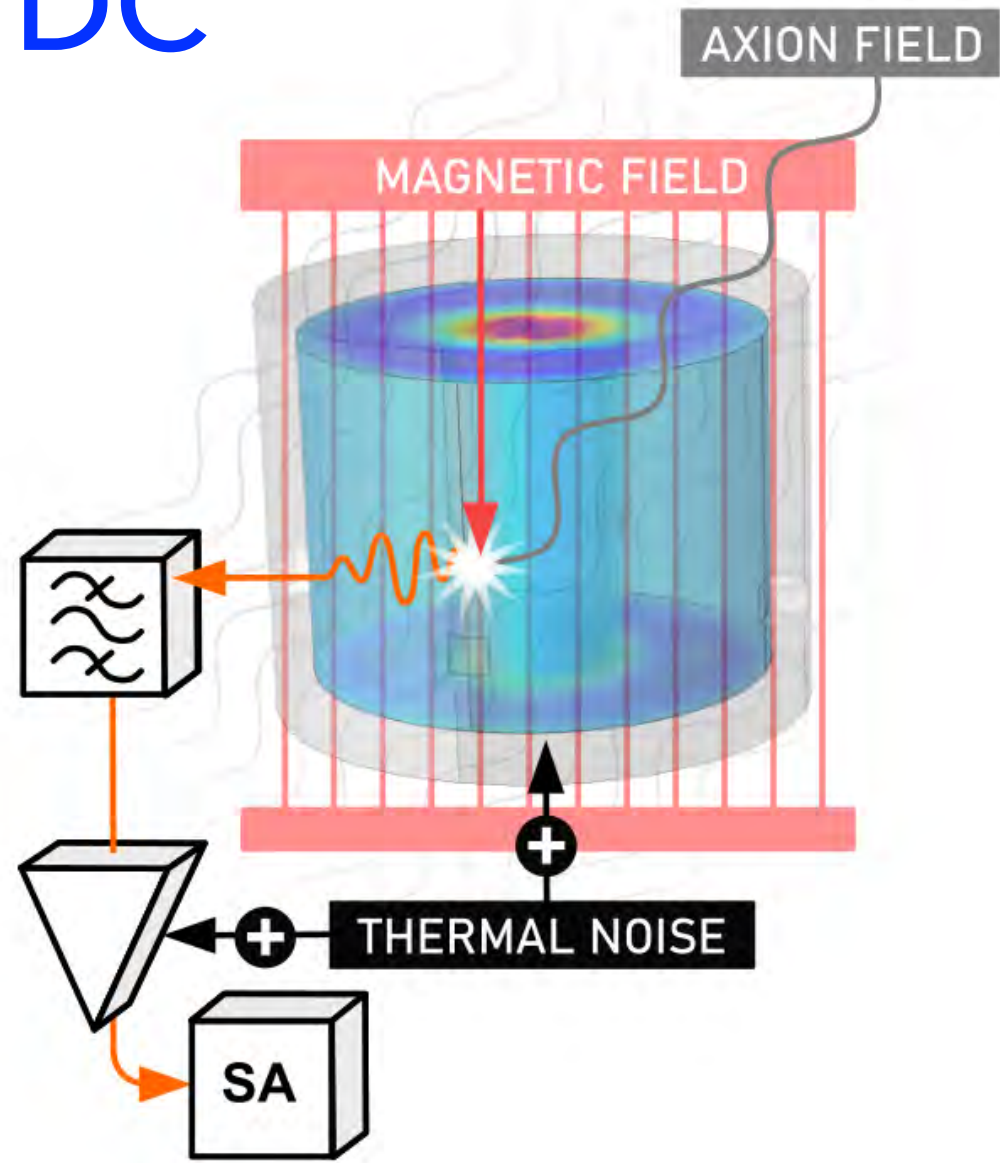
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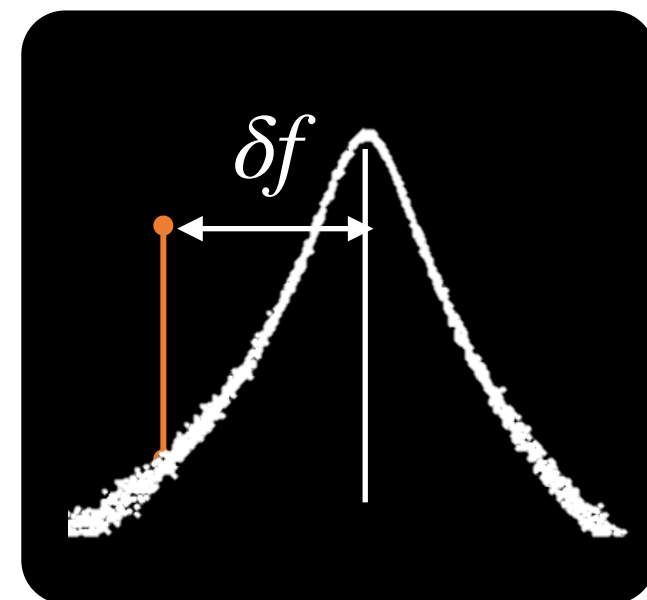
DC



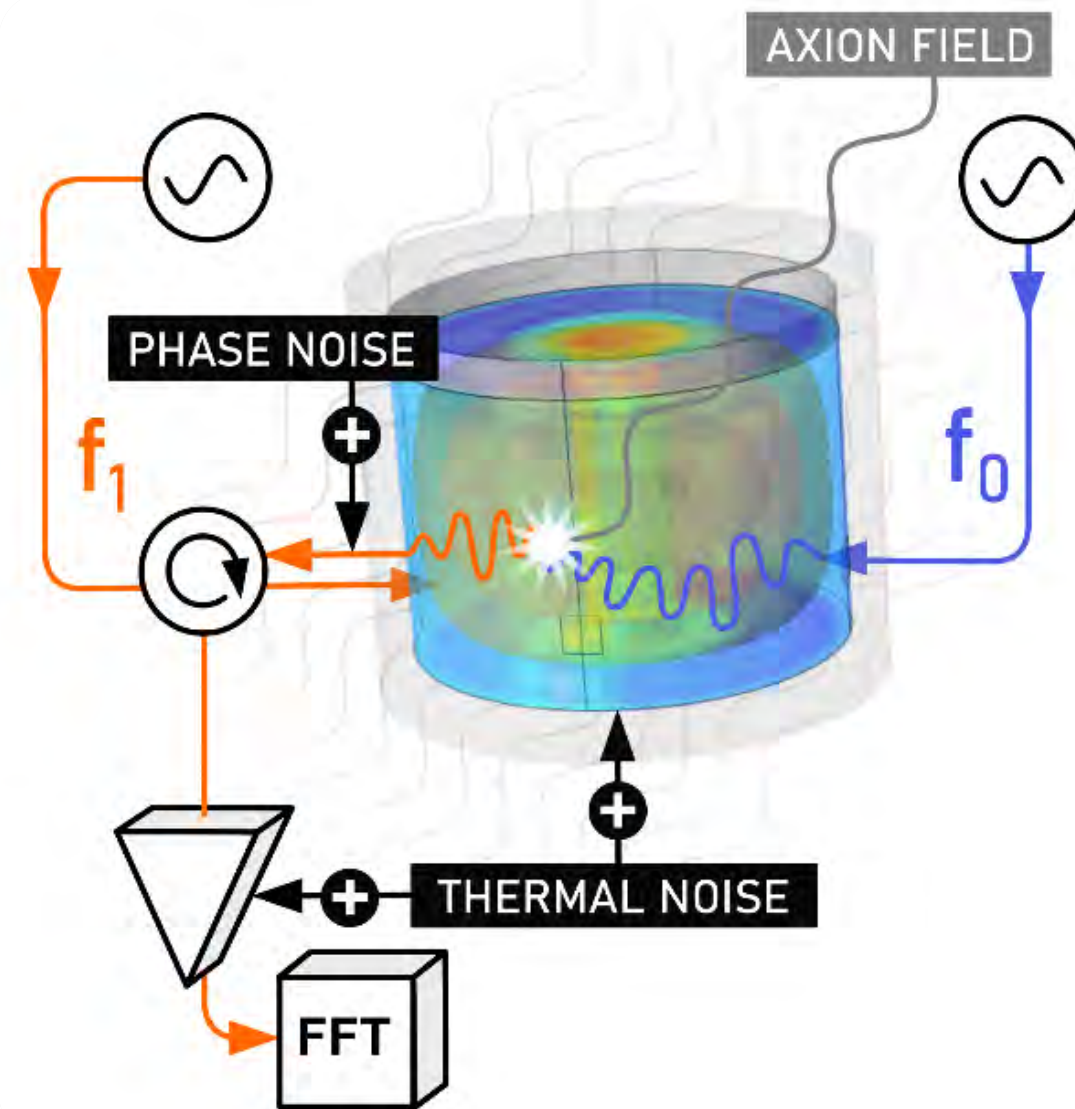
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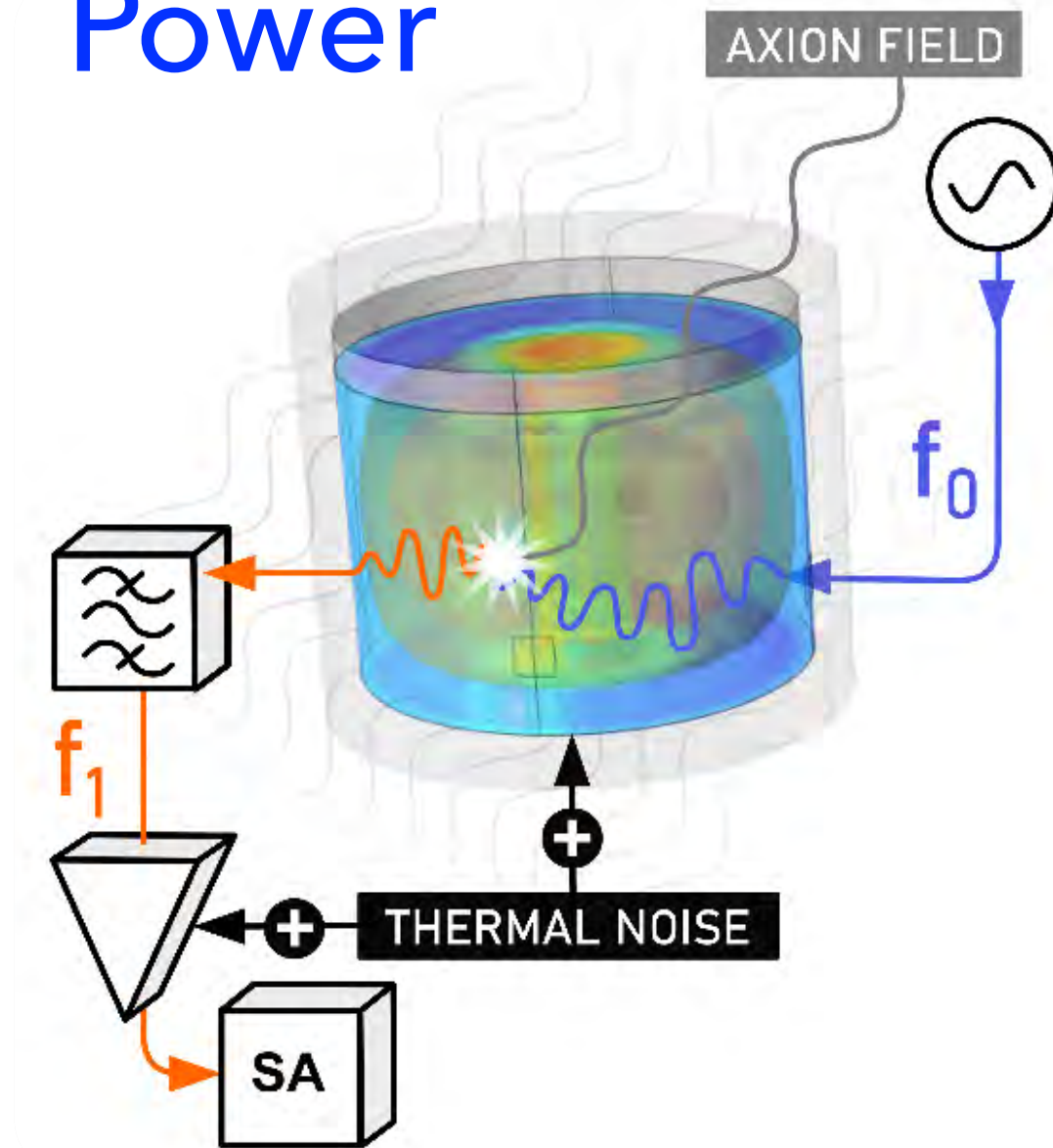


AC Frequency



- Use a mode 0 as the background “magnetic field” AC source
- Two modes in one cylindrical cavity

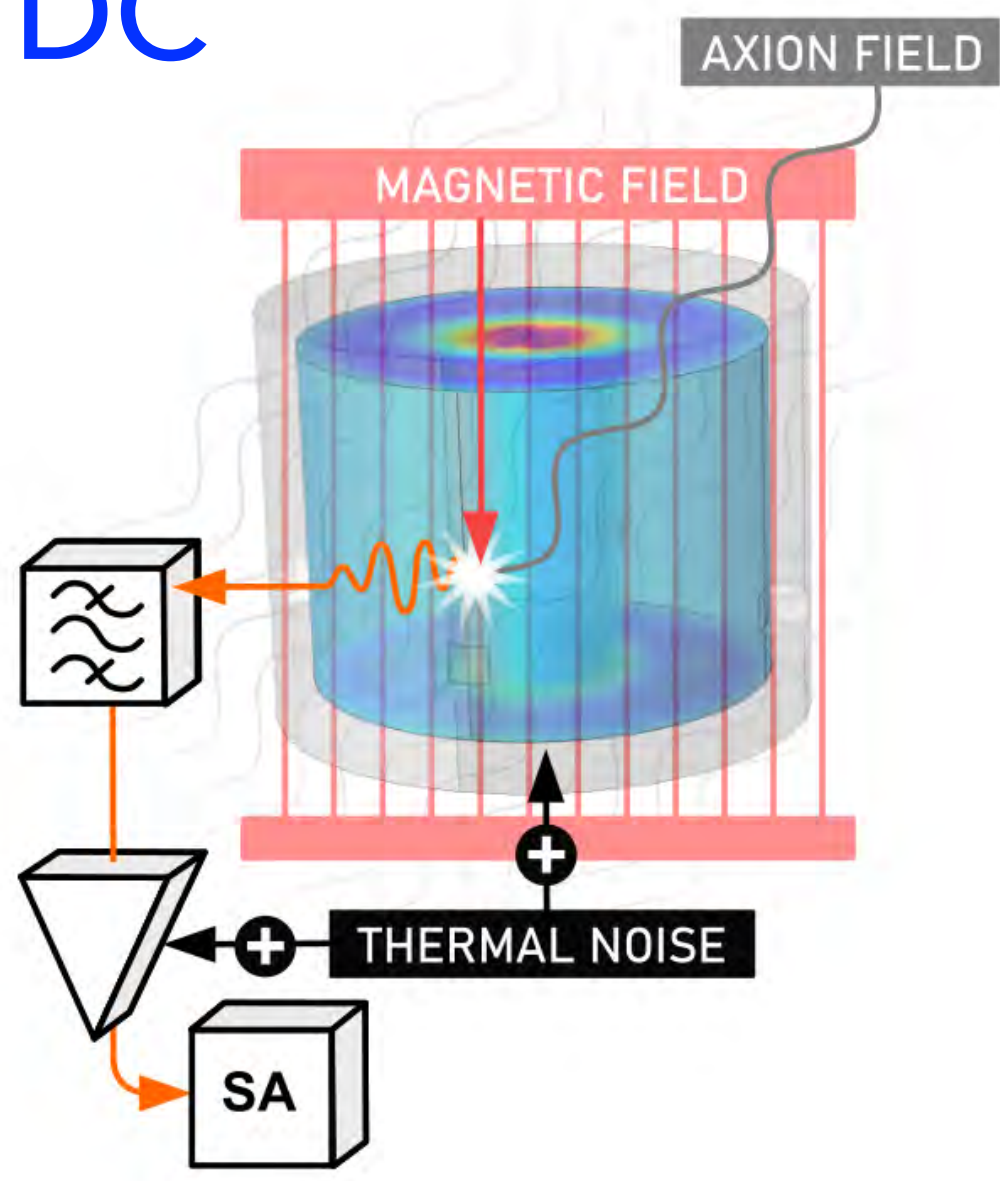
AC Power



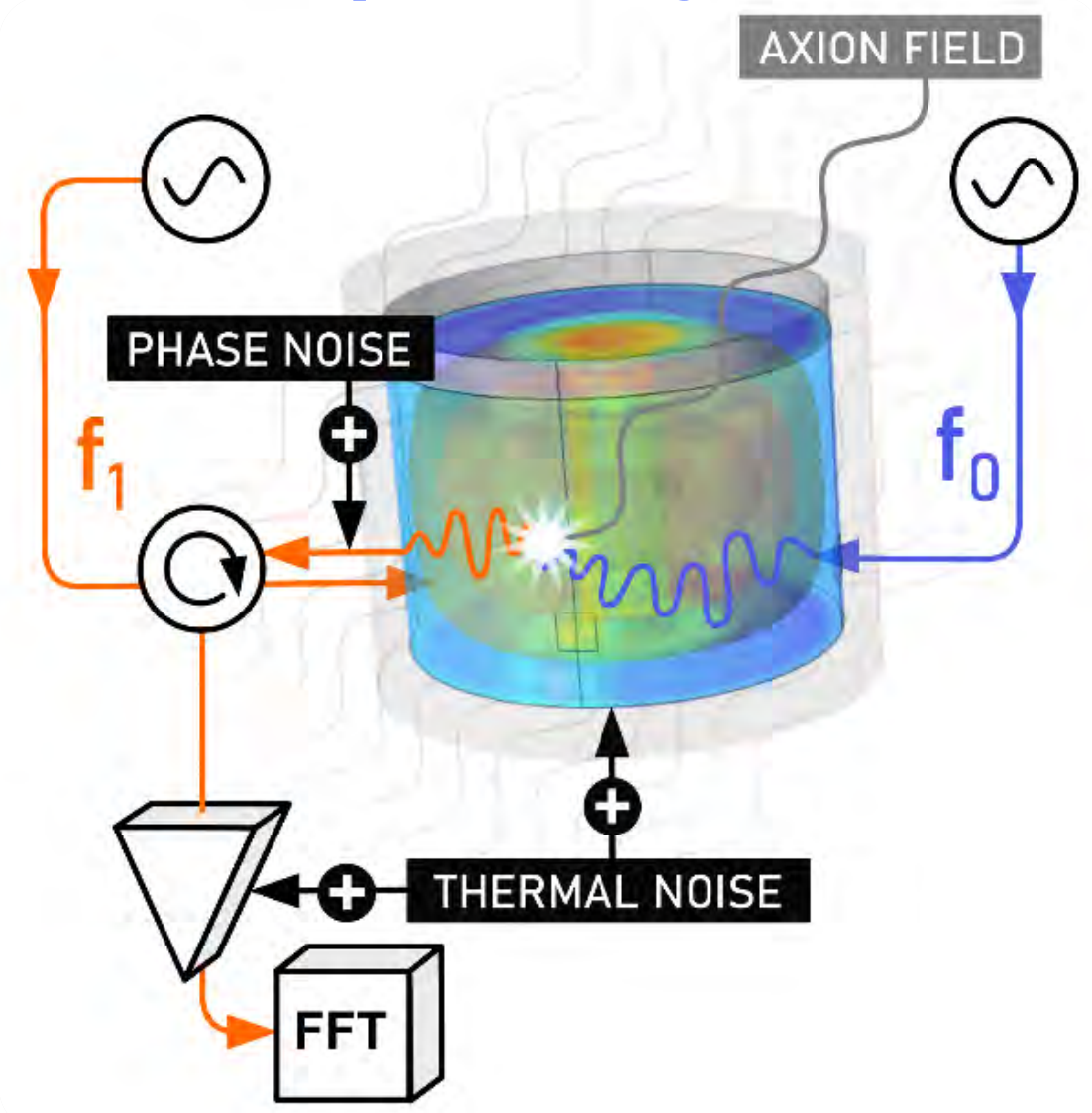
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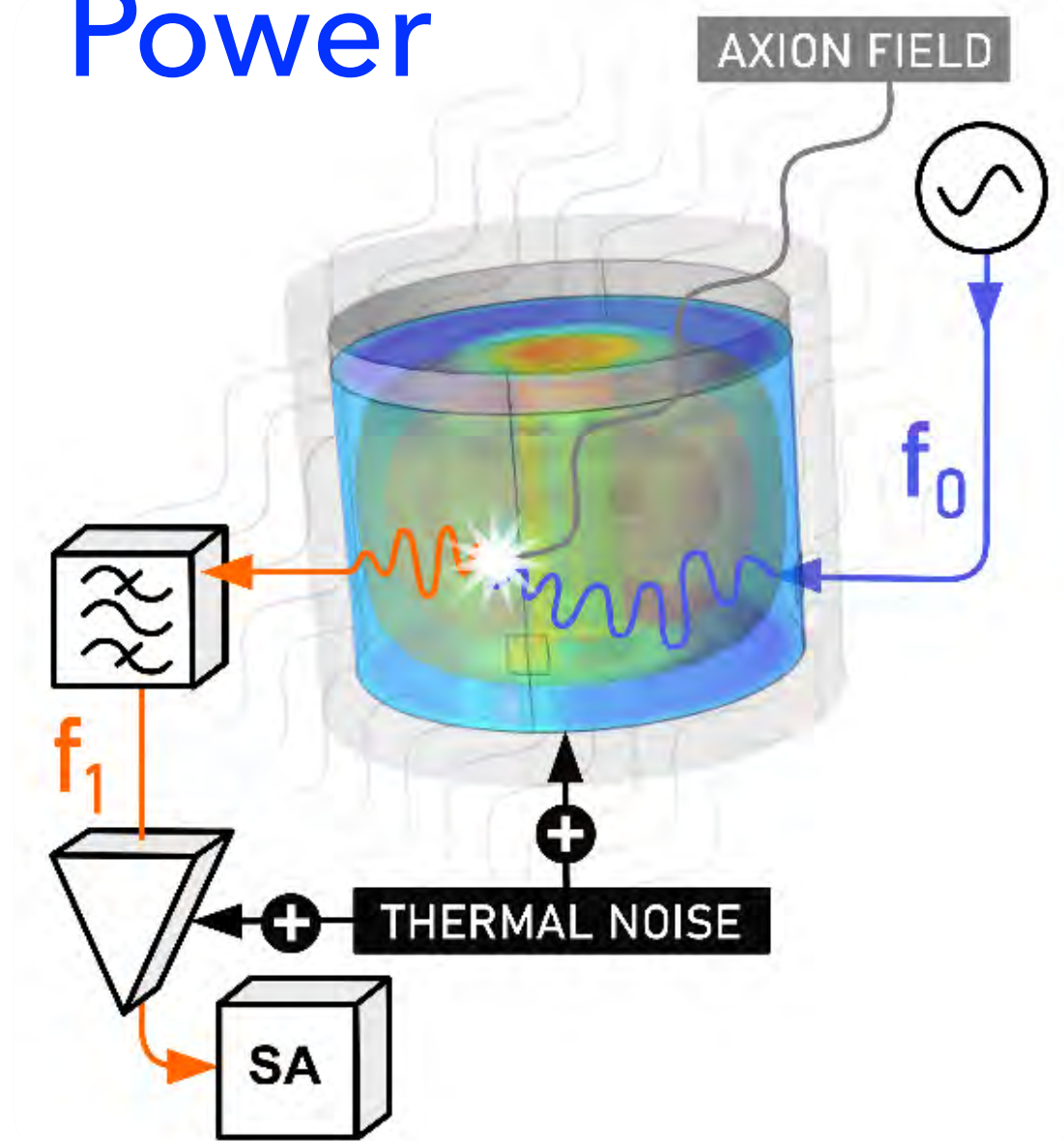
DC



AC Frequency



AC Power

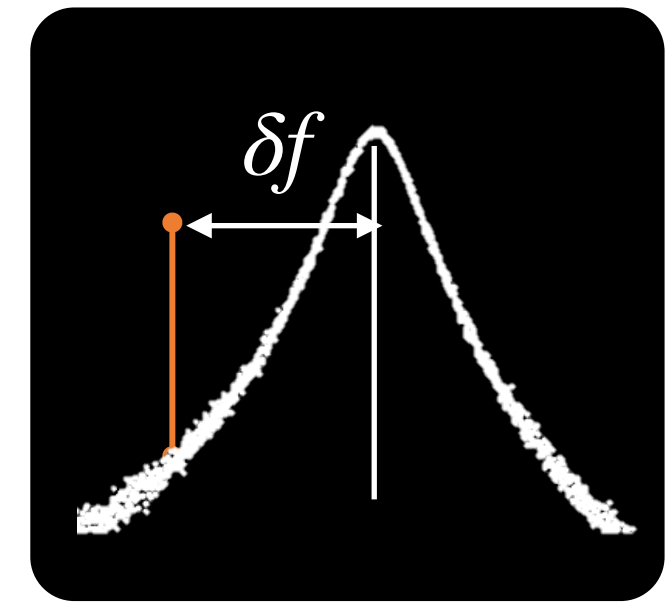


**Photon 1:** E field of cavity's resonant transverse magnetic mode,  $m_a = f_1 + \delta f$

**Photon 0,** Back ground DC B field of surrounding magnet

- Use a mode 0 as the background “magnetic field” AC source
- Two modes in one cylindrical cavity
- Upconversion limit  $m_a = |f_1 - f_0| + \delta f$

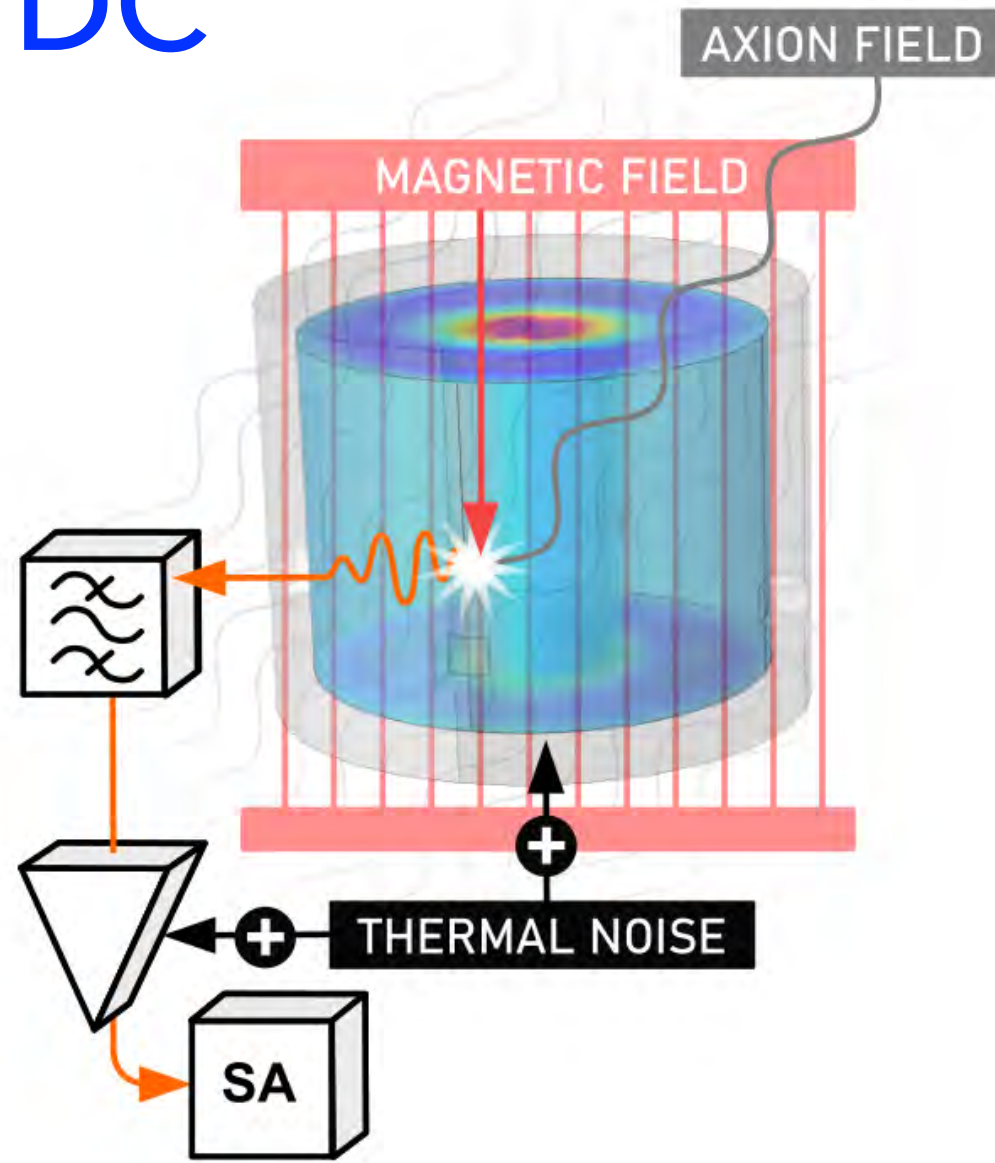
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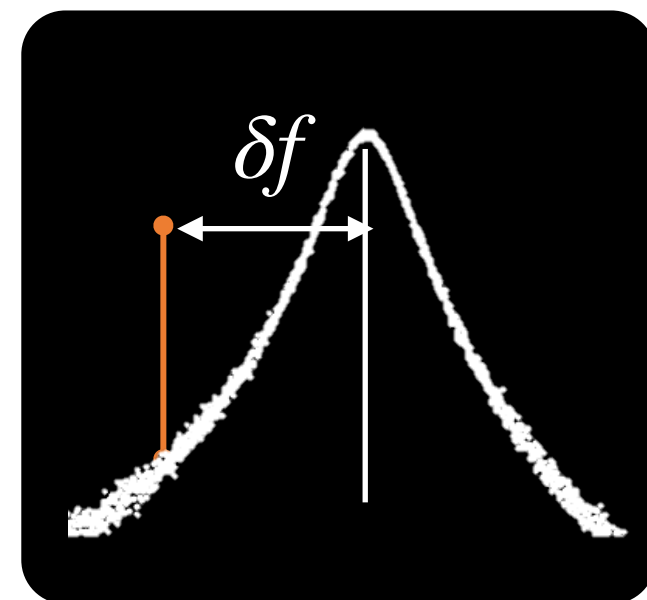
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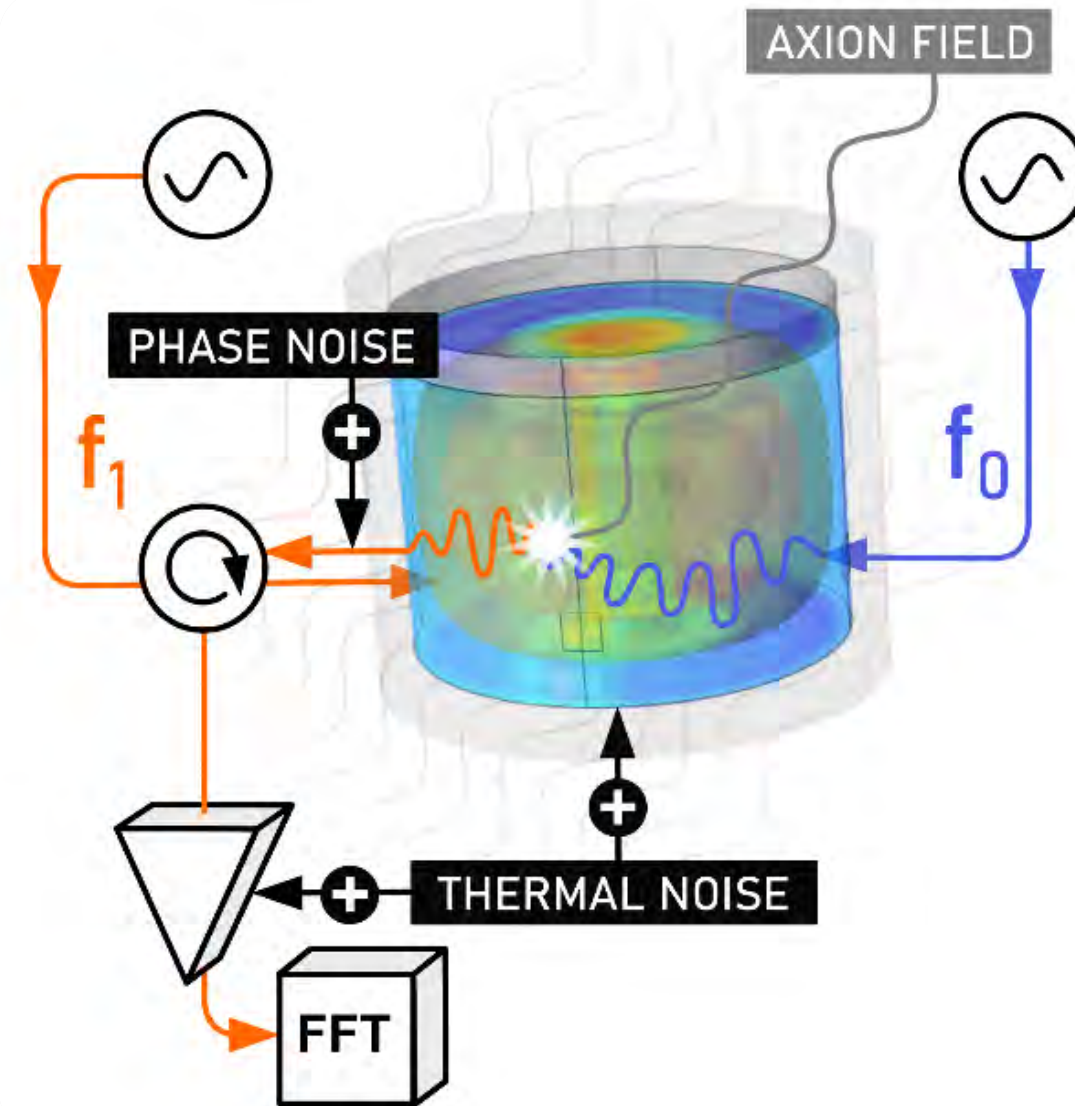
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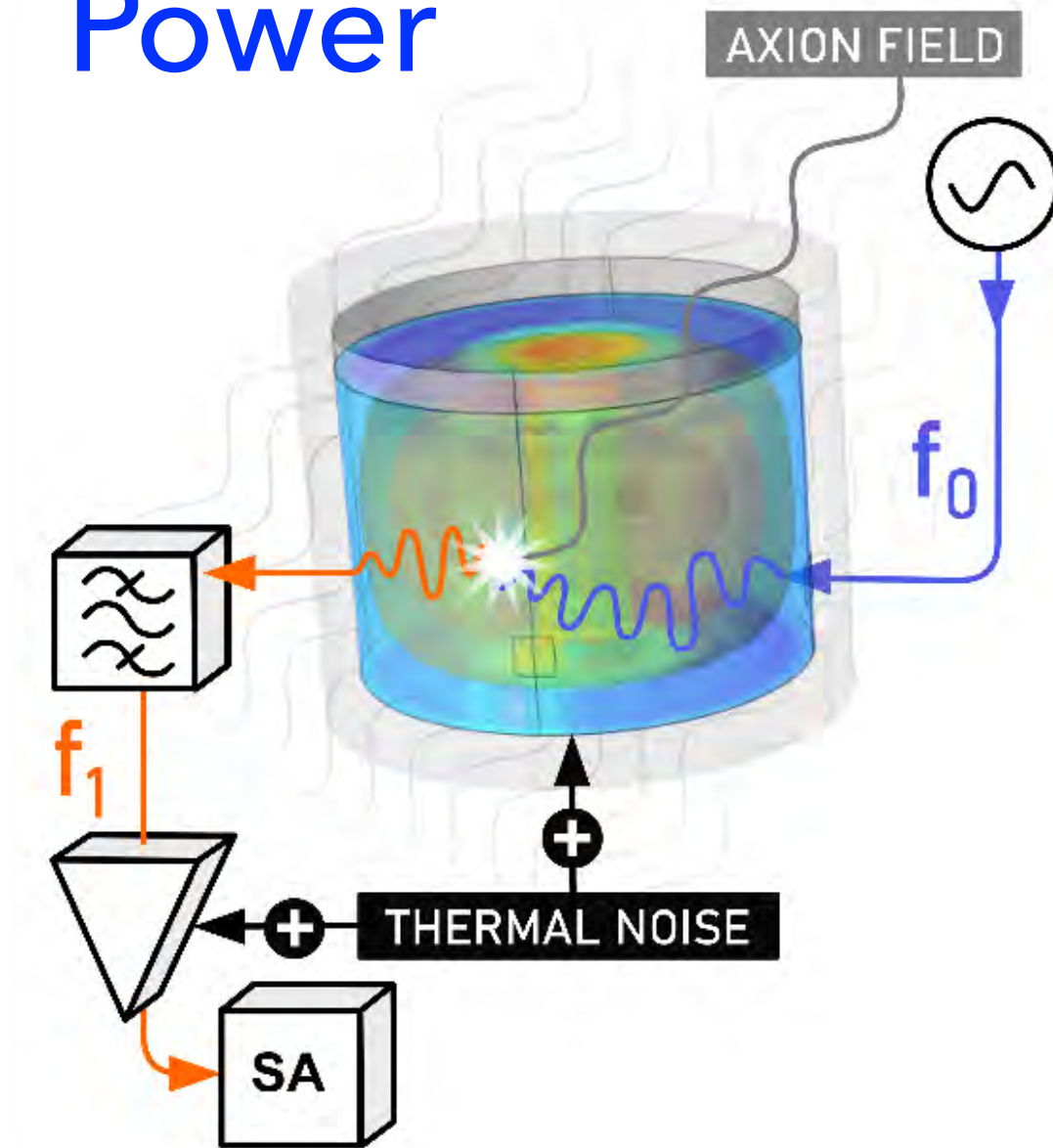


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Photon 1: Transverse Magnetic Mode

(Longitudinal Electric)

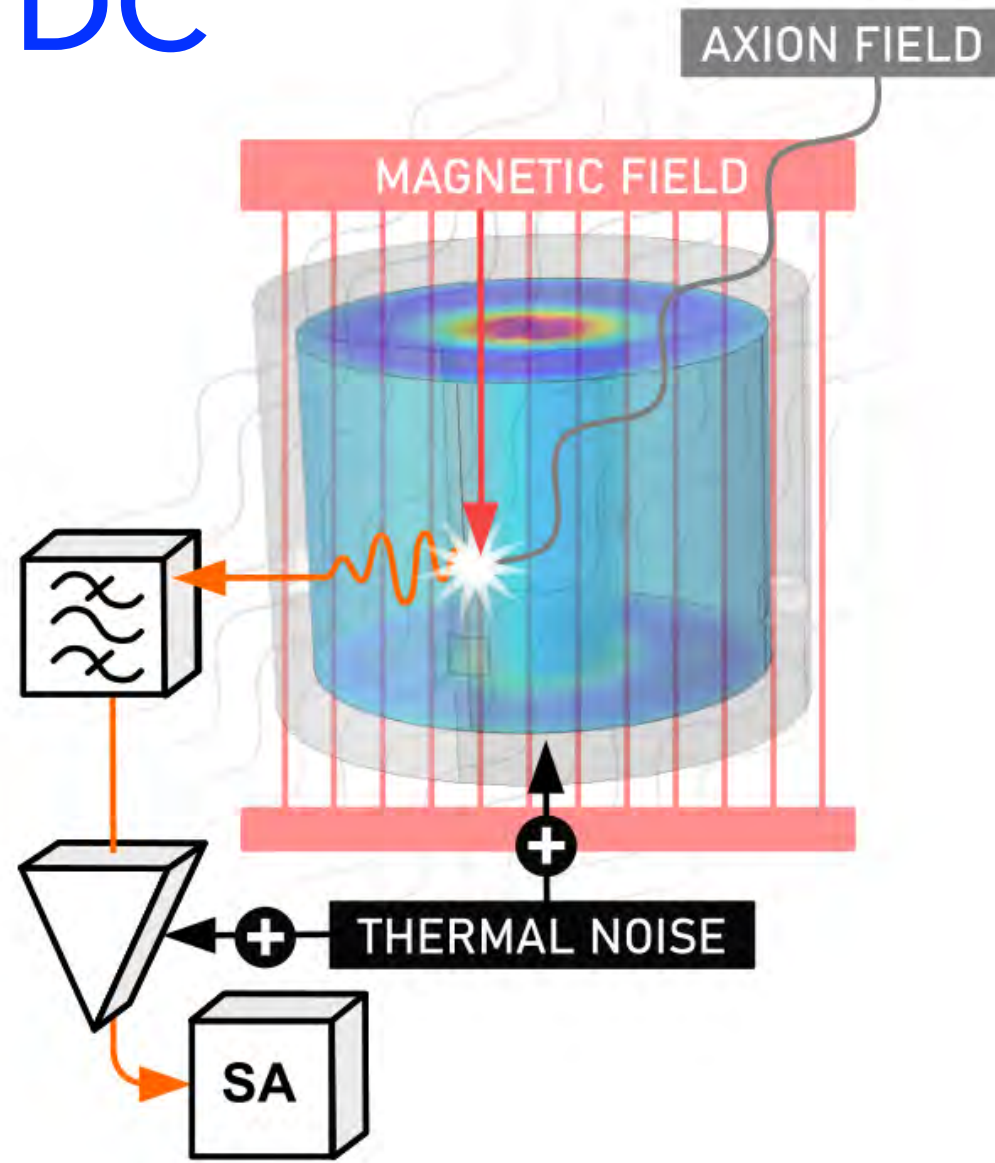
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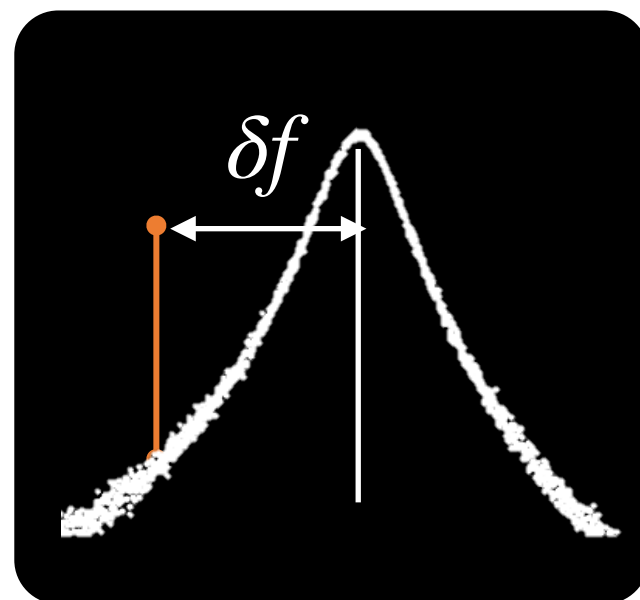
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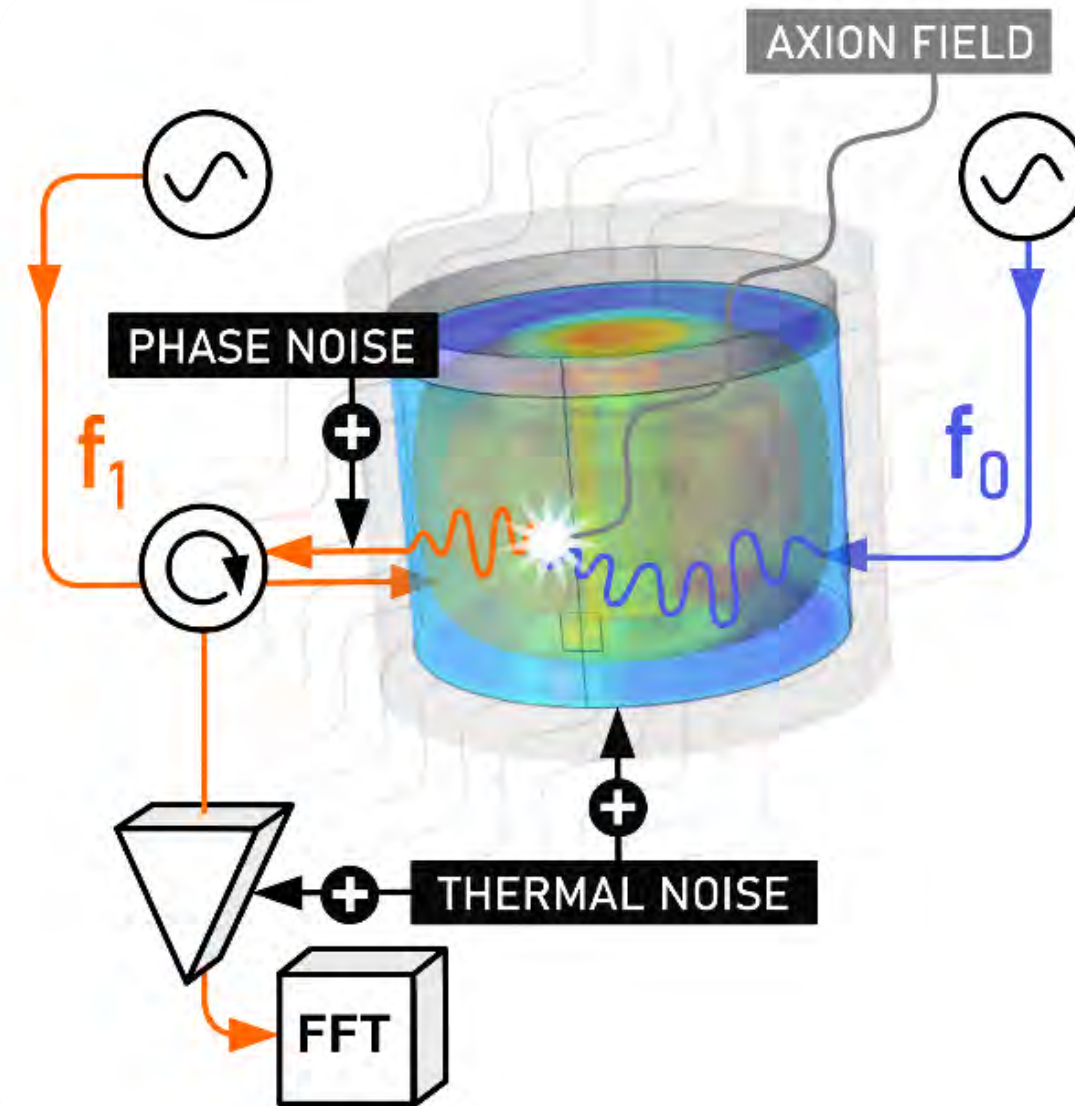
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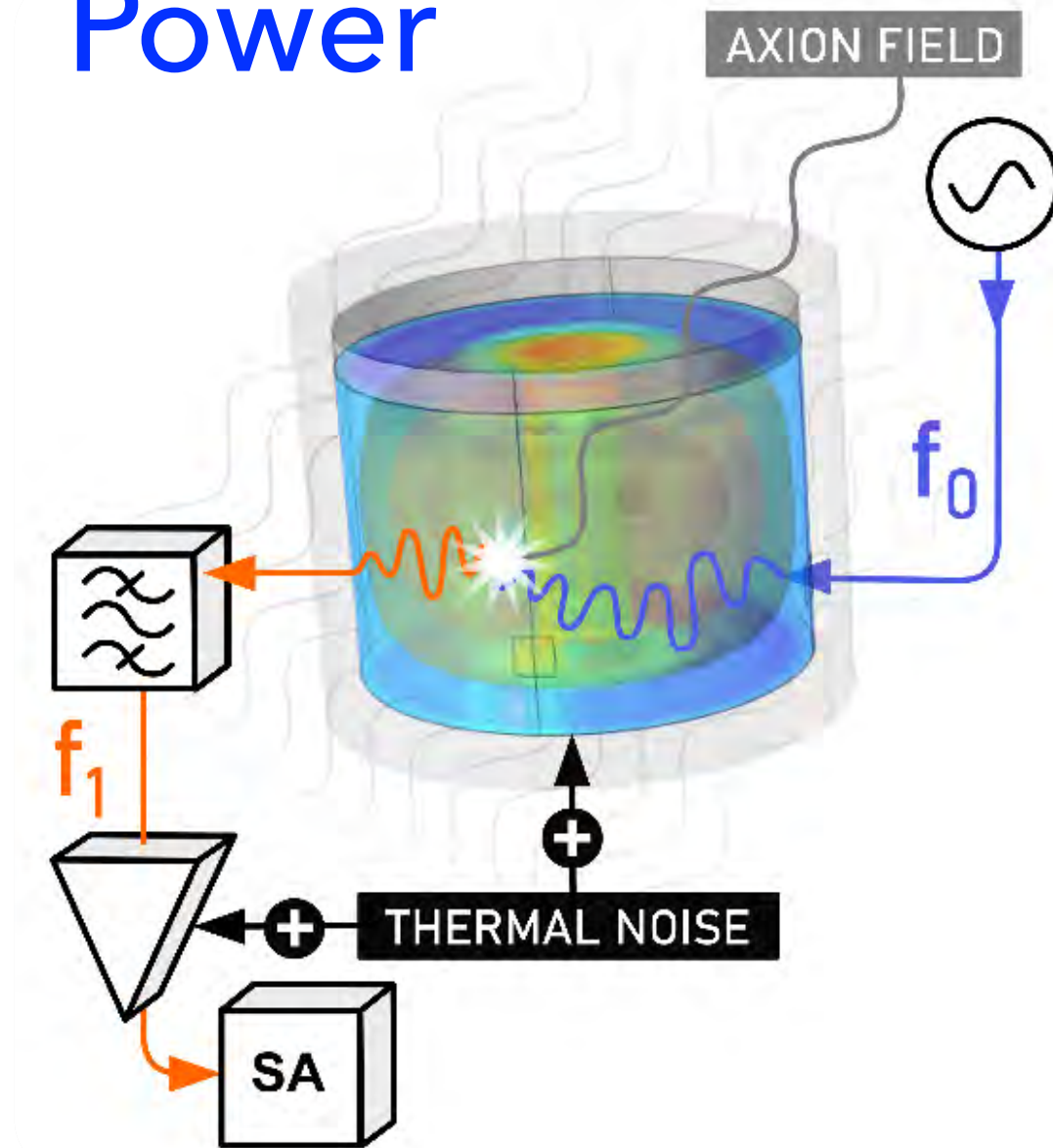


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AC Power



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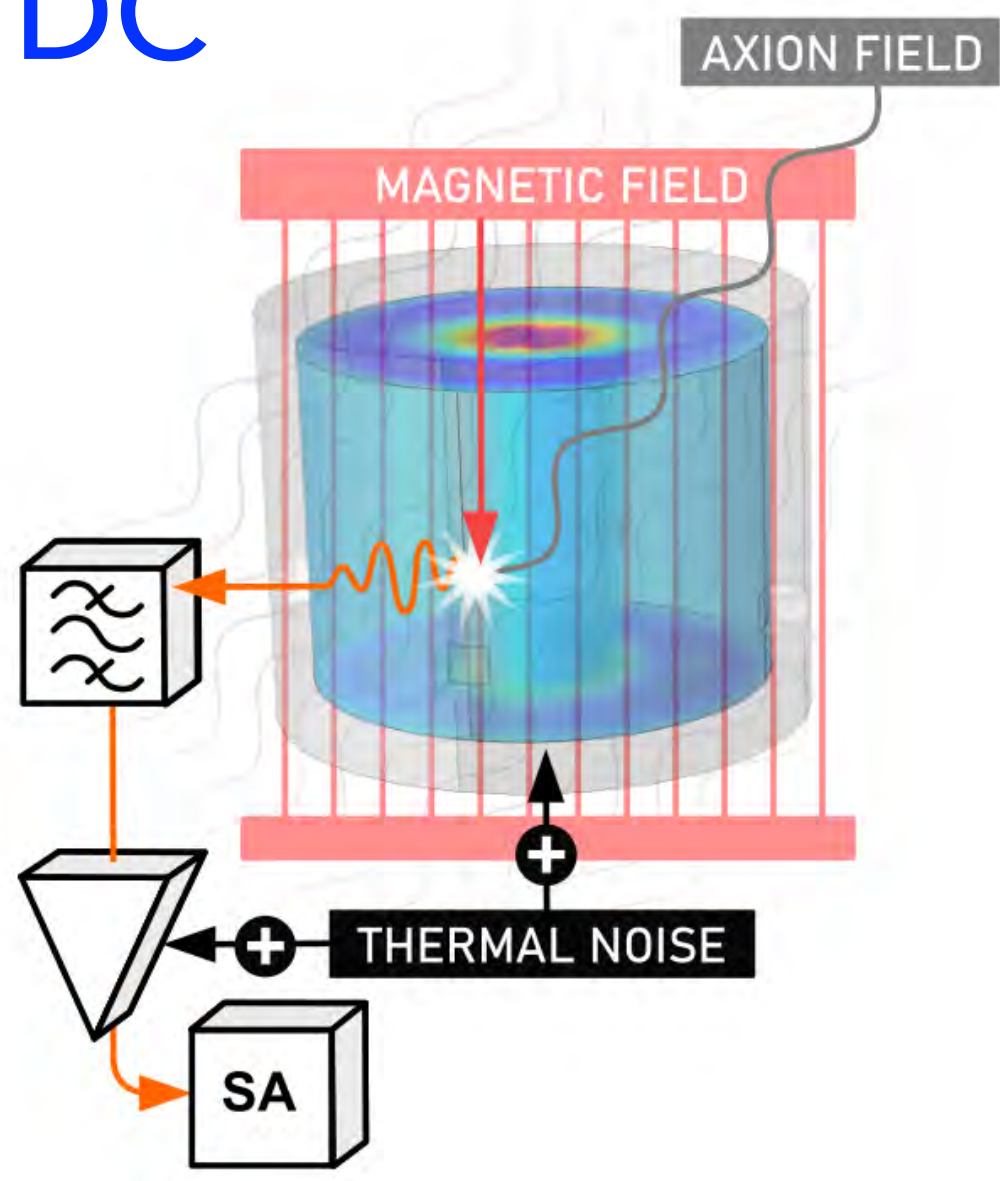
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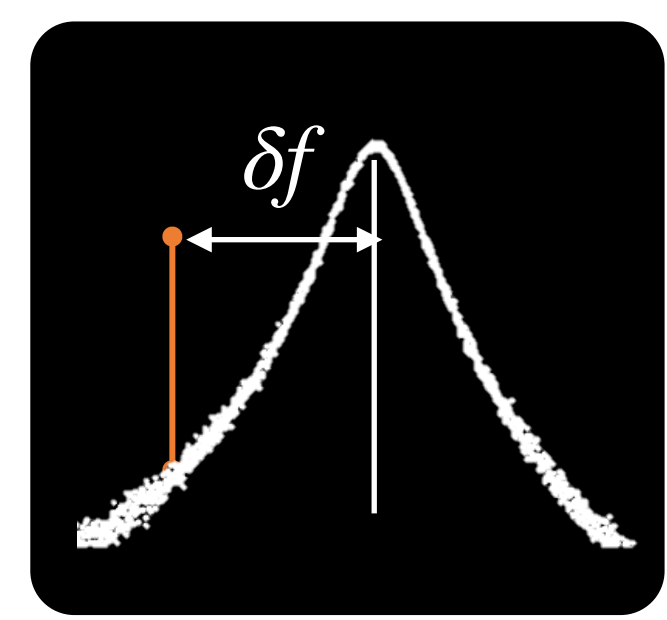
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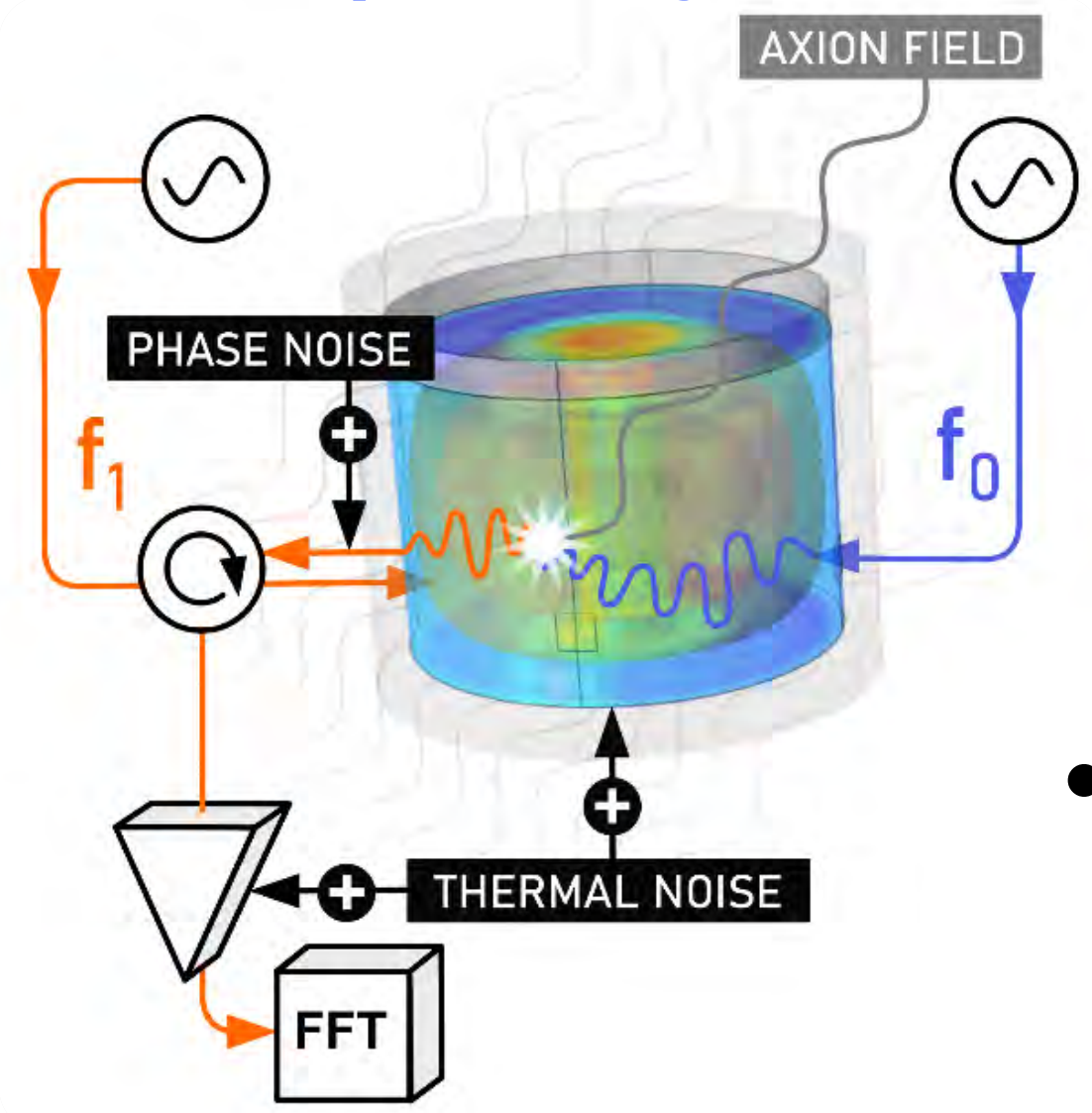
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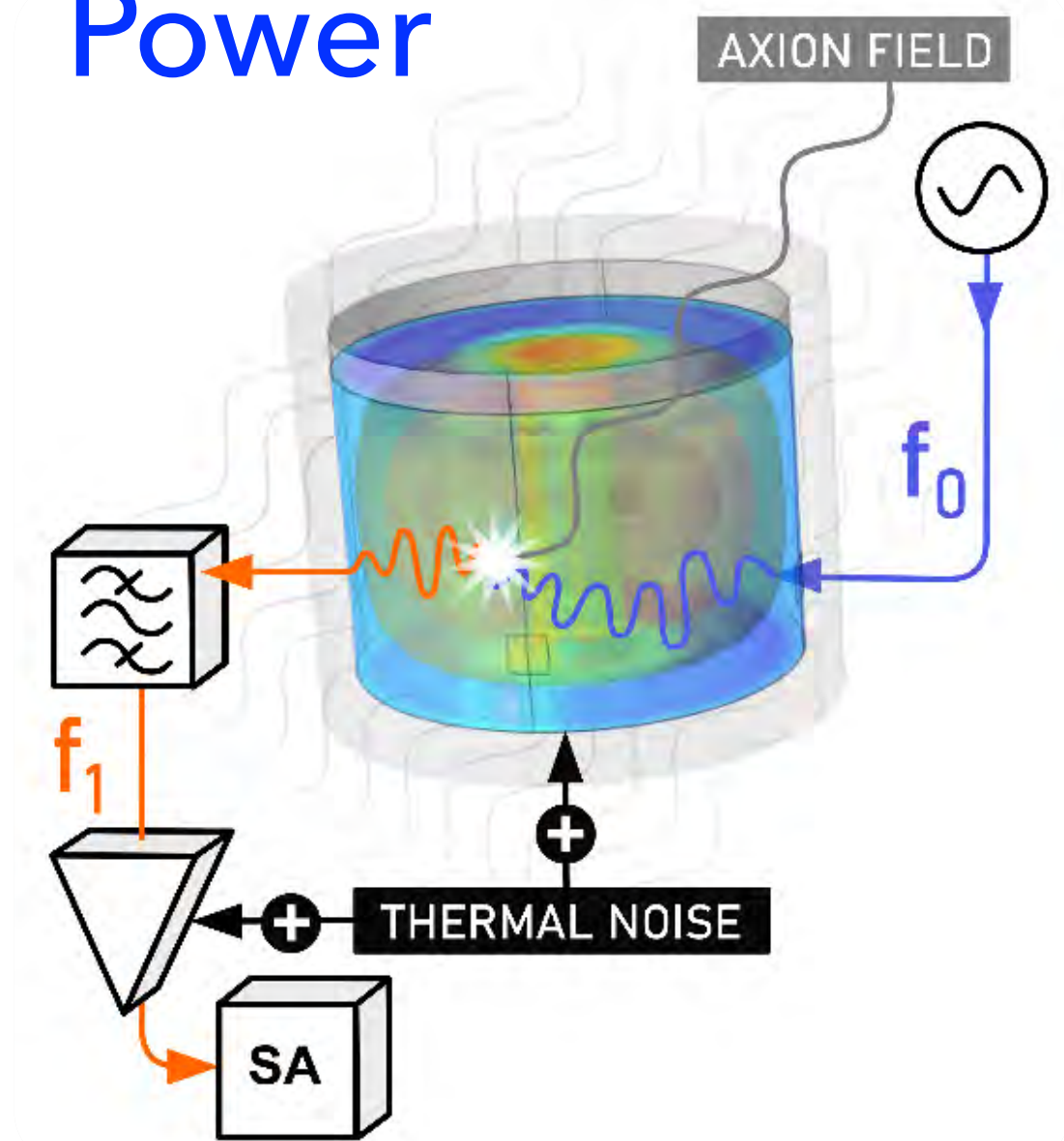
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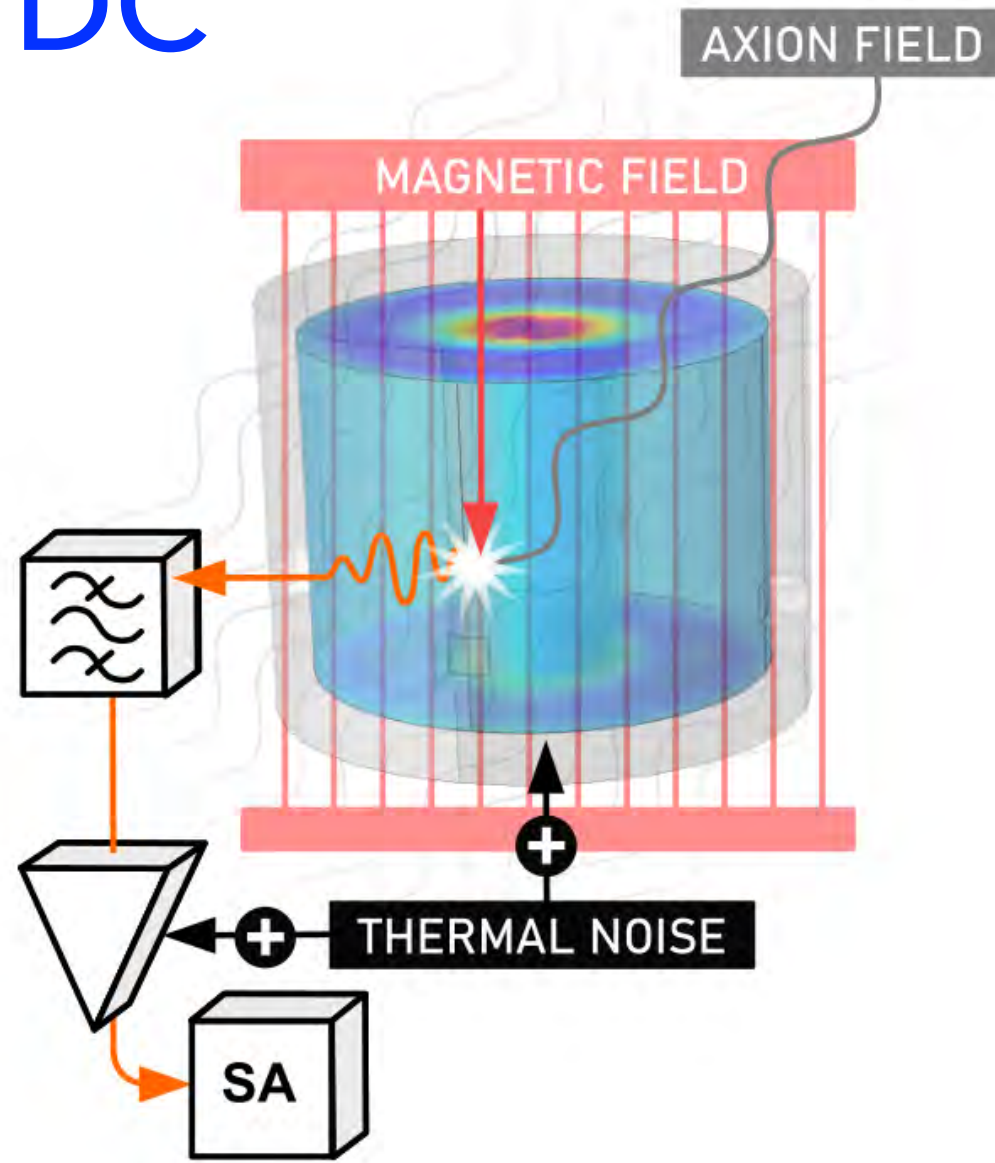
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• UPLOAD

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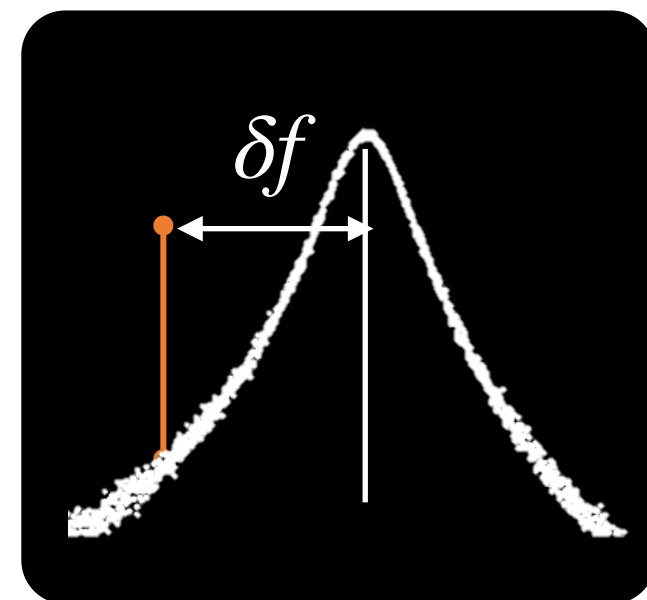
DC



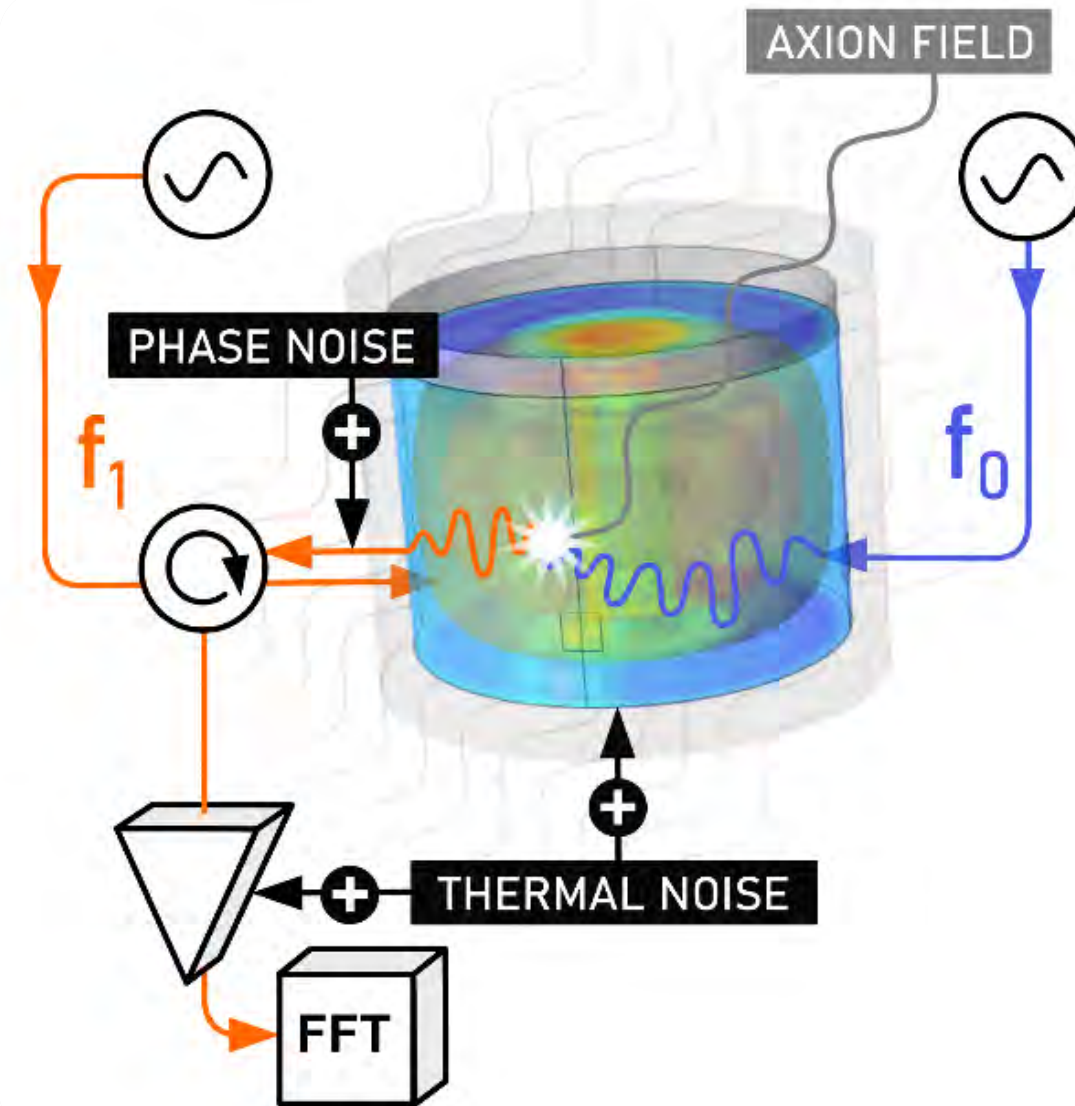
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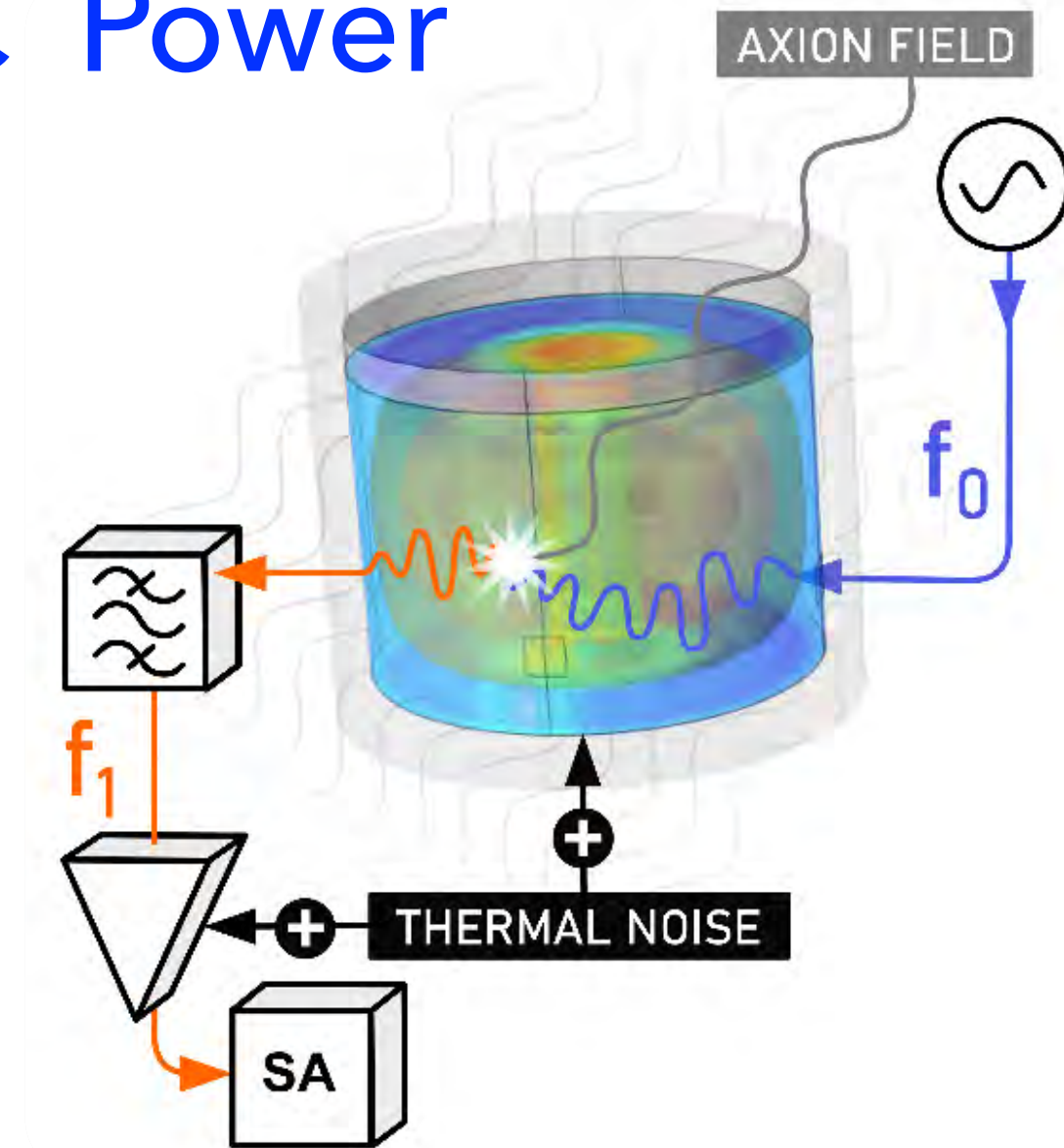
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AC Power



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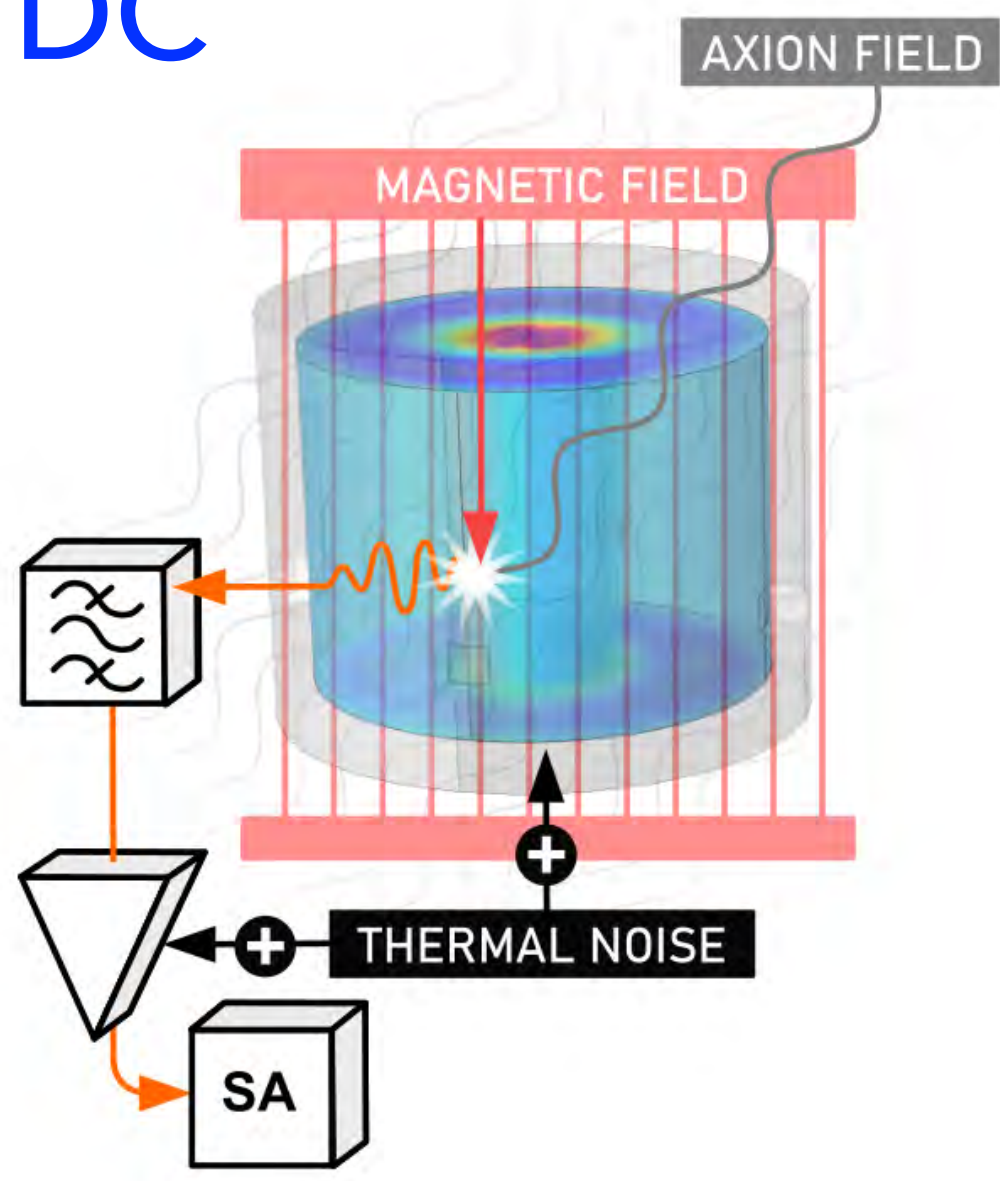
• UPLOAD

AC Frequency: Excite two modes: Measure  $f_1$  Frequency Fluctuation Spectrum

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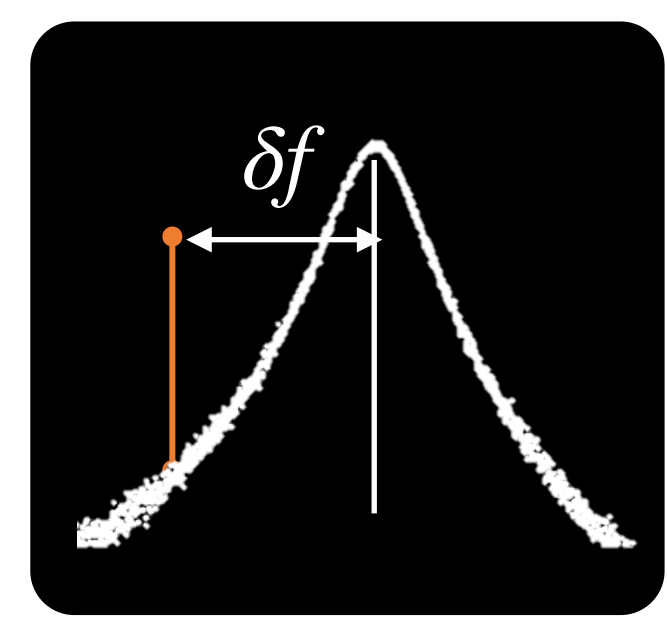
DC



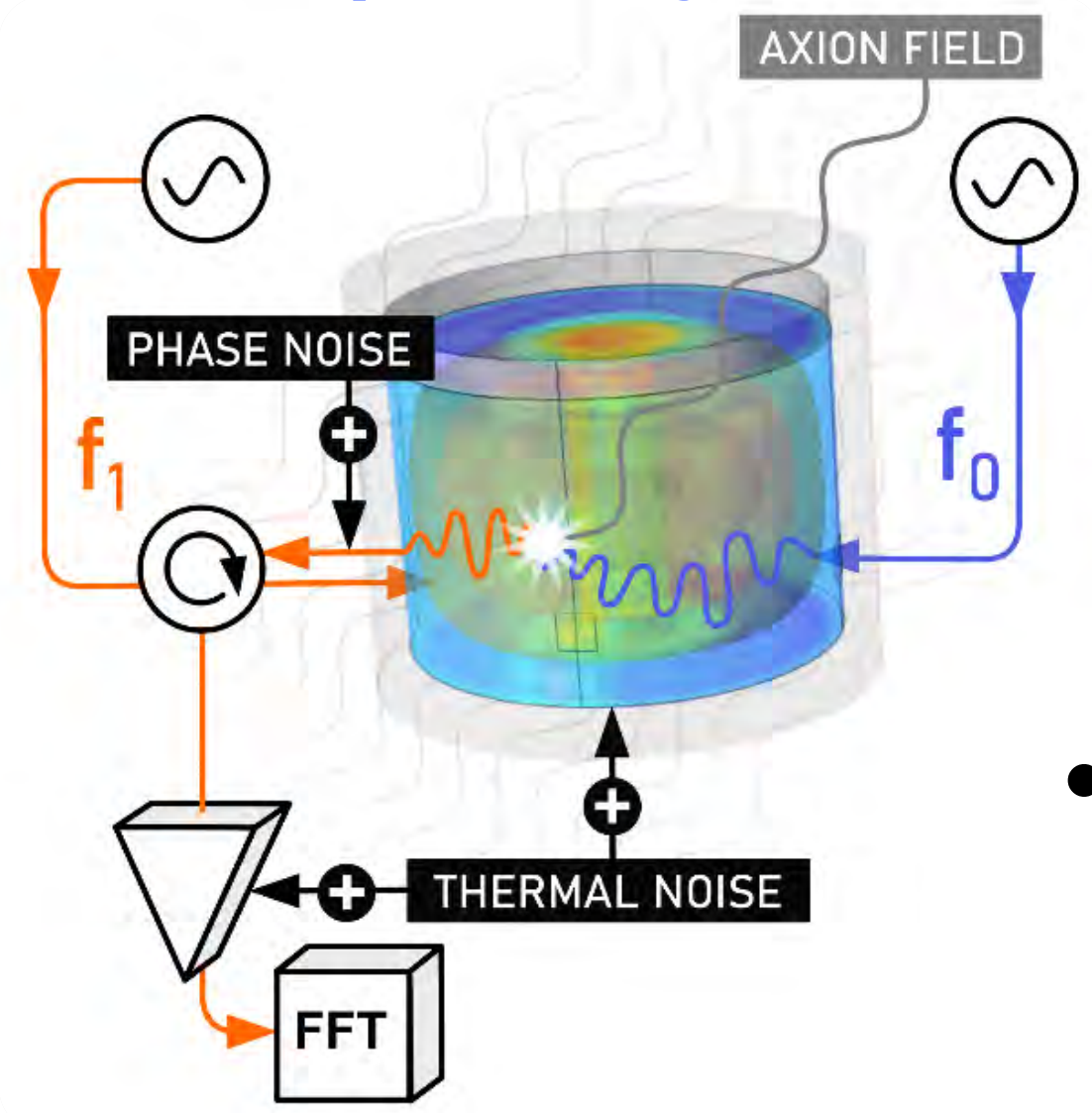
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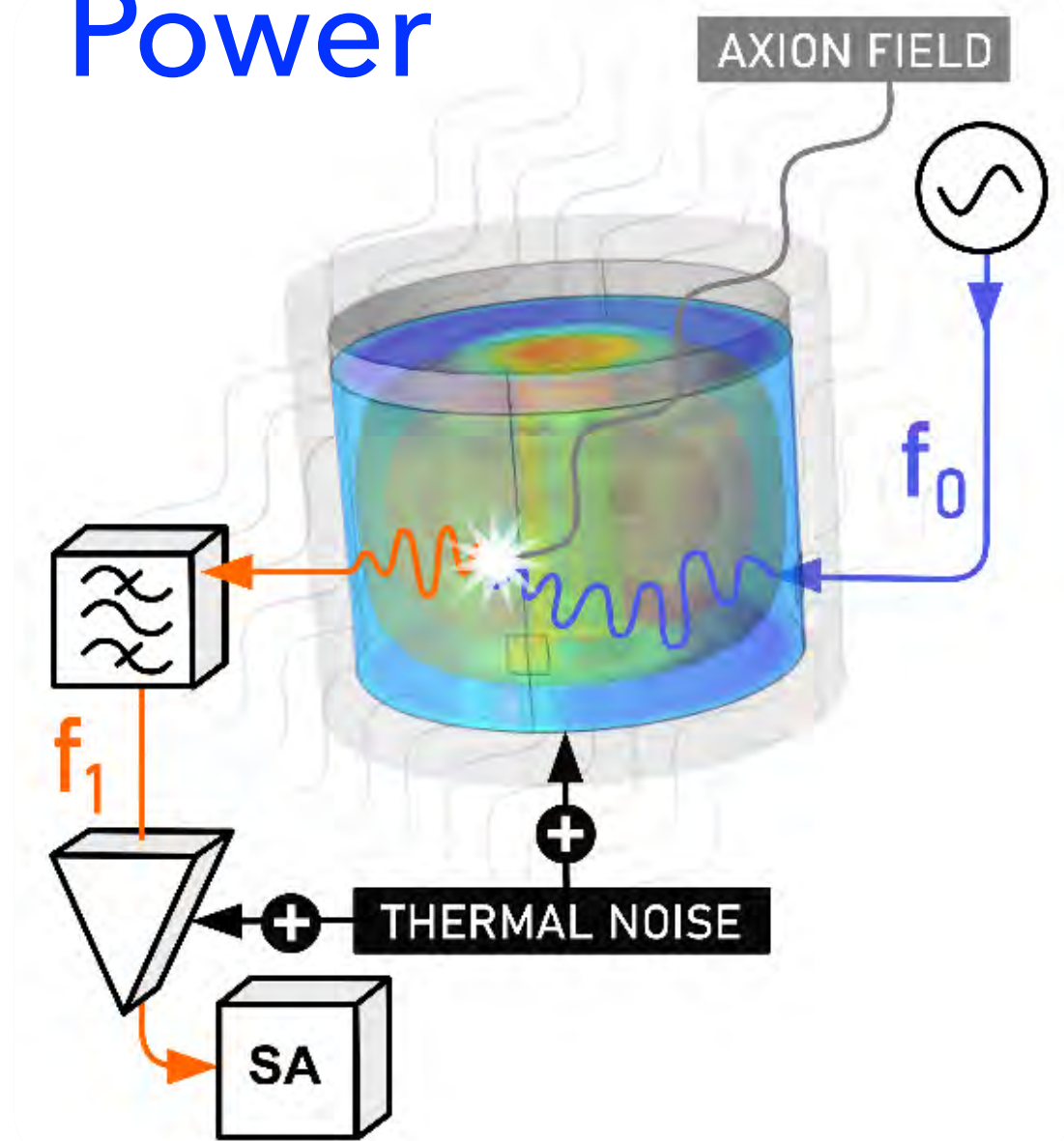
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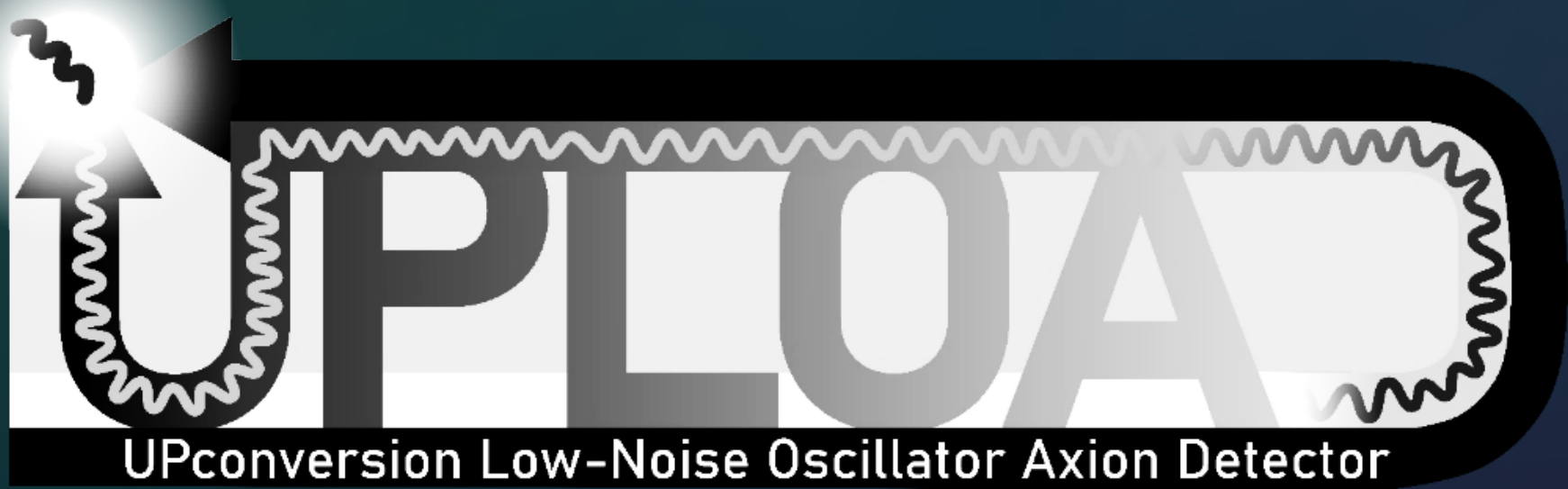


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(Longitudinal Magnetic)

AC Frequency: Excite two modes: Measure  $f_1$  Frequency Fluctuation Spectrum

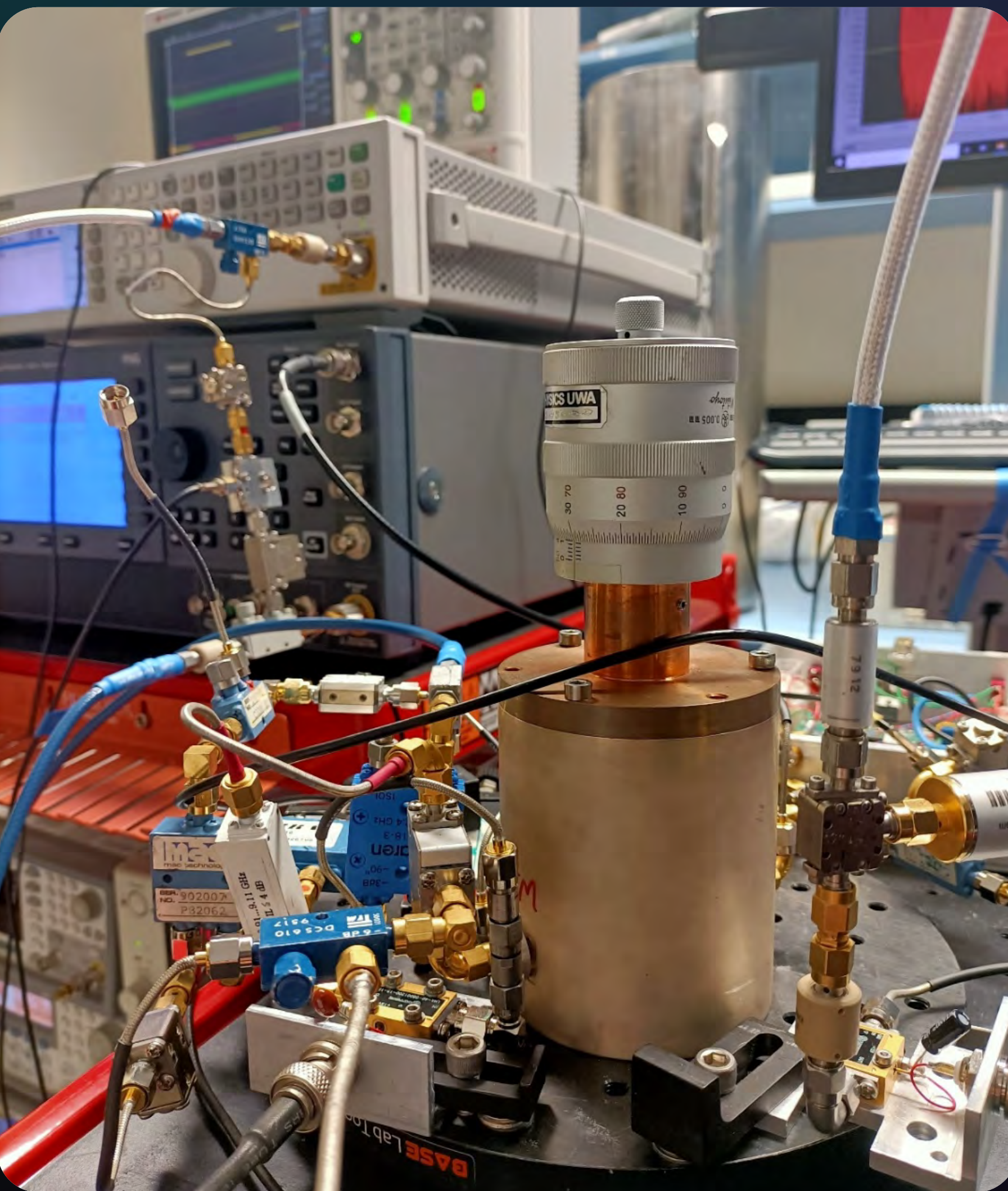
AC Power: Excite  $f_0$ : Measure  $f_1$  Power Fluctuation Spectrum

• UPLOAD



# UPconversion Low-Noise Oscillator Axion Detection Experiment

- Cavity resonator haloscope
- No externally applied magnetic field
- TM and TE modes ( ~ 9 GHz modes)
- Height Tunable
- Accessing MHz axions via upconversion



PHYSICAL REVIEW D **107**, 112003 (2023)

## Searching for low-mass axions using resonant upconversion

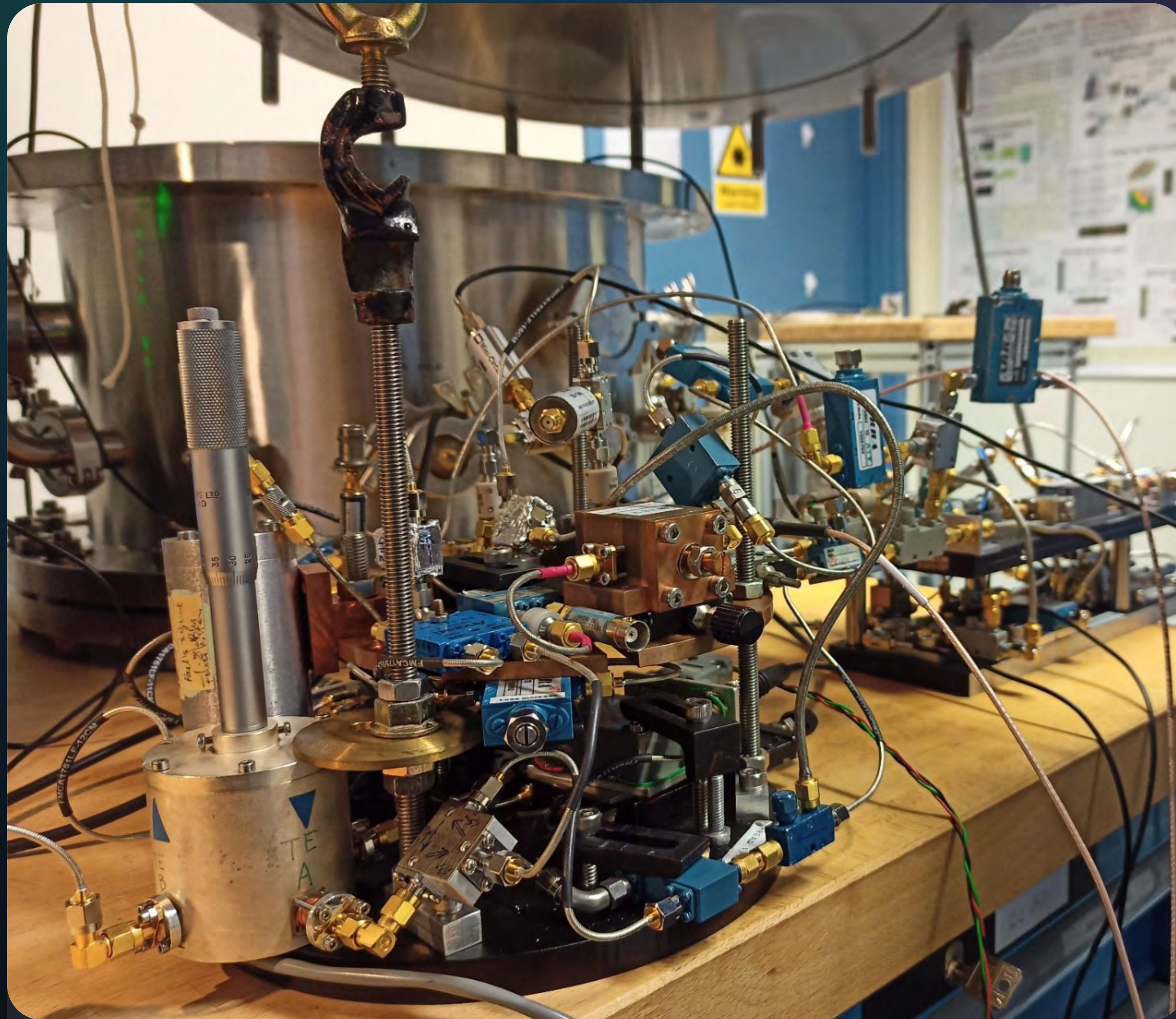
Catriona A. Thomson<sup>1,\*</sup>, Maxim Goryachev,<sup>1</sup> Ben T. McAllister,<sup>1,2</sup> Eugene N. Ivanov,<sup>1</sup>  
Paul Altin,<sup>3</sup> and Michael E. Tobar<sup>1,†</sup>

<sup>1</sup>*Quantum Technologies and Dark Matter Labs, Department of Physics, University of Western Australia,  
35 Stirling Highway, Crawley, Western Australia 6009, Australia*

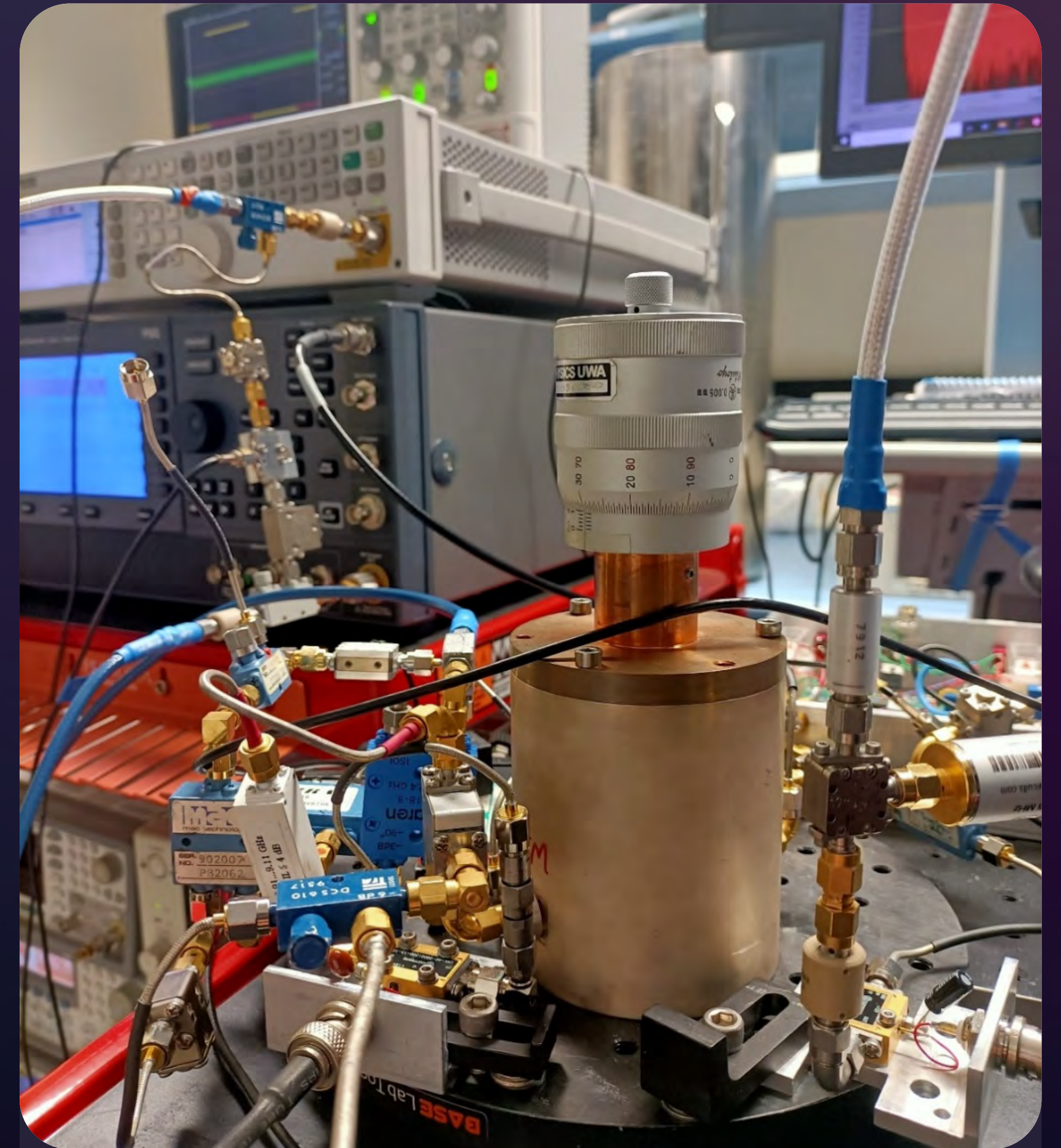
<sup>2</sup>*Centre for Astrophysics and Supercomputing, Swinburne University of Technology,  
John St, Hawthorn, Victoria 3122, Australia*

<sup>3</sup>*ARC Centre of Excellence For Engineered Quantum Systems, The Australian National University,  
Canberra, Australian Capital Territory 2600 Australia*

(Received 17 January 2023; accepted 5 May 2023; published 5 June 2023)

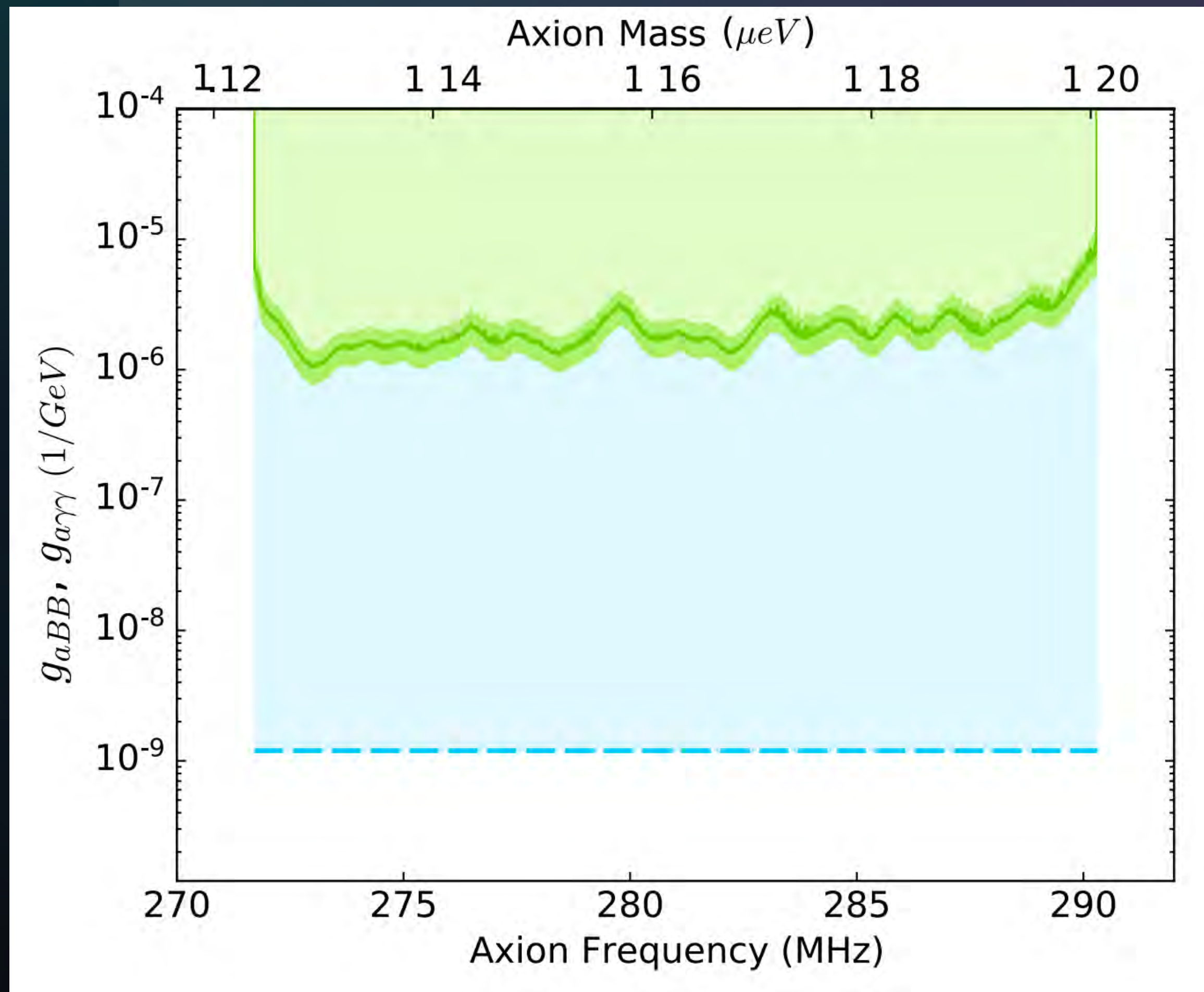


V1: readout via frequency metrology



V2: readout via thermal noise peak  
(power)

# UPLOAD V2: Exclusion limits



PHYSICAL REVIEW D **107**, 112003 (2023)

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Paul Altin,<sup>3</sup> and Michael E. Tobar<sup>1,†</sup>

FIG. 7. In green, the 95% confidence axion exclusion zone for both  $g_{a\gamma\gamma}$  and  $g_{aBB}$  for the measured mass range between 1.12 – 1.20  $\mu eV$  (271.7 MHz—290.3 MHz) for a measurement period of 30 days, which is an improvement of 3 orders of magnitude over our previous result [29]. The bright green region represents the uncertainty on excluded  $g_{a\gamma\gamma}$ , which is detailed in Appendix C. The blue dashed line represents the approximate sensitivity achievable with a niobium resonator of loaded quality factors around  $10^7$  and cooled to a temperature of 4 K, measuring for a period of 30 days, and using a cryogenic amplifier of noise temperature 4 K. Construction for this setup is underway.

# UPLOAD V3: Cryogenic Niobium

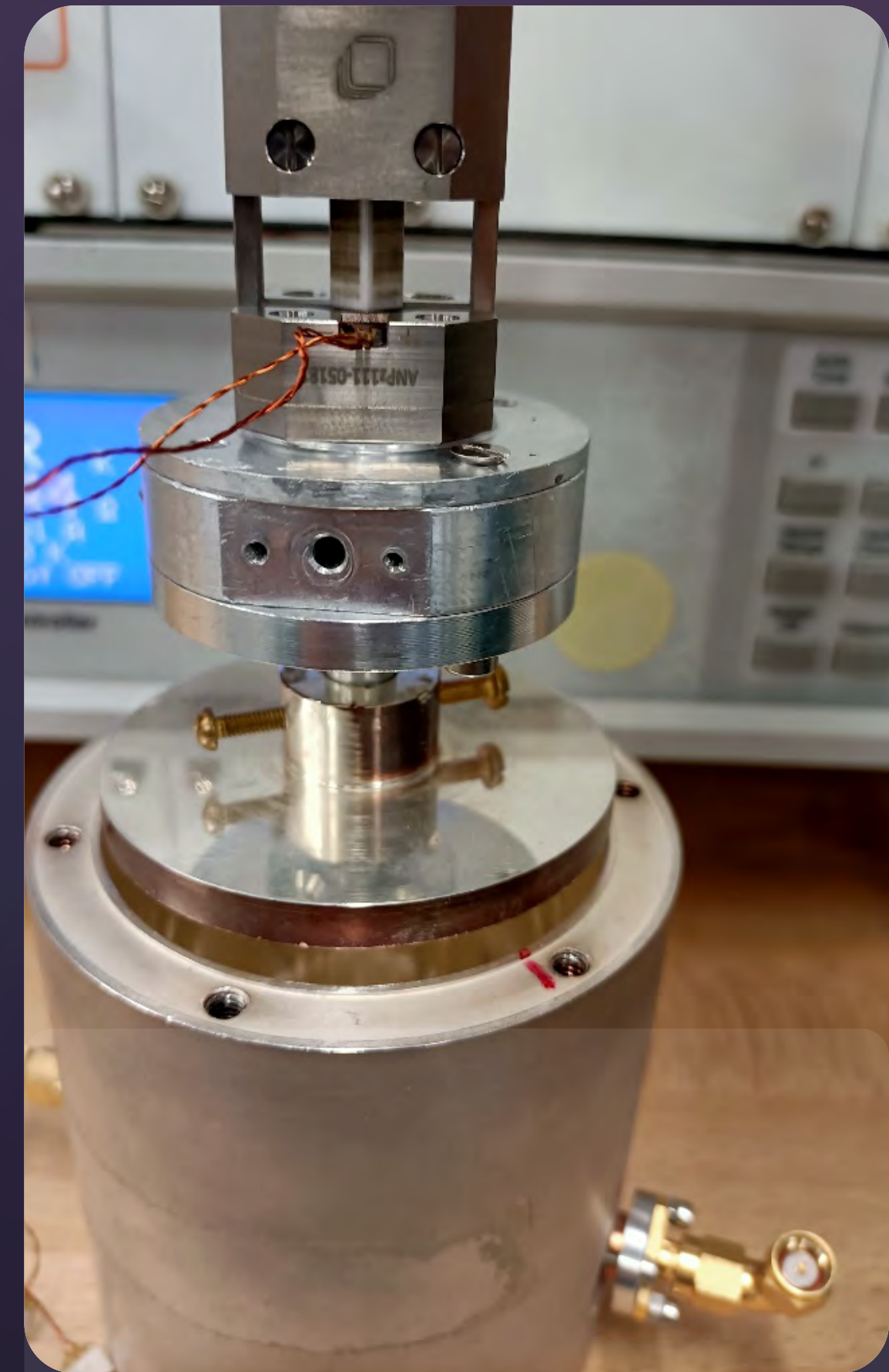
An experiment targeting 350 MHz axions with a dual mode cavity (~12 GHz), height tuning with a piezo actuated lid. Gain in noise temperature and quality factor.

290 K → 4 K

$$\langle H \rangle = k_B T$$

$$g_{a\gamma\gamma} = \frac{\frac{f_a}{\sqrt{f_1 f_0}} \frac{(2\sqrt{2}\sqrt{\beta_1\beta_0})}{\sqrt{1+\beta_1(\beta_0+1)}} \sqrt{P_a}}{\sqrt{1+4(Q_{L1})^2 \left(\frac{f_a+f_0-f_1}{f_1}\right)^2}} \frac{2\pi f_a}{\sqrt{\rho c^3}} \sqrt{Q_{L1} Q_{L0} FFP_{0inc}}$$

Q ~ 13,000 → > 20,000,000



Trialing attocube actuator in silver plated cavity

# If Magnetic Charge Exist at High Energy

-> Further Modifications to Axion Electrodynamics

arXiv > hep-ph > arXiv:2303.10170

High Energy Physics – Phenomenology

[Submitted on 17 Mar 2023]

## Generic axion Maxwell equations: path integral approach

Anton V. Sokolov, Andreas Ringwald

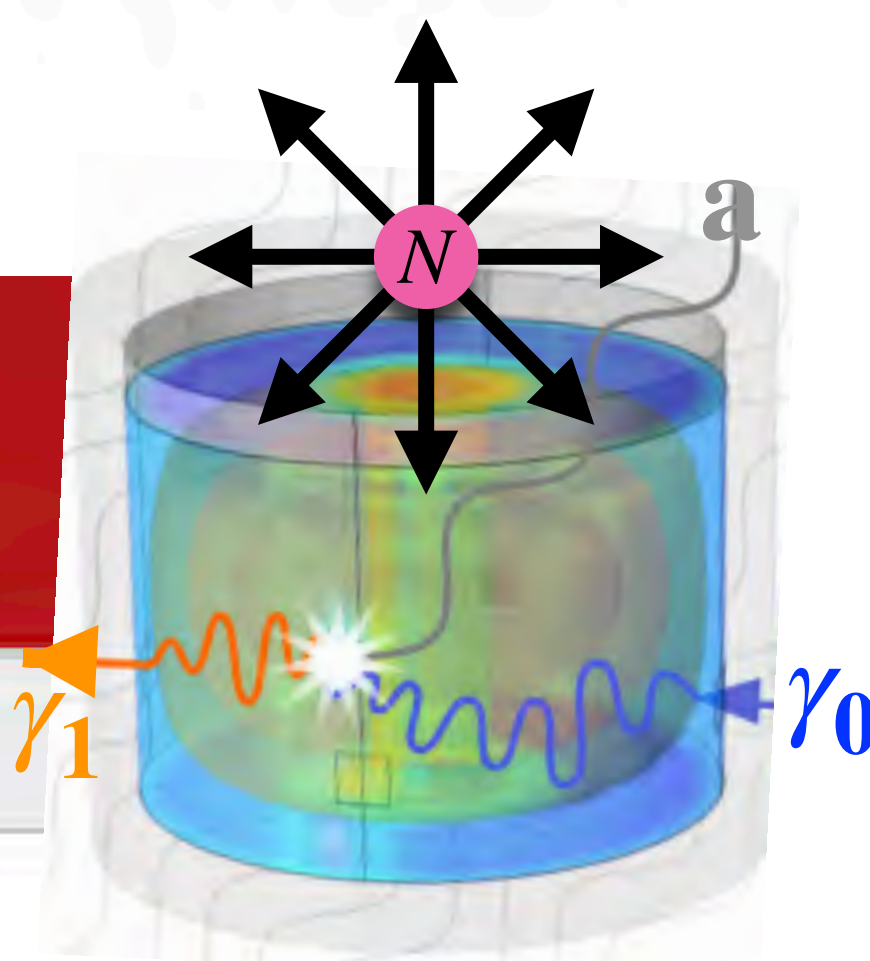
arXiv > hep-ph > arXiv:2205.02605

High Energy Physics – Phenomenology

[Submitted on 5 May 2022]

## Electromagnetic Couplings of Axions

Anton V. Sokolov, Andreas Ringwald





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-> Can test the existence of Magnetic Charge through Axions

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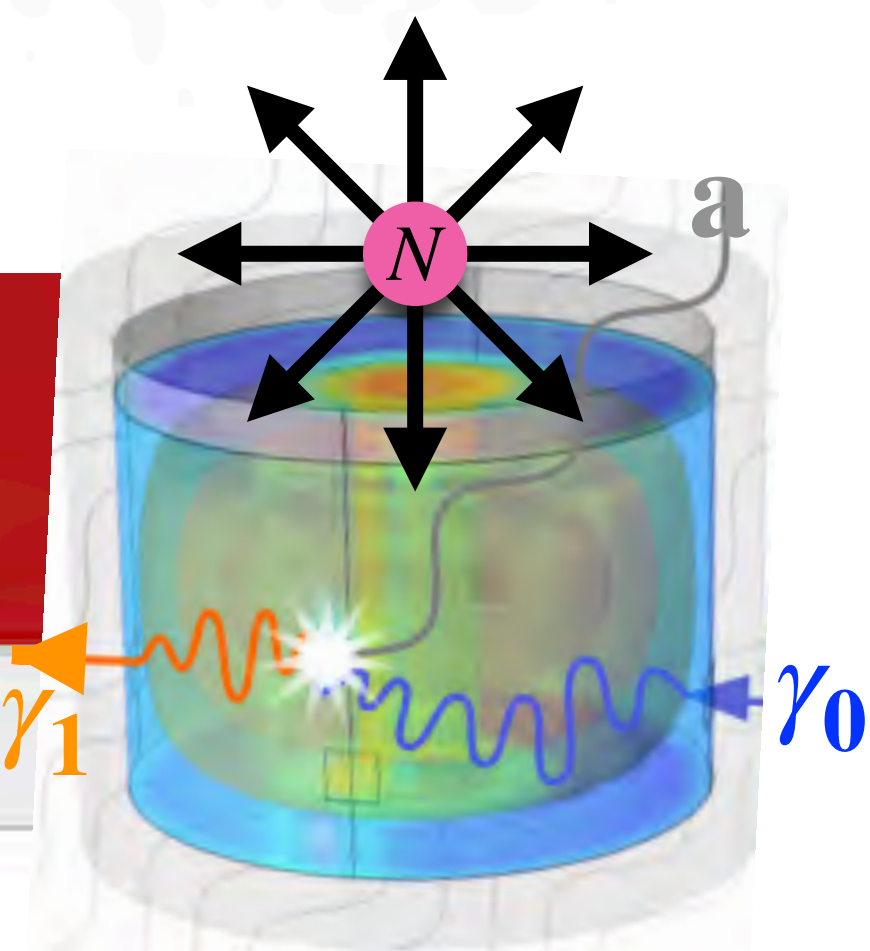
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The diagram shows a cylindrical container with a blue liquid inside. At the top center of the container, there is a pink circle labeled 'N', representing a magnetic charge. Eight black arrows radiate outwards from this charge. A blue wavy line labeled  $\gamma_0$  and an orange wavy line labeled  $\gamma_1$  are shown near the bottom of the container, representing electromagnetic radiation. A small 'a' is also visible near the top right of the container.

# If Magnetic Charge Exist at High Energy

-> Further Modifications to Axion Electrodynamics

-> Can test the existence of Magnetic Charge through Axions

Axion-photon coupling parameter space is expanded from one parameter to three

$$g_{a\gamma\gamma} \rightarrow (g_{a\gamma\gamma}, g_{aEM}, g_{aMM})$$

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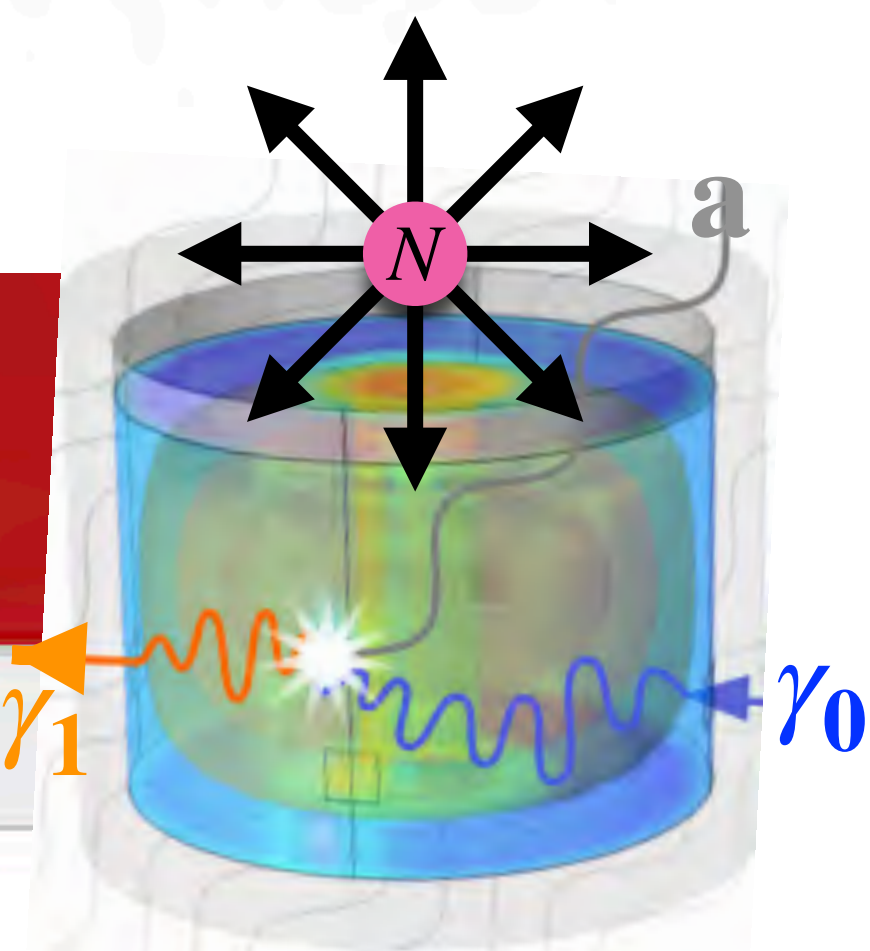
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-> Further Modifications to Axion Electrodynamics

-> Can test the existence of Magnetic Charge through Axions

Axion-photon coupling parameter space is expanded from one parameter to three

$$g_{a\gamma\gamma} \rightarrow (g_{a\gamma\gamma}, g_{aEM}, g_{aMM})$$

$$\vec{\nabla} \cdot \vec{E}_1 = g_{a\gamma\gamma} c \vec{B}_0 \cdot \vec{\nabla} a - g_{aEM} \vec{E}_0 \cdot \vec{\nabla} a + \epsilon_0^{-1} \rho_{e1},$$

$$\begin{aligned} \mu_0^{-1} \vec{\nabla} \times \vec{B}_1 &= \epsilon_0 \partial_t \vec{E}_1 + \vec{J}_{e1} \\ &+ g_{a\gamma\gamma} c \epsilon_0 \left( -\vec{\nabla} a \times \vec{E}_0 - \partial_t a \vec{B}_0 \right) \\ &+ g_{aEM} \epsilon_0 \left( -\vec{\nabla} a \times c^2 \vec{B}_0 + \partial_t a \vec{E}_0 \right), \end{aligned}$$

$$\vec{\nabla} \cdot \vec{B}_1 = -\frac{g_{aMM}}{c} \vec{E}_0 \cdot \vec{\nabla} a + g_{aEM} \vec{B}_0 \cdot \vec{\nabla} a,$$

$$\begin{aligned} \vec{\nabla} \times \vec{E}_1 &= -\partial_t \vec{B}_1 + \frac{g_{aMM}}{c} \left( c^2 \nabla a \times \vec{B}_0 - \partial_t a \vec{E}_0 \right) \\ &+ g_{aEM} \left( \nabla a \times \vec{E}_0 + \partial_t a \vec{B}_0 \right). \end{aligned}$$

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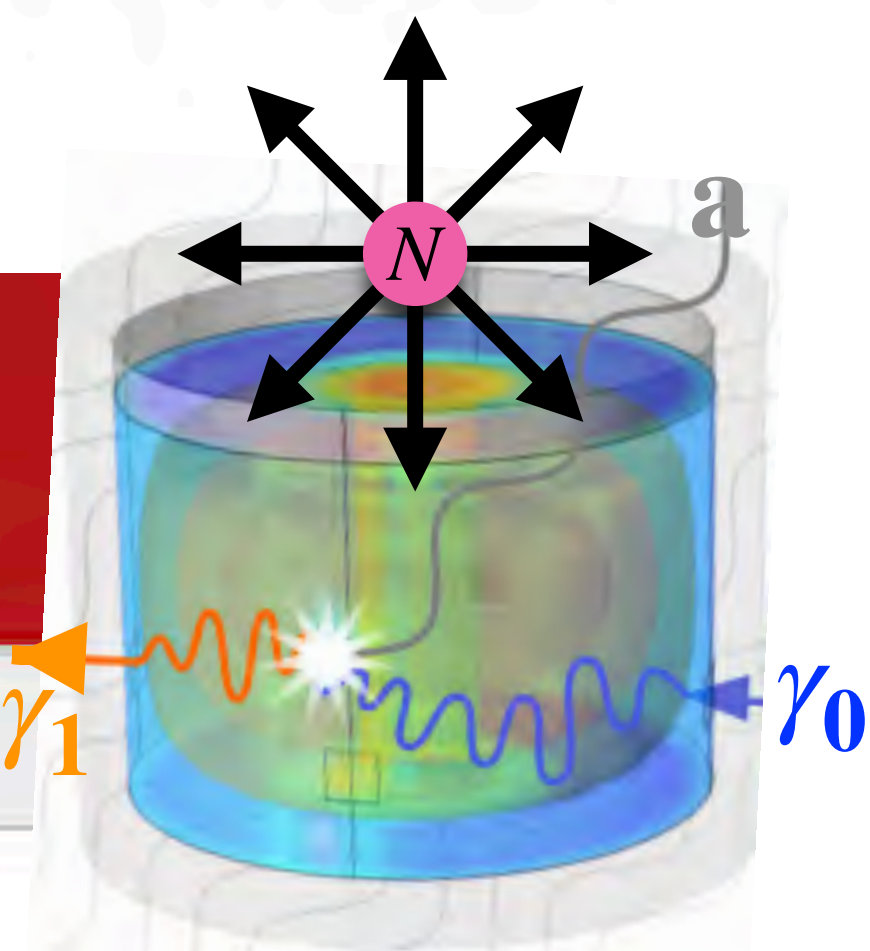
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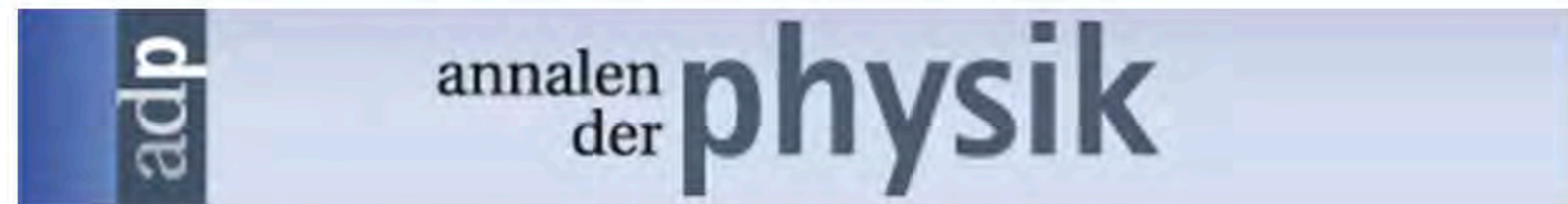


**Calculate Form Factors for Resonant Experiment with Static and Time varying Background Electric and Magnetic Fields -> Poynting Theorem**

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Michael E. Tobar , Catriona A. Thomson, Benjamin T. McAllister, Maxim Goryachev, Anton V. Sokolov, Andreas Ringwald

First published: 22 April 2023 | <https://doi.org/10.1002/andp.202200594>

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PHYSICAL REVIEW D **108**, 035024 (2023)

## Searching for GUT-scale QCD axions and monopoles with a high-voltage capacitor

Michael E. Tobar ,<sup>1,\*</sup> Anton V. Sokolov ,<sup>2</sup> Andreas Ringwald ,<sup>3</sup> and Maxim Goryachev<sup>1</sup>

<sup>1</sup>Quantum Technologies and Dark Matter Labs, Department of Physics, University of Western Australia, 35 Stirling Highway, Crawley, Western Australia 6009, Australia

<sup>2</sup>Department of Mathematical Sciences, University of Liverpool, Liverpool, L69 7ZL, United Kingdom

<sup>3</sup>Deutsches Elektronen-Synchrotron DESY, Notkestraße 85, 22607 Hamburg, Germany

(Received 20 June 2023; accepted 2 August 2023; published 17 August 2023)

arXiv:2306.13320v1 [hep-ph] 23 Jun 2023



# SENSITIVITY OF AXION RESONANT HALOSCOPES UNDER DC MAGNETIC FIELDS

$$P_{s1} = P_d = \frac{\omega_1 U_1}{Q_1} = g_{a\gamma\gamma} \frac{\omega_a \epsilon_0 \langle a_0 \rangle}{\sqrt{2} Q_1} \int \vec{B}_0 \cdot \text{Re}(\mathbf{E}_1) dV + g_{aEM} \frac{\omega_a \epsilon_0 \langle a_0 \rangle c}{\sqrt{2} Q_1} \int \vec{B}_0 \cdot \text{Re}(\mathbf{B}_1) dV$$

$$\sqrt{P_1} = \sqrt{\omega_a Q_1 U_1} = (g_{a\gamma\gamma} \sqrt{C_{1a\gamma\gamma}} + g_{aEM} \sqrt{C_{1aEM}}) \langle a_0 \rangle c B_0 \sqrt{\omega_a Q_1 \epsilon_0 V_1} = (g_{a\gamma\gamma} \sqrt{C_{1a\gamma\gamma}} + g_{aEM} \sqrt{C_{1aEM}}) B_0 \sqrt{\frac{\rho_a Q_1 \epsilon_0 c^5 V_1}{\omega_a}}$$

Form Factors

$$C_{1a\gamma\gamma} = \frac{(\int \vec{B}_0 \cdot \text{Re}(\mathbf{E}_1) dV)^2}{B_0^2 V_1 \int \mathbf{E}_1 \cdot \mathbf{E}_1^* dV} \quad C_{1aEM} = \frac{(\int \vec{B}_0 \cdot \text{Re}(\mathbf{B}_1) dV)^2}{B_0^2 V_1 \int \mathbf{B}_1 \cdot \mathbf{B}_1^* dV}$$

# SENSITIVITY OF AXION RESONANT HALOSCOPES UNDER DC ELECTRIC FIELDS

$$\sqrt{P_1} = \sqrt{\omega_a Q_1 U_1} = (g_{aMM} \sqrt{C_{1aMM}} + g_{aEM} \sqrt{C_{1aEMm}}) \langle a_0 \rangle E_0 \sqrt{\omega_a Q_1 \epsilon_0 V_1} = (g_{aMM} \sqrt{C_{1aMM}} + g_{aEM} \sqrt{C_{1aEMm}}) E_0 \sqrt{\frac{\rho_a Q_1 \epsilon_0 c^3 V_1}{\omega_a}},$$

## Form Factors

$$C_{1aEMm} = \frac{(\int \vec{E}_0 \cdot \text{Re}(\mathbf{E}_1) dV)^2}{E_0^2 V_1 \int \mathbf{E}_1 \cdot \mathbf{E}_1^* dV} \quad C_{1aMM} = \frac{(\int \vec{E}_0 \cdot \text{Re}(\mathbf{B}_1) dV)^2}{E_0^2 V_1 \int \mathbf{B}_1 \cdot \mathbf{B}_1^* dV},$$

## Searching for GUT-scale QCD axions and monopoles with a high-voltage capacitor

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The QCD axion has been postulated to exist because it solves the strong- $CP$  problem. Furthermore, if it exists axions should be created in the early Universe and could account for all the observed dark matter. In particular, axion masses of order  $10^{-10}$  eV to  $10^{-7}$  eV correspond to axions in the vicinity of the grand unified theory scale (GUT-scale). In this mass range many experiments have been proposed to search for the axion through the standard QED coupling parameter  $g_{a\gamma\gamma}$ . Recently axion electrodynamics has been expanded to include two more coupling parameters,  $g_{aEM}$  and  $g_{aMM}$ , which could arise if heavy magnetic monopoles exist. In this work we show that both  $g_{aMM}$  and  $g_{aEM}$  may be searched for using a high-voltage capacitor. Since the experiment is not sensitive to  $g_{a\gamma\gamma}$ , it gives a new way to search for effects of heavy monopoles if the GUT-scale axion is shown to exist, or to simultaneously search for both the axion and the monopole at the same time.

DOI: [10.1103/PhysRevD.108.035024](https://doi.org/10.1103/PhysRevD.108.035024)

arXiv:2306.13320v1 [hep-ph] 23 Jun 2023

# AC Capacitor: Apply Poynting Theorem: Sensitive to $g_{aEM}$

Vector Phasor Amplitudes

$$\oint \text{Im} (\mathbf{S}_1) \cdot \hat{n} ds = \omega_a \int \left( \left( \frac{1}{2\mu_0} \mathbf{B}_1^* \cdot \mathbf{B}_1 - \frac{\epsilon_0}{2} \mathbf{E}_1 \cdot \mathbf{E}_1^* \right) - \frac{g_{aEM} a_0 \epsilon_0}{4} (\mathbf{E}_1 + \mathbf{E}_1^*) \cdot \vec{E}_0 + \frac{g_{aMM} a_0 \epsilon_0}{4} (\mathbf{B}_1 + \mathbf{B}_1^*) \cdot \vec{E}_0 \right) dV.$$

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$$U_1 = \frac{\epsilon_0 a_0^2 \left( \int \left( g_{aEM} (\mathbf{E}_1^* + \mathbf{E}_1) - g_{aMM} c (\mathbf{B}_1^* + \mathbf{B}_1) \right) \cdot \vec{E}_0 dv \right)^2}{8 \int \left( c^2 \mathbf{B}_1^* \cdot \mathbf{B}_1 - \mathbf{E}_1 \cdot \mathbf{E}_1^* \right) dv}$$

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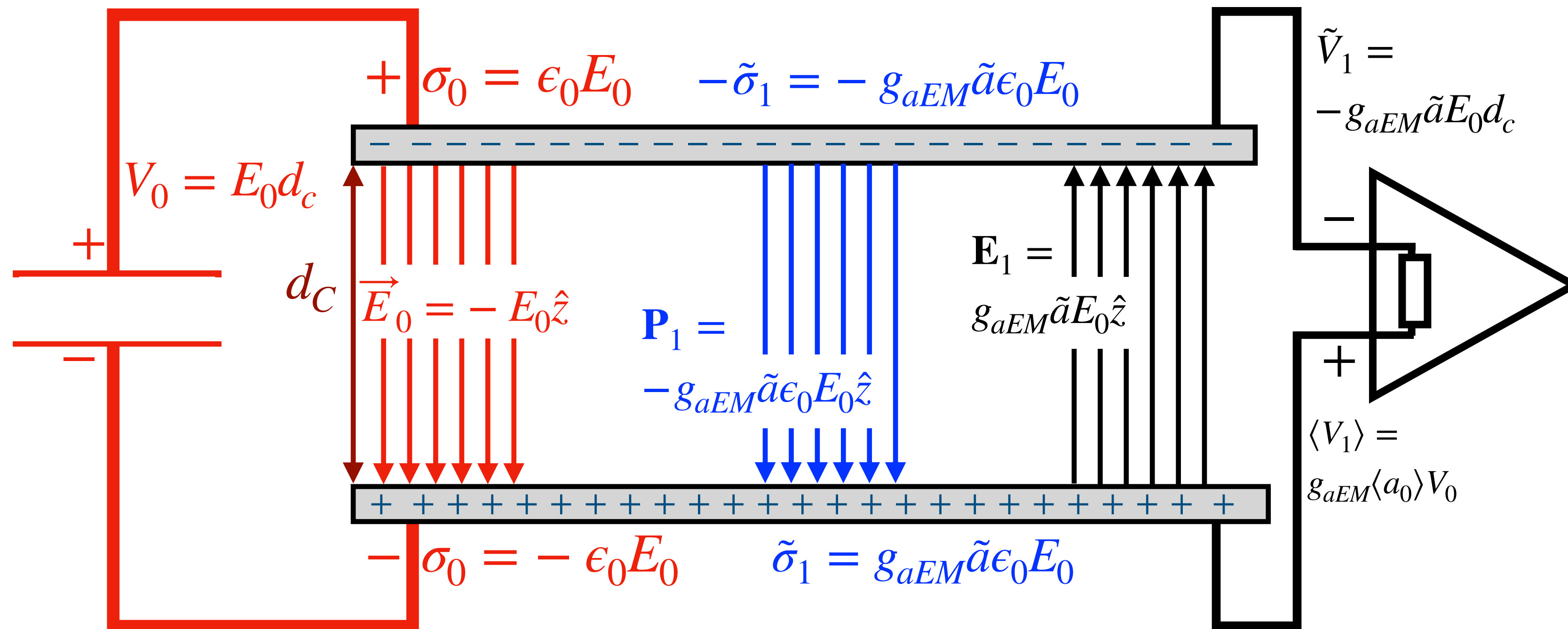
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## Axion generated Electric Field





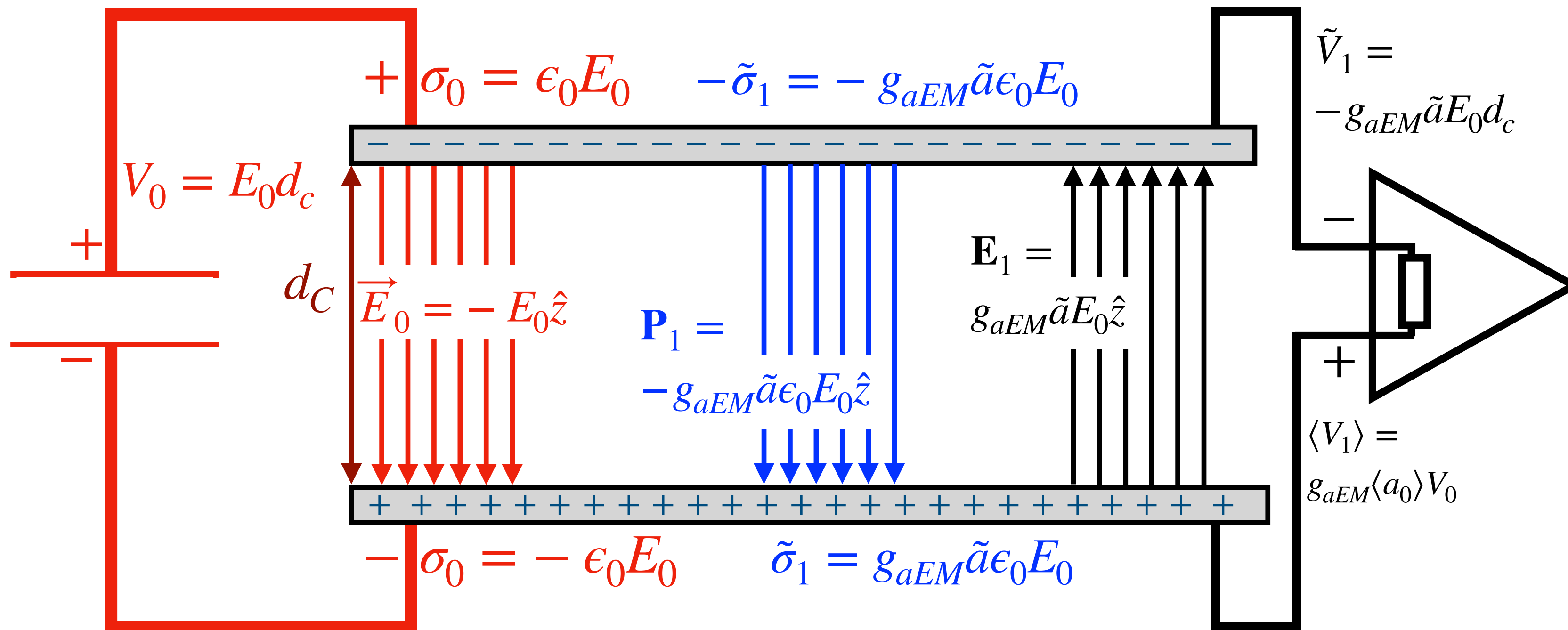
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$$U_1 = \frac{\epsilon_0 a_0^2 \left( \int \left( g_{aEM} (\mathbf{E}_1^* + \mathbf{E}_1) - g_{aMM} (\mathbf{B}_1^* + \mathbf{B}_1) \right) \cdot \vec{E}_0 dv \right)^2}{8 \int \left( c^2 \mathbf{B}_1^* \cdot \mathbf{B}_1 - \mathbf{E}_1 \cdot \mathbf{E}_1^* \right) dv} \quad \mathbf{B}_1 + \mathbf{B}_1^* \sim 0 \quad \mathbf{E}_1 + \mathbf{E}_1^* \sim 2\mathbf{E}_1 \quad U_1 \approx - \frac{g_{aEM}^2 a_0^2 \epsilon_0 \left( \int \mathbf{E}_1 \cdot \vec{E}_0 dv \right)^2}{2 \int \mathbf{E}_1 \cdot \mathbf{E}_1^* dv}$$

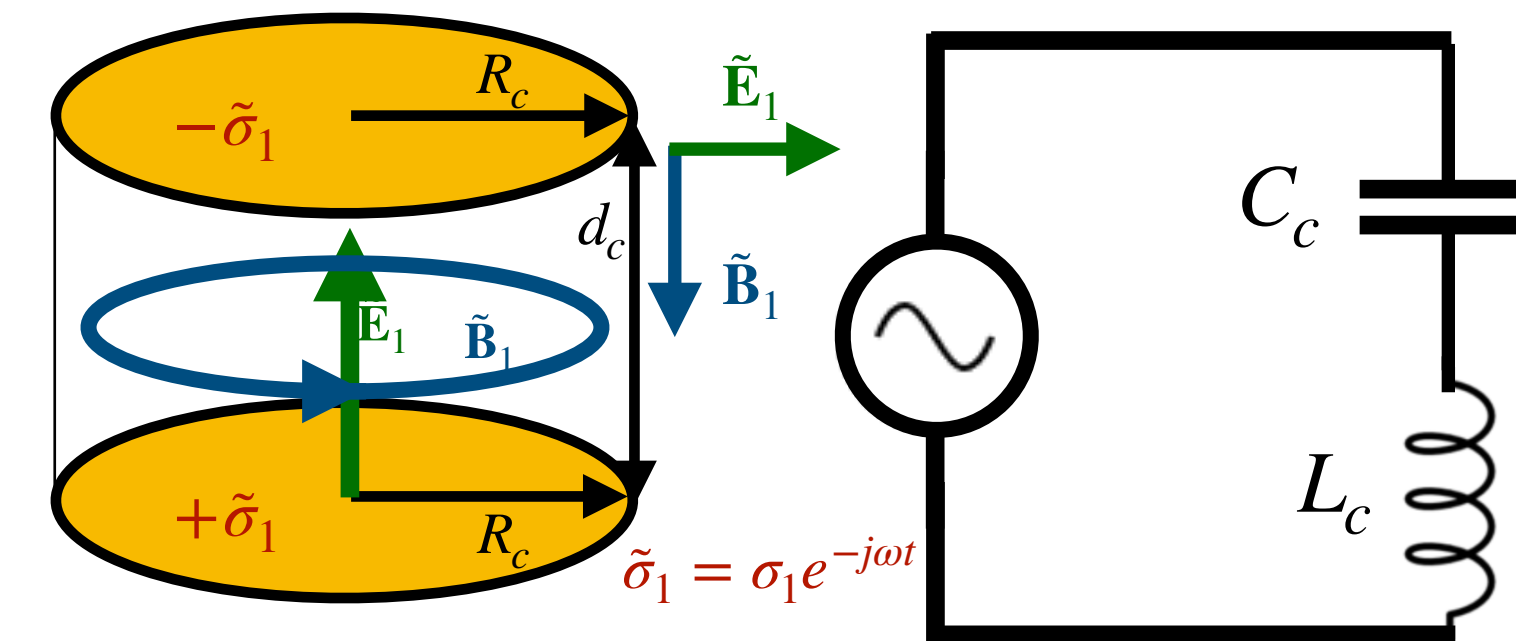
## Axion generated Electric Field



Cylindrical // Plate Capacitor

$$\tilde{\mathbf{E}}_1 = \tilde{E}_{01} J_0 \left( \frac{\omega_1 r}{c} \right) e^{-j\omega_1 t \hat{z}}$$

$$\tilde{\mathbf{B}}_1 = -j \frac{\tilde{E}_{01}}{c} J_1 \left( \frac{\omega_1 r}{c} \right) e^{-j\omega_1 t \hat{\phi}} \quad \tilde{E}_{01} = \frac{\tilde{q}_1}{\pi R_c^2 \epsilon_0}$$



# Axion Generated Magnetic Field-> Magnetic Circuit Readout Sensitive to $g_{aMM}$

$$\frac{\oint \text{Im}(\mathbf{S}_1) \cdot \hat{n} ds}{\omega_a} = \int \left( \left( \frac{1}{2\mu_0} \mathbf{B}_1^* \cdot \mathbf{B}_1 - \frac{\epsilon_0}{2} \mathbf{E}_1 \cdot \mathbf{E}_1^* \right) - \frac{g_{aEM} a_0 \epsilon_0}{4} (\mathbf{E}_1 + \mathbf{E}_1^*) \cdot \vec{E}_0 + \frac{g_{aMM} a_0 \epsilon_0 c}{4} (\mathbf{B}_1 + \mathbf{B}_1^*) \cdot \vec{E}_0 \right) dV$$

$$\mathbf{E}_1 + \mathbf{E}_1^* \sim 0 \quad \mathbf{B}_1 + \mathbf{B}_1^* \sim 2\mathbf{B}_1$$

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$$\mathbf{E}_1 + \mathbf{E}_1^* \sim 0 \quad \mathbf{B}_1 + \mathbf{B}_1^* \sim 2\mathbf{B}_1$$

$$U_1 = \frac{\left( \frac{g_{aMM} a_0 \epsilon_0 c}{2} \int \mathbf{B}_1 \cdot \vec{E}_0 dV \right)^2}{\int \left( \frac{1}{2\mu_0} \mathbf{B}_1^* \cdot \mathbf{B}_1 - \frac{\epsilon_0}{2} \mathbf{E}_1 \cdot \mathbf{E}_1^* \right) dV}$$

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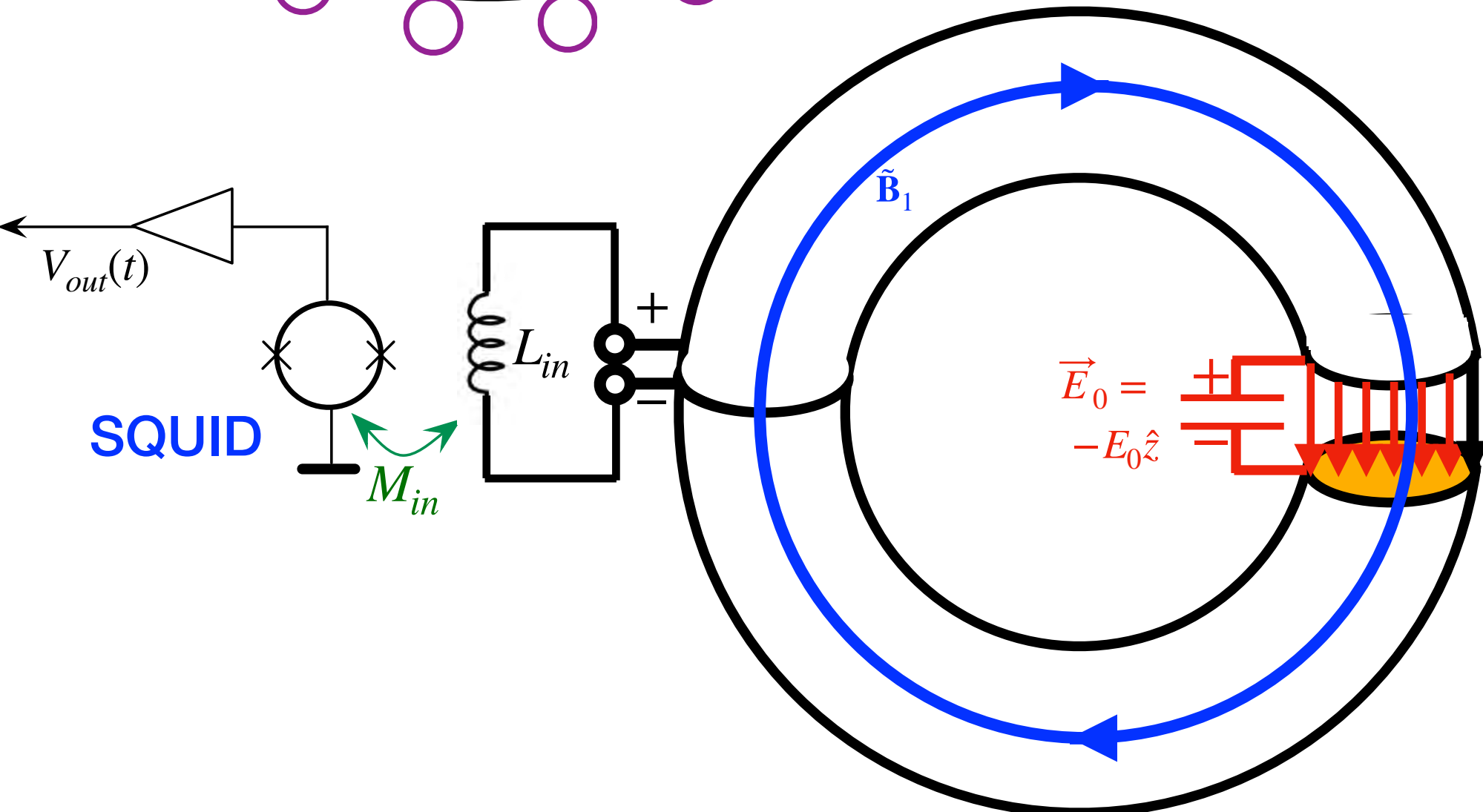
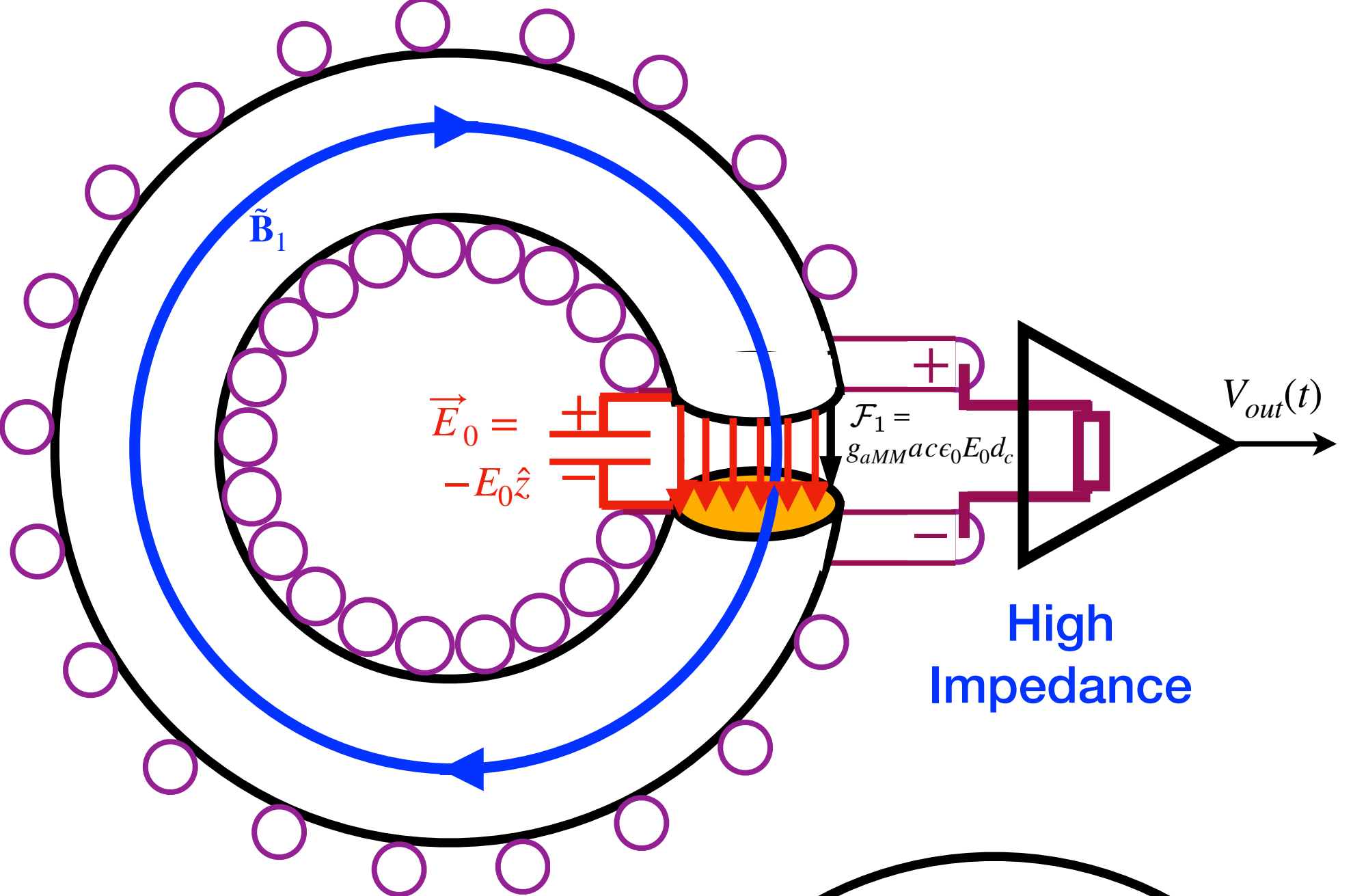
# Axion Generated Magnetic Field -> Magnetic Circuit Readout Sensitive to $g_{aMM}$

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$$U_1 \approx \frac{g_{aMM}^2 a_0^2 \epsilon_0}{2} \frac{\left( \int \mathbf{B}_1 \cdot \vec{E}_0 dV \right)^2}{\int \mathbf{B}_1^* \cdot \mathbf{B}_1 dV}$$

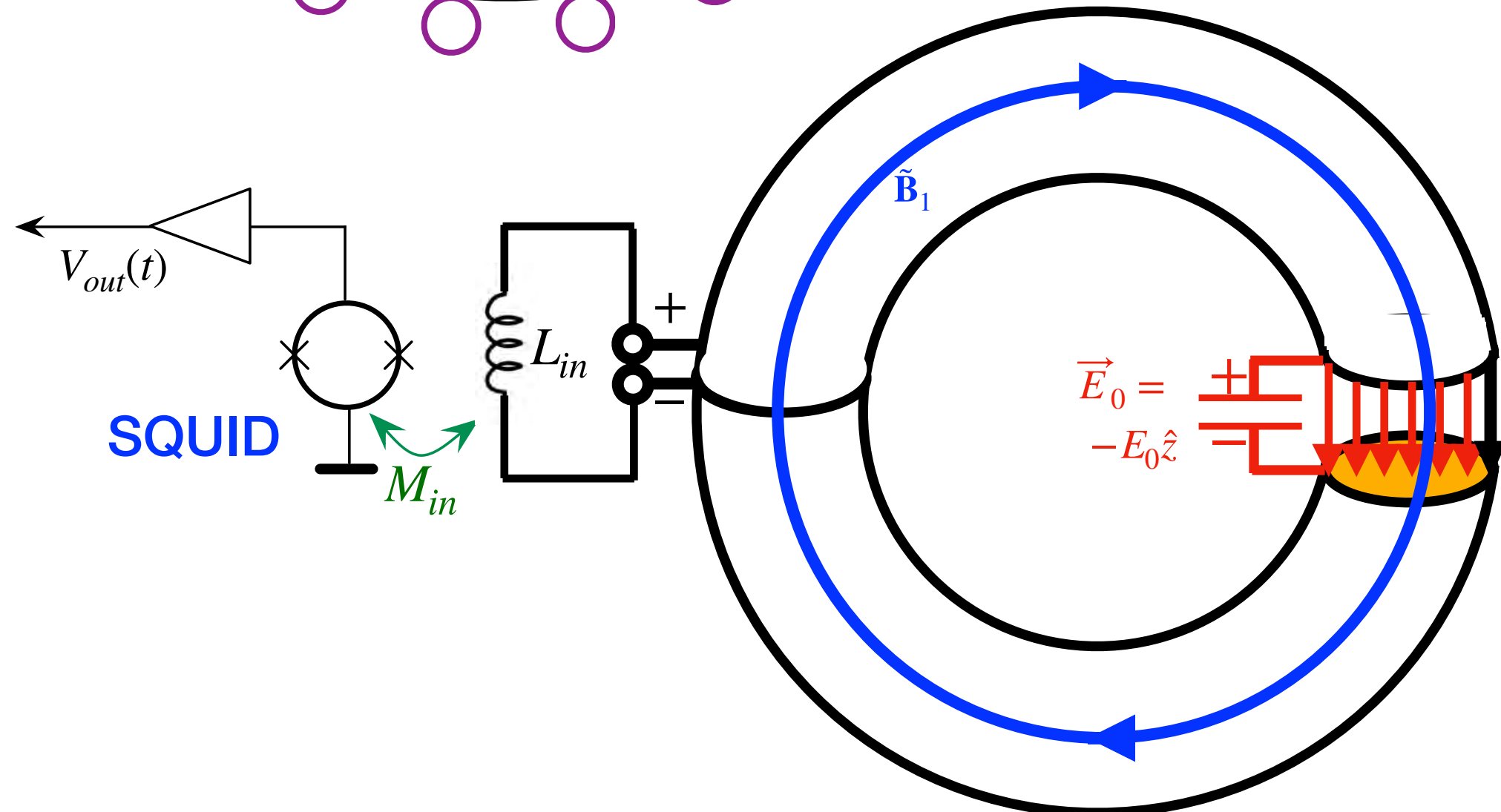
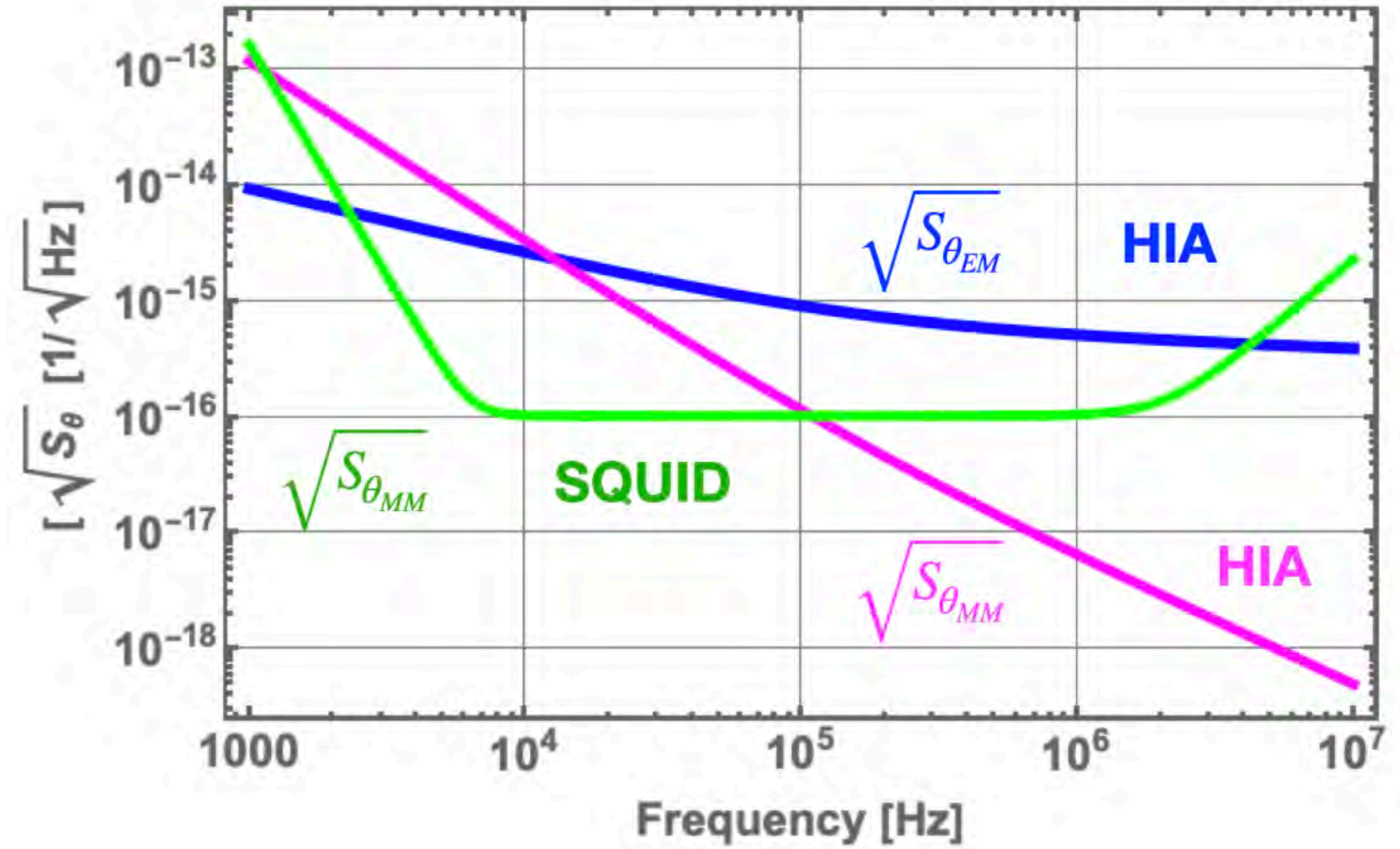
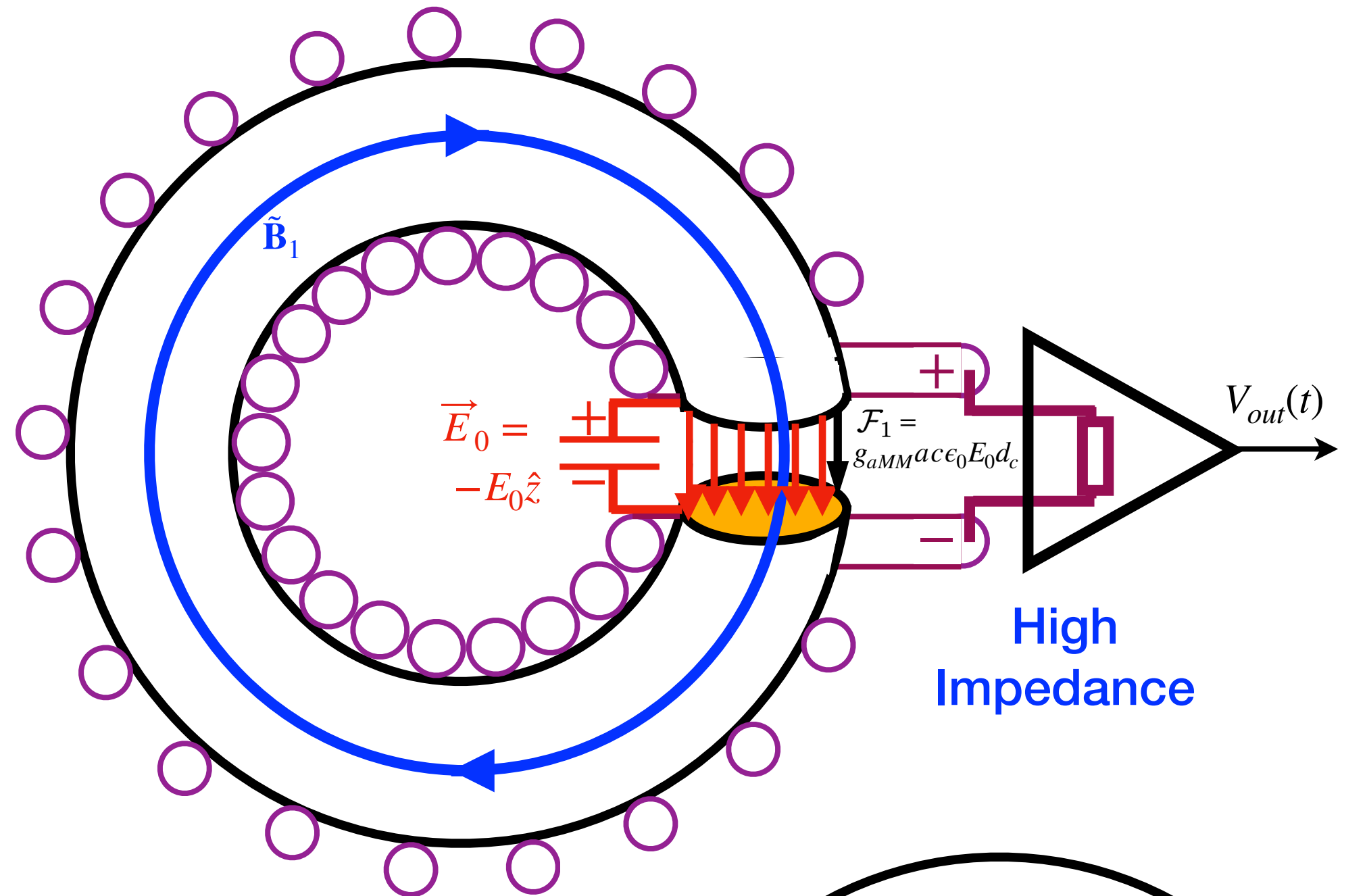


# Axion Generated Magnetic Field -> Magnetic Circuit Readout Sensitive to $g_{aMM}$

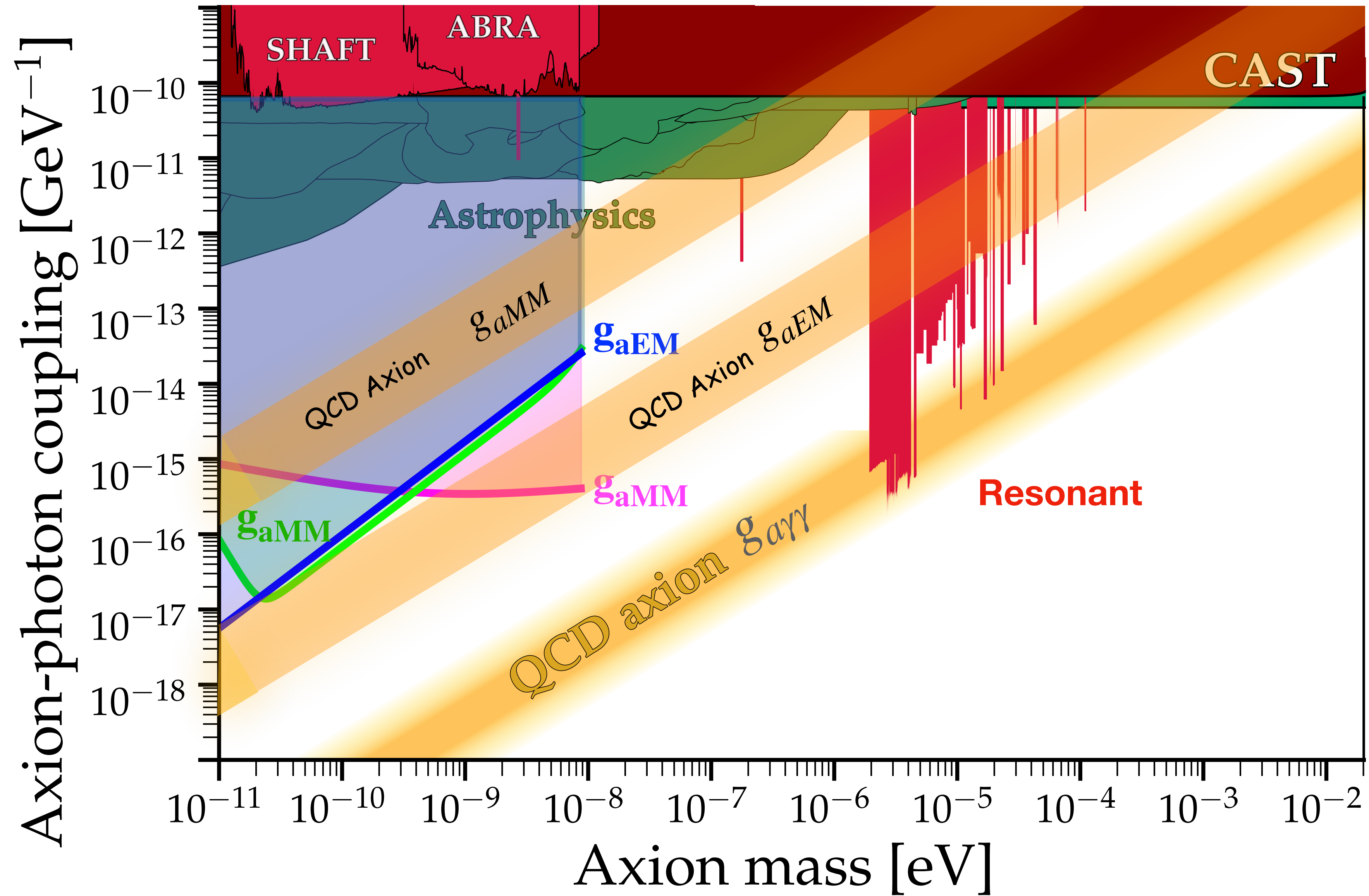
$$\frac{\oint \text{Im}(\mathbf{S}_1) \cdot \hat{n} ds}{\omega_a} = \int \left( \left( \frac{1}{2\mu_0} \mathbf{B}_1^* \cdot \mathbf{B}_1 - \frac{\epsilon_0}{2} \mathbf{E}_1 \cdot \mathbf{E}_1^* \right) - \frac{g_{aEM} a_0 \epsilon_0}{4} (\mathbf{E}_1 + \mathbf{E}_1^*) \cdot \vec{E}_0 + \frac{g_{aMM} a_0 \epsilon_0 c}{4} (\mathbf{B}_1 + \mathbf{B}_1^*) \cdot \vec{E}_0 \right) dV$$

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$$U_1 = \frac{\left( \frac{g_{aMM} a_0 \epsilon_0 c}{2} \int \mathbf{B}_1 \cdot \vec{E}_0 dV \right)^2}{\int \left( \frac{1}{2\mu_0} \mathbf{B}_1^* \cdot \mathbf{B}_1 - \frac{\epsilon_0}{2} \mathbf{E}_1 \cdot \mathbf{E}_1^* \right) dV} \quad U_1 \approx \frac{g_{aMM}^2 a_0^2 \epsilon_0}{2} \frac{\left( \int \mathbf{B}_1 \cdot \vec{E}_0 dV \right)^2}{\int \mathbf{B}_1^* \cdot \mathbf{B}_1 dV}$$



# Low-Mass Sensitivity to the QCD Axion



18 days of continuous data taking

# SCALAR DARK MATTER: ELECTROMAGNETIC TECHNIQUES

PHYSICAL REVIEW D **106**, 055037 (2022)

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## Searching for scalar field dark matter using cavity resonators and capacitors

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<sup>3</sup>*ARC Centre of Excellence for Dark Matter Particle Physics, Centre for Astrophysics and Supercomputing, Swinburne University of Technology, John St, Hawthorn VIC 3122, Australia*

$$g_{aEM} \equiv g_{\phi\gamma\gamma}$$



# The Team



**Professor Michael Tobar**  
Director—QDM Lab, EQUS Node Director, CDM Node Director



**Dr Maxim Goryachev**  
Lecturer—Research Intensive, EQUS Chief Investigator, CDM Chief Investigator



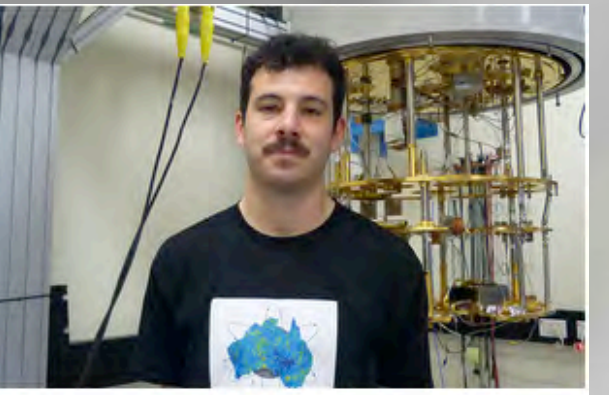
**Dr Ben McAllister**  
Forrest Prospect Fellow



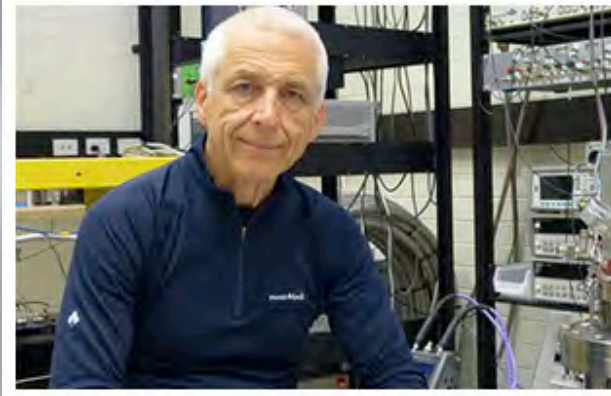
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Adjunct Professor



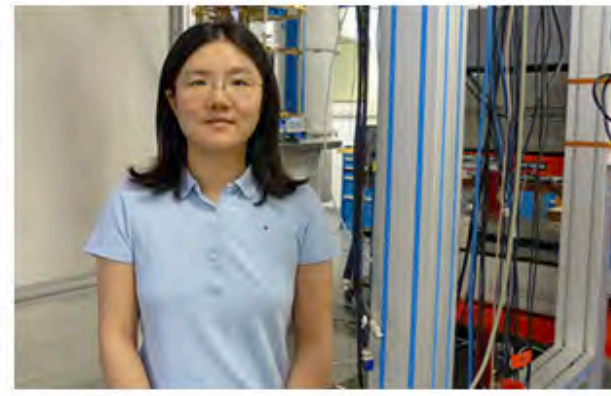
**Graeme Flower**  
Research Associate



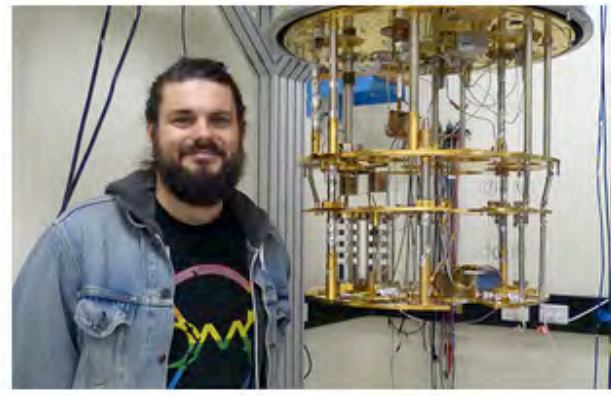
**Will Campbell**  
PhD



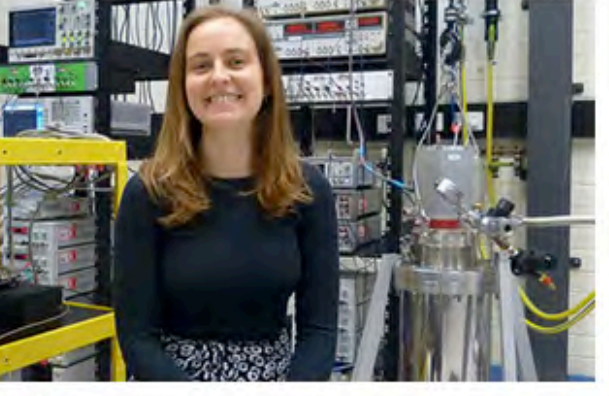
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Senior Principle Research Fellow



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**Dr Jeremy Bourhill**  
Postdoctoral Research Associate



**Catriona Thomson**  
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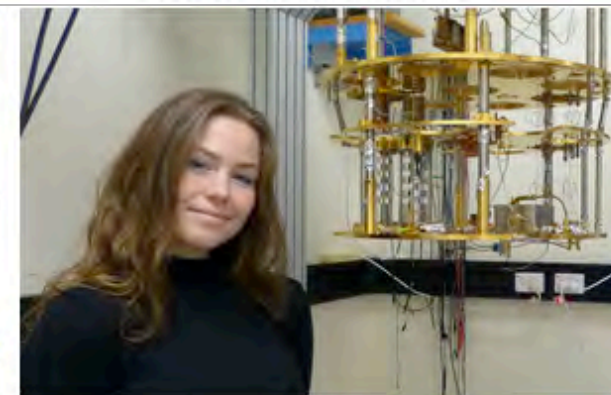
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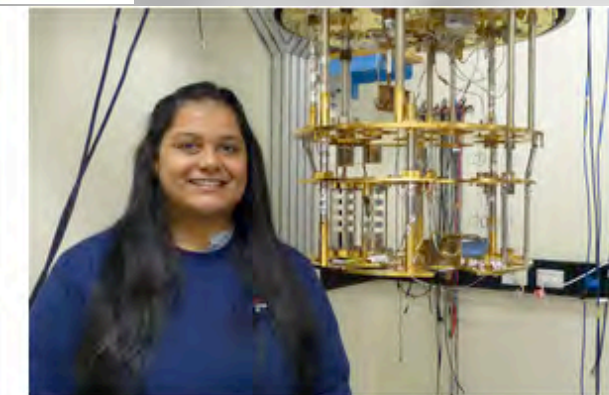
**Elina Hartman**  
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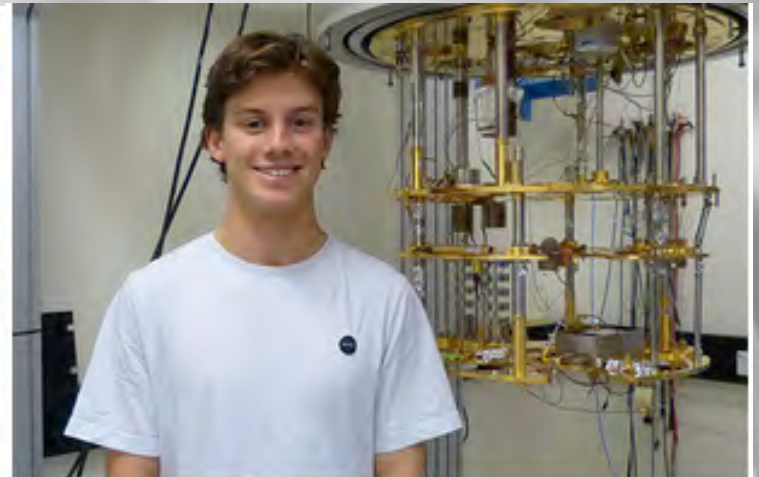
**Steven Samuels**  
PhD



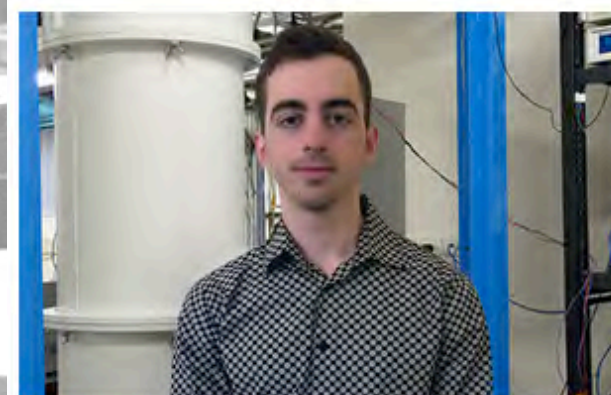
**Emma Paterson**  
BPhil (Hons) Honours Dissertation



**Sonali Parashar**  
Master of Physics—Coursework and Dissertation



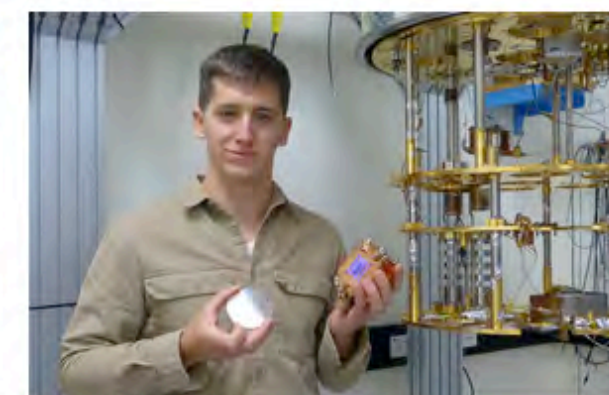
**Hugh Mitchell**  
BPhil (Hons) Honours Placement



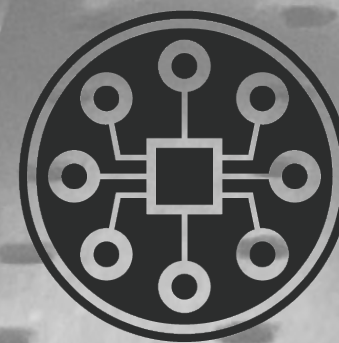
**Michael Hatzon**  
BPhil (Hons) Honours Dissertation



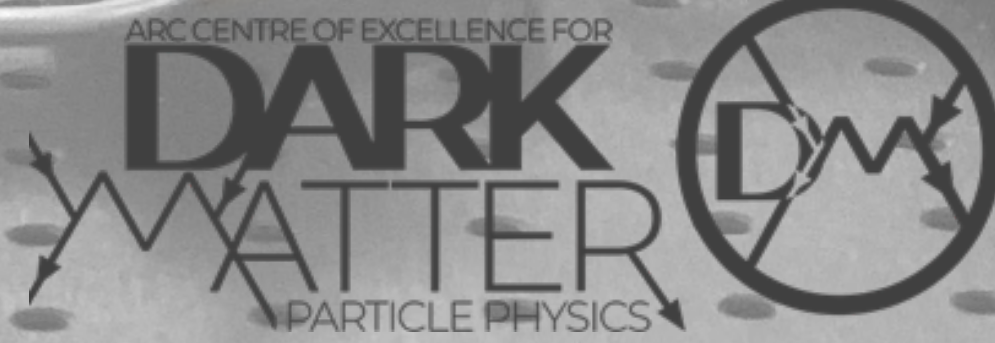
**Robert Crew**  
BPhil (Hons) Honours Dissertation



**Jerzy Cuper**  
Visiting Research Student, Warsaw University of Technology  
1 October 2022 - 1 October 2023



**EQUS**  
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