

Axions and Wave Like Dark Matter



Michael Tobar



THE UNIVERSITY OF
**WESTERN
AUSTRALIA**

QDM

Searching for Putative Wave-Like Dark Matter

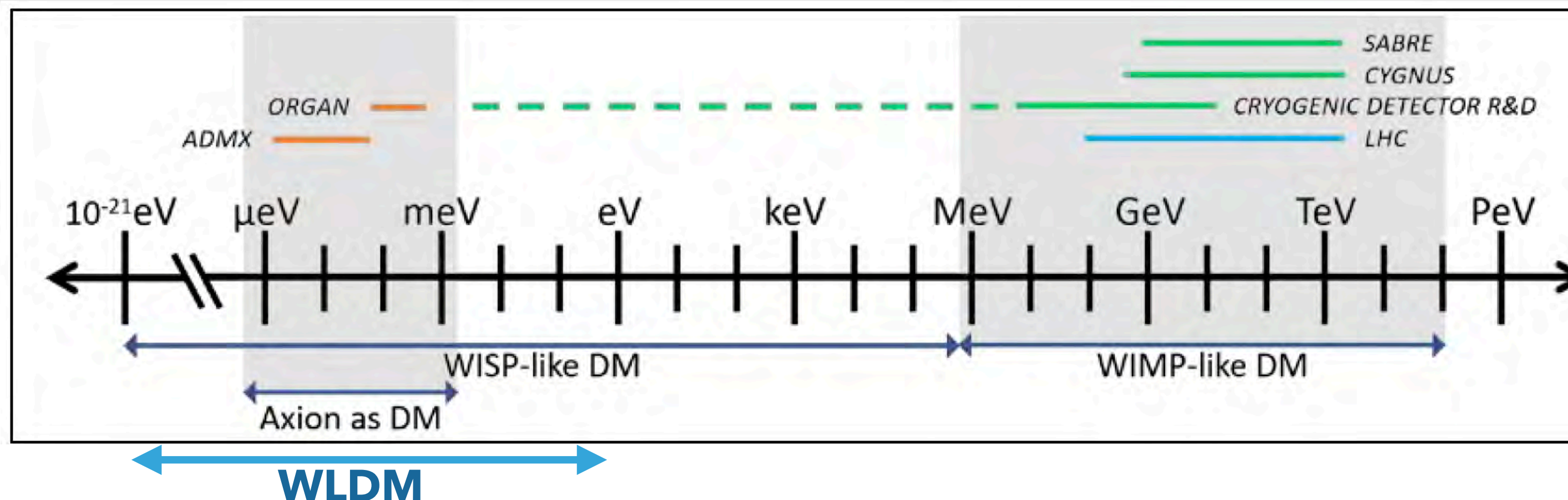


Figure 4: Dark matter mass ranges to be searched in Centre WIMP and WISP direct detection experiments and the LHC Program.

SNOWMASS

Cosmic Frontier: Wave-Like Dark Matter

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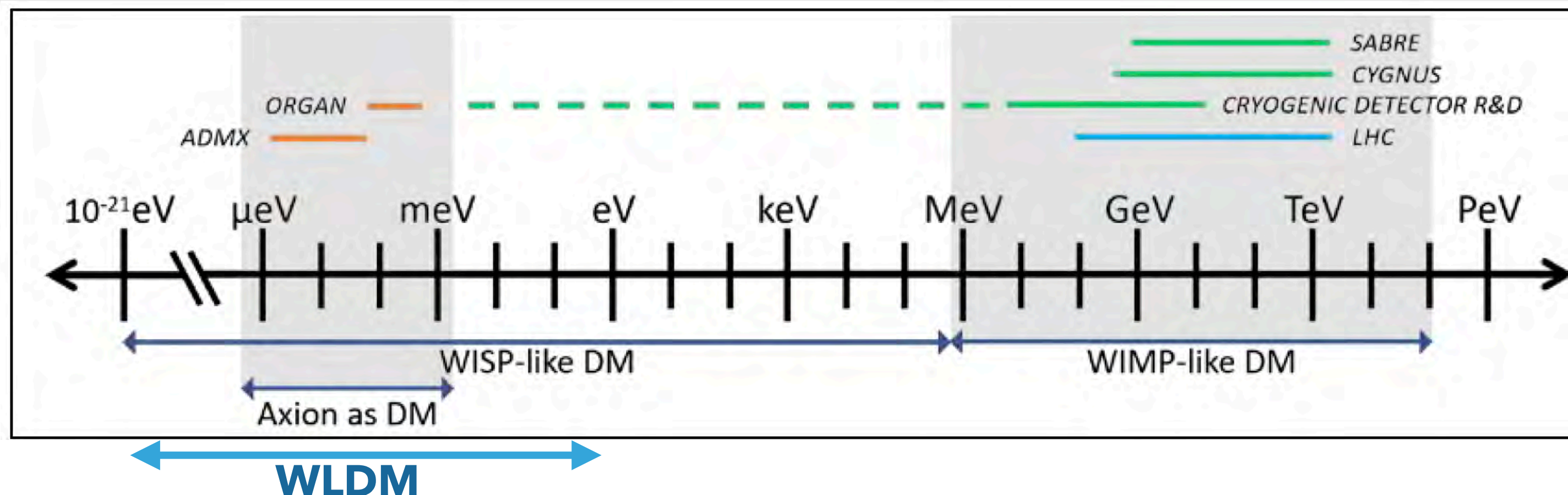


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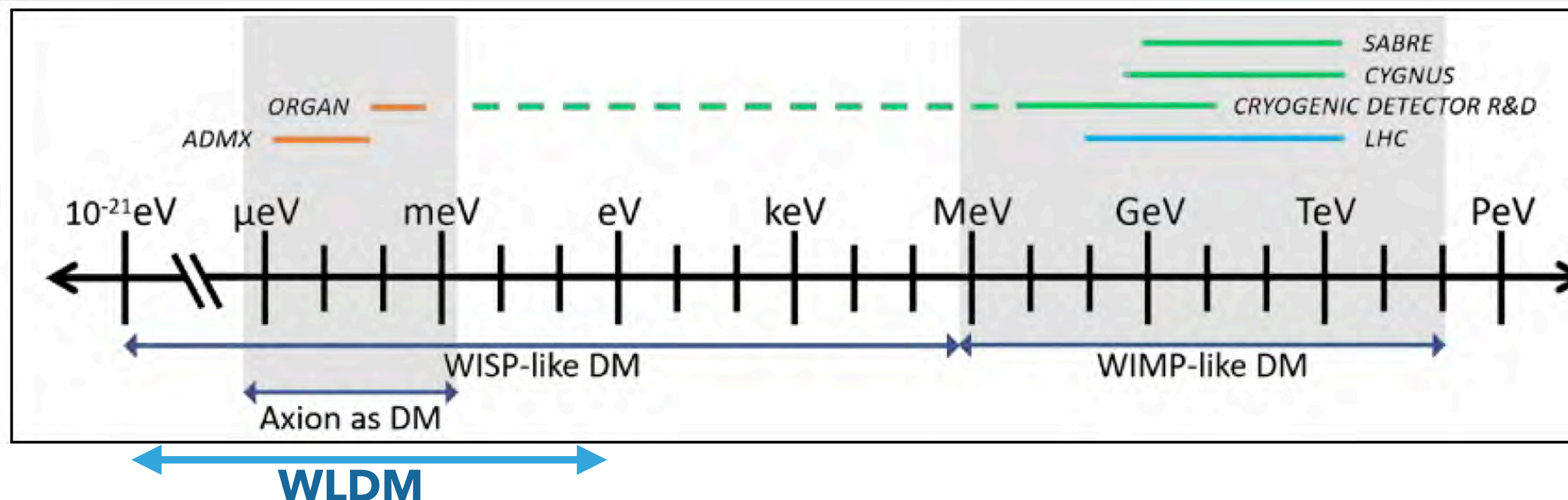


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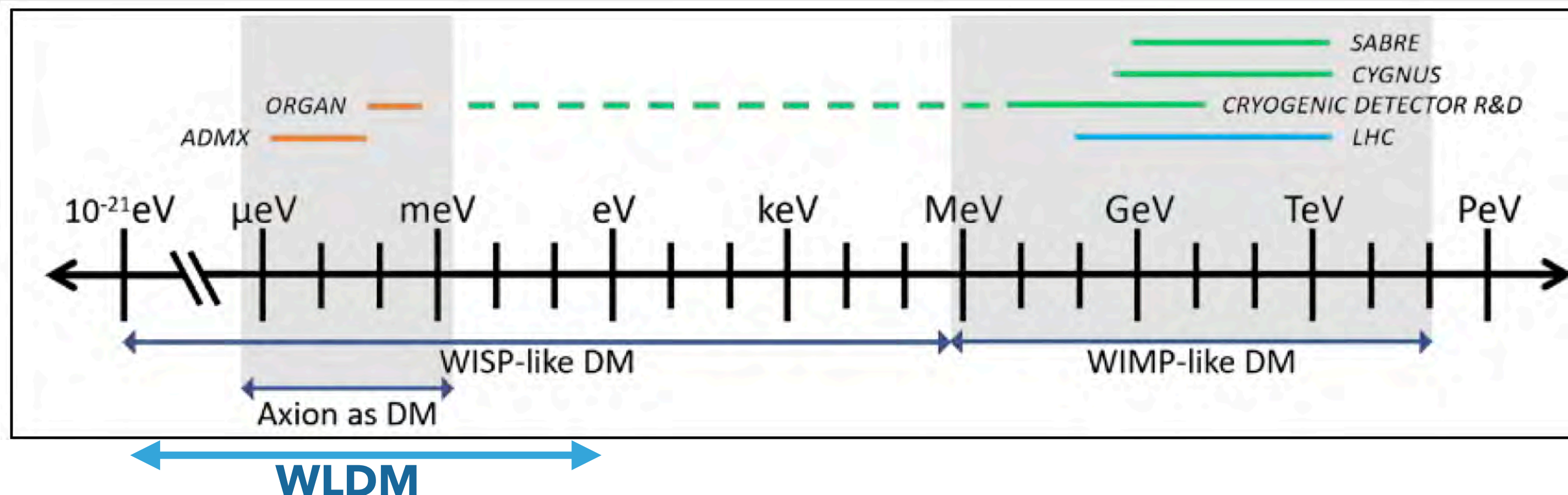


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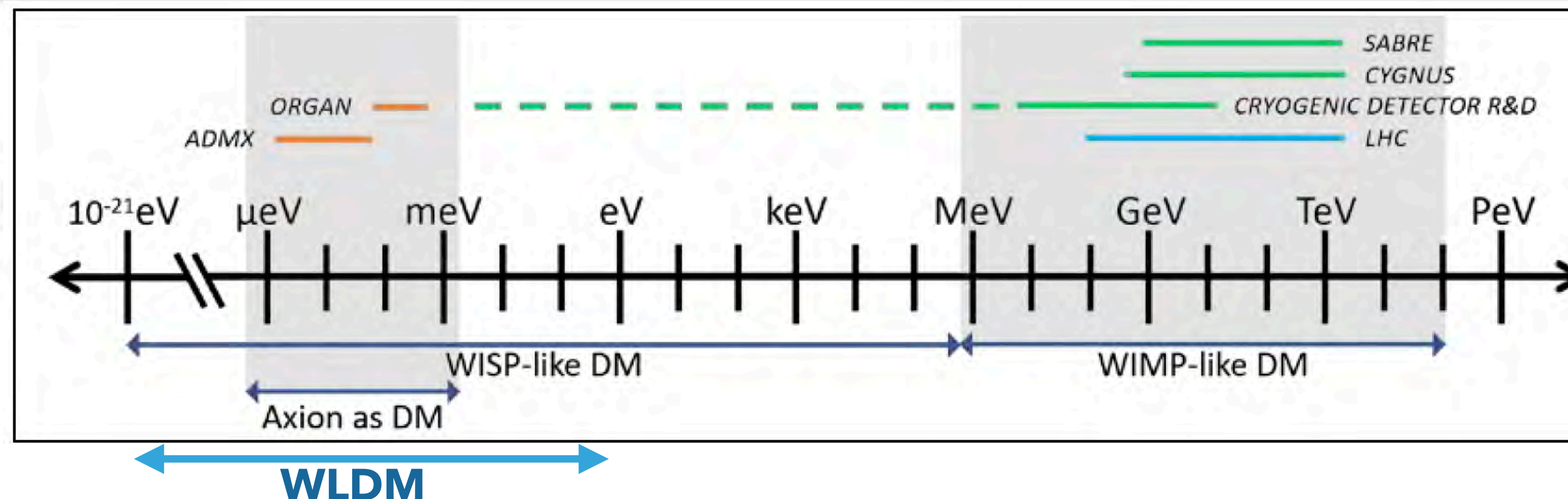


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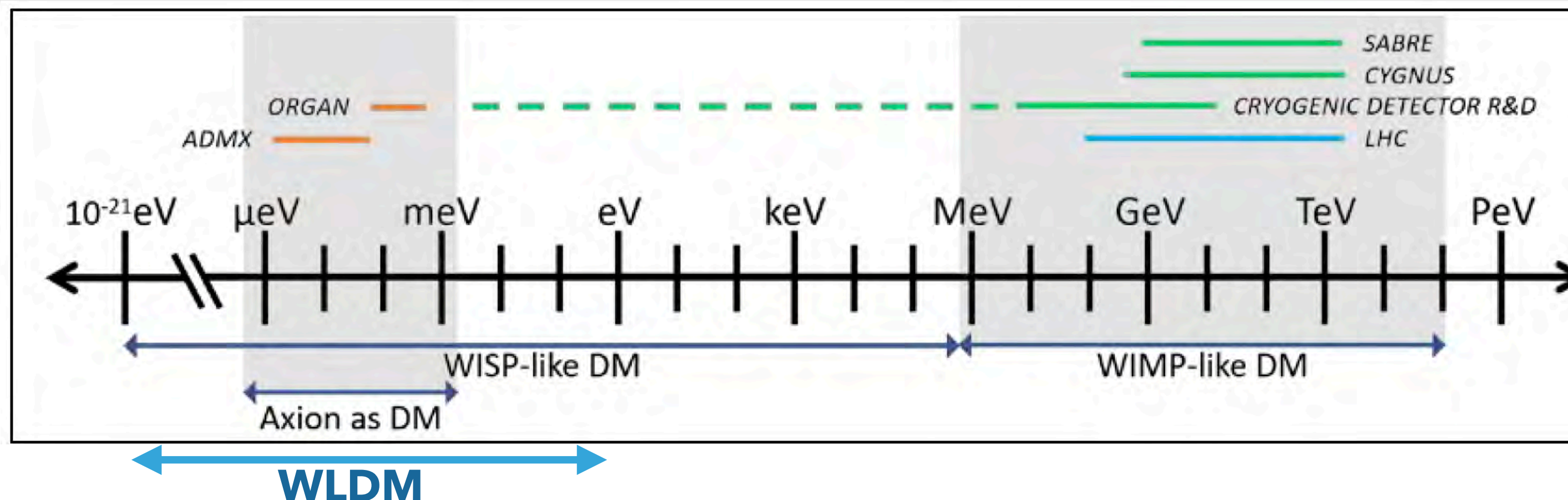


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- > Theory interacts with Experiment: How Dark Matter interacts with SM Particles: Optimise Signal

Searching for Putative Wave-Like Dark Matter

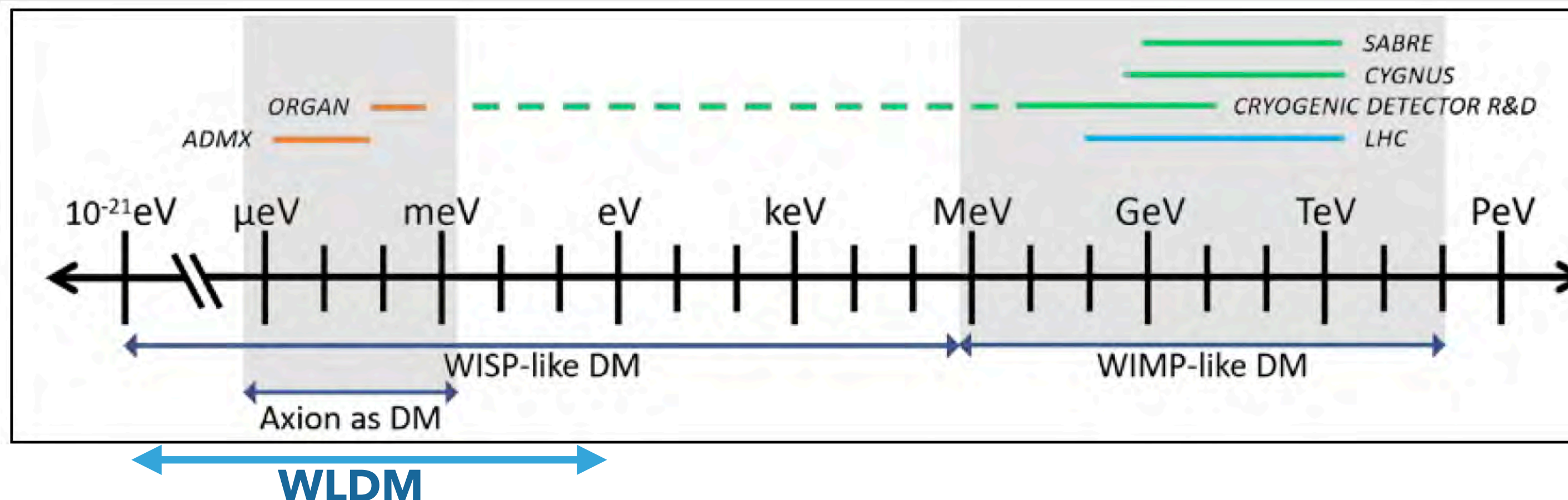


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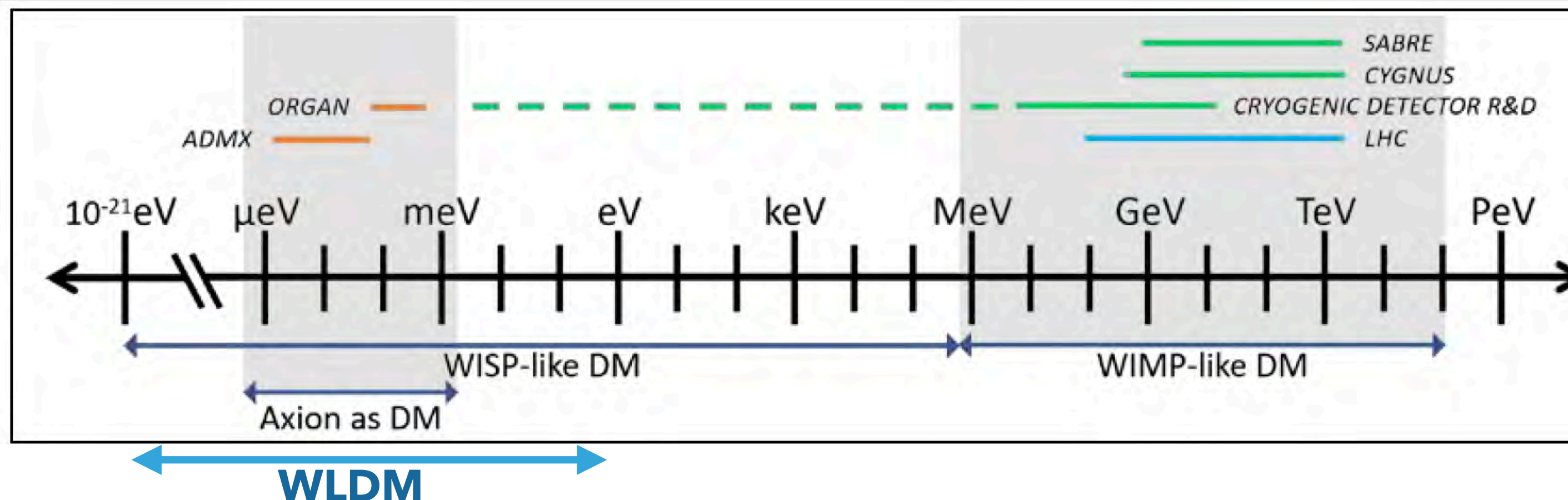


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- > Reduce Noise, Fundamental Limit is Quantum Noise
- > Surpass Quantum Limit: Quantum Metrology

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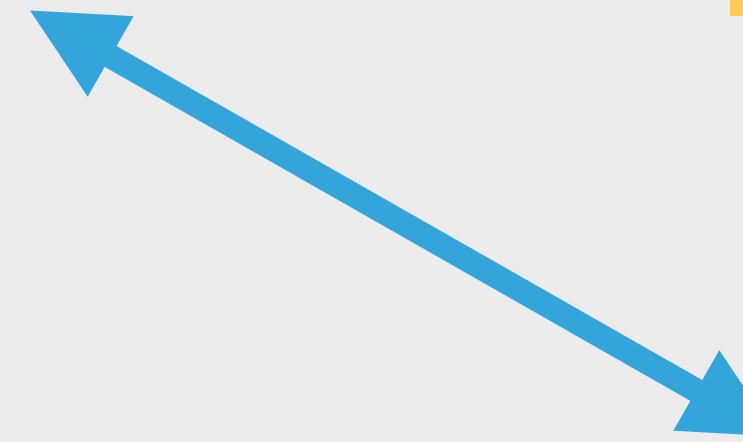
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2020 J. J. Sakurai Prize for Theoretical Particle Physics



Frank Wilczek

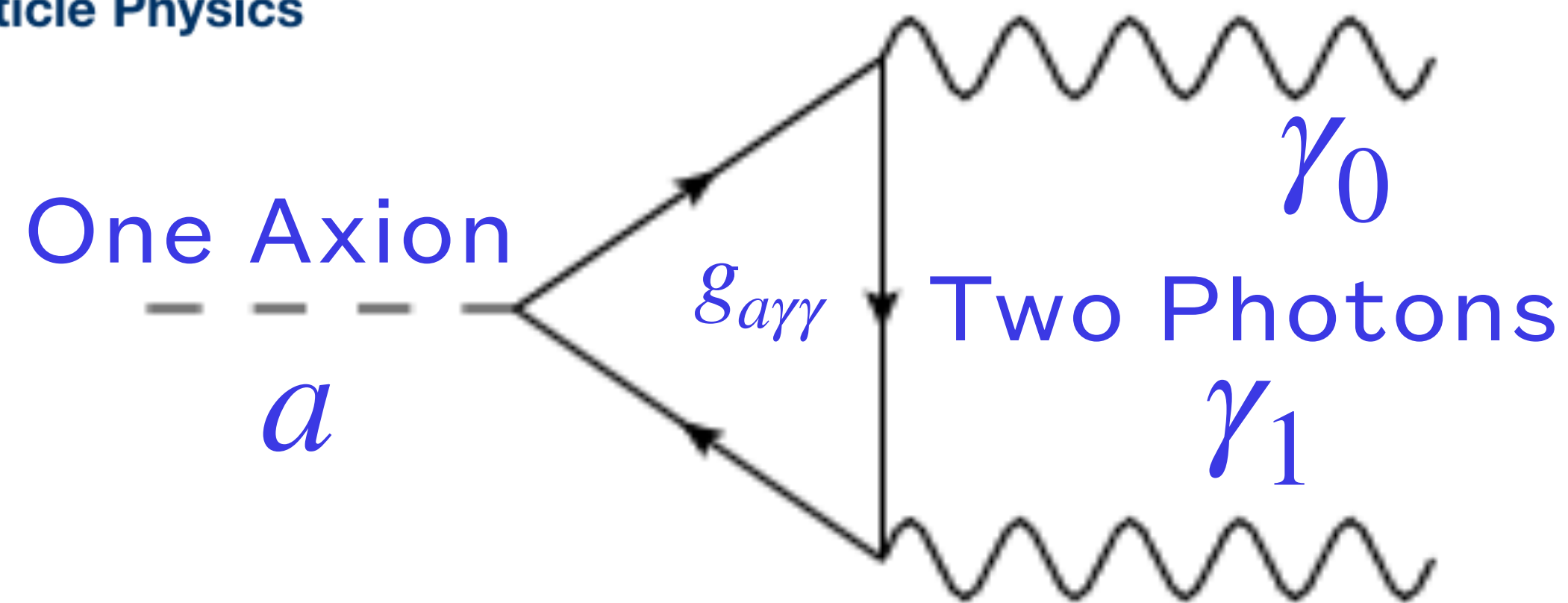
The Axion Particle Should it Exist!

- 1) Solves Strong CP Problem
- 2) Predicted to form in Early Universe
- 3) Is Dark Matter the Axion?



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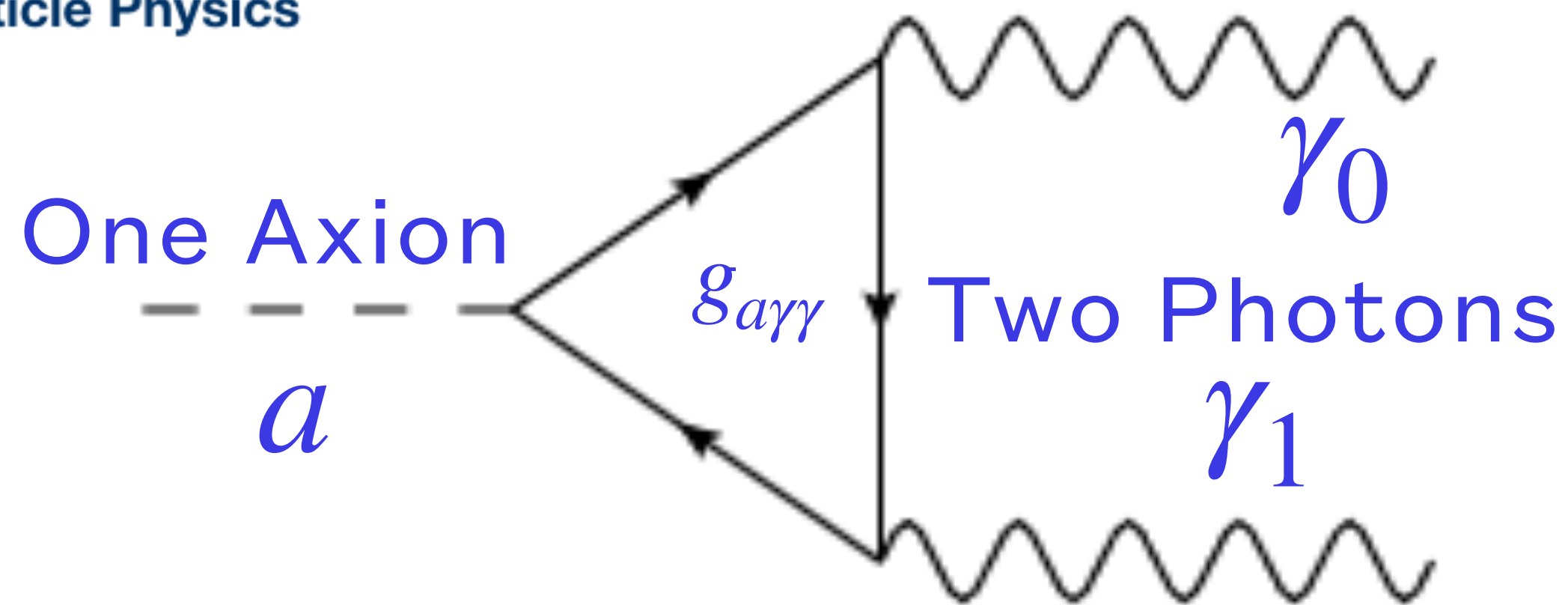
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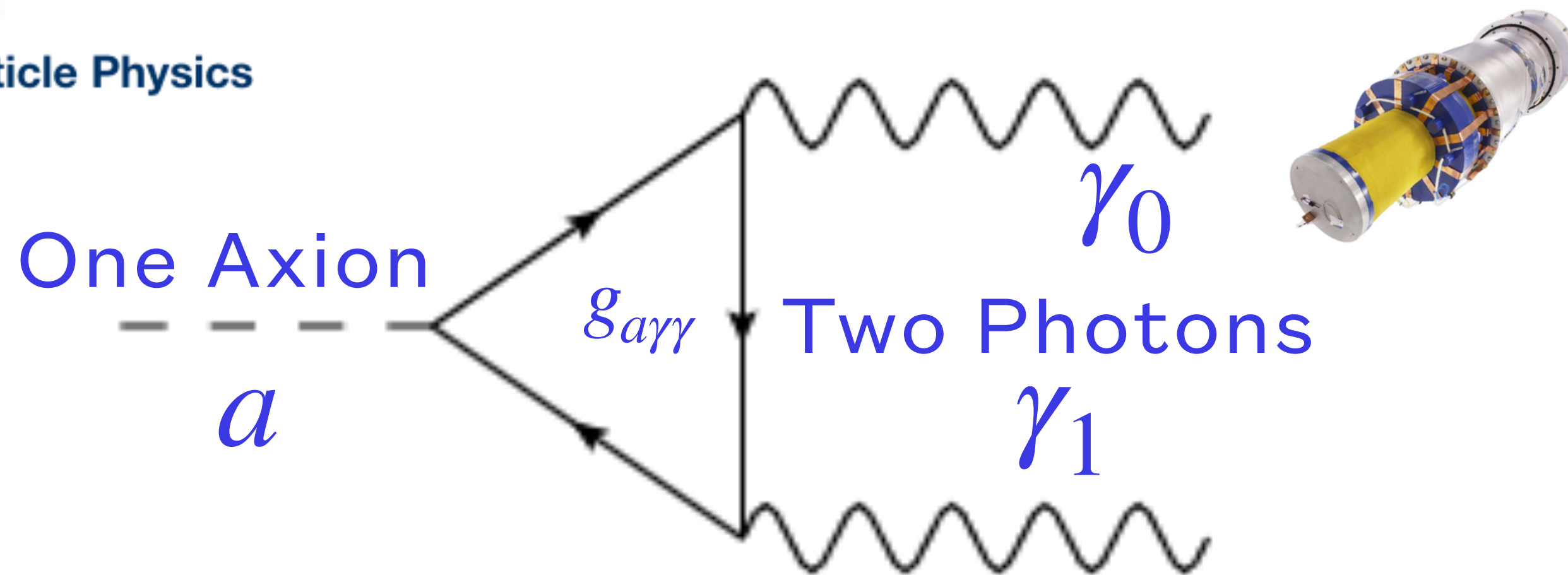


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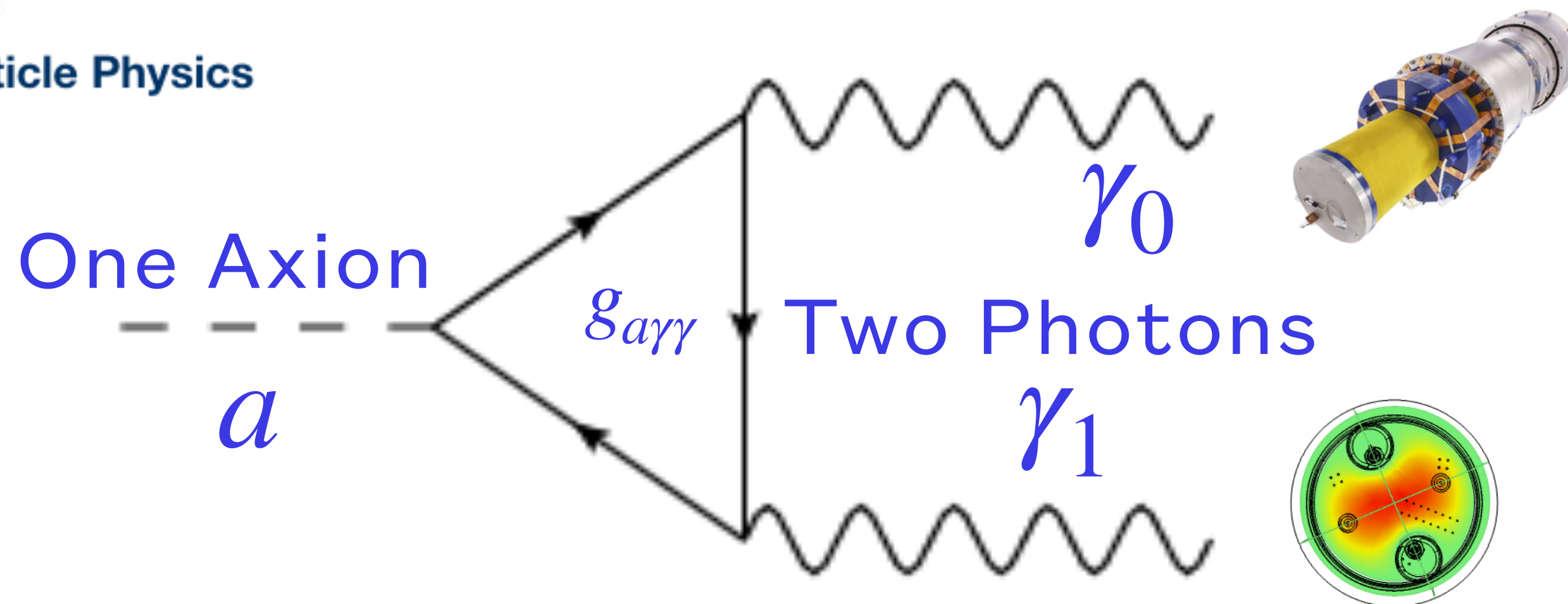
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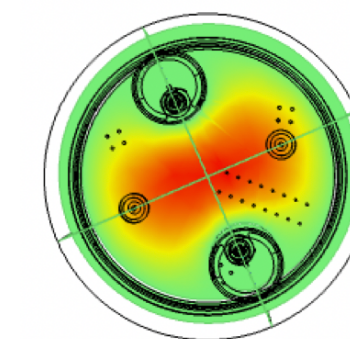
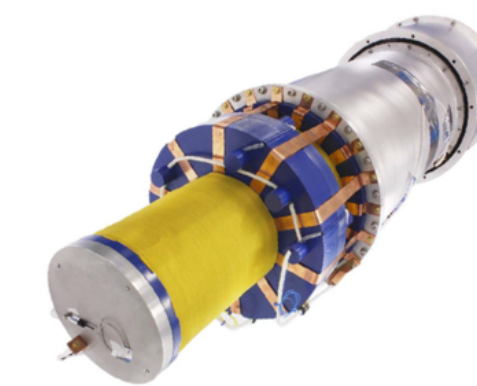
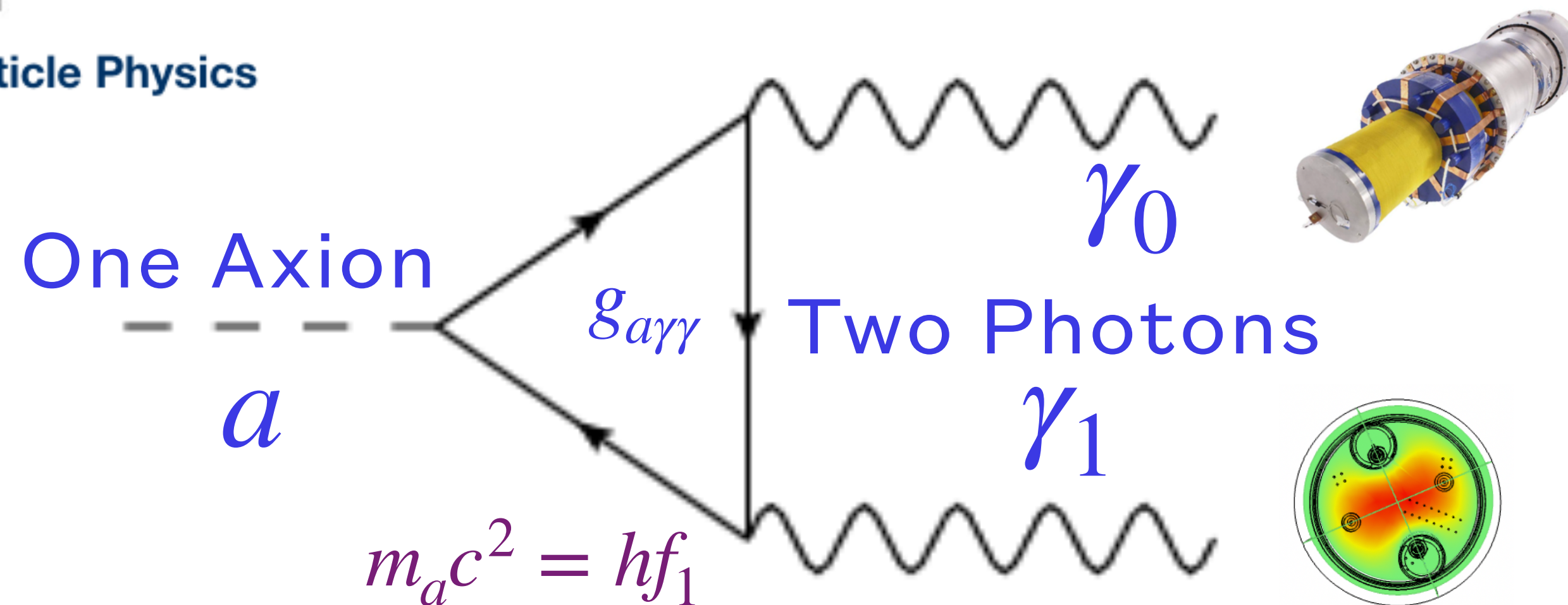


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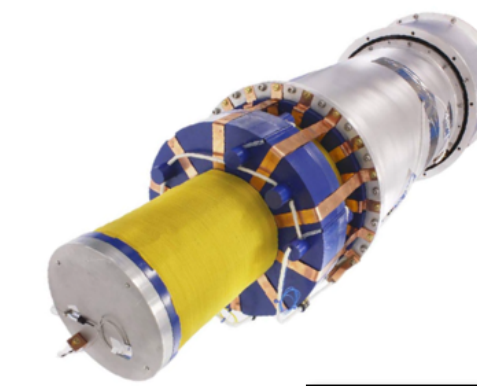
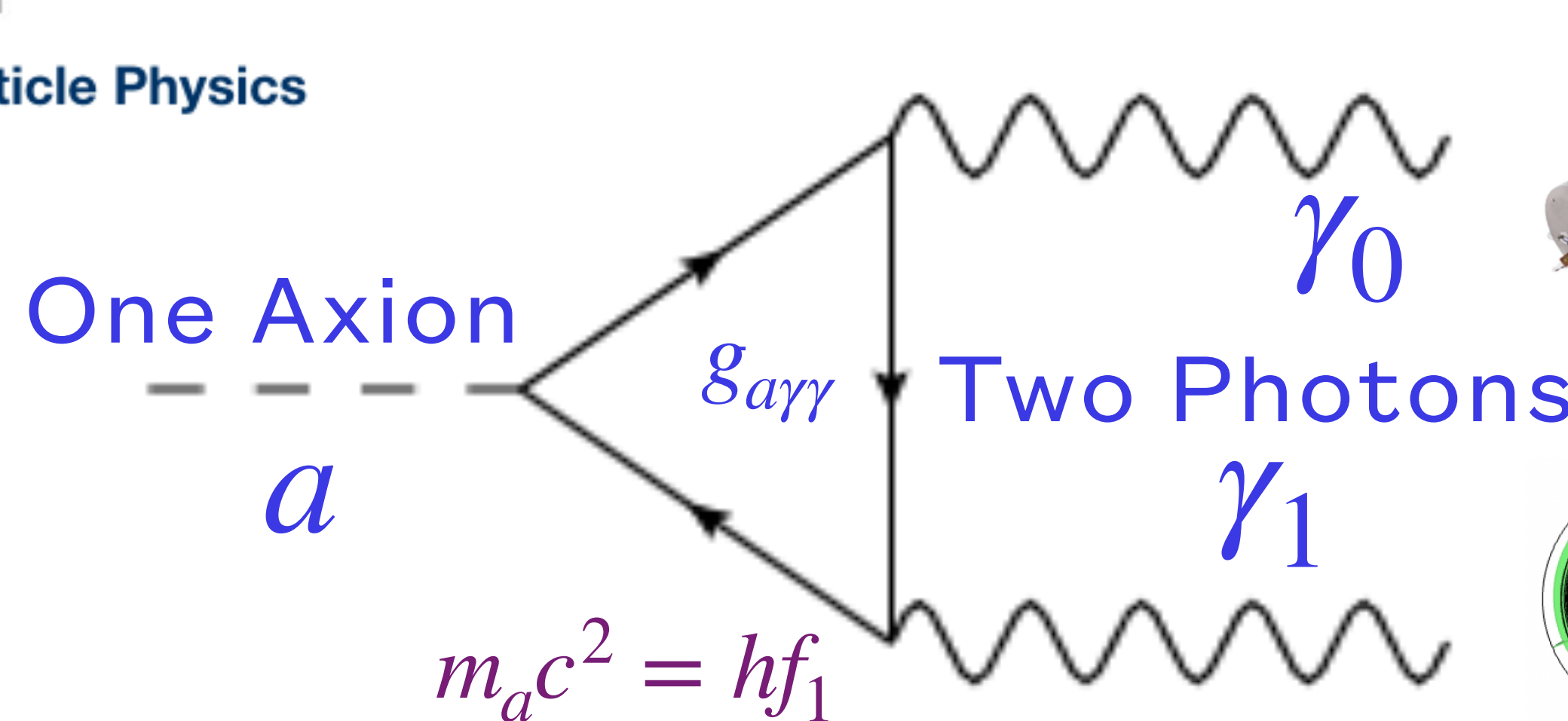


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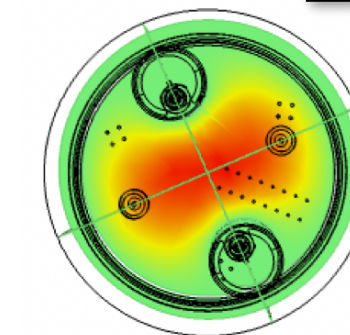


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$$\mathcal{H}_{int} = \epsilon_0 c g_{a\gamma\gamma} a \mathbf{E}_1 \cdot \mathbf{B}_0$$



Measure

Photon Haloscopes

Modified Axion Electrodynamics

(Represents two photons)

Axion Equation of Motion:

Klein-Gordon equation
for massive spin 0
particle

$$a(t) = \frac{1}{2} (\tilde{a}e^{-j\omega_a t} + \tilde{a}^*e^{j\omega_a t}) \\ = \text{Re} (\tilde{a}e^{-j\omega_a t})$$

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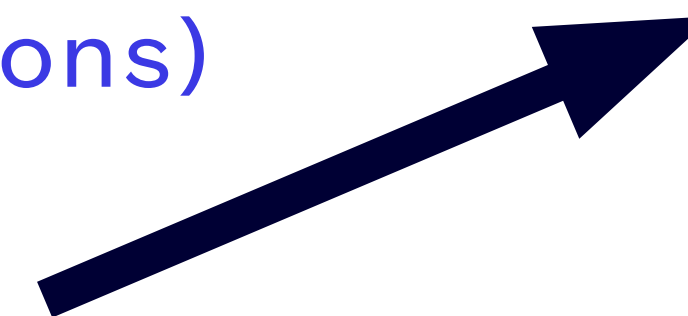
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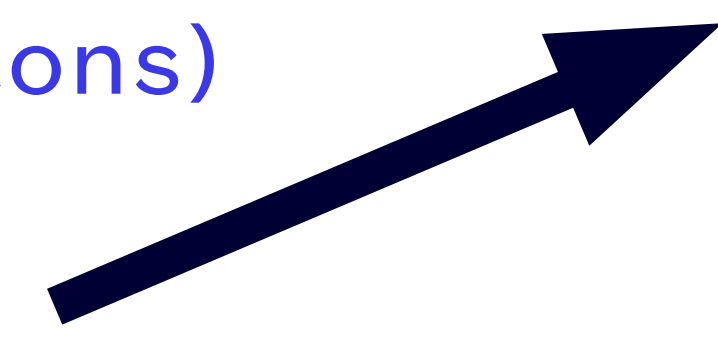
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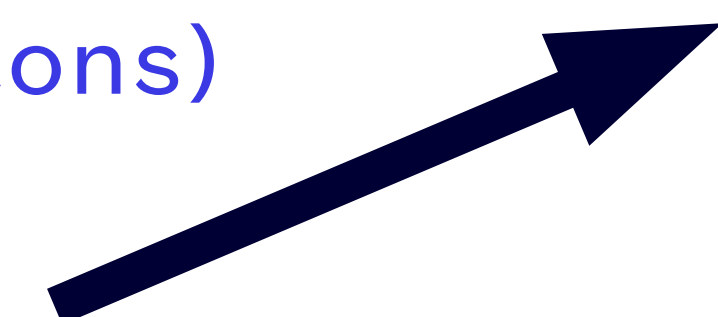
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**Source Terms Generate Photons->
From Background Fields Mixing with Axion**

Measure Created Photon

$$\nabla \cdot \left(\vec{E}_1(\vec{r}, t) - g_{a\gamma\gamma} a(t) c \vec{B}_0(\vec{r}, t) \right) = \frac{\rho_{e_1}}{\epsilon_0}$$

$$\nabla \times \left(\vec{B}_1(\vec{r}, t) + \frac{g_{a\gamma\gamma} a(t)}{c} \vec{E}_0(\vec{r}, t) \right)$$

$$- \frac{1}{c^2} \partial_t \left(\vec{E}_1(\vec{r}, t) - g_{a\gamma\gamma} a(\vec{r}, t) c \vec{B}_0(\vec{r}, t) \right) = \mu_0 \vec{J}_{e_1}$$

$$\nabla \cdot \vec{B}_1(\vec{r}, t) = 0$$

$$\nabla \times \vec{E}_1(\vec{r}, t) + \partial_t \vec{B}_1(\vec{r}, t) = 0.$$

Applied Background Field

$$\nabla \times \vec{B}_0 = \mu_0 \epsilon_0 \partial_t \vec{E}_0 + \mu_0 \vec{J}_{e_0}$$

$$\nabla \times \vec{E}_0 = - \partial_t \vec{B}_0$$

$$\nabla \cdot \vec{B}_0 = 0$$

$$\nabla \cdot \vec{E}_0 = \epsilon_0^{-1} \rho_{e_0}$$

Photonic Haloscope Equations in terms of Auxiliary Fields

Measure Created Photon

$$\nabla \cdot \left(\vec{E}_1(\vec{r}, t) - g_{a\gamma\gamma} a(t) c \vec{B}_0(\vec{r}, t) \right) = \frac{\rho_{e_1}}{\epsilon_0}$$

$$\nabla \times \left(\vec{B}_1(\vec{r}, t) + \frac{g_{a\gamma\gamma} a(t)}{c} \vec{E}_0(\vec{r}, t) \right)$$

$$-\frac{1}{c^2} \partial_t \left(\vec{E}_1(\vec{r}, t) - g_{a\gamma\gamma} a(\vec{r}, t) c \vec{B}_0(\vec{r}, t) \right) = \mu_0 \vec{J}_{e_1}$$

$$\nabla \cdot \vec{B}_1(\vec{r}, t) = 0$$

$$\nabla \times \vec{E}_1(\vec{r}, t) + \partial_t \vec{B}_1(\vec{r}, t) = 0.$$



$$\nabla \cdot \vec{D}_1 = \rho_{e_1}$$

$$\nabla \times \vec{H}_1 - \partial_t \vec{D}_1 = \vec{J}_{e_1}$$

$$\nabla \cdot \vec{B}_1(\vec{r}, t) = 0$$

$$\nabla \times \vec{E}_1(\vec{r}, t) + \partial_t \vec{B}_1(\vec{r}, t) = 0,$$

Applied Background Field

$$\nabla \times \vec{B}_0 = \mu_0 \epsilon_0 \partial_t \vec{E}_0 + \mu_0 \vec{J}_{e_0}$$

$$\nabla \times \vec{E}_0 = -\partial_t \vec{B}_0$$

$$\nabla \cdot \vec{B}_0 = 0$$

$$\nabla \cdot \vec{E}_0 = \epsilon_0^{-1} \rho_{e_0}$$

Photonic Haloscope Equations in terms of Auxiliary Fields

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**Constitutive Relations (Include Matter)
Effective Magnetisation and Polarisation**

Applied Background Field

$$\nabla \times \vec{B}_0 = \mu_0 \epsilon_0 \partial_t \vec{E}_0 + \mu_0 \vec{J}_{e_0}$$

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Photonic Haloscope Equations in terms of Auxiliary Fields

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$$\vec{H}_1(\vec{r}, t) = \frac{\vec{B}_1}{\mu_0} - \vec{M}_1 - \vec{M}_{a1};$$

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Effective Magnetisation and Polarisation**

$$\vec{H}_1(\vec{r}, t) = \frac{\vec{B}_1}{\mu_0} - \vec{M}_1 - \vec{M}_{a1};$$

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Applied Background Field

$$\nabla \times \vec{B}_0 = \mu_0 \epsilon_0 \partial_t \vec{E}_0 + \mu_0 \vec{J}_{e_0}$$

$$\nabla \times \vec{E}_0 = -\partial_t \vec{B}_0$$

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Measure Created Photon

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$$\nabla \times \vec{P}_{a1} \neq 0 = -g_{a\gamma\gamma} a(t) c \nabla \times \vec{B}_0(\vec{r}, t) \quad (\nabla a = 0)$$

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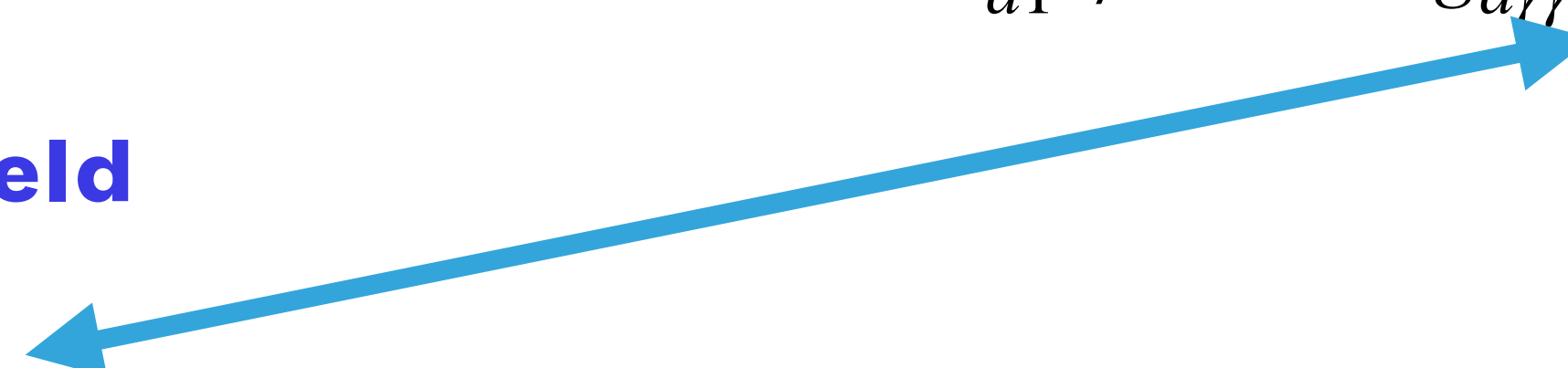
Applied Background Field

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Photonic Haloscope Equations in terms of Auxiliary Fields

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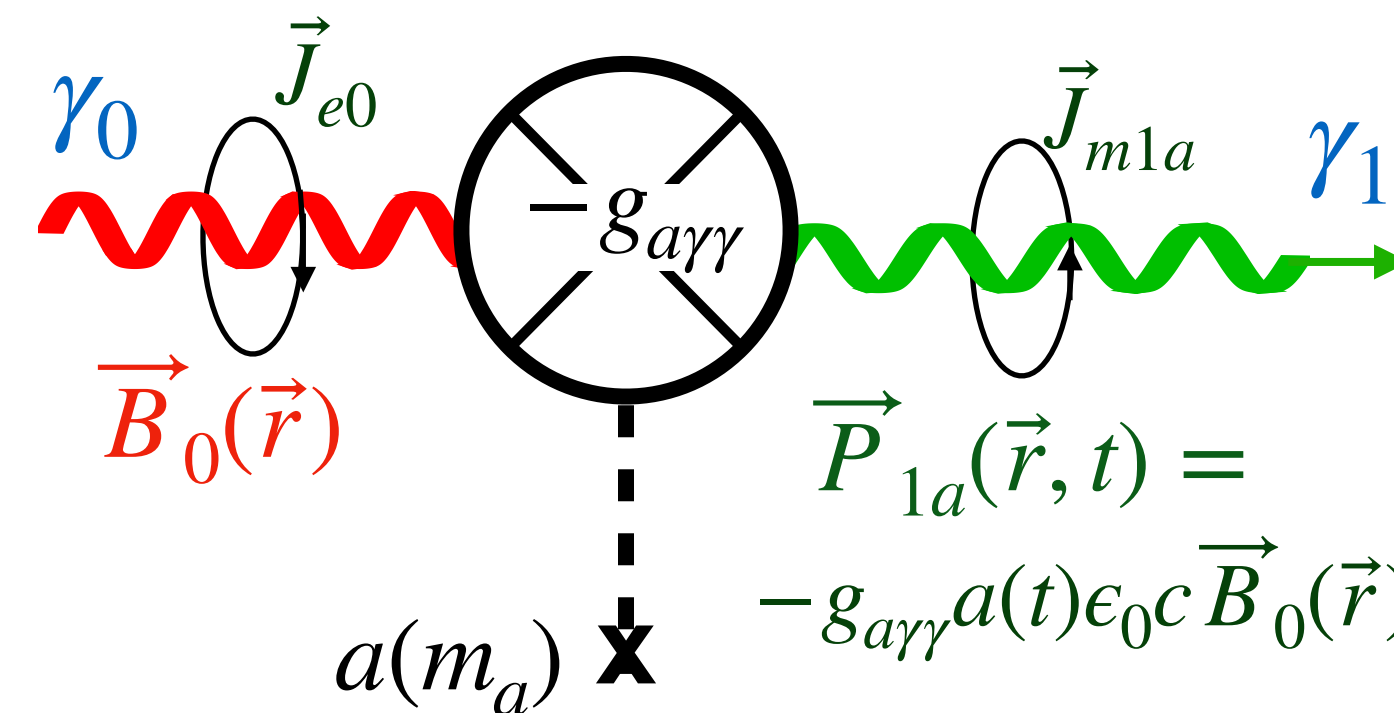
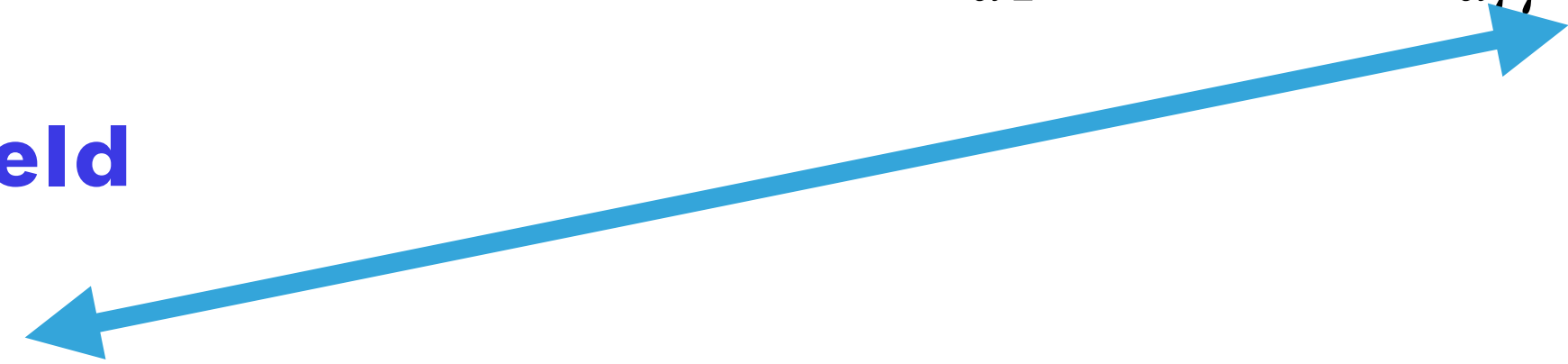
Applied Background Field

$$\nabla \times \vec{B}_0 = \mu_0 \epsilon_0 \partial_t \vec{E}_0 + \mu_0 \vec{J}_{e_0}$$

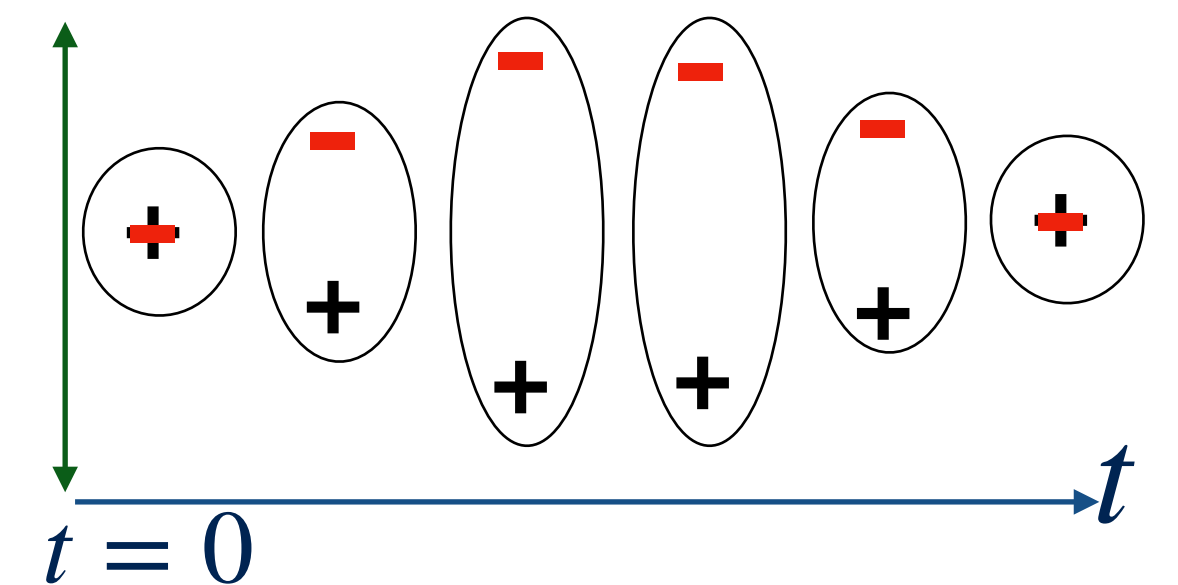
$$\nabla \times \vec{E}_0 = -\partial_t \vec{B}_0$$

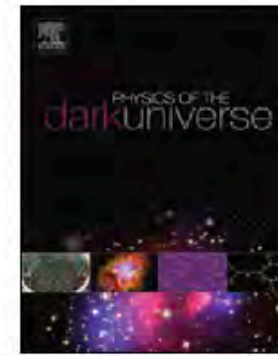
$$\nabla \cdot \vec{B}_0 = 0$$

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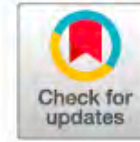


$$\vec{J}_{ab}(\vec{r}, t) = \frac{\partial \vec{P}_{a1}(\vec{r}, t)}{\partial t}$$





Modified axion electrodynamics as impressed electromagnetic sources through oscillating background polarization and magnetization

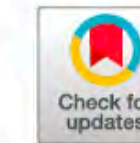


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Broadband electrical action sensing techniques with conducting wires for low-mass dark matter axion detection



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Few thoughts on θ and the electric dipole moments

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Department of Physics and Astronomy, University of British Columbia, Vancouver, British Columbia V6T 1Z1, Canada

Electric polarization as a nonquantized topological response and boundary Luttinger theorem

Xue-Yang Song^{1,2}, Yin-Chen He², Ashvin Vishwanath¹ and Chong Wang²

¹Department of Physics, Harvard University, Cambridge, Massachusetts 02138, USA

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Emergent electric field from magnetic resonances in a one-dimensional chiral magnet

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¹Department of Applied Physics, The University of Tokyo, Tokyo 113-8656, Japan

(Dated: July 18, 2023)

The emergent electric field (EEF) is a fictitious electric field acting on conduction electrons through the Berry phase mechanism.

DC Magnetic Haloscopes

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- Axions convert into photons in presence of strong magnetic field: Mass is unknown

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$$\lambda_a > d_{exp}$$

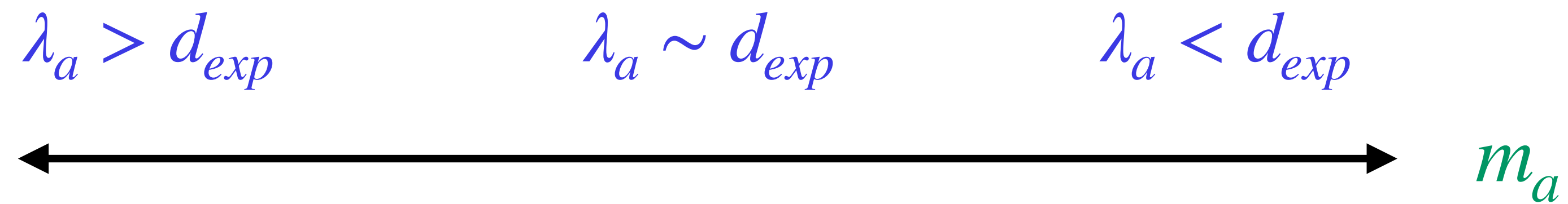
$$\lambda_a \sim d_{exp}$$

$$\lambda_a < d_{exp}$$



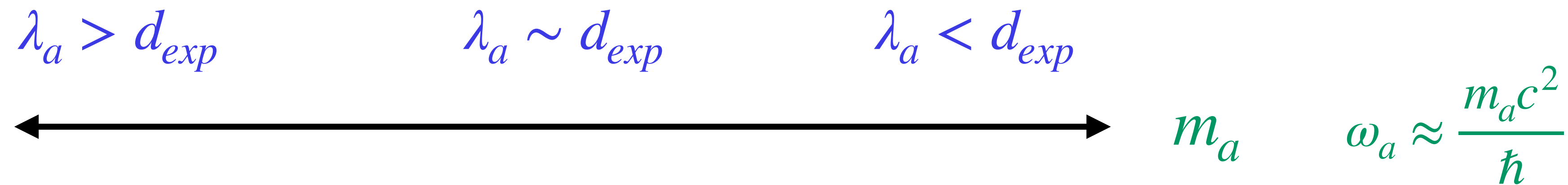
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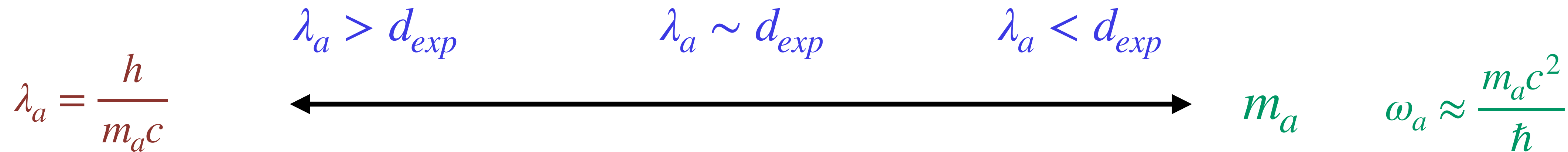
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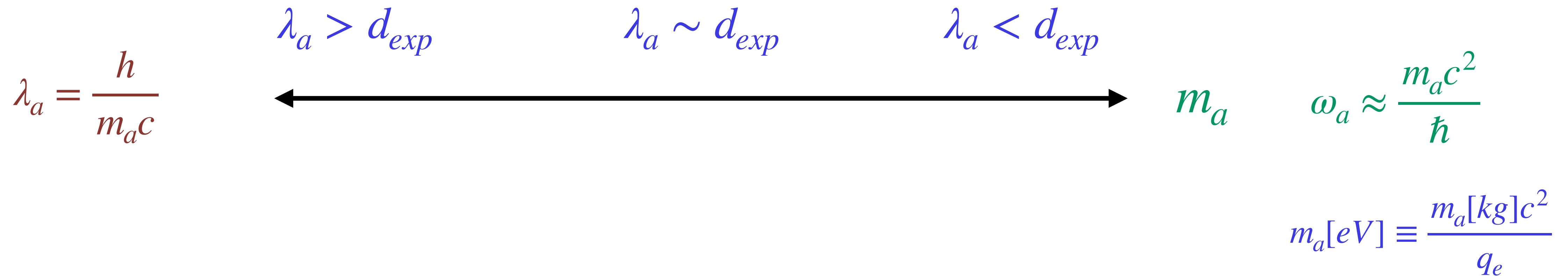
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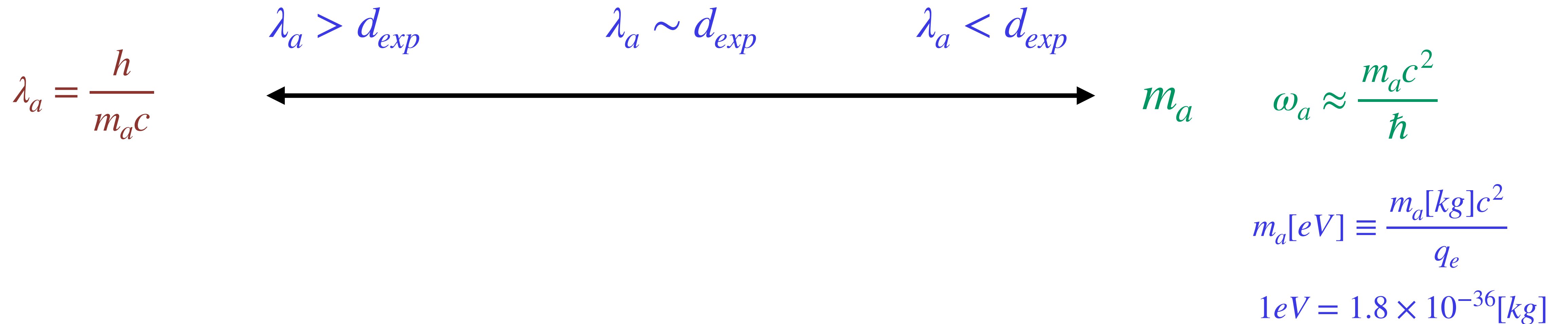
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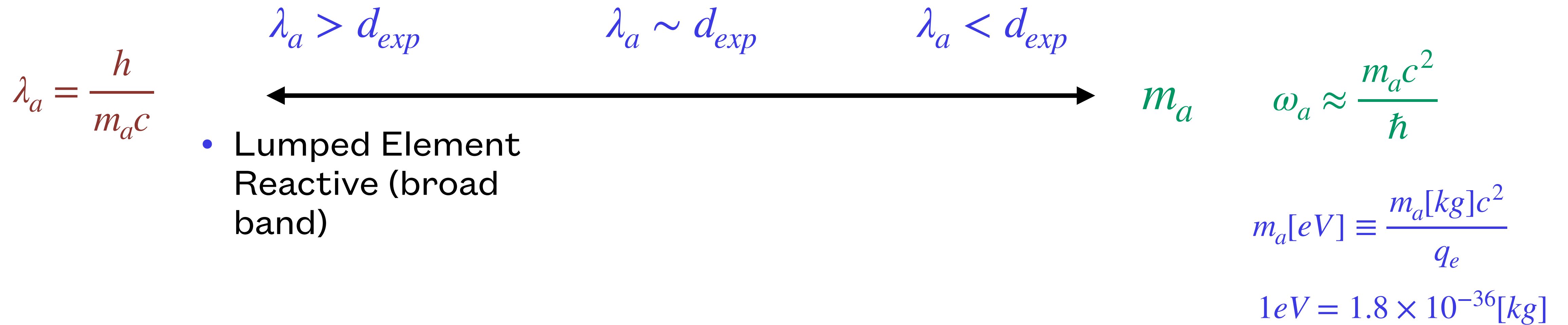
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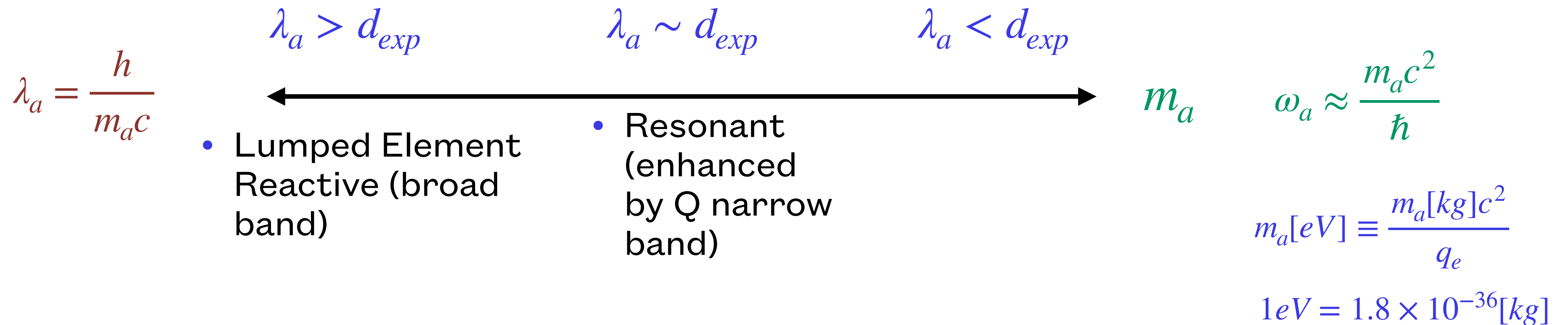
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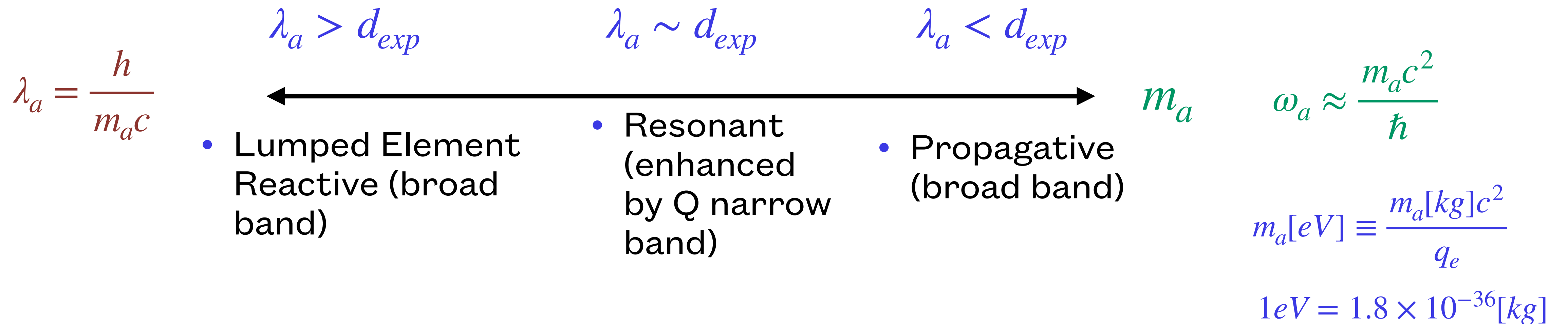
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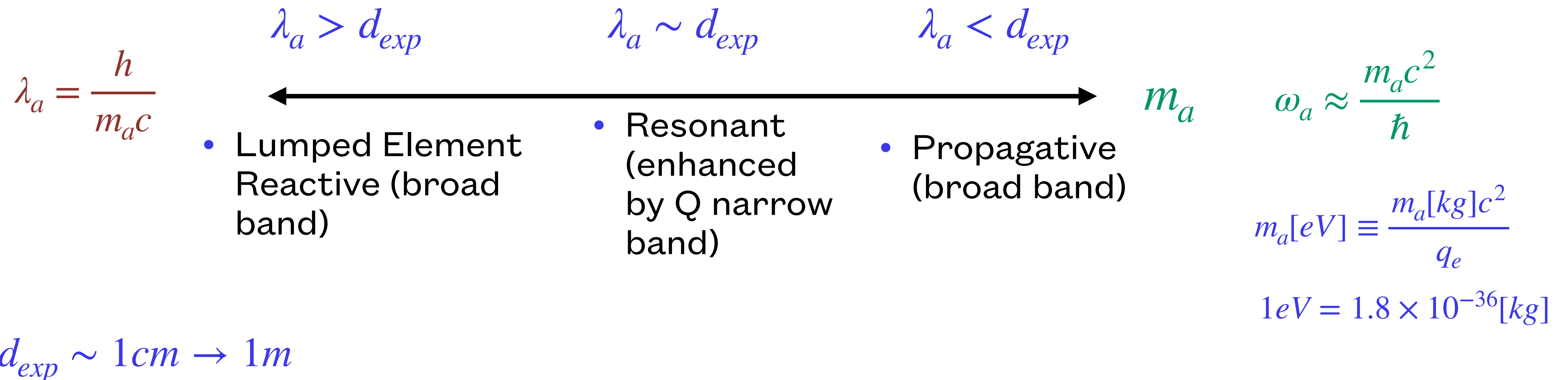
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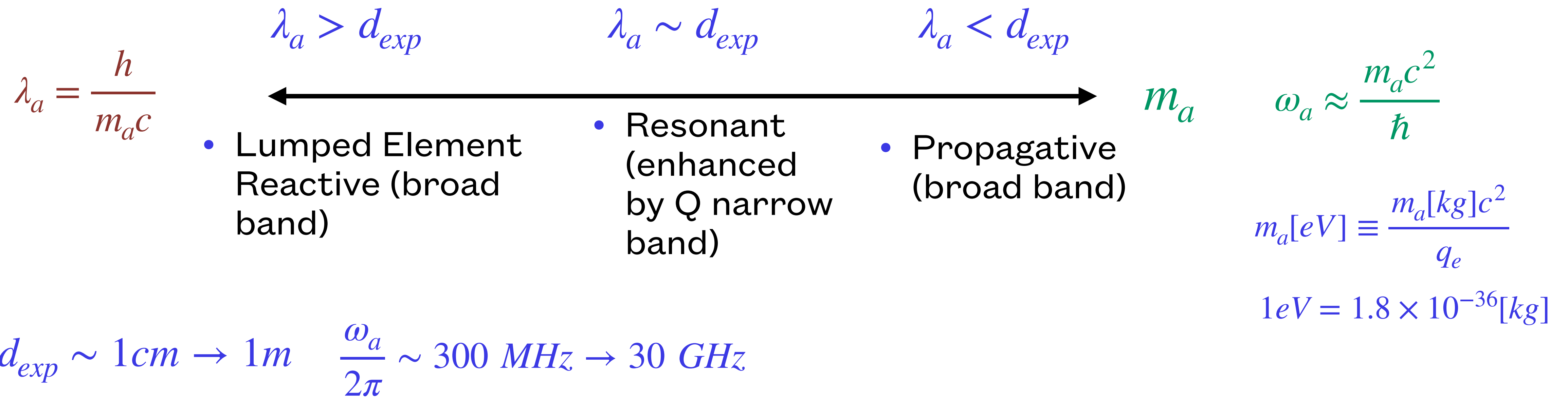
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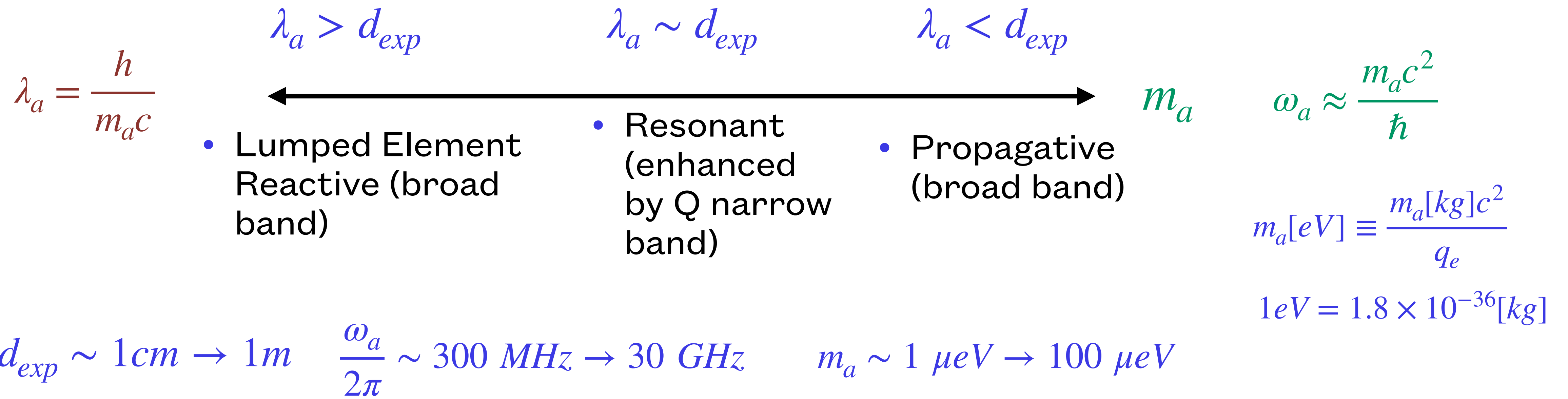
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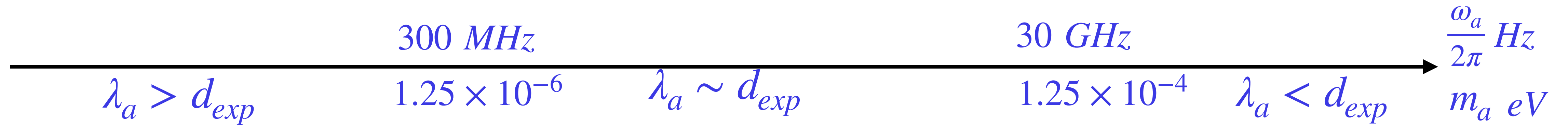
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DC Magnetic Haloscopes

Type Depends on Axion Compton Wavelength

$$\lambda_a = \frac{h}{cm_a}$$



DC Magnetic Haloscopes

Type Depends on Axion Compton Wavelength

$$\lambda_a = \frac{h}{cm_a}$$

Low Mass: Lumped Element

Reactive

300 MHz

30 GHz

$\frac{\omega_a}{2\pi}$ Hz

$$\lambda_a > d_{exp}$$

$$1.25 \times 10^{-6}$$

$$\lambda_a \sim d_{exp}$$

$$1.25 \times 10^{-4}$$

$$\lambda_a < d_{exp}$$

$$m_a \text{ eV}$$

ADMX SLIC

RE-ENTRANT CAVITY

ABRACADABRA

SHAFT

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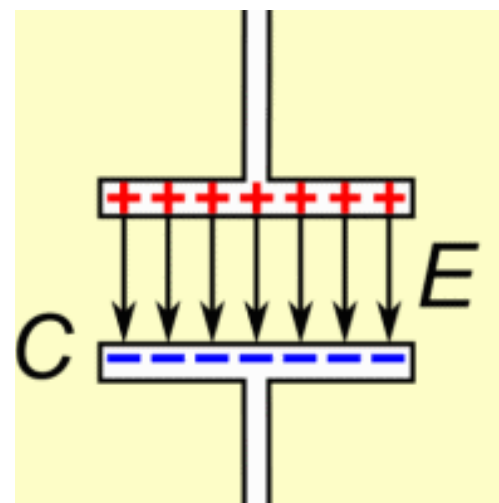
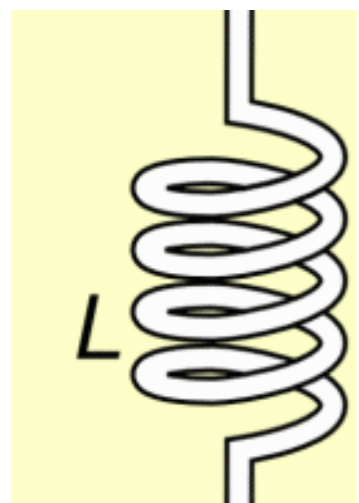
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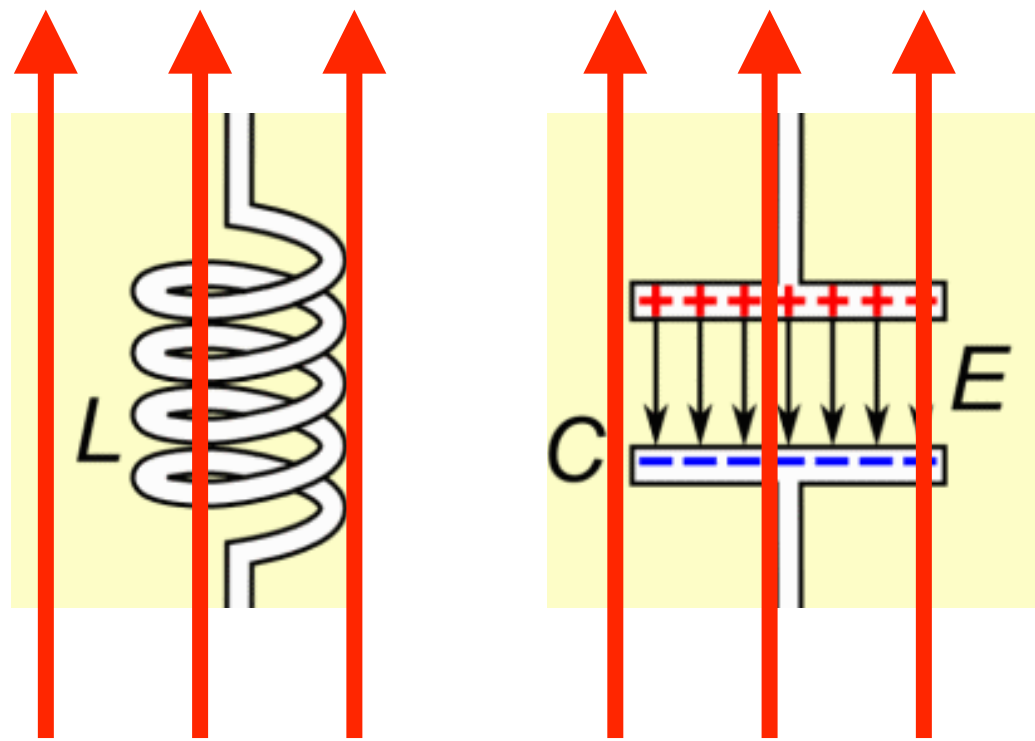
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$$\vec{B} = B_{DC} \hat{z}$$

DC Magnetic Haloscopes

Type Depends on Axion Compton Wavelength

$$\lambda_a = \frac{h}{cm_a}$$

Middle Mass: Resonant Cavity
Reactive and Dissipative

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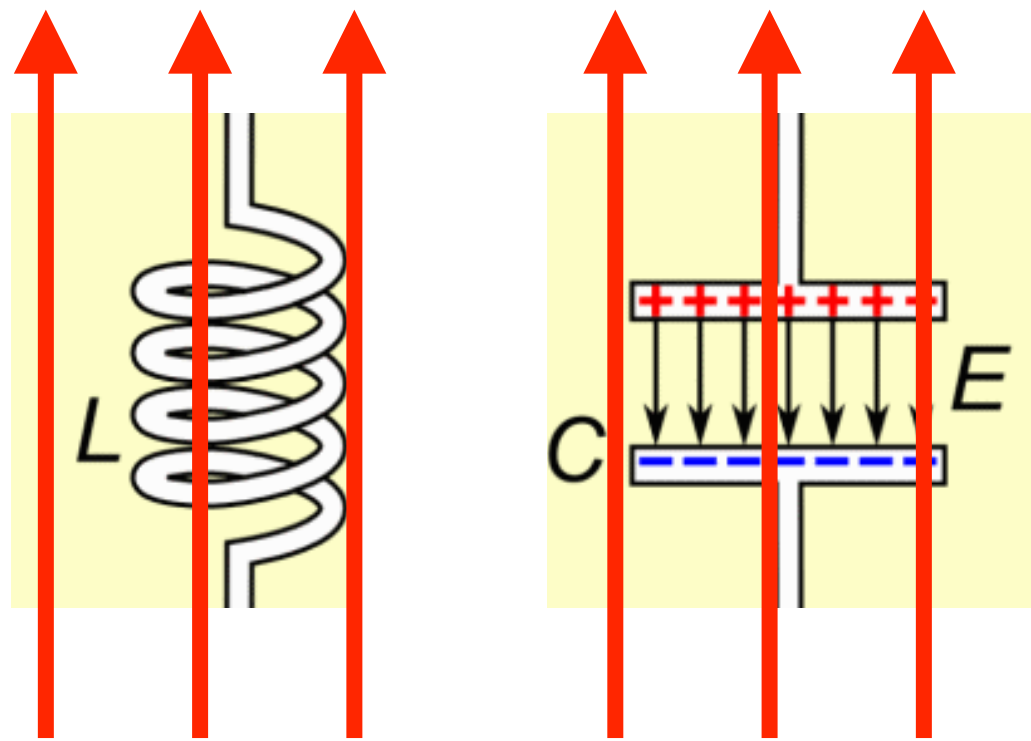
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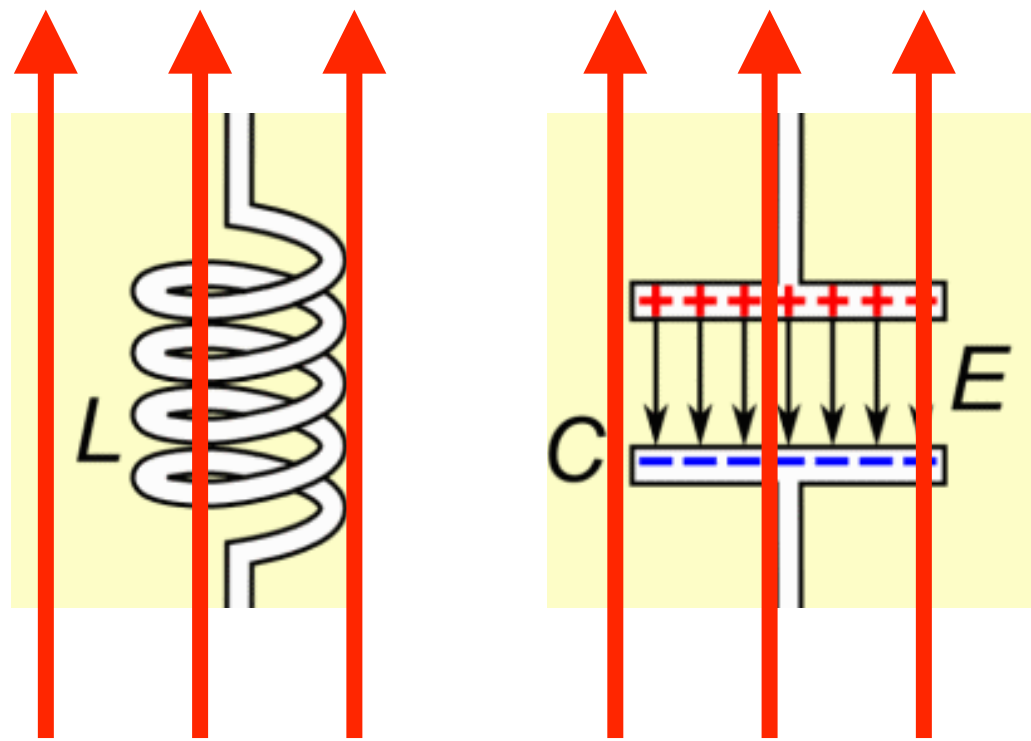
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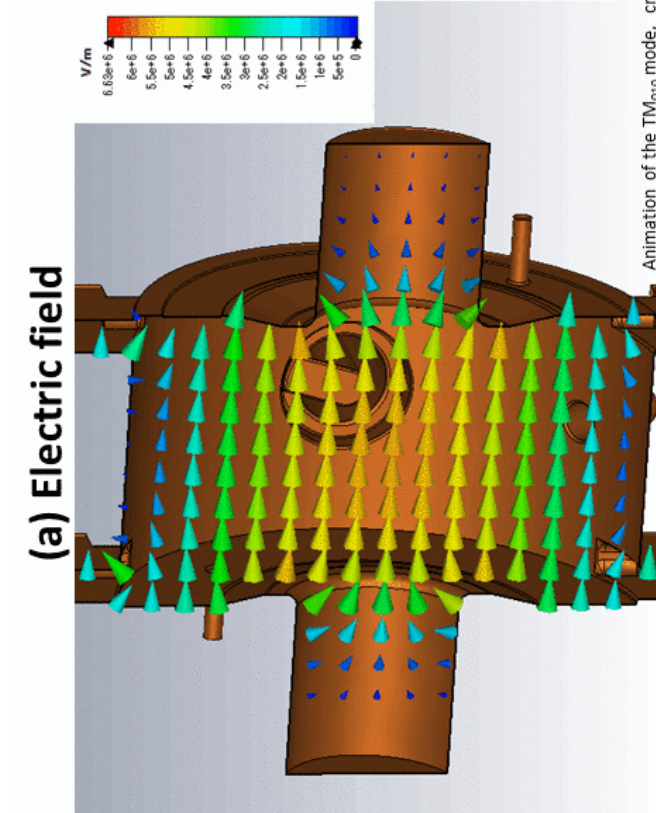
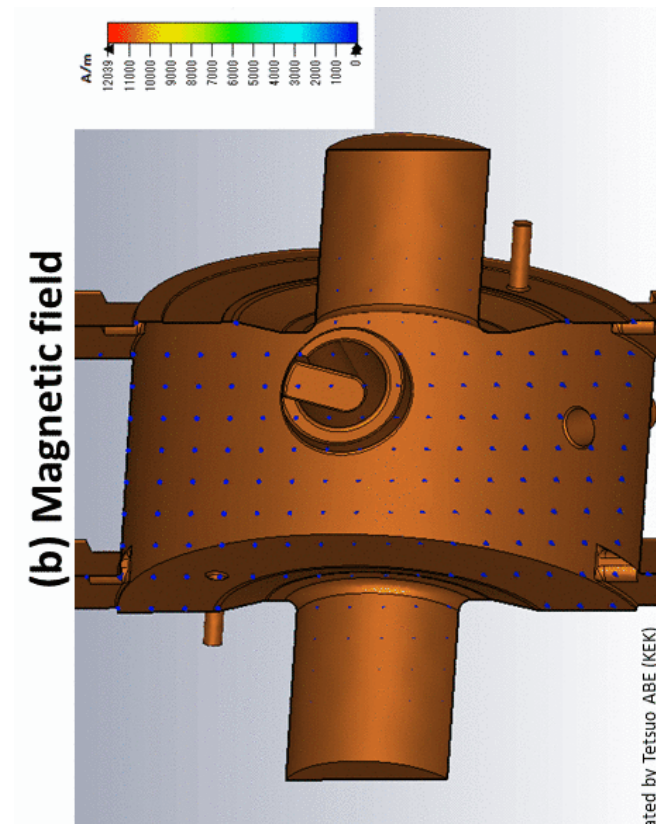
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Animation of the TM₀₁₀ mode, created by Tatsuo ABE (KEK)

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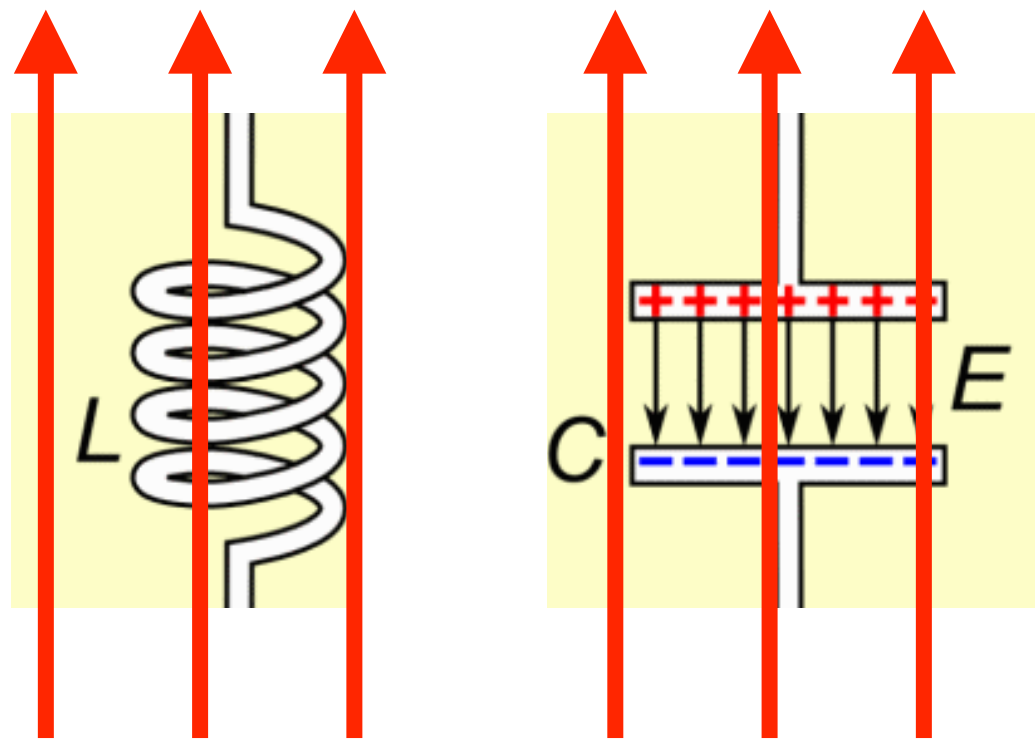
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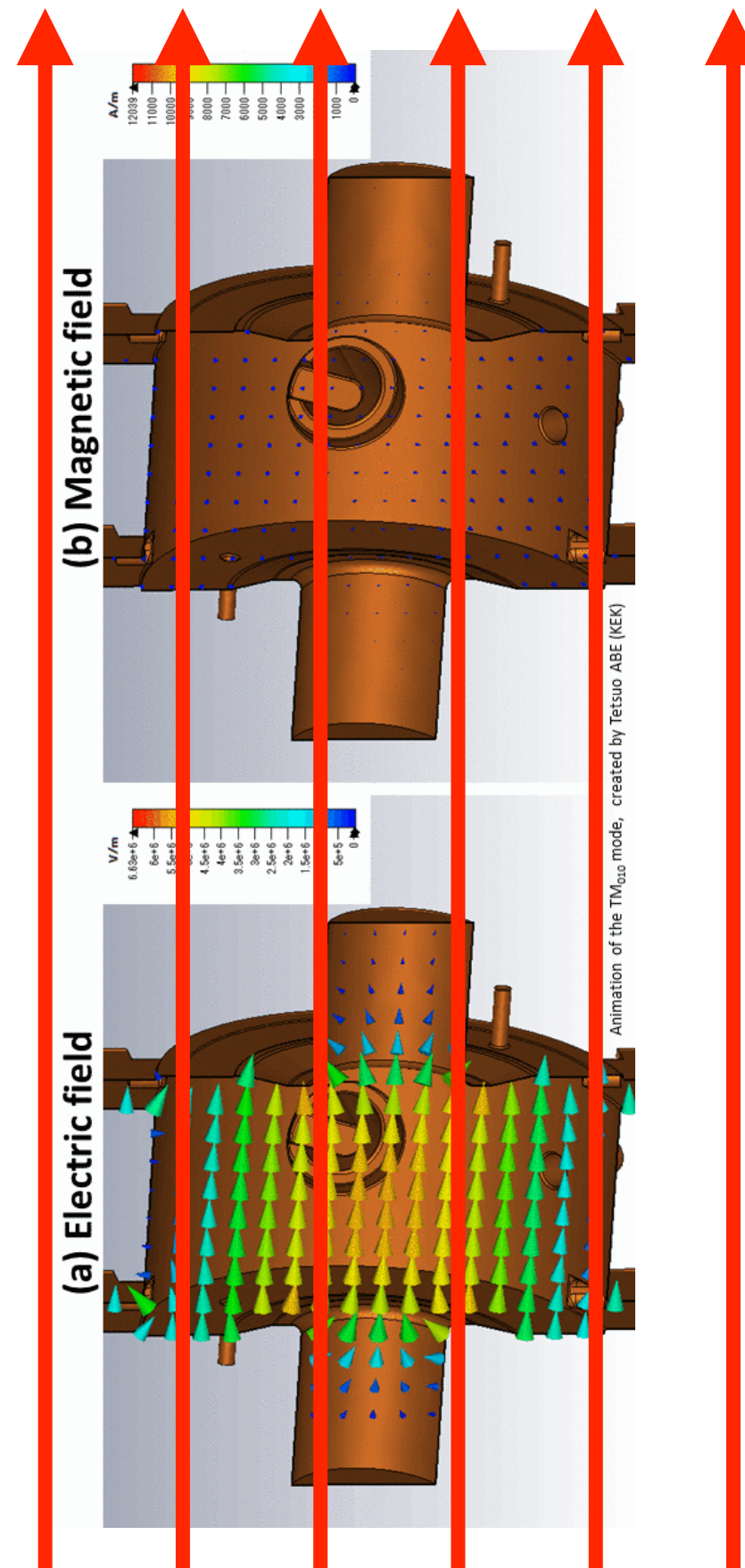
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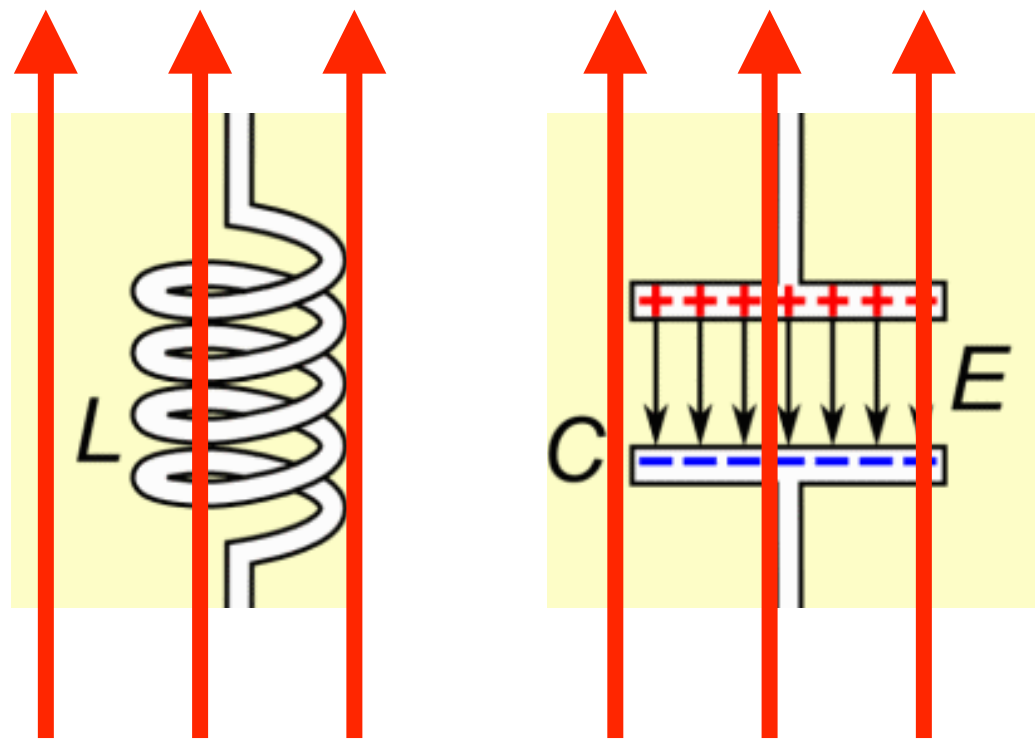
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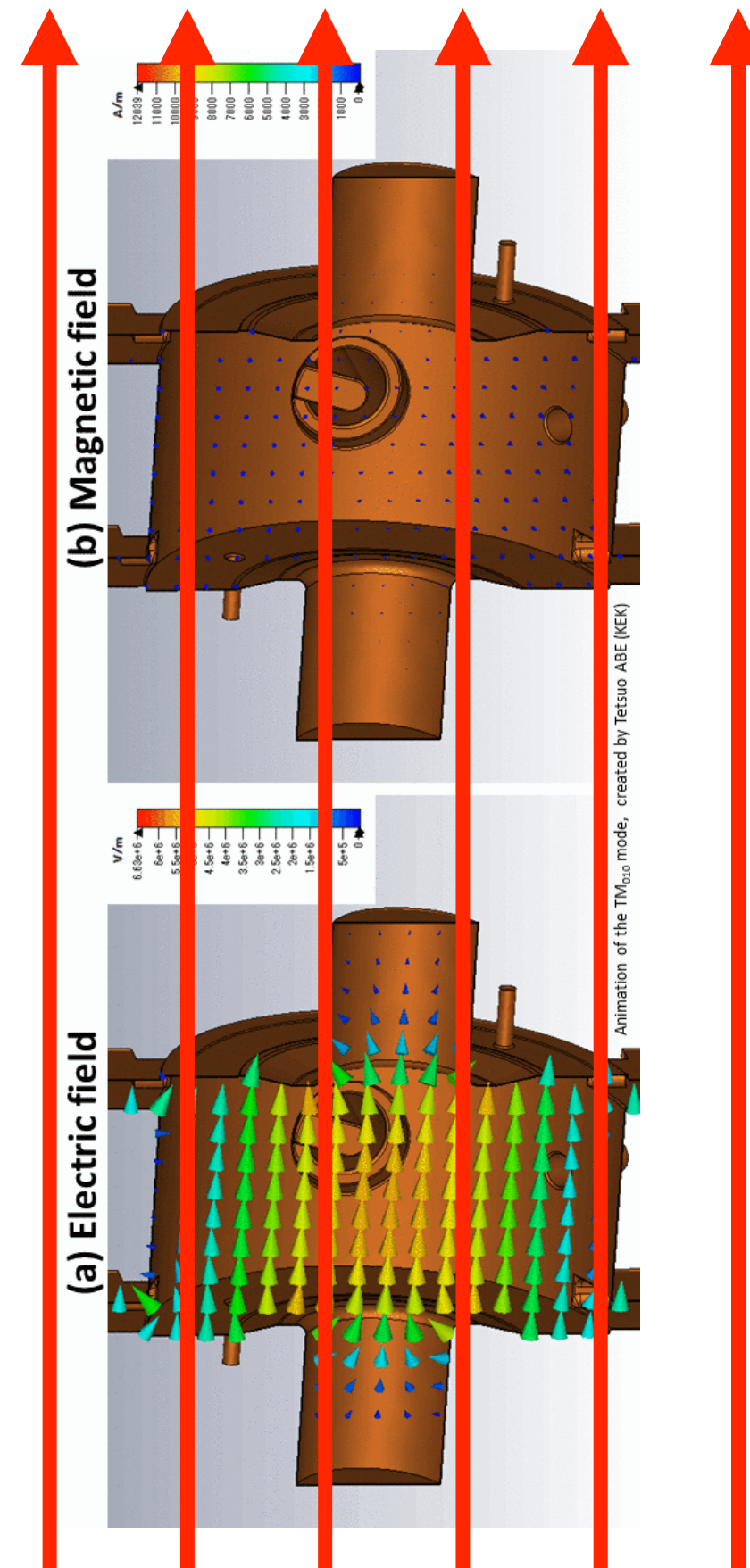
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CULTASK
ORGAN
QUAX
RADES

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Reactive and Dissipative

$$\lambda_a \sim d_{exp}$$



30 GHz

$$1.25 \times 10^{-4}$$

MADMAX
BREAD

High Mass: Propagating

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DC Magnetic Haloscopes

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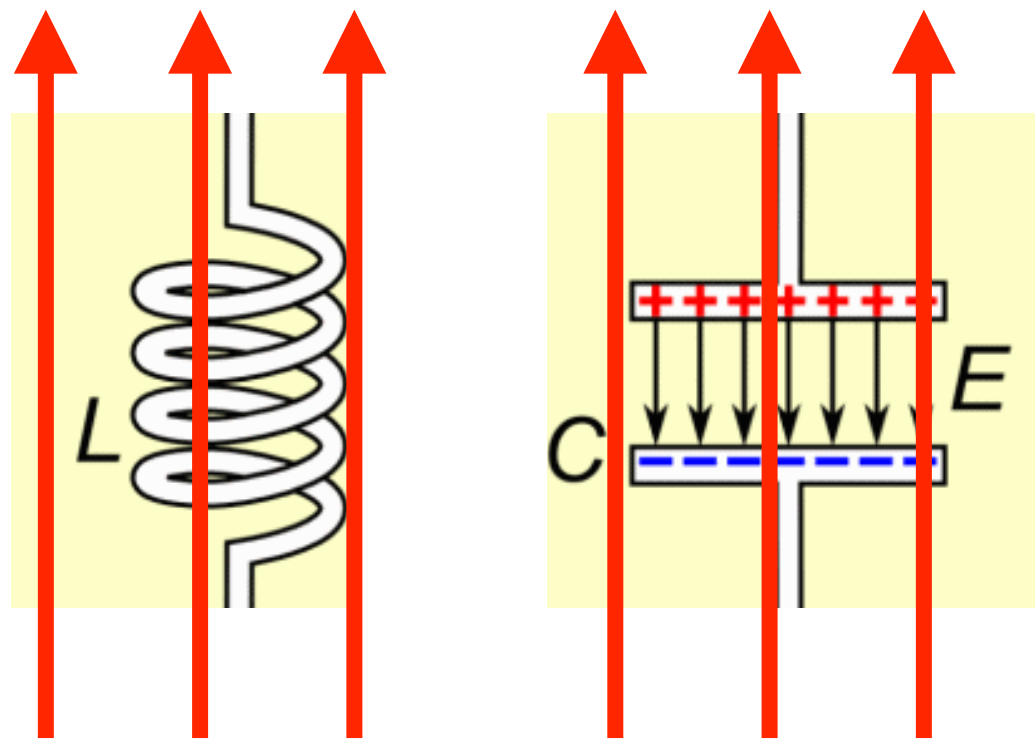
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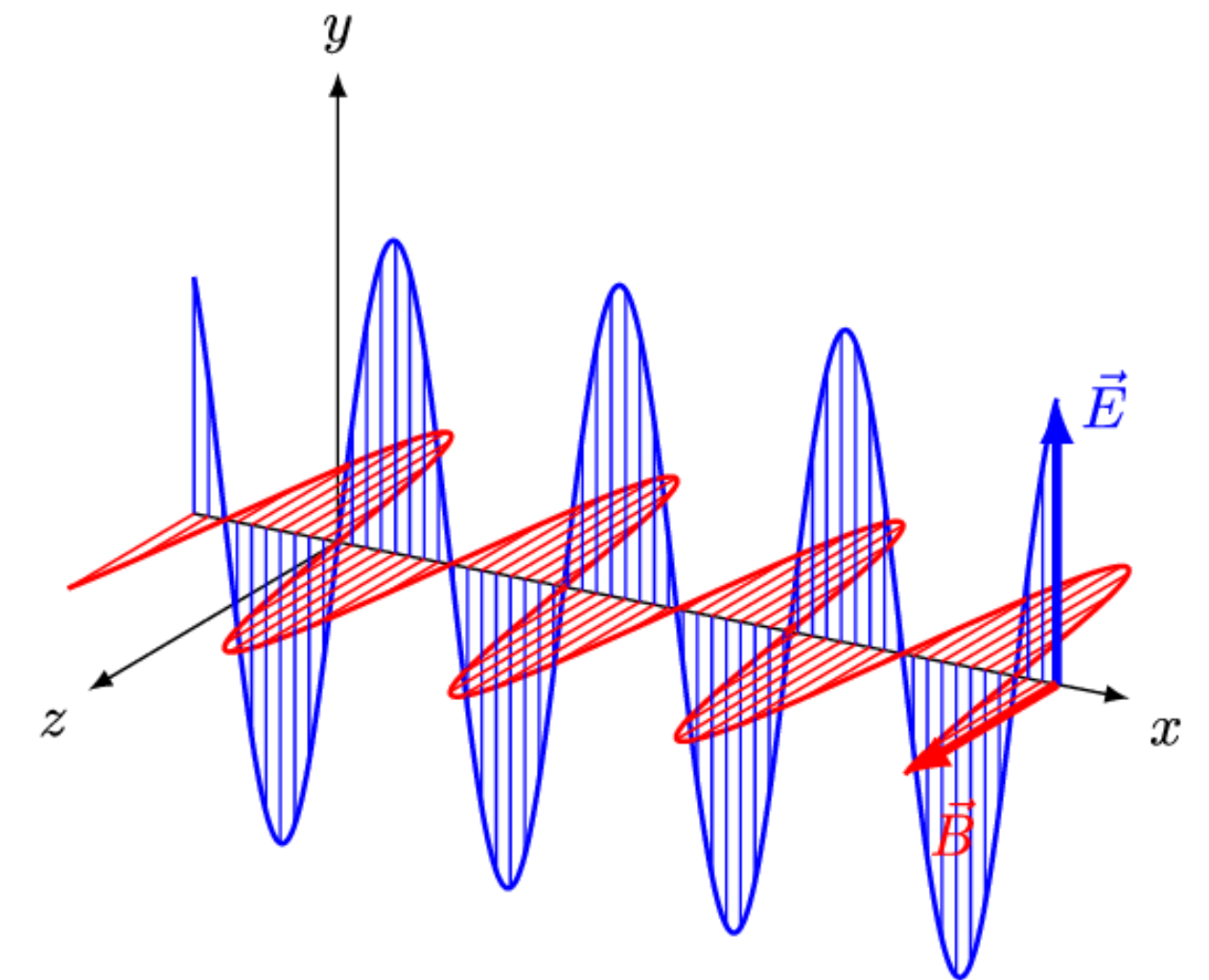
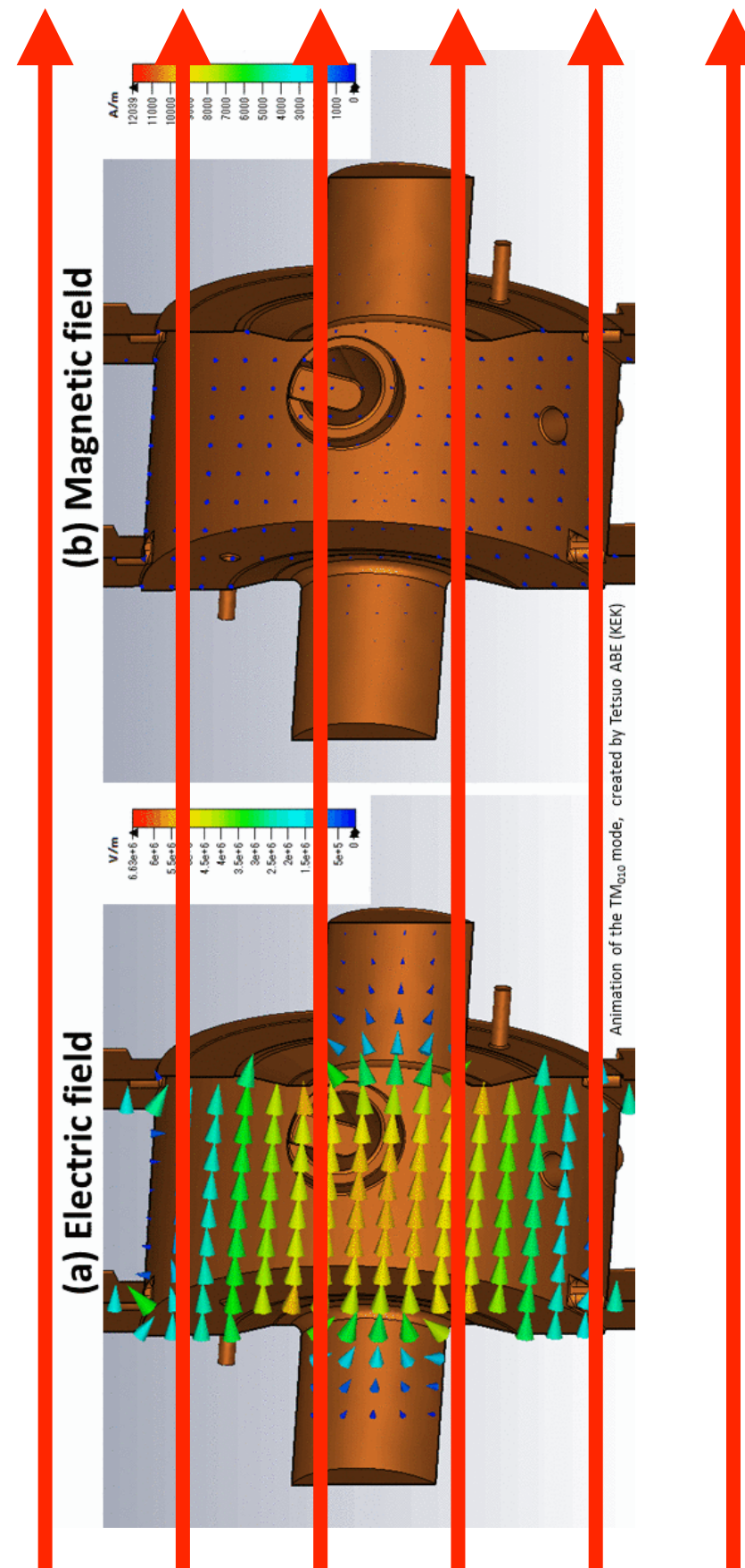
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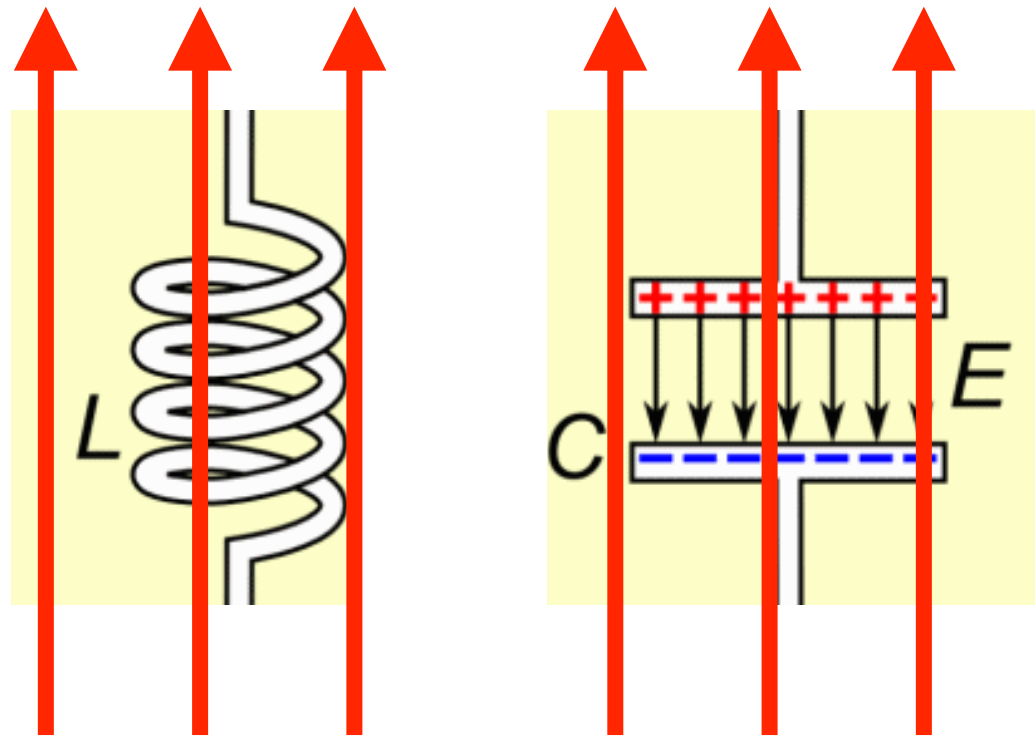
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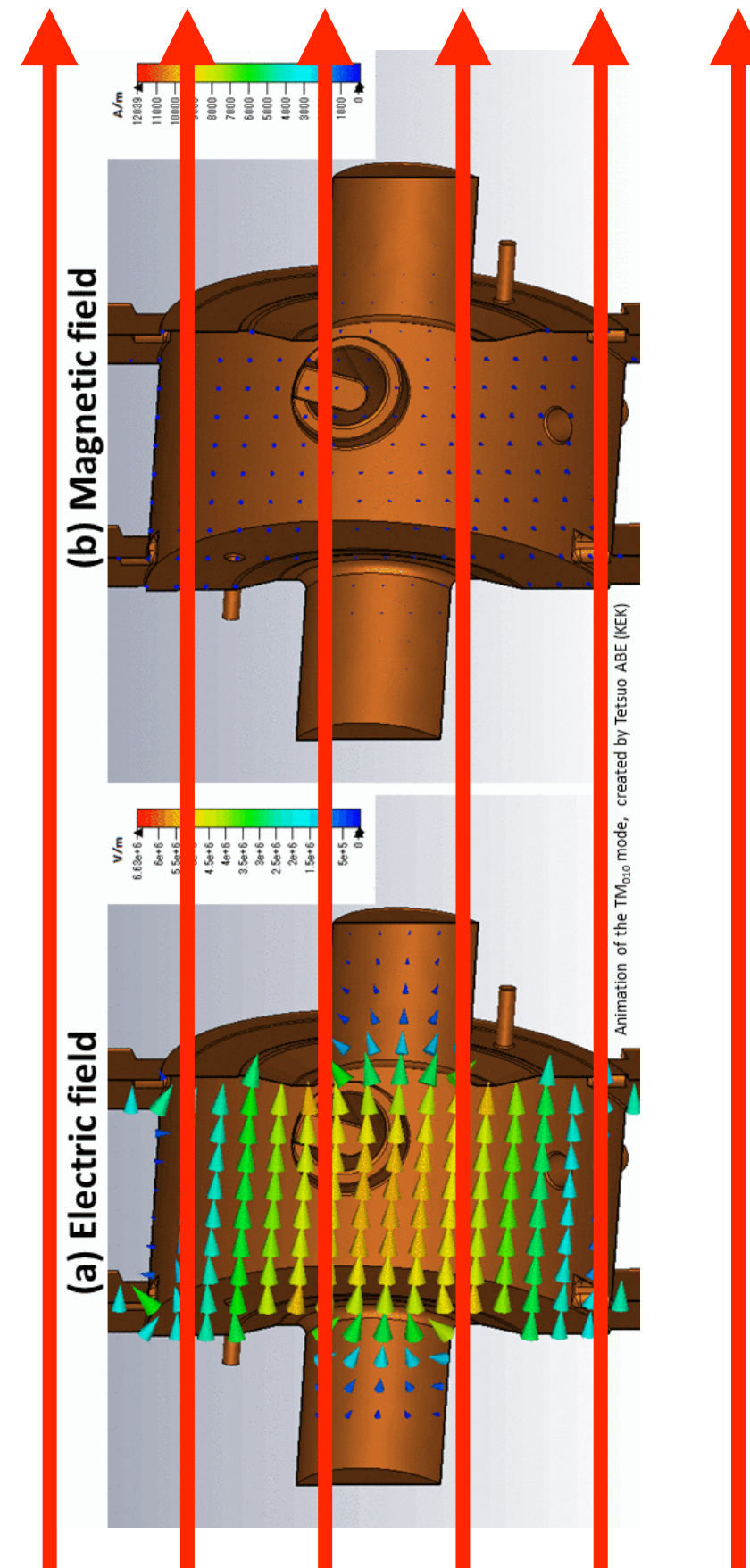
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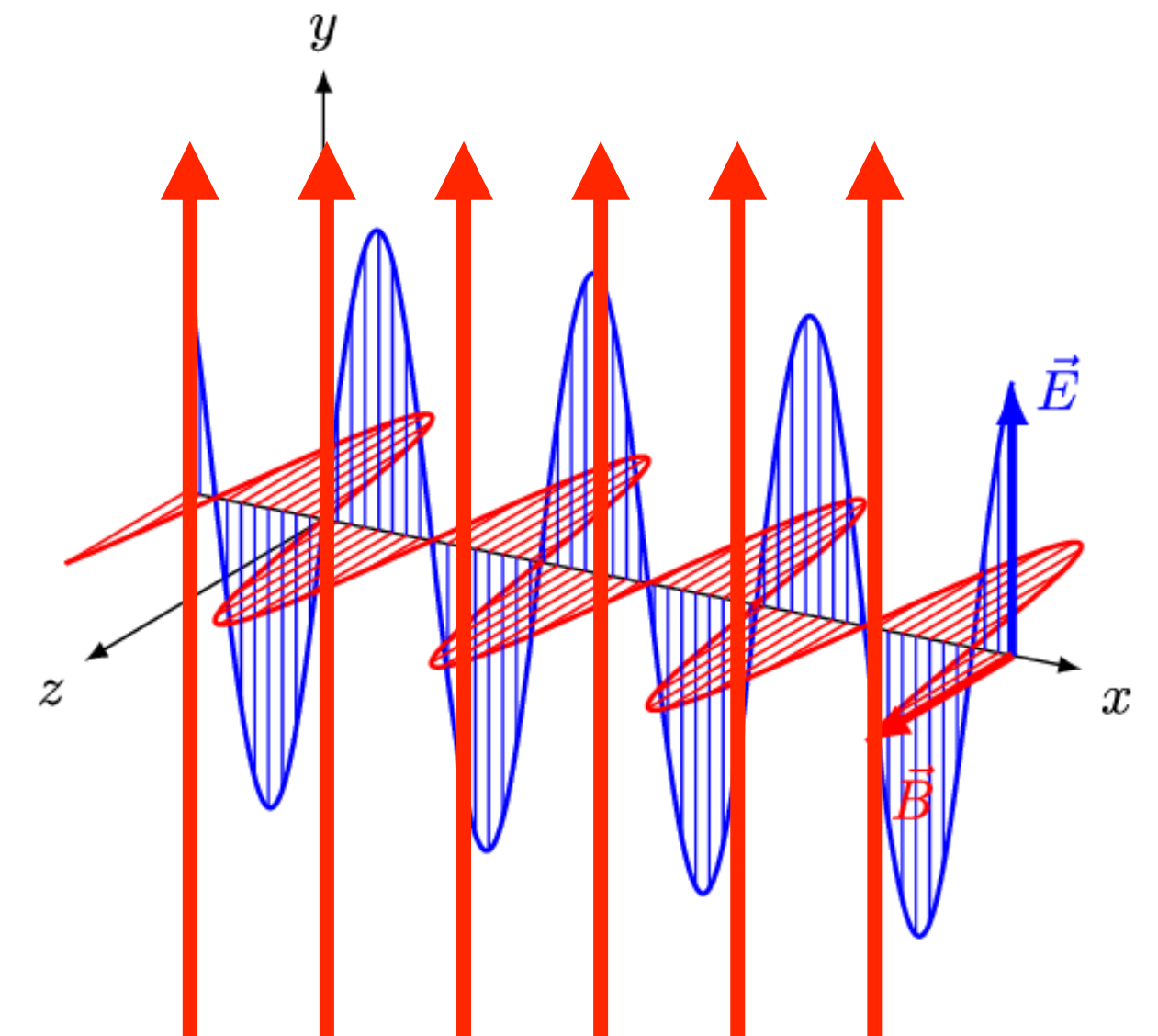
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MADMAX
BREAD

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POYNTING THEOREM

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Instantaneous Poynting vector

$$\begin{aligned}\vec{S}_1(t) &= \frac{1}{\mu_0} \vec{E}_1(t) \times \vec{B}_1(t) = \frac{1}{2} \left(\mathbf{E}_1 e^{-j\omega_1 t} + \mathbf{E}_1^* e^{j\omega_1 t} \right) \times \frac{1}{2\mu_0} \left(\mathbf{B}_1 e^{-j\omega_1 t} + \mathbf{B}_1^* e^{j\omega_1 t} \right) \\ &= \frac{1}{2\mu_0} \operatorname{Re} \left(\mathbf{E}_1 \times \mathbf{B}_1^* \right) + \frac{1}{2\mu_0} \operatorname{Re} \left(\mathbf{E}_1 \times \mathbf{B}_1 e^{-j2\omega_1 t} \right),\end{aligned}$$

$$\langle \vec{S}_1 \rangle = \frac{1}{T} \int_0^T \vec{S}_1(t) dt = \frac{1}{T} \int_0^T \left[\frac{1}{2} \operatorname{Re} \left(\mathbf{E}_1 \times \mathbf{B}_1^* \right) + \frac{1}{2} \operatorname{Re} \left(\mathbf{E}_1 \times \mathbf{B}_1 e^{-2j\omega t} \right) \right] dt = \frac{1}{2} \operatorname{Re} \left(\mathbf{E}_1 \times \mathbf{B}_1^* \right)$$

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Complex Poynting vector

- The corresponding phasor form of the Poynting vector

$$\mathbf{S}_1 = \frac{1}{2\mu_0} \mathbf{E}_1 \times \mathbf{B}_1^* \quad \text{and} \quad \mathbf{S}_1^* = \frac{1}{2\mu_0} \mathbf{E}_1^* \times \mathbf{B}_1,$$

$$\operatorname{Re}(\mathbf{S}_1) = \frac{1}{2}(\mathbf{S}_1 + \mathbf{S}_1^*) \quad \text{and} \quad j \operatorname{Im}(\mathbf{S}_1) = \frac{1}{2}(\mathbf{S}_1 - \mathbf{S}_1^*).$$

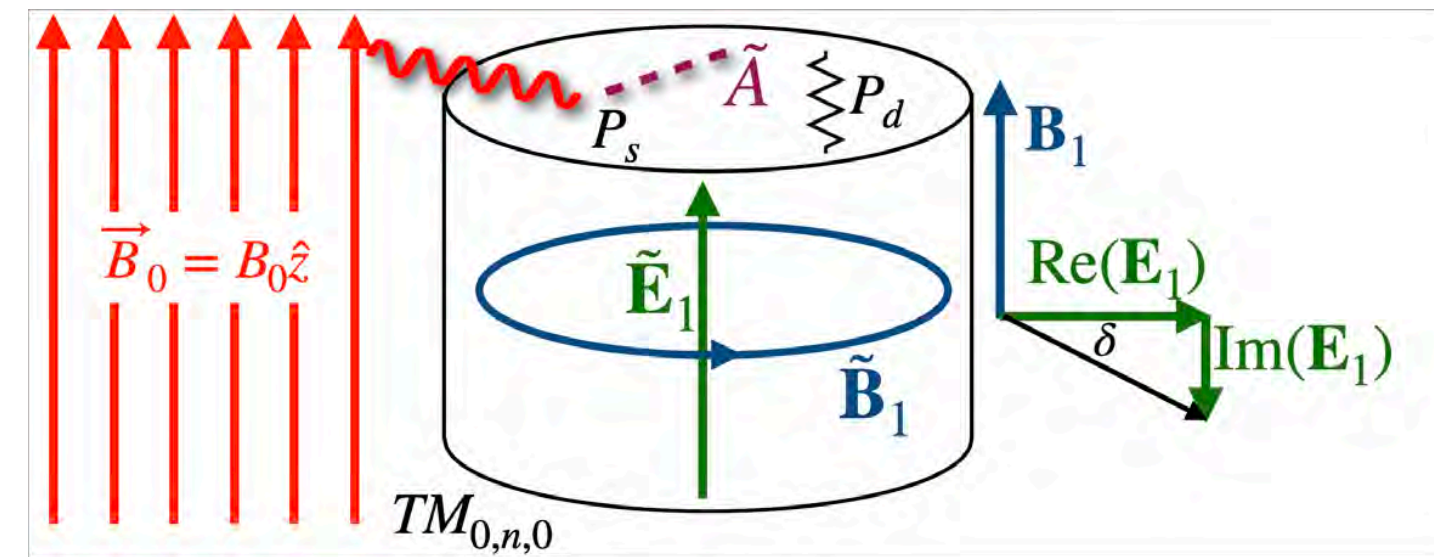
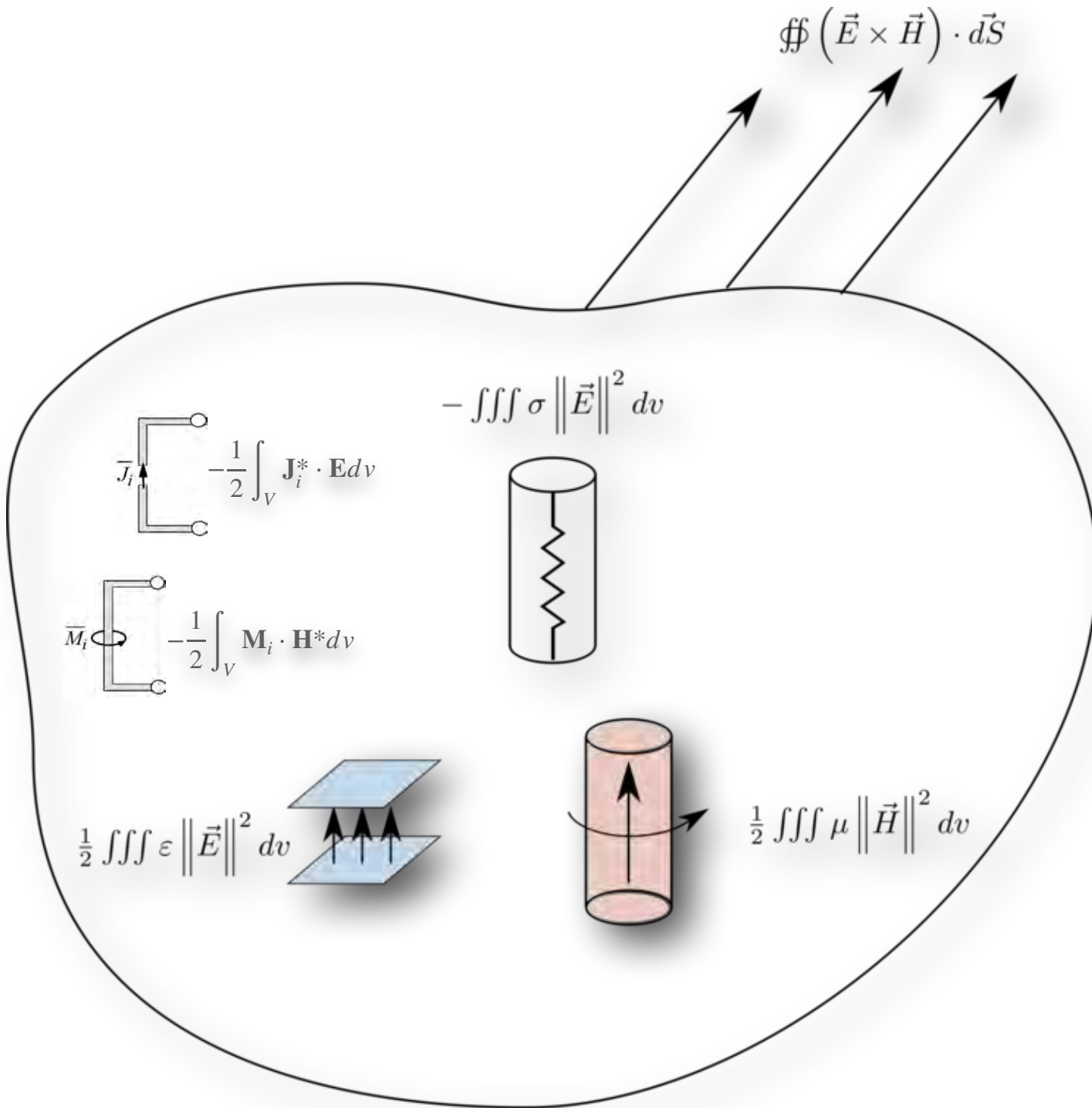
Time Average Power

Reactive Power

Sensitivity of a Resonant Haloscope

$$P_{av} = \frac{1}{2} \operatorname{Re} \oint_{S_c} (\mathbf{E} \times \mathbf{H}^*) \cdot d\mathbf{s}$$

Average radiated power outside volume



Poynting vector controversy in axion modified electrodynamics

Michael E. Tobar^{✉,*}, Ben T. McAllister, and Maxim Goryachev

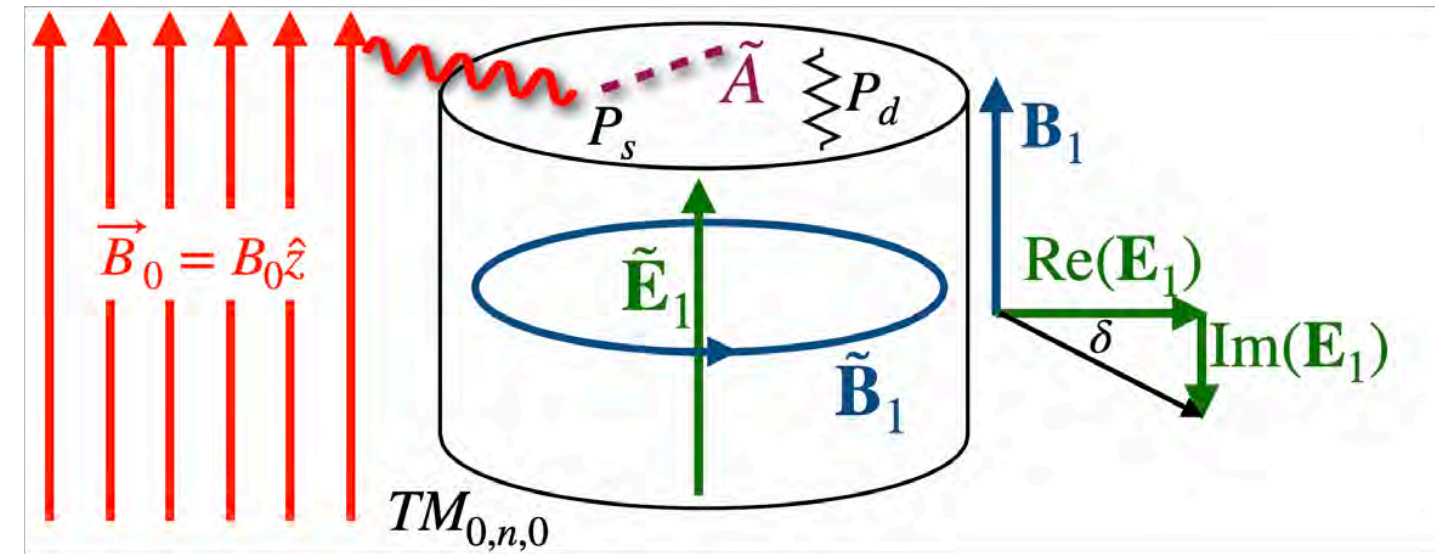
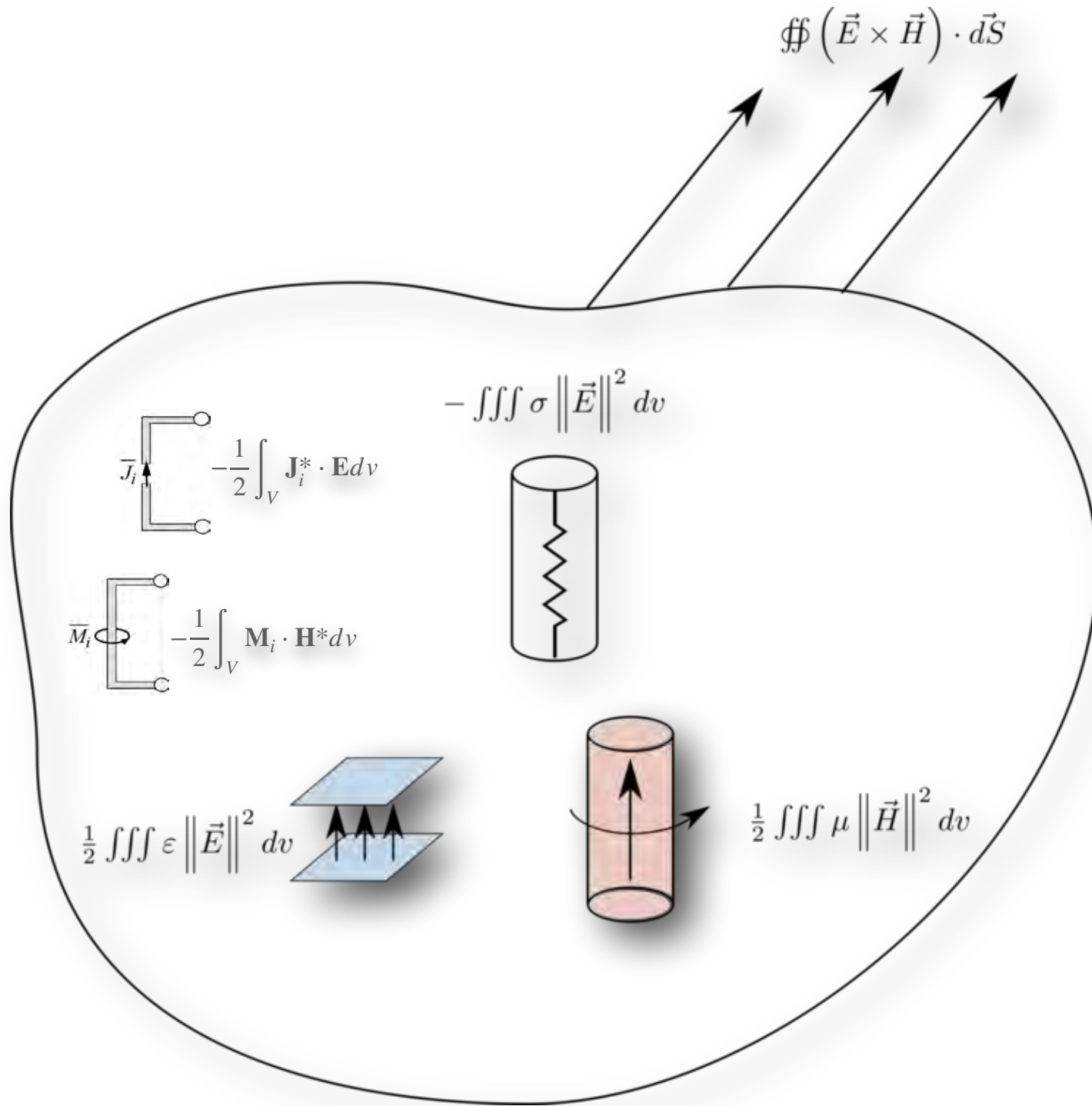
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On resonance: Real part of Complex Poynting Theorem = 0 for closed system

$$\oint \operatorname{Re}(\mathbf{S}) \cdot \hat{n} ds = \frac{j\omega_a g_{a\gamma\gamma} \epsilon_0 c}{4} \int (\mathbf{E}_1 \cdot \tilde{a}^* \mathbf{B}_0^* - \mathbf{E}_1^* \cdot \tilde{a} \mathbf{B}_0) d\tau - \frac{1}{4} \int (\mathbf{E}_1 \cdot \mathbf{J}_{e1}^* + \mathbf{E}_1^* \cdot \mathbf{J}_{e1}) d\tau$$

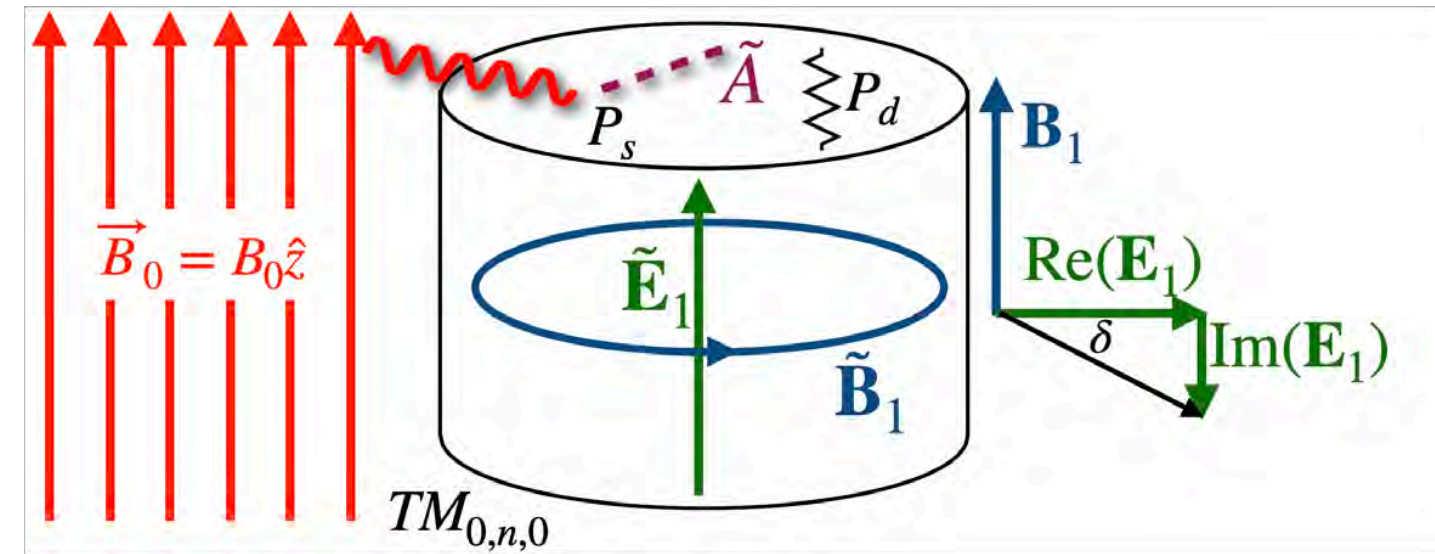
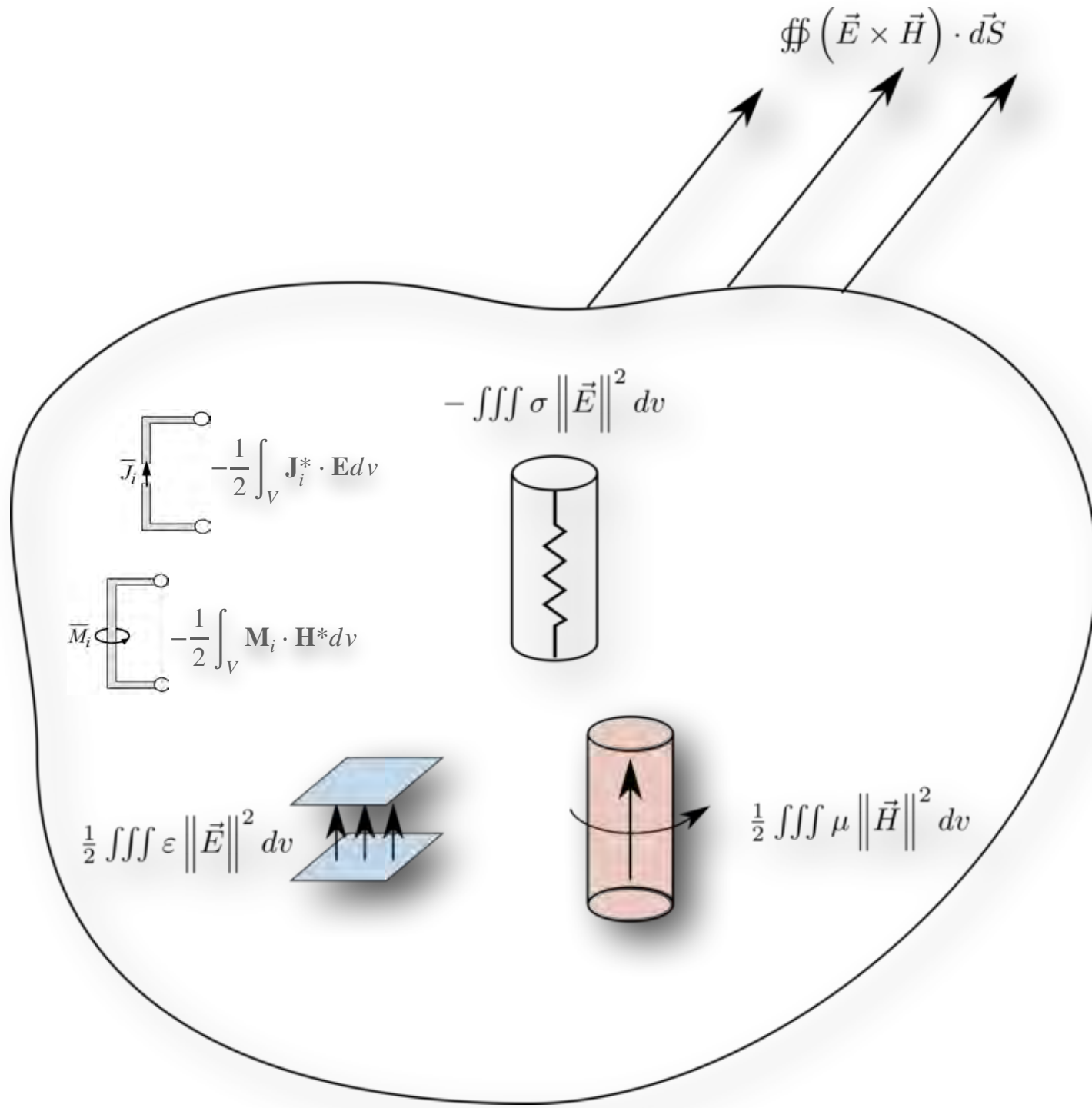
P_s Axion power input

P_d Cavity power distribution

Sensitivity of a Resonant Haloscope

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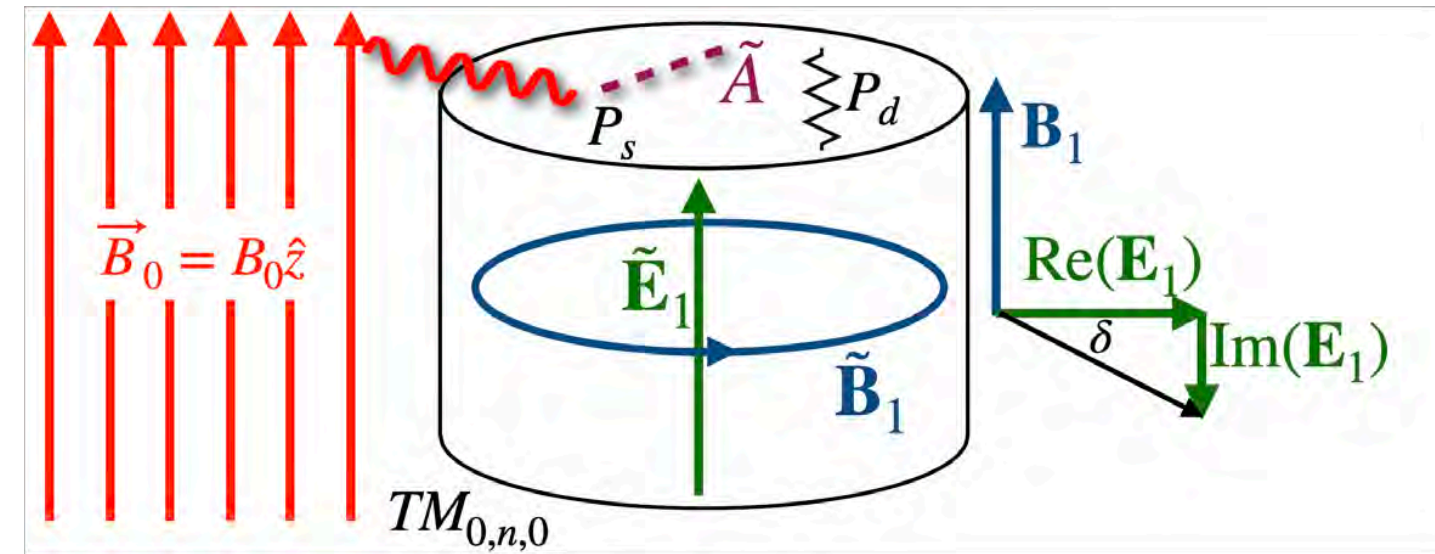
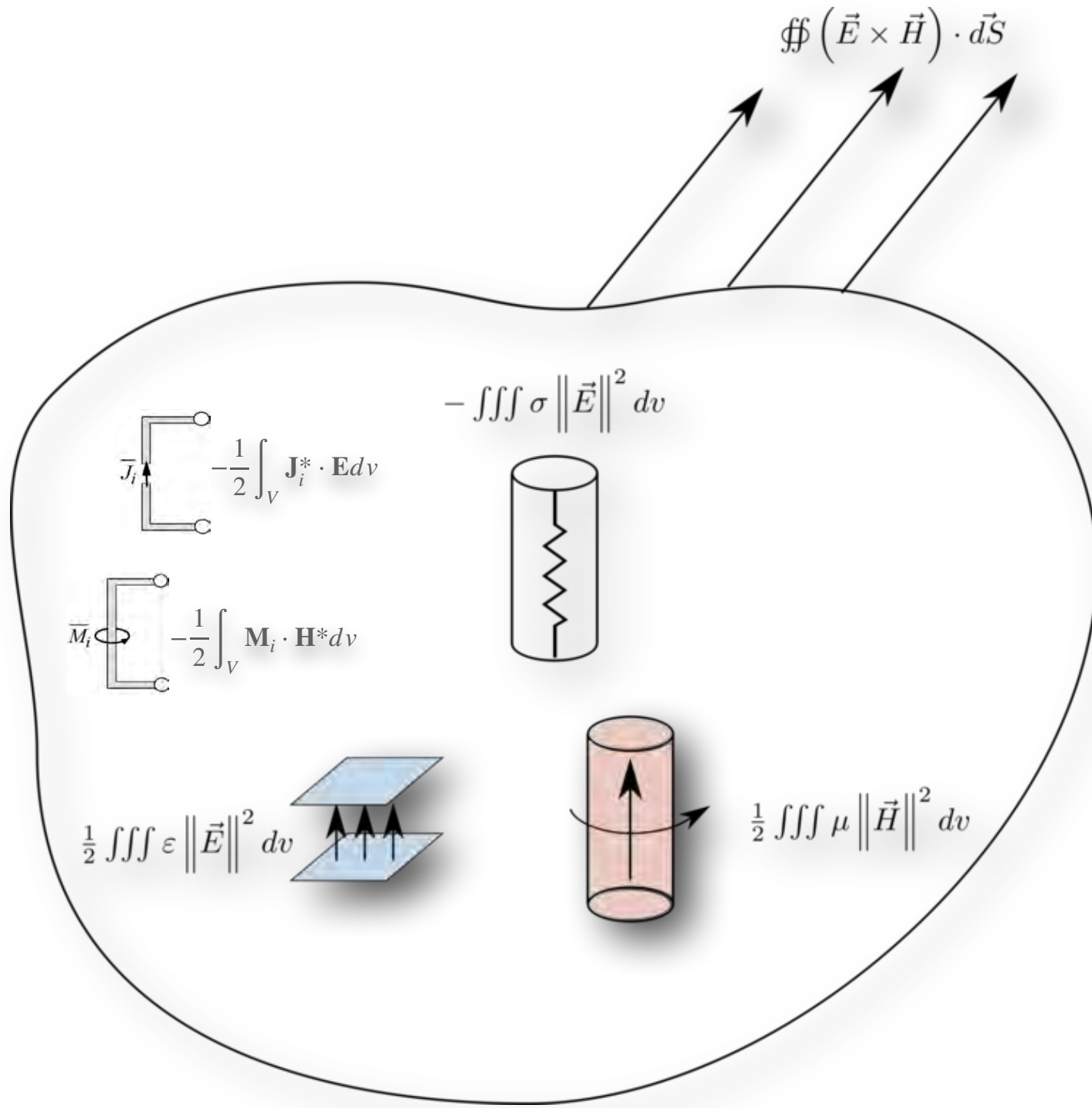
P_d Cavity power distribution

$$P_d = \frac{1}{4} \int (\mathbf{E}_1 \cdot \mathbf{J}_{e1}^* + \mathbf{E}_1^* \cdot \mathbf{J}_{e1}) d\tau = \frac{\omega_1 \epsilon_0}{2Q_1} \int \mathbf{E}_1 \cdot \mathbf{E}_1^* dV = \frac{\omega_1 U_1}{Q_1}$$

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$$\mathbf{S} = \frac{1}{2\mu_0} \mathbf{E}_1 \times \mathbf{B}_1^* \quad \text{and} \quad \mathbf{S}^* = \frac{1}{2\mu_0} \mathbf{E}_1^* \times \mathbf{B}_1$$

$$\nabla \cdot \mathbf{S} = \frac{1}{2\mu_0} \nabla \cdot (\mathbf{E}_1 \times \mathbf{B}_1^*) = \frac{1}{2\mu_0} \mathbf{B}_1^* \cdot (\nabla \times \mathbf{E}_1) - \frac{1}{2\mu_0} \mathbf{E}_1 \cdot (\nabla \times \mathbf{B}_1^*)$$

$$\nabla \cdot \mathbf{S}^* = \frac{1}{2\mu_0} \nabla \cdot (\mathbf{E}_1^* \times \mathbf{B}_1) = \frac{1}{2\mu_0} \mathbf{B}_1 \cdot (\nabla \times \mathbf{E}_1^*) - \frac{1}{2\mu_0} \mathbf{E}_1^* \cdot (\nabla \times \mathbf{B}_1)$$

On resonance: Real part of Complex Poynting Theorem = 0 for closed system

$$\oint \operatorname{Re}(\mathbf{S}) \cdot \hat{n} ds = \frac{j\omega_a g_{a\gamma\gamma} \epsilon_0 c}{4} \int (\mathbf{E}_1 \cdot \tilde{a}^* \mathbf{B}_0^* - \mathbf{E}_1^* \cdot \tilde{a} \mathbf{B}_0) d\tau - \frac{1}{4} \int (\mathbf{E}_1 \cdot \mathbf{J}_{e1}^* + \mathbf{E}_1^* \cdot \mathbf{J}_{e1}) d\tau$$

P_s Axion power input

P_d Cavity power distribution

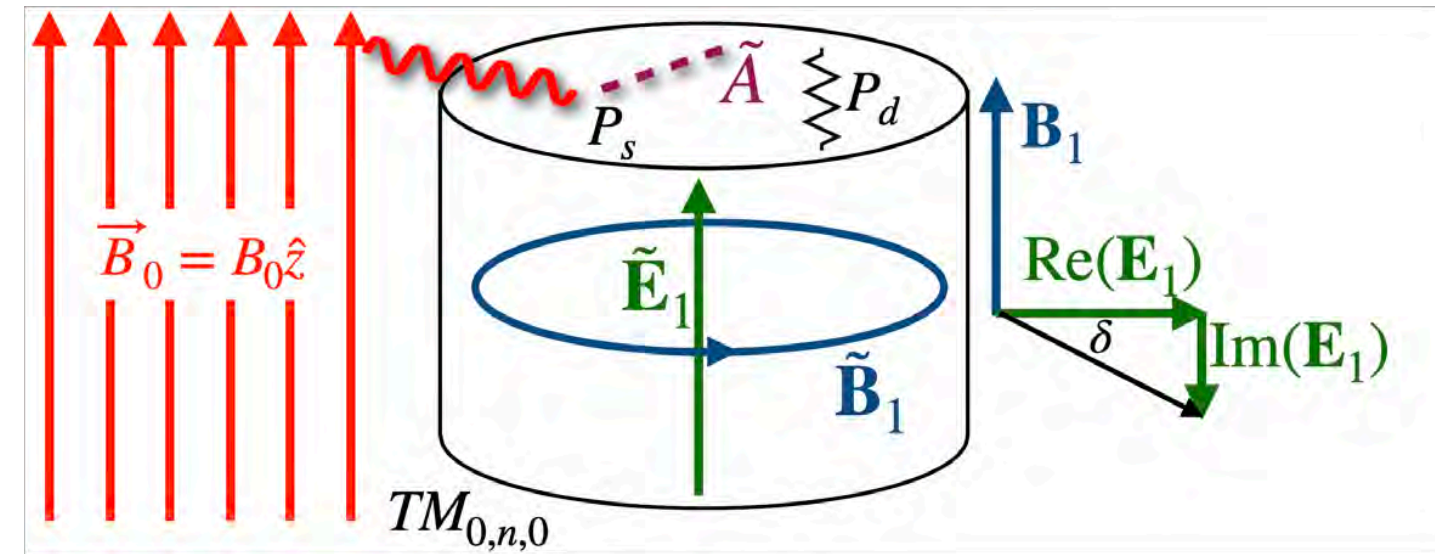
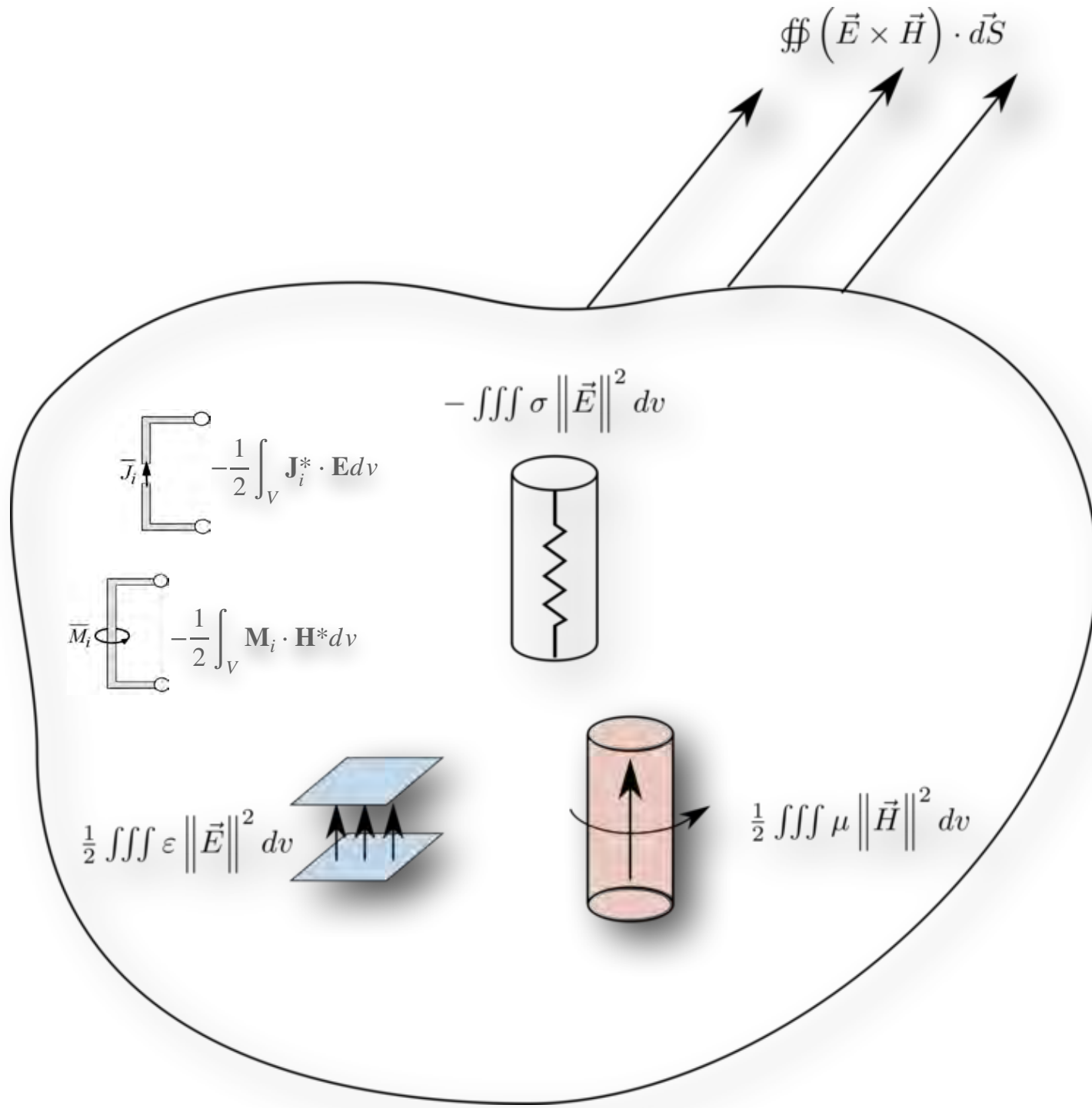
$$P_d = \frac{1}{4} \int (\mathbf{E}_1 \cdot \mathbf{J}_{e1}^* + \mathbf{E}_1^* \cdot \mathbf{J}_{e1}) d\tau = \frac{\omega_1 \epsilon_0}{2Q_1} \int \mathbf{E}_1 \cdot \mathbf{E}_1^* dV = \frac{\omega_1 U_1}{Q_1}$$

$$P_{a1} = \frac{\omega_a g_{a\gamma\gamma} a_0 \epsilon_0 c}{2Q_1} \int (\operatorname{Re}(\mathbf{E}_1) \cdot \operatorname{Re}(\mathbf{B}_0)) d\tau = P_d = \frac{\omega_1 U_1}{Q_1}$$

Sensitivity of a Resonant Haloscope

$$P_{av} = \frac{1}{2} \operatorname{Re} \oint_{S_c} (\mathbf{E} \times \mathbf{H}^*) \cdot d\mathbf{s}$$

Average radiated power outside volume



Poynting vector controversy in axion modified electrodynamics

Michael E. Tobar[✉], Ben T. McAllister, and Maxim Goryachev

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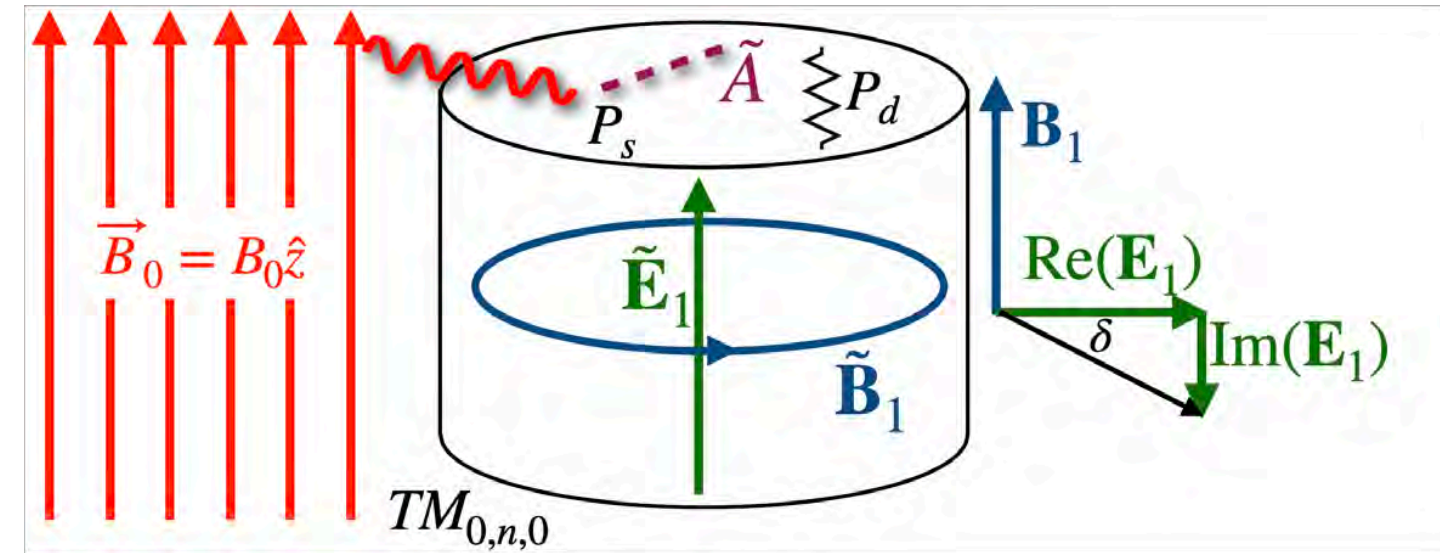
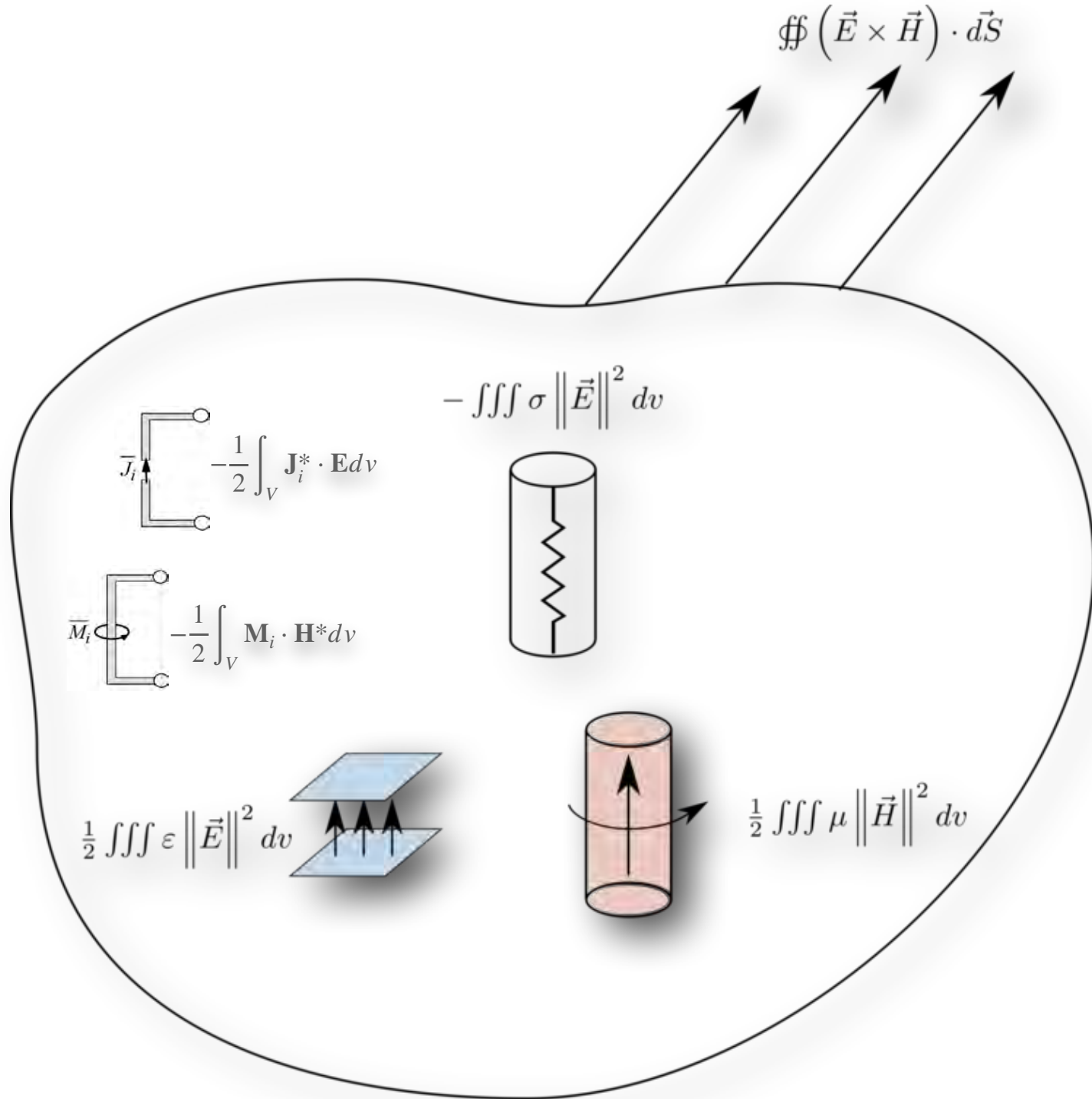
$$P_{a1} = \omega_a Q U_1 = g_{a\gamma\gamma}^2 \langle a_0 \rangle^2 \omega_a Q_1 \epsilon_0 c^2 B_0^2 V_1 C_1,$$

$$C_1 = \frac{\left(\int \vec{B}_0 \cdot \operatorname{Re}(\mathbf{E}_1) d\tau \right)^2}{B_0^2 V_1 \int \mathbf{E}_1 \cdot \mathbf{E}_1^* d\tau},$$

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Average radiated power outside volume



Poynting vector controversy in axion modified electrodynamics

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$$P_d = \frac{1}{4} \int (\mathbf{E}_1 \cdot \mathbf{J}_{e1}^* + \mathbf{E}_1^* \cdot \mathbf{J}_{e1}) d\tau = \frac{\omega_1 \epsilon_0}{2Q_1} \int \mathbf{E}_1 \cdot \mathbf{E}_1^* dV = \frac{\omega_1 U_1}{Q_1}$$

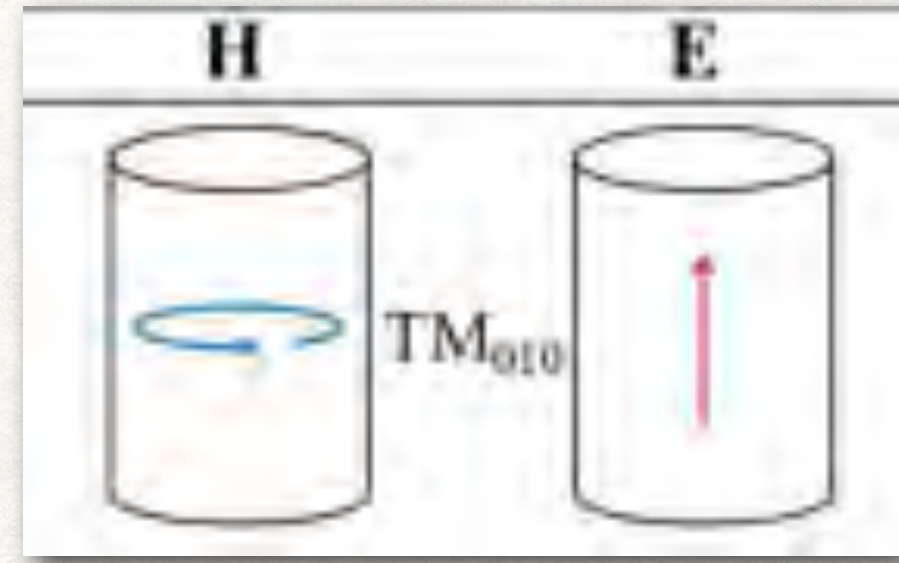
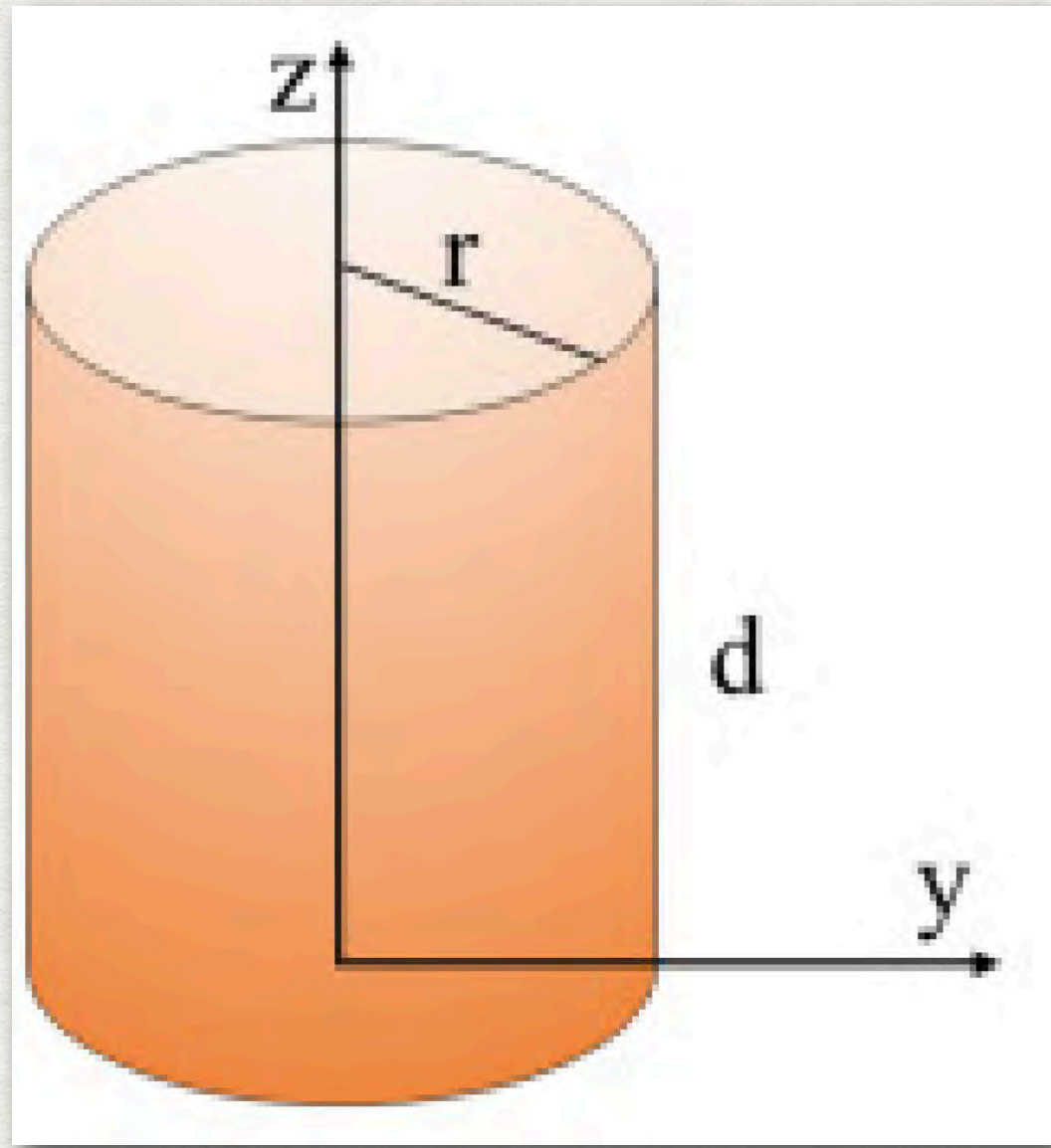
$$P_{a1} = \frac{\omega_a g_{a\gamma\gamma} a_0 \epsilon_0 c}{2Q_1} \int (\operatorname{Re}(\mathbf{E}_1) \cdot \operatorname{Re}(\mathbf{B}_0)) d\tau = P_d = \frac{\omega_1 U_1}{Q_1}$$

$$P_{a1} = \omega_a Q U_1 = g_{a\gamma\gamma}^2 \langle a_0 \rangle^2 \omega_a Q_1 \epsilon_0 c^2 B_0^2 V_1 C_1,$$

$$C_1 = \frac{\left(\int \vec{B}_0 \cdot \operatorname{Re}(\mathbf{E}_1) d\tau \right)^2}{B_0^2 V_1 \int \mathbf{E}_1 \cdot \mathbf{E}_1^* d\tau},$$

Resonant Haloscope, on resonance,
 Reactive Power = 0

IMAGINARY POYNTING VECTOR INSIDE CAVITY

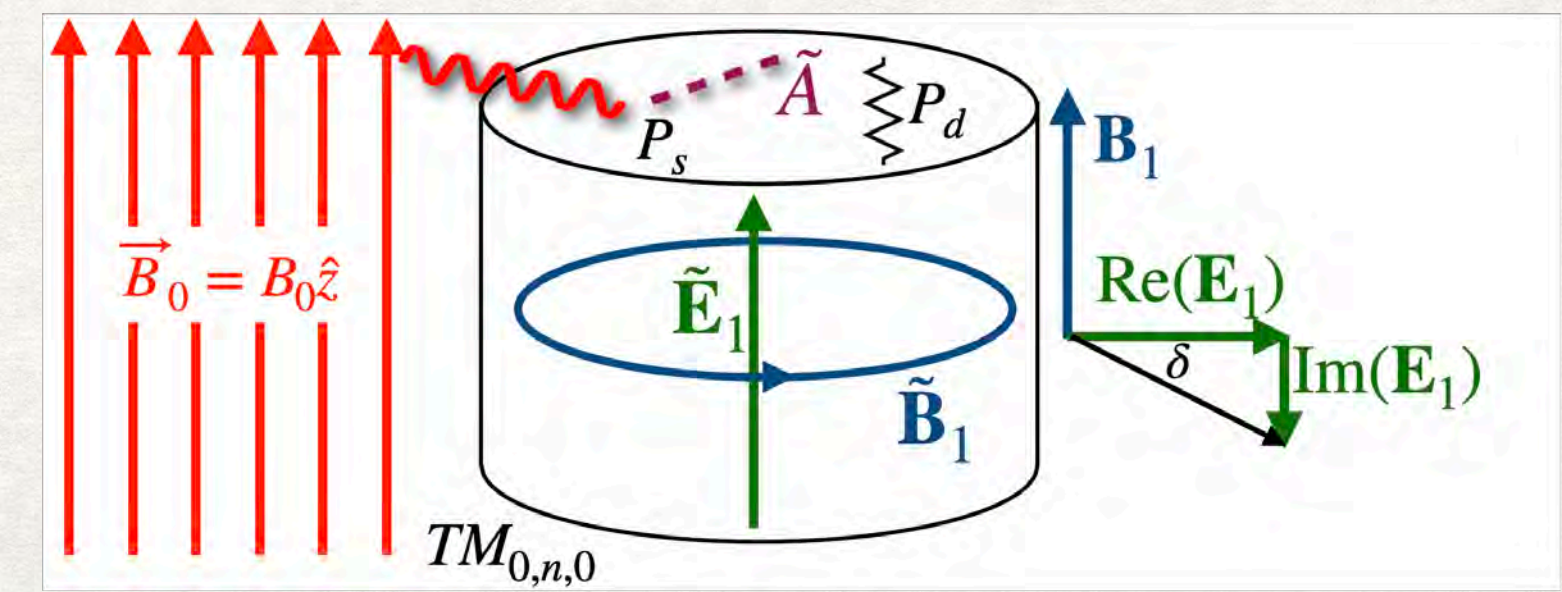
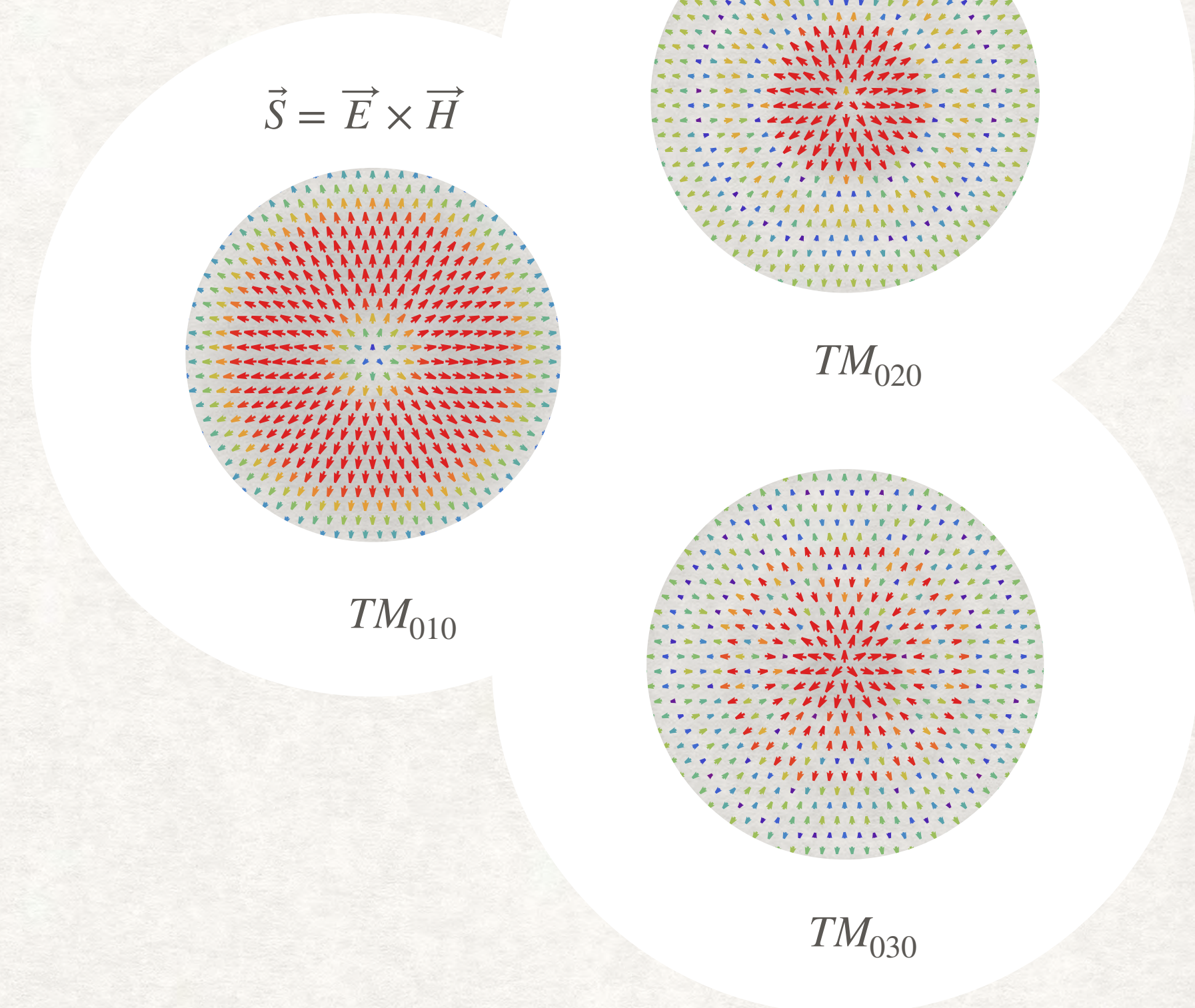
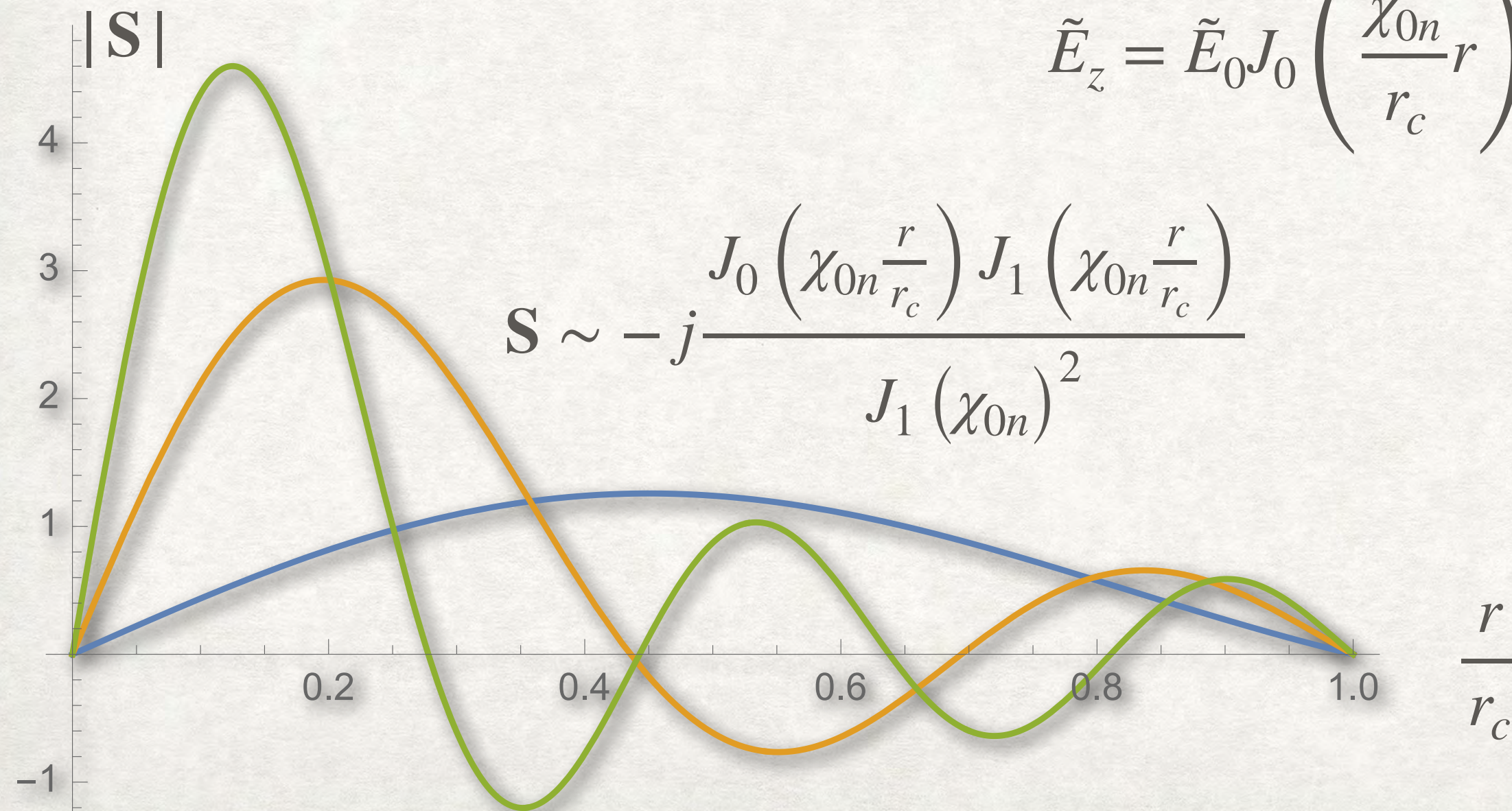


TM_{0n0}

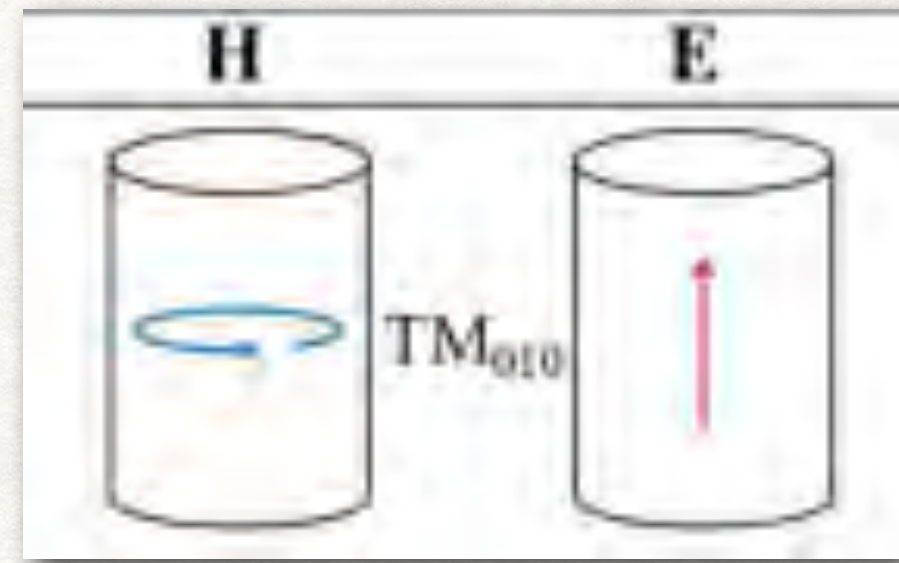
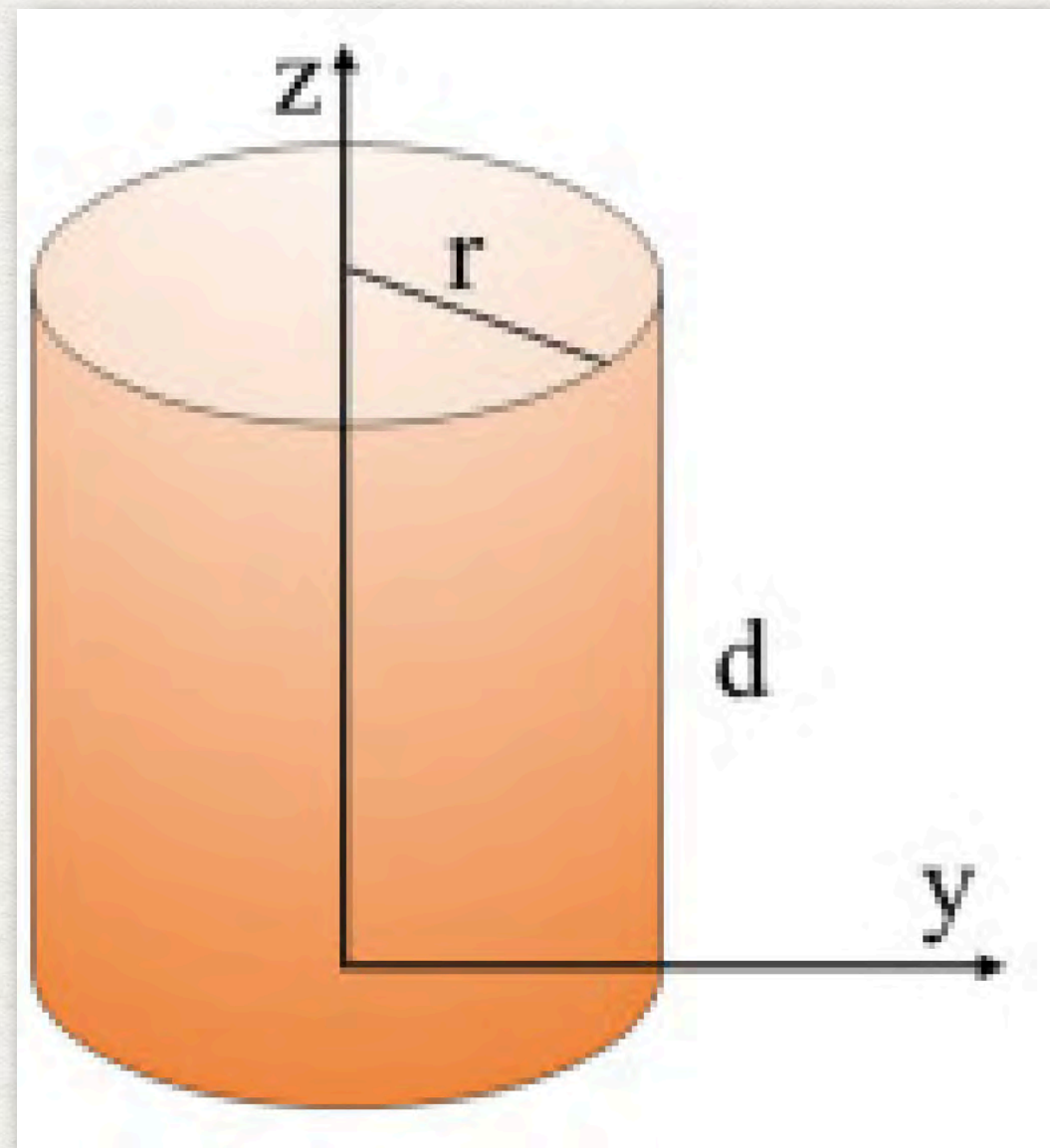
$$\tilde{H}_\phi = -j\tilde{E}_0(\omega\epsilon)\frac{r_c}{\chi_{0n}}J'_0\left(\frac{\chi_{0n}r}{r_c}\right)$$

$$\tilde{E}_z = \tilde{E}_0J_0\left(\frac{\chi_{0n}r}{r_c}\right)$$

$$\mathbf{S} \sim -j\frac{J_0\left(\chi_{0n}\frac{r}{r_c}\right)J_1\left(\chi_{0n}\frac{r}{r_c}\right)}{J_1(\chi_{0n})^2}$$



IMAGINARY POYNTING VECTOR INSIDE CAVITY



TM_{0n0}

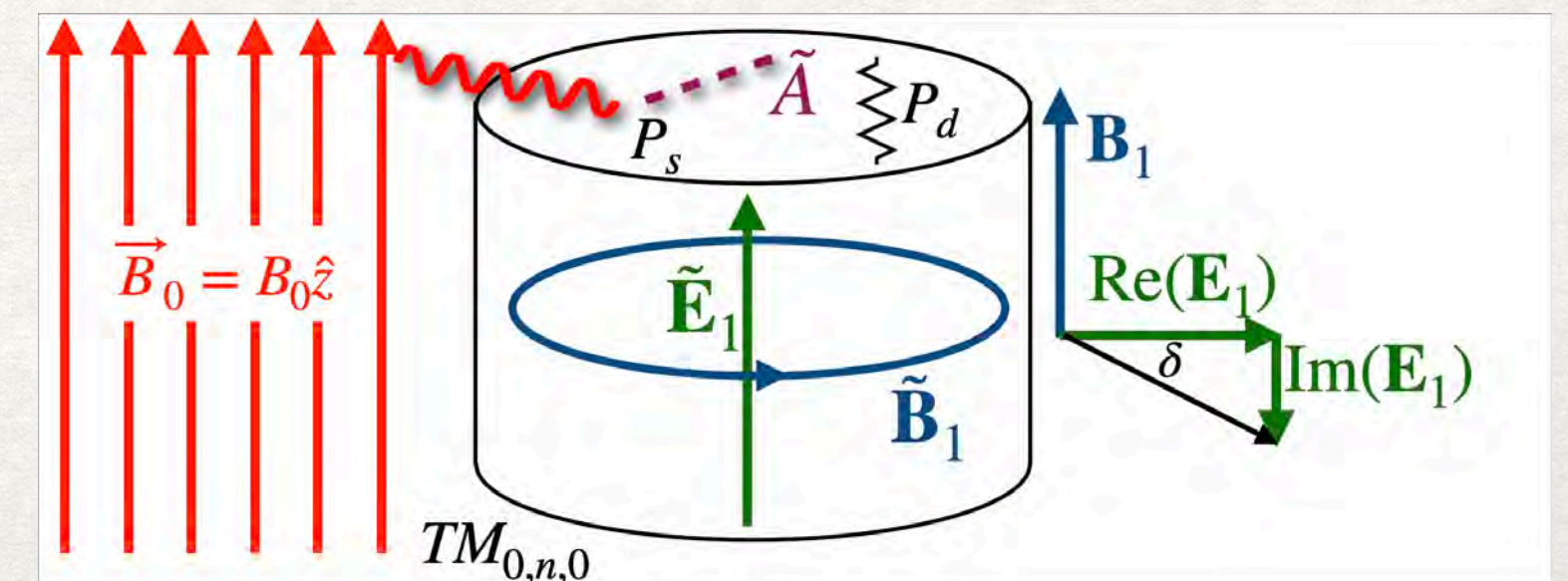
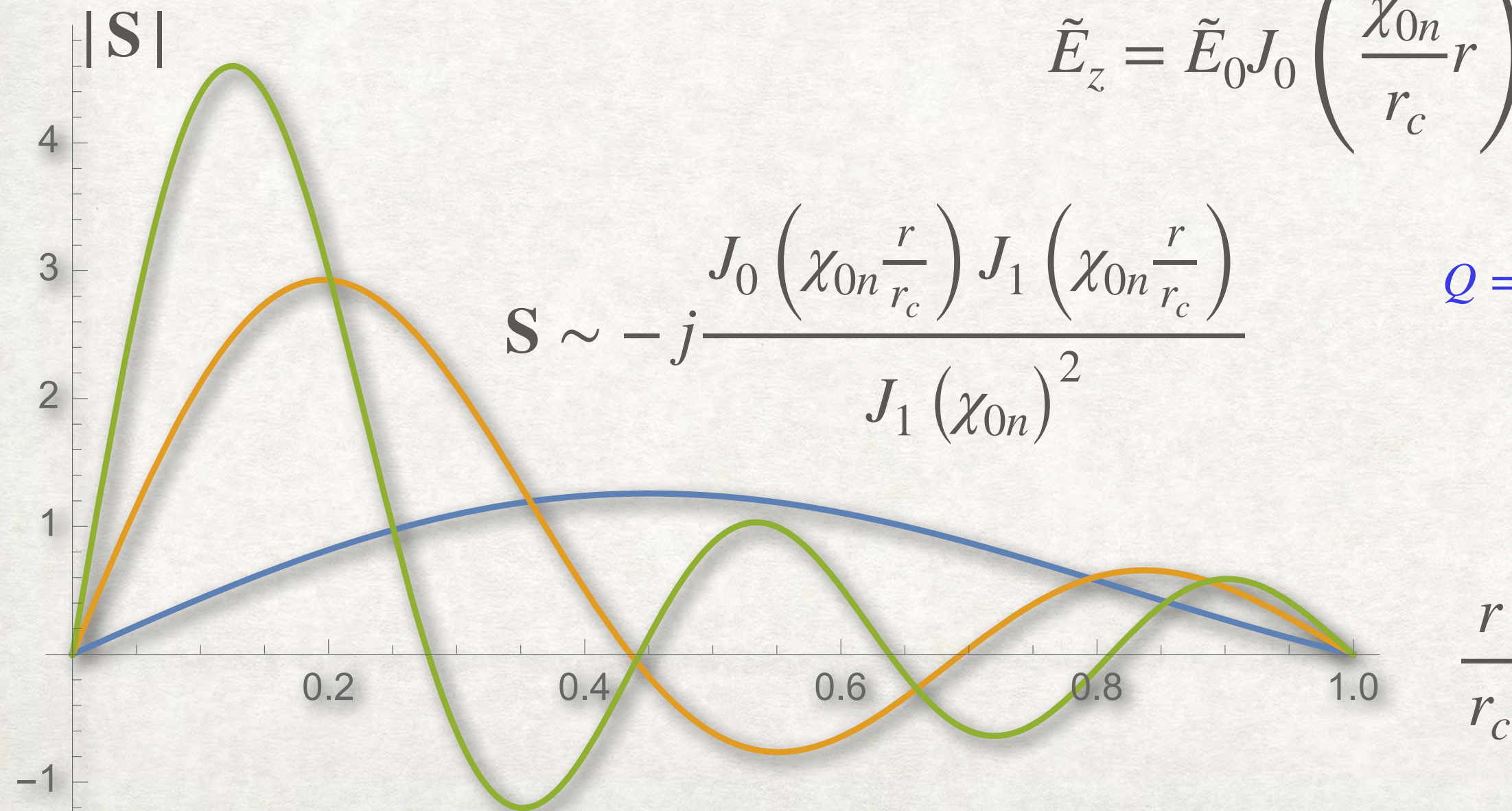
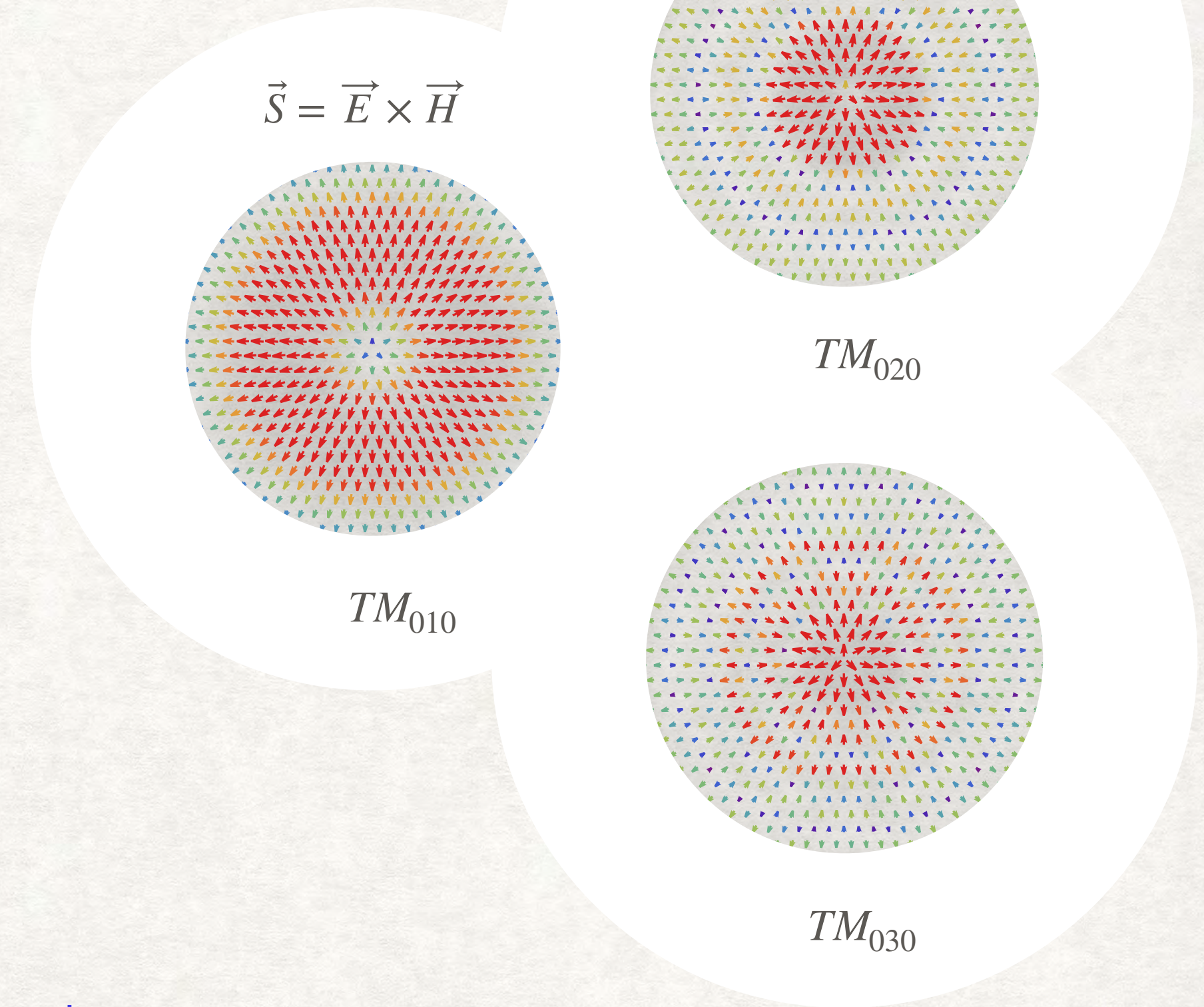
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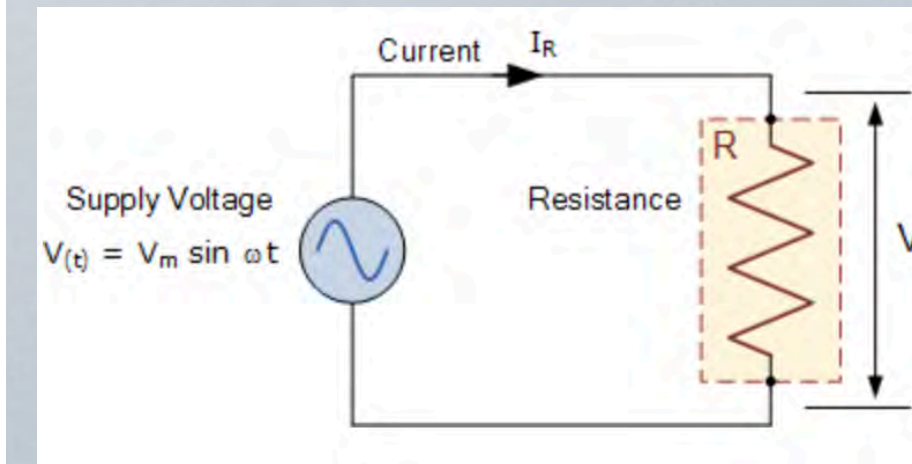
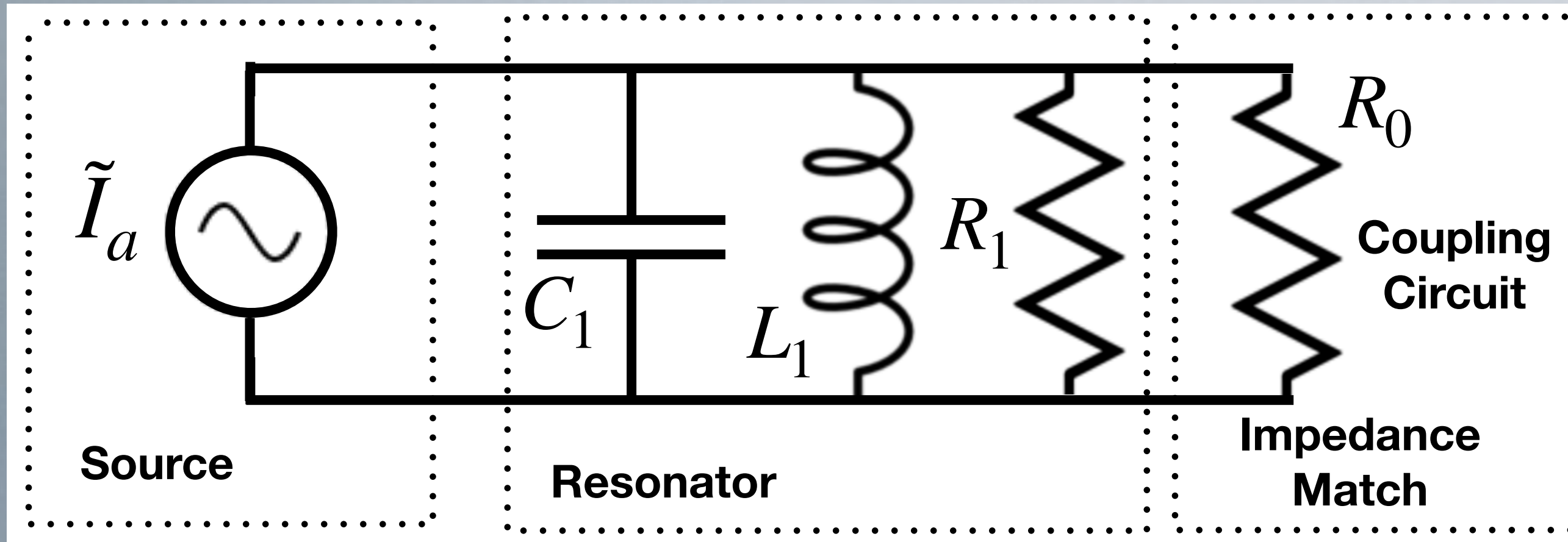
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$$Q = \omega_1 \frac{U_{tot}}{P_d} = 2\pi \frac{\text{stored energy}}{\text{energy dissipated during one period}}$$

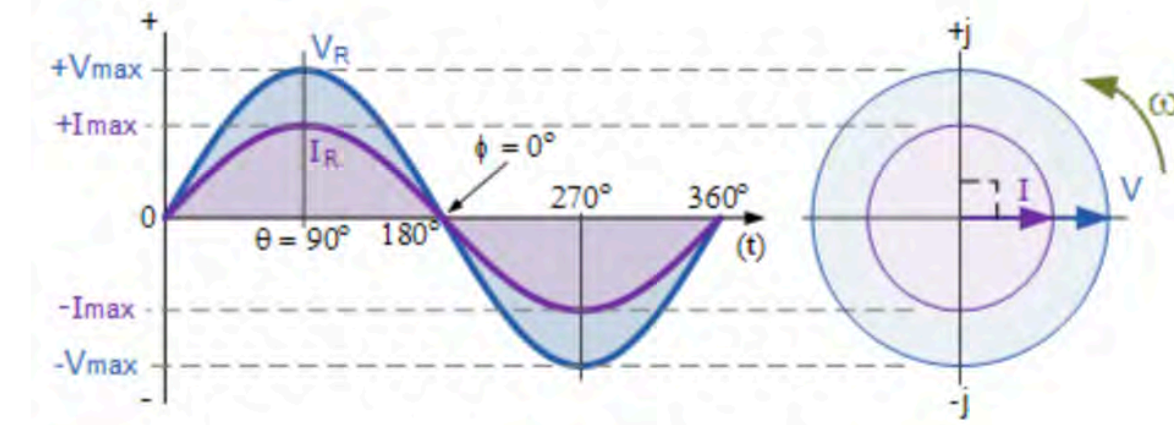
$$P_d = \frac{\omega_1 U_{tot}}{Q}$$



Resonator Measurement: Impedance match; set coupling =1; Take Photons from Source

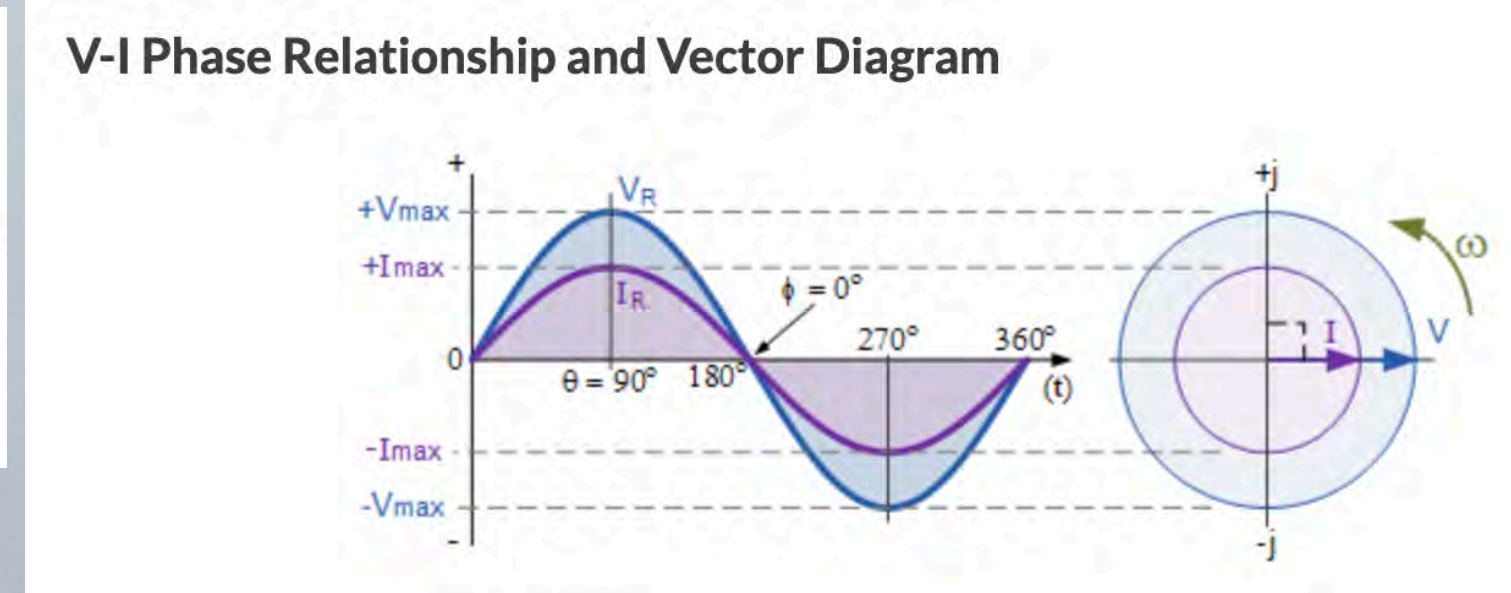
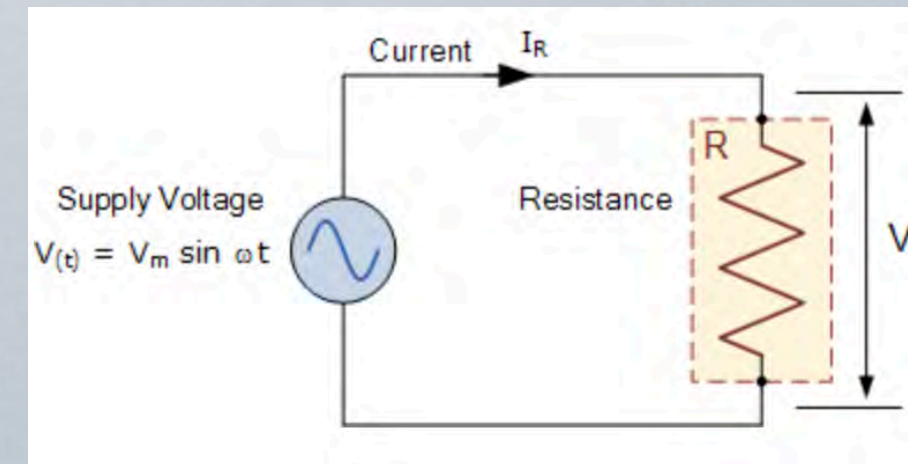
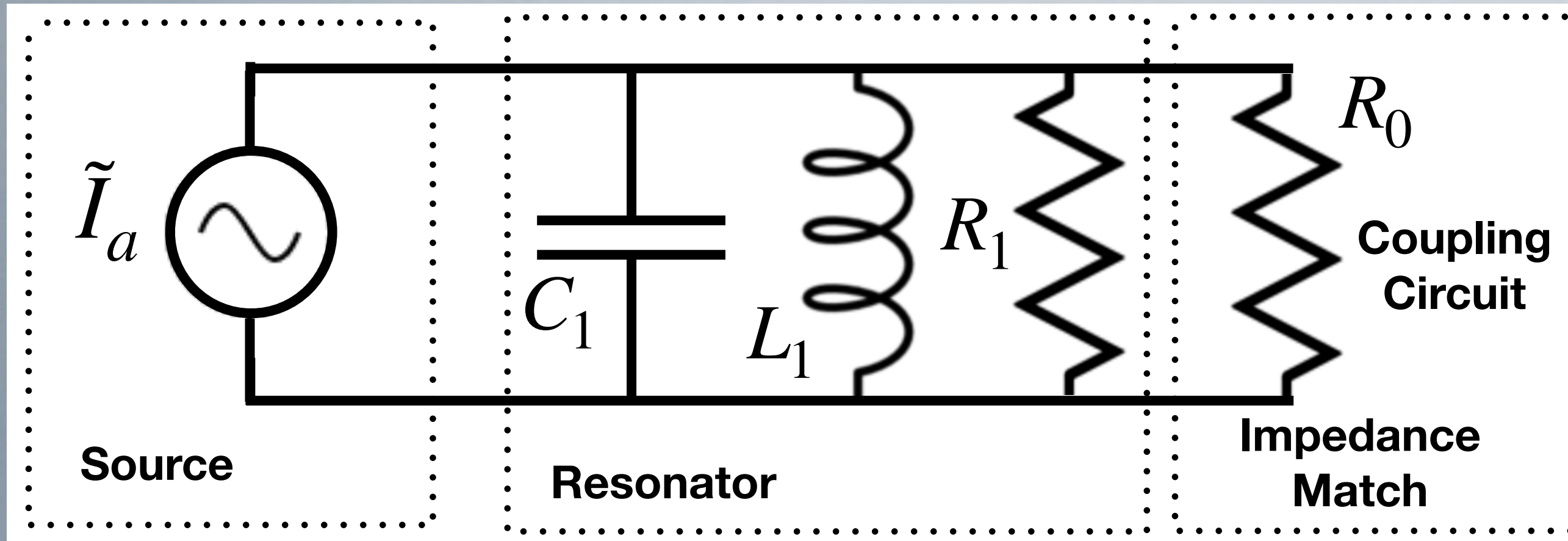


V-I Phase Relationship and Vector Diagram

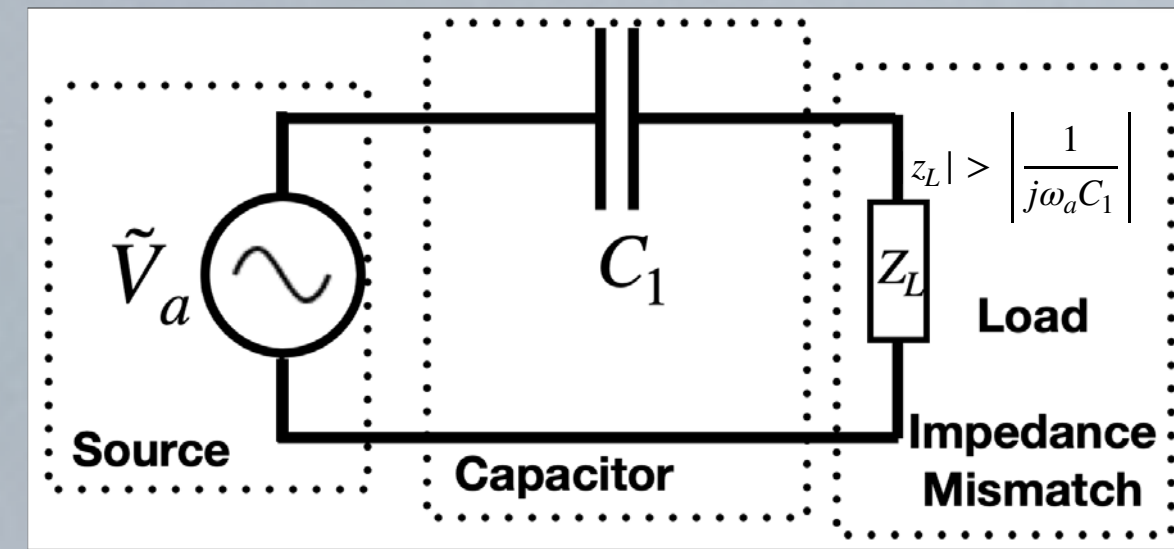
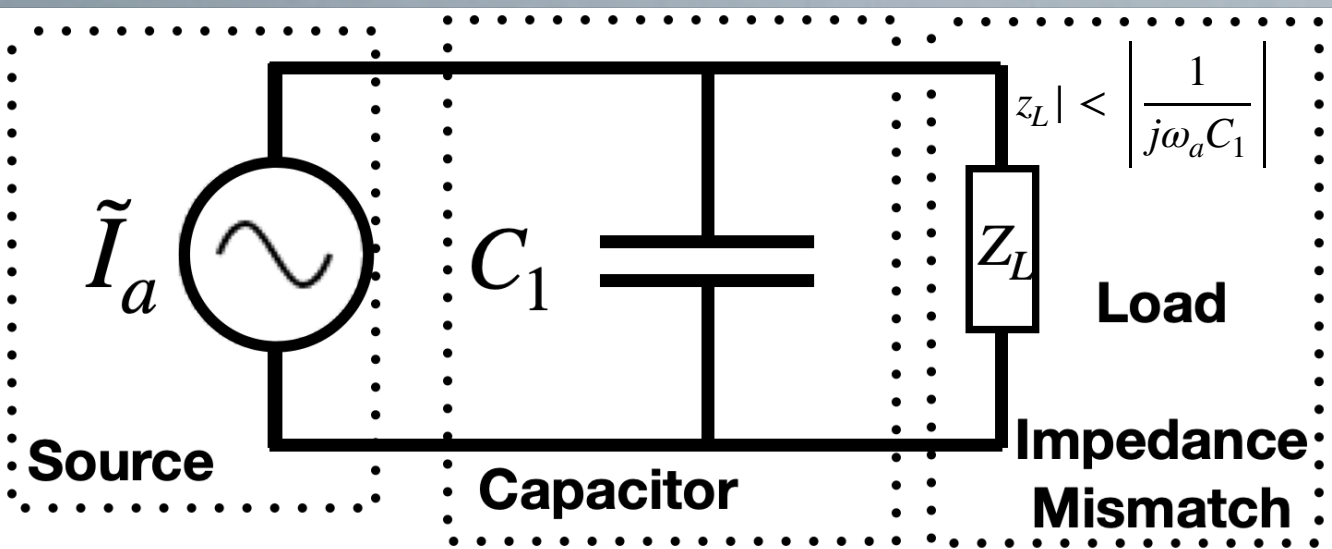


Real Power Measurement, Absorbs Energy: $P_a = I_0^2 R_o = \frac{V_0^2}{R_0}$

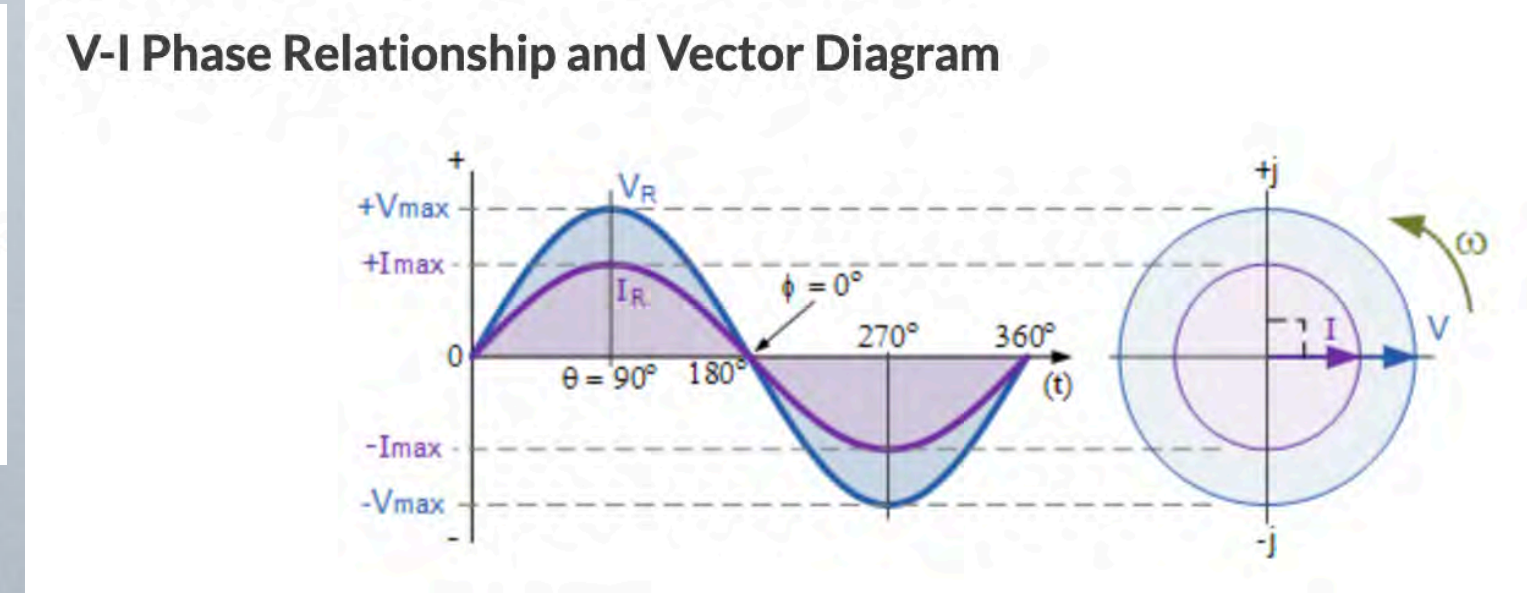
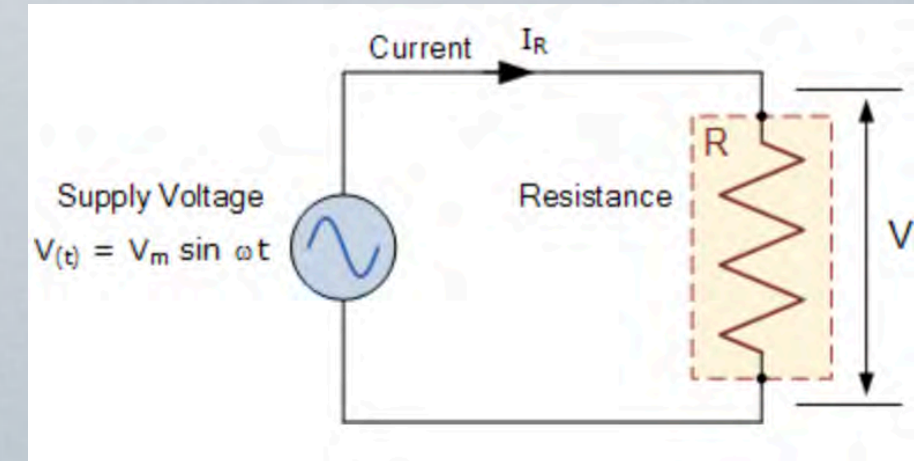
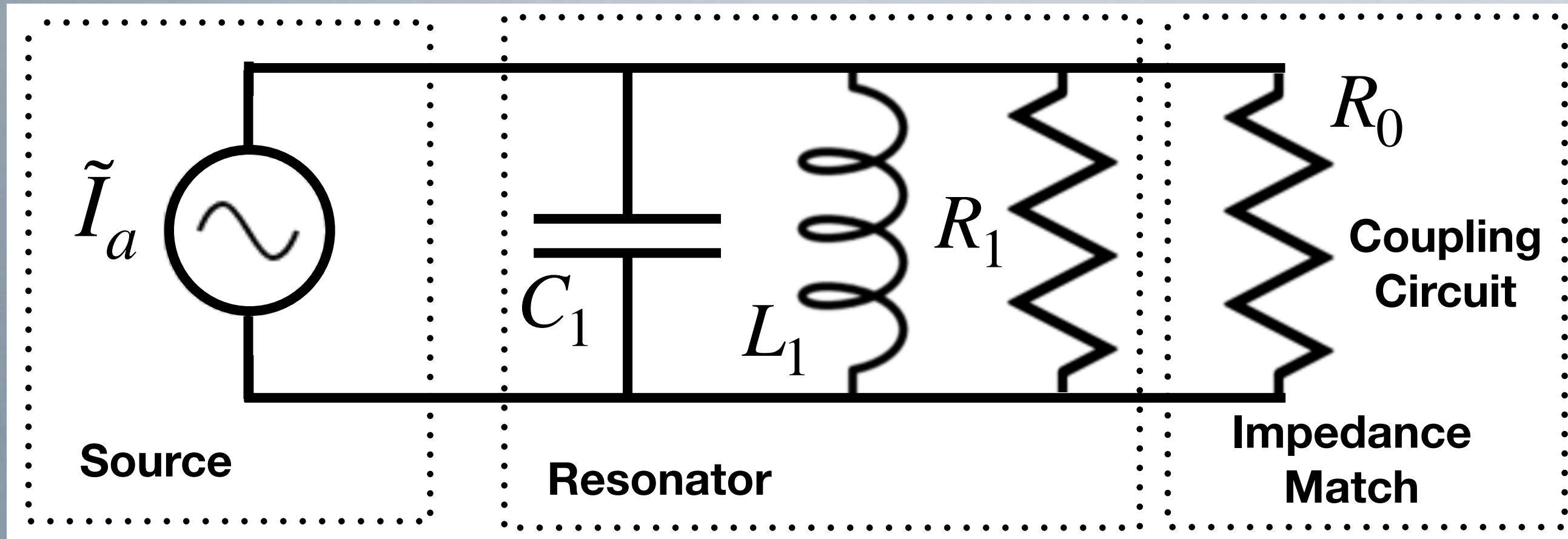
Resonator Measurement: Impedance match; set coupling =1; Take Photons from Source



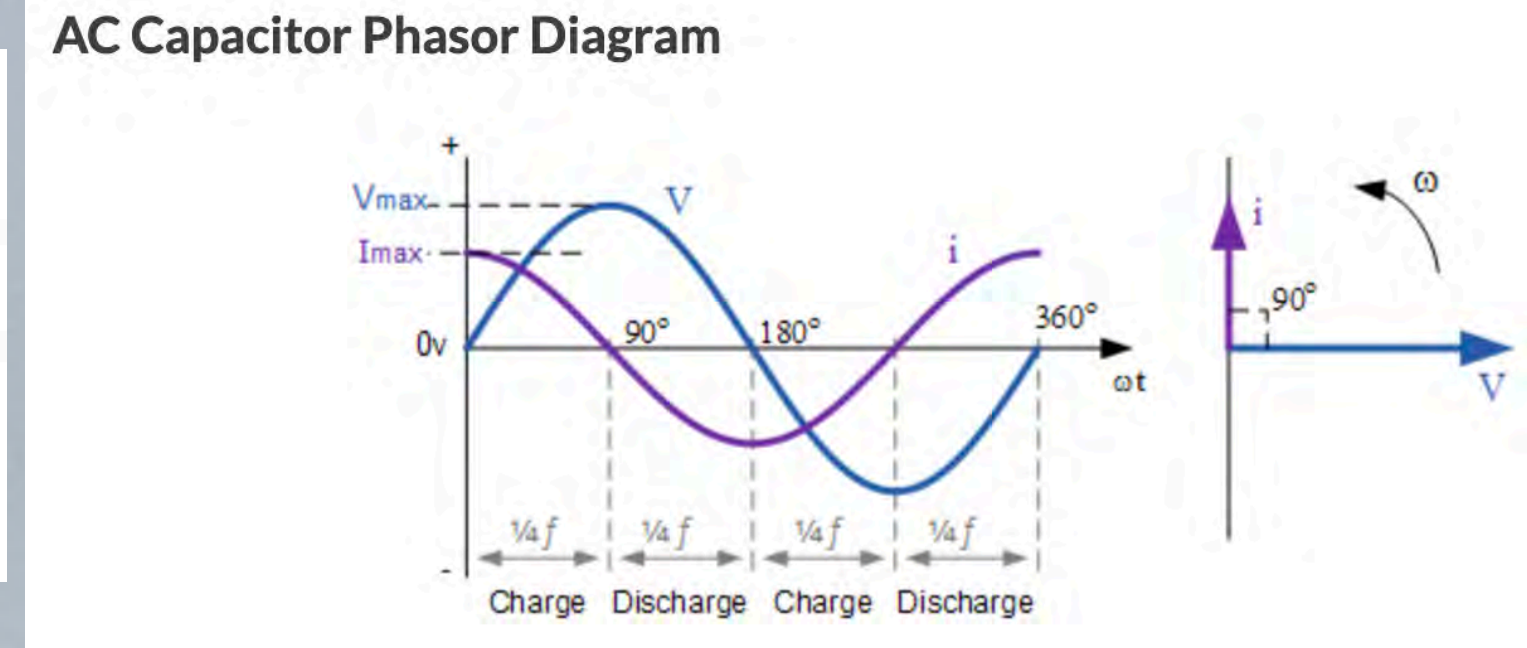
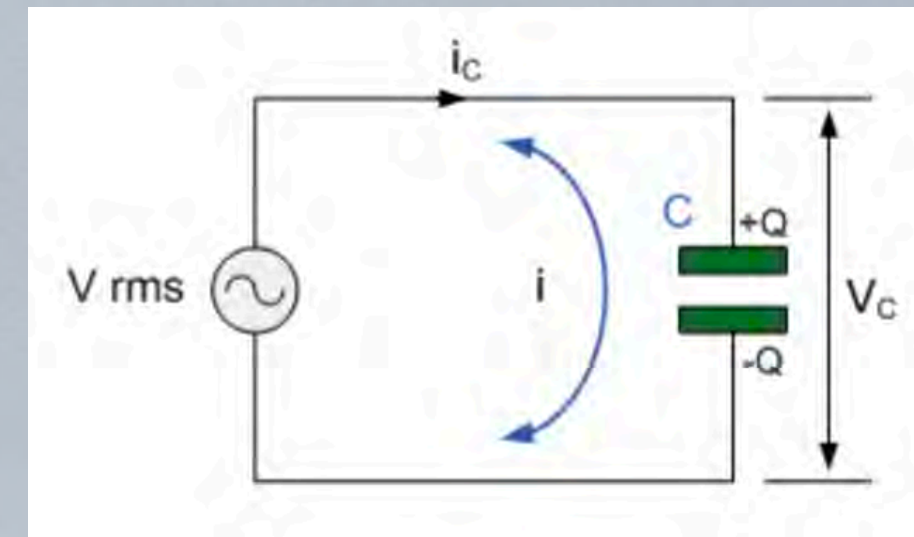
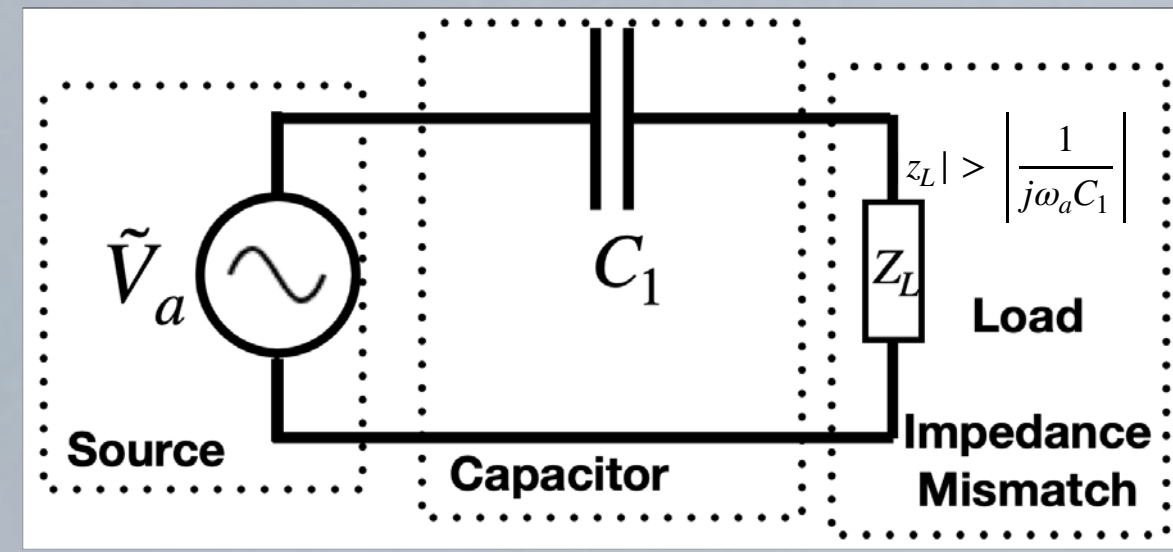
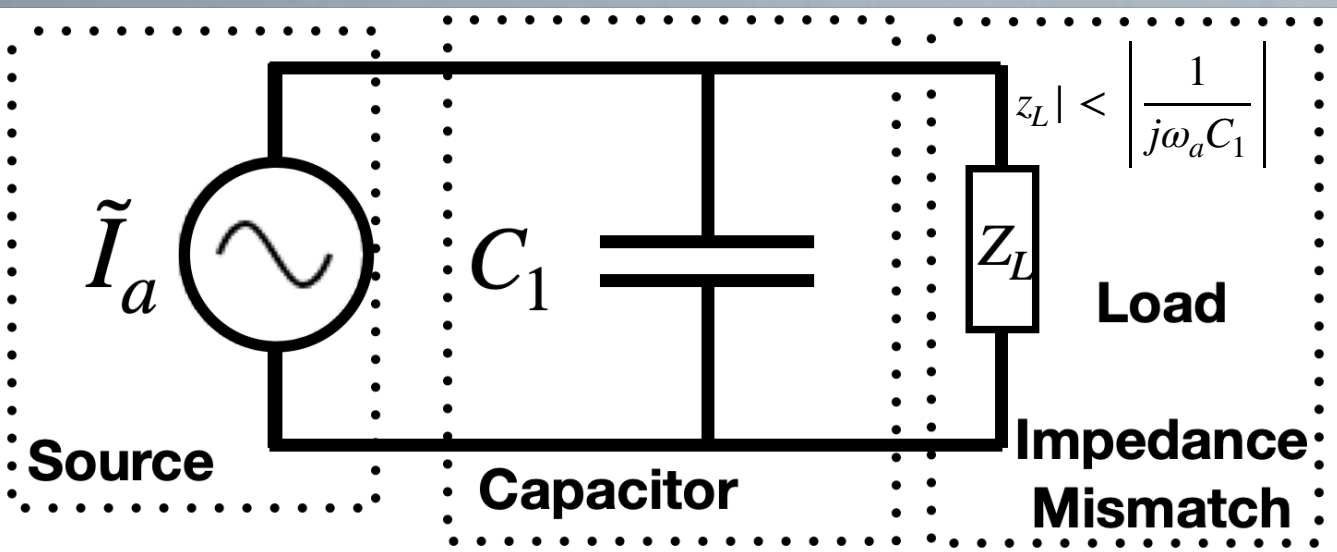
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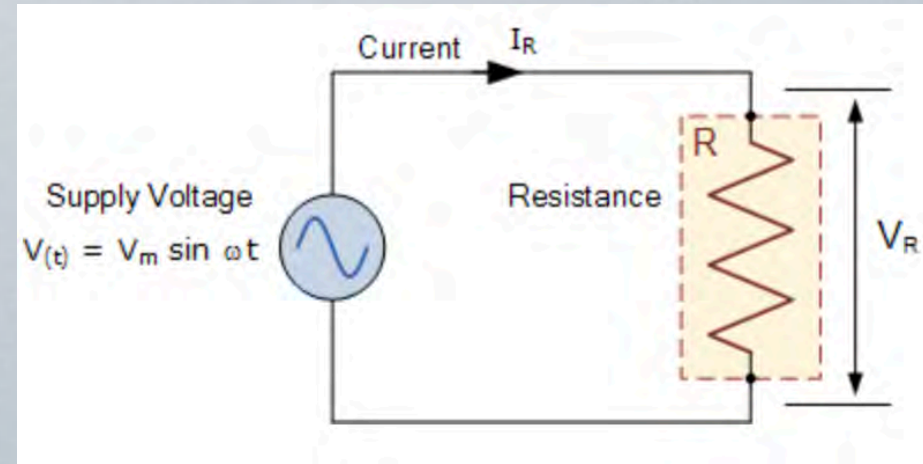
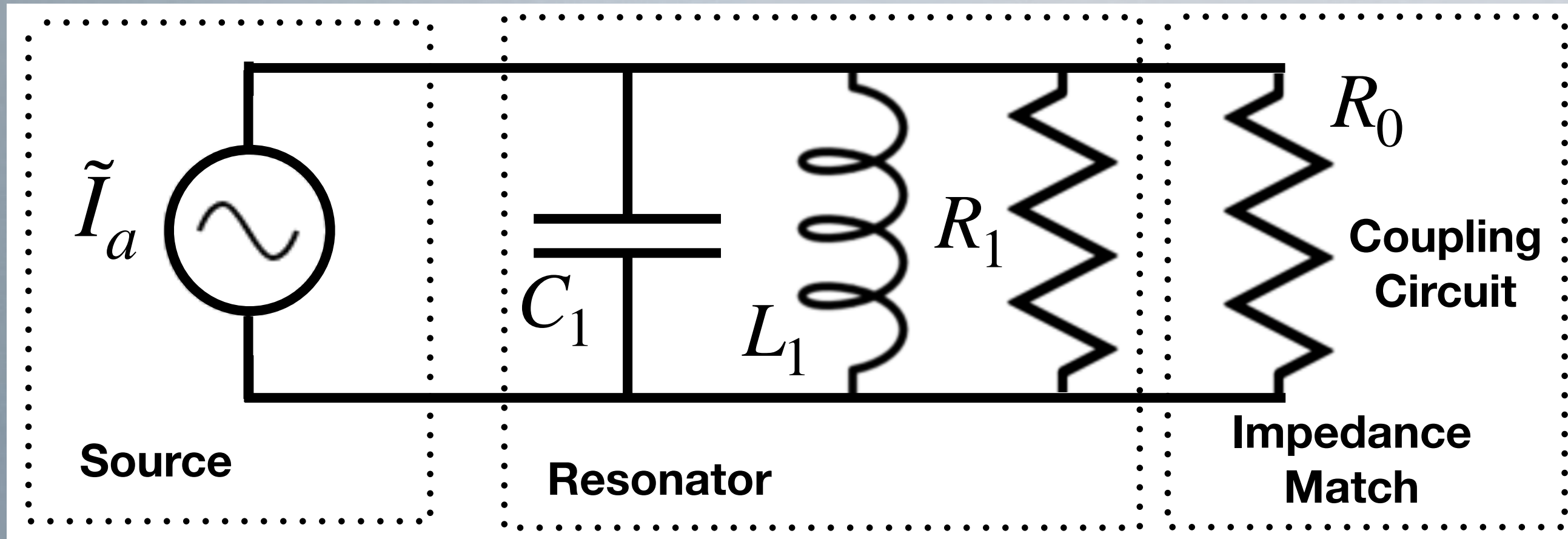
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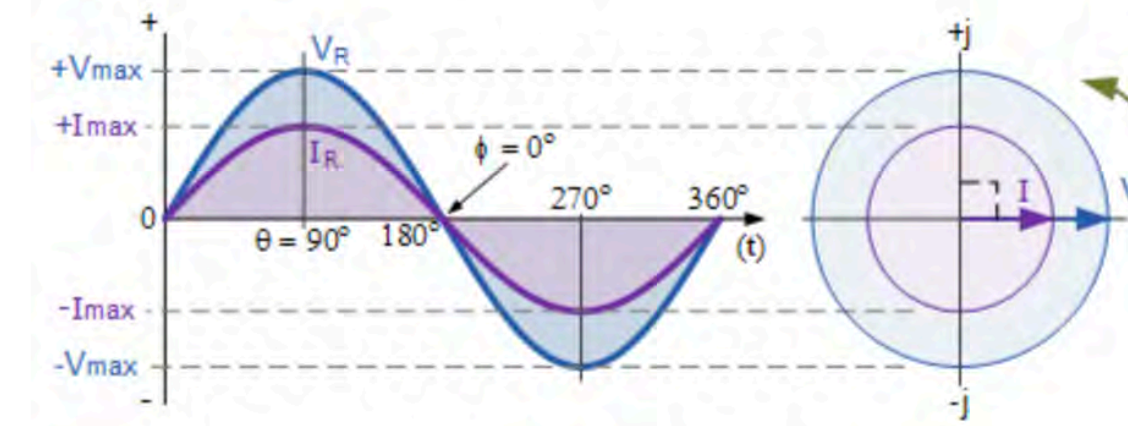
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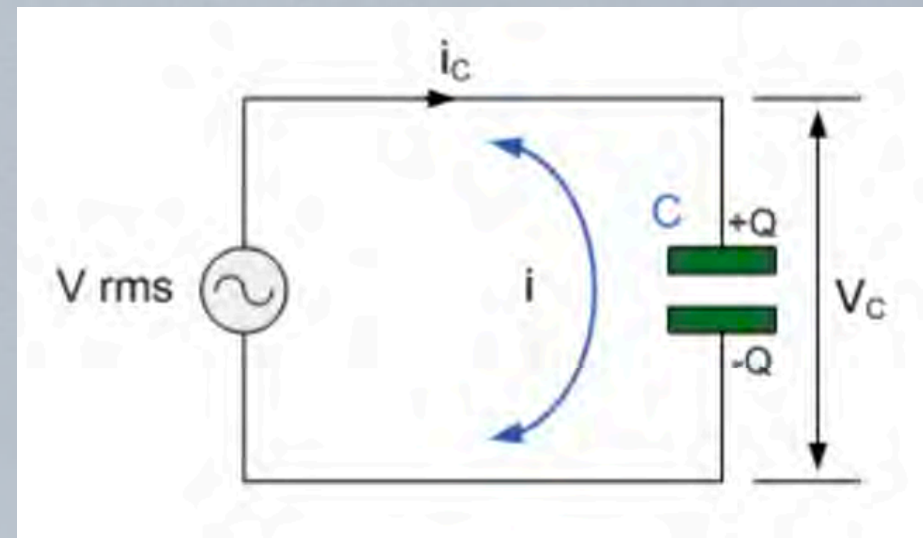
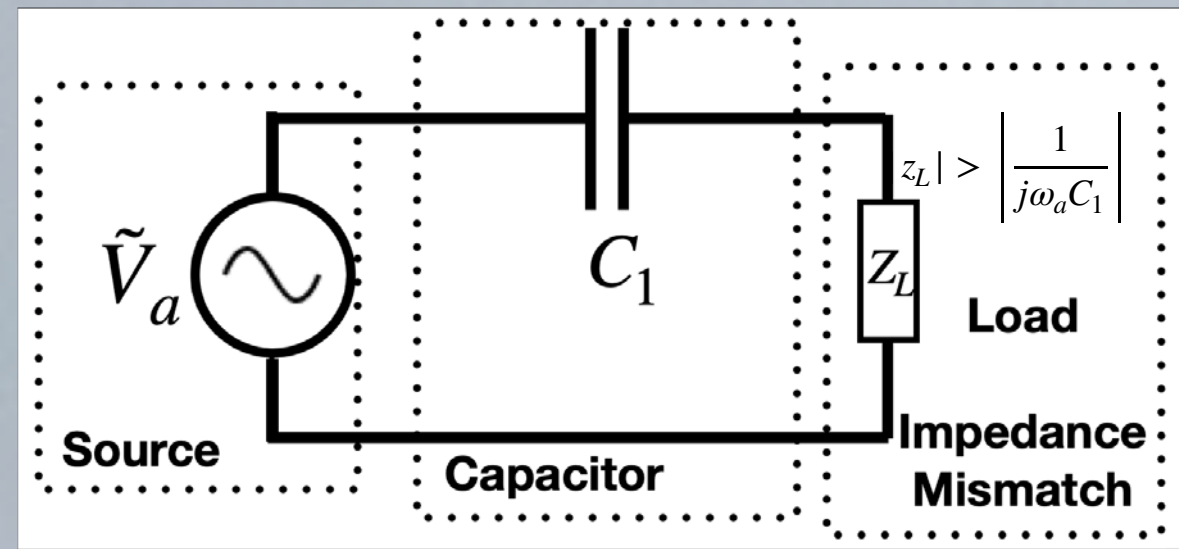
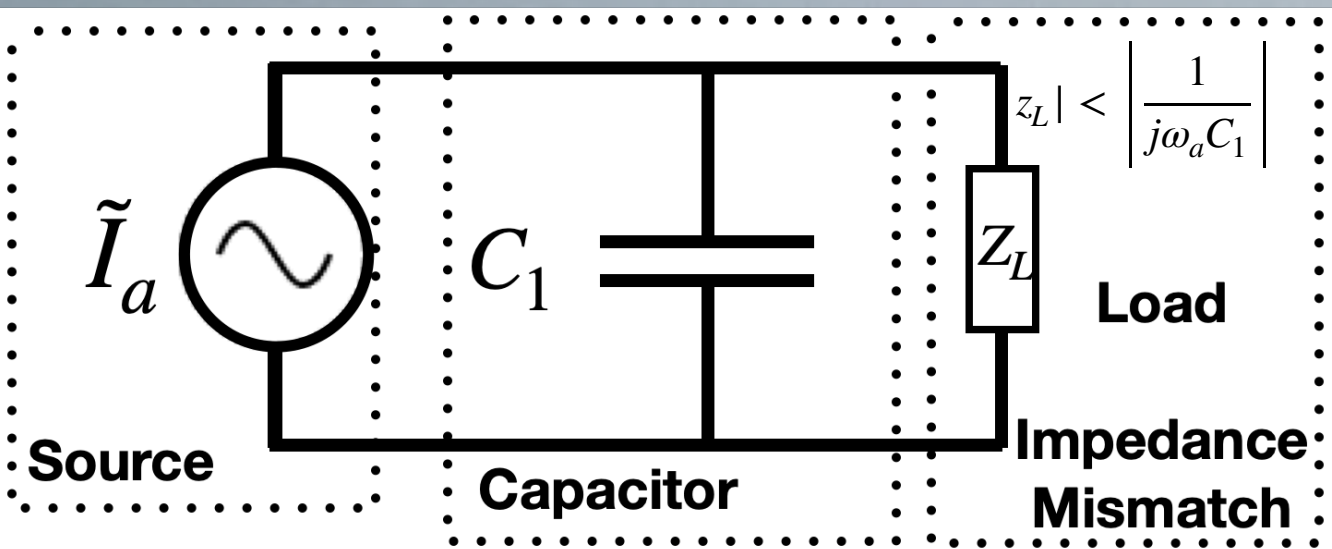
Resonator Measurement: Impedance match; set coupling = 1; Take Photons from Source



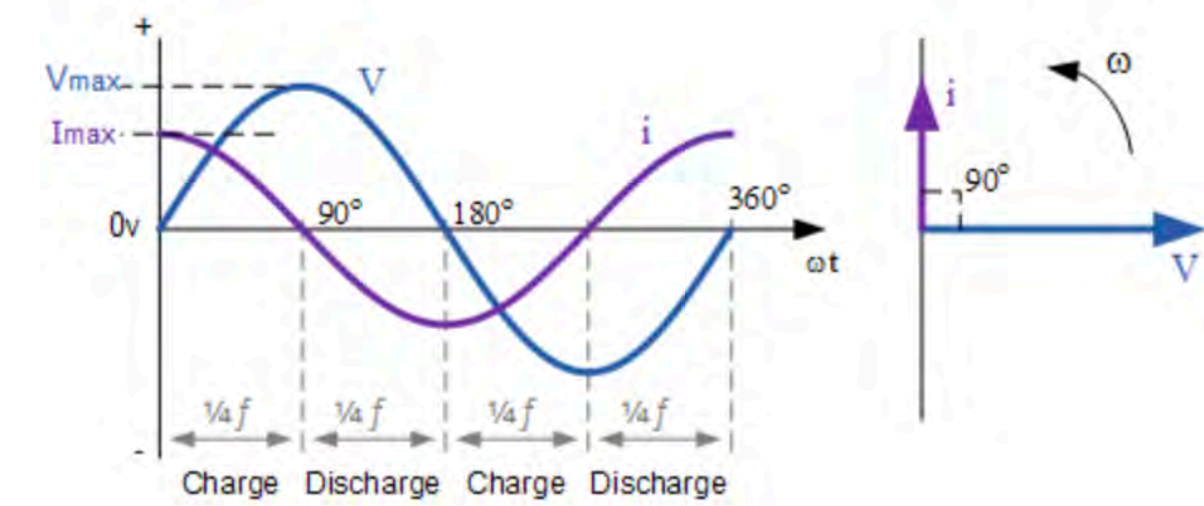
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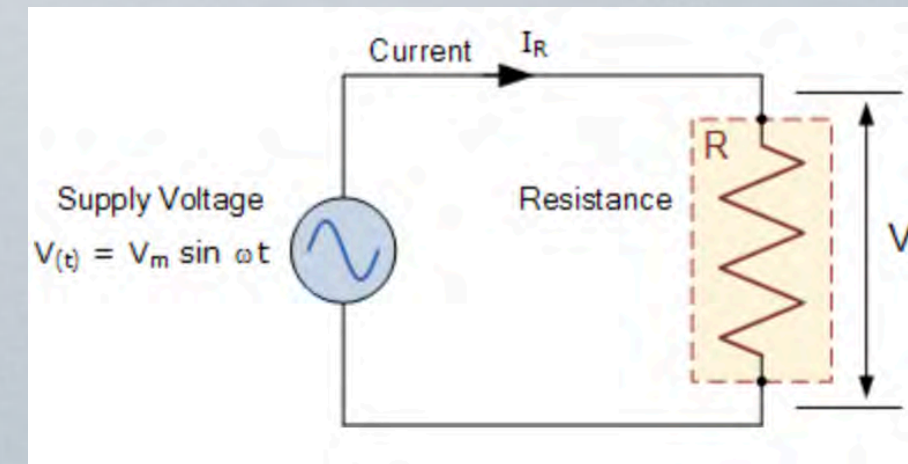
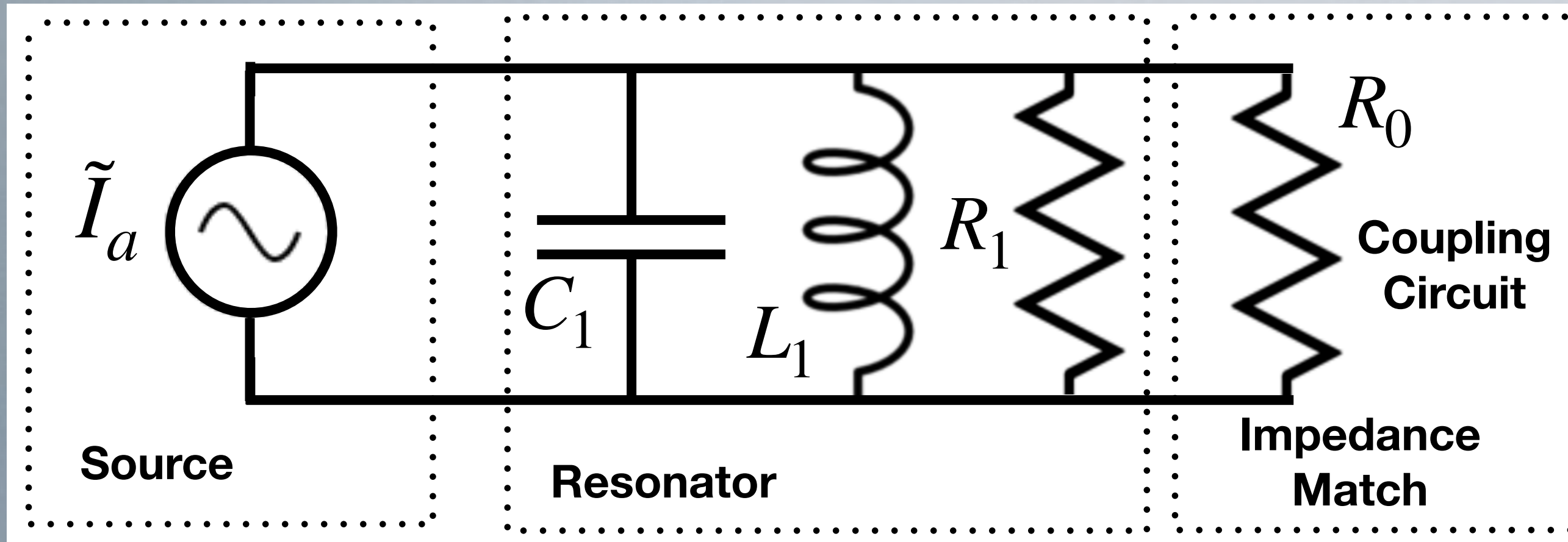


AC Capacitor Phasor Diagram

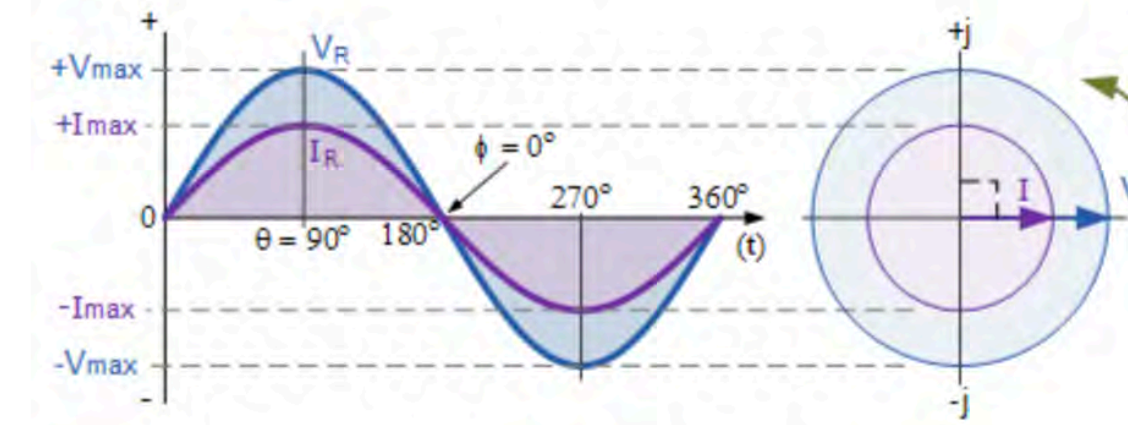


Reactive Power Measurement, Does Not Absorb Energy:

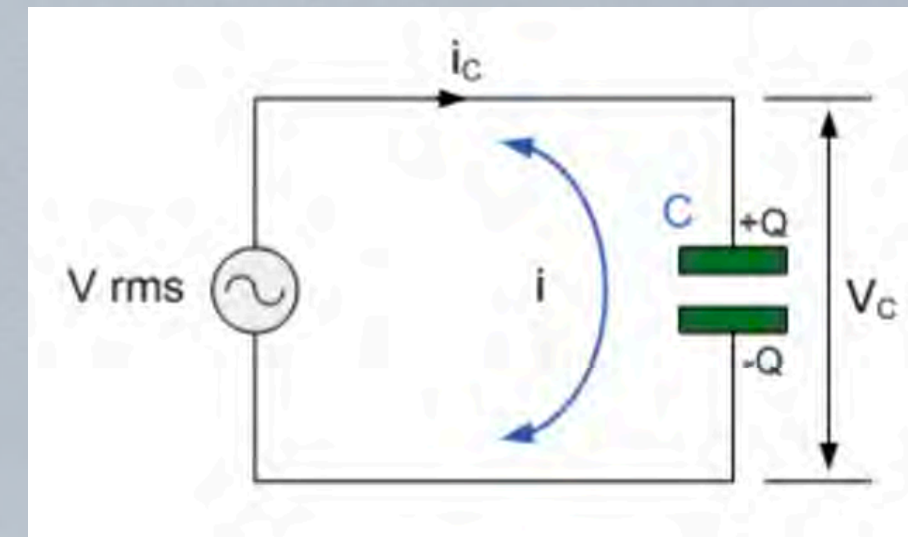
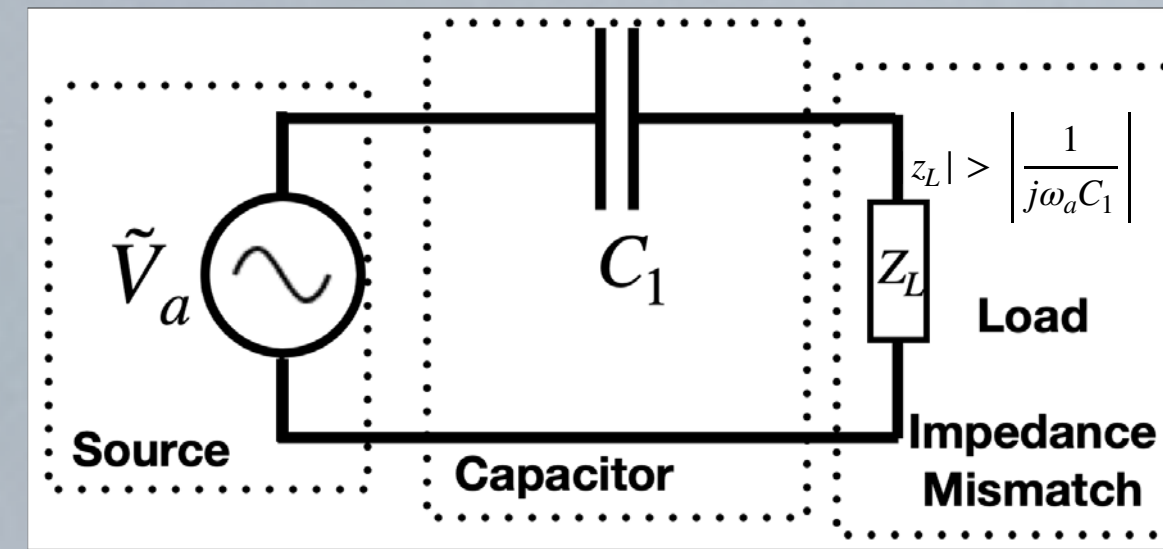
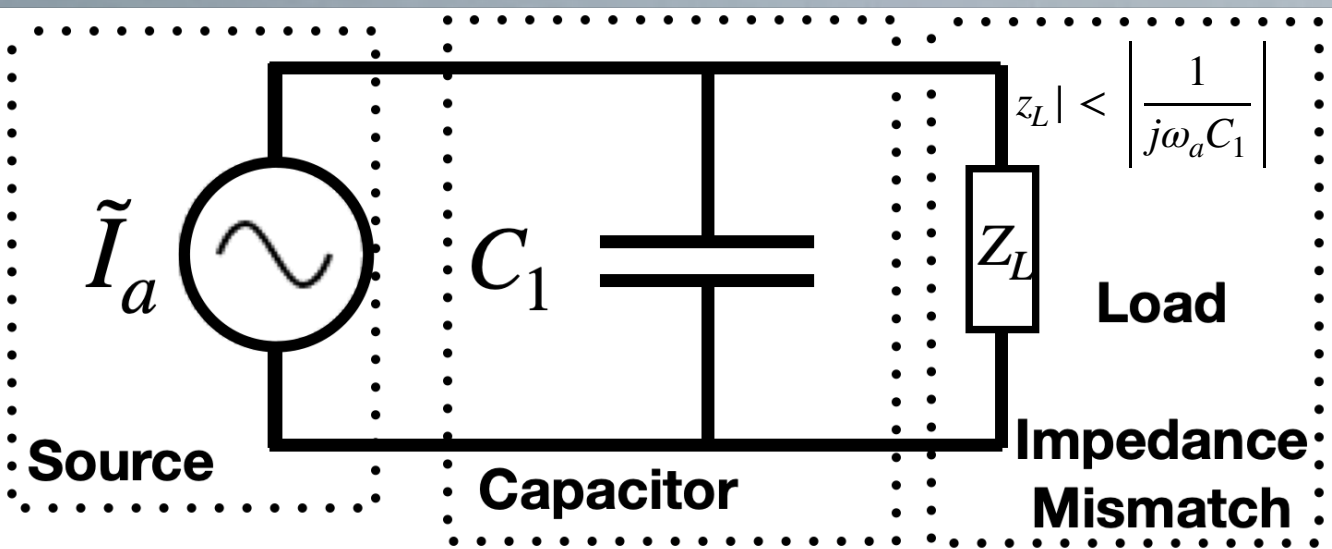
Resonator Measurement: Impedance match; set coupling =1; Take Photons from Source



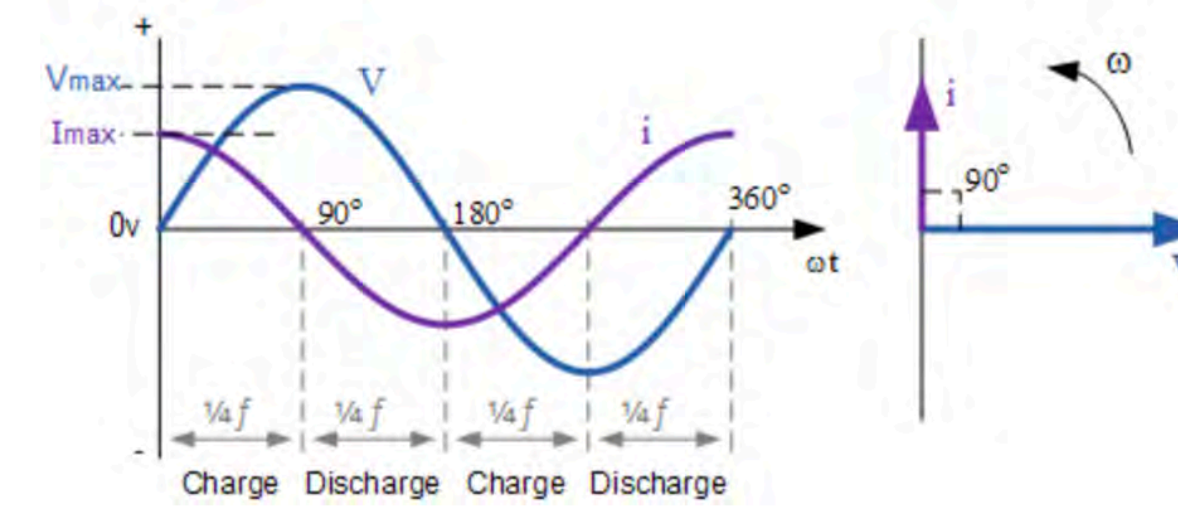
V-I Phase Relationship and Vector Diagram



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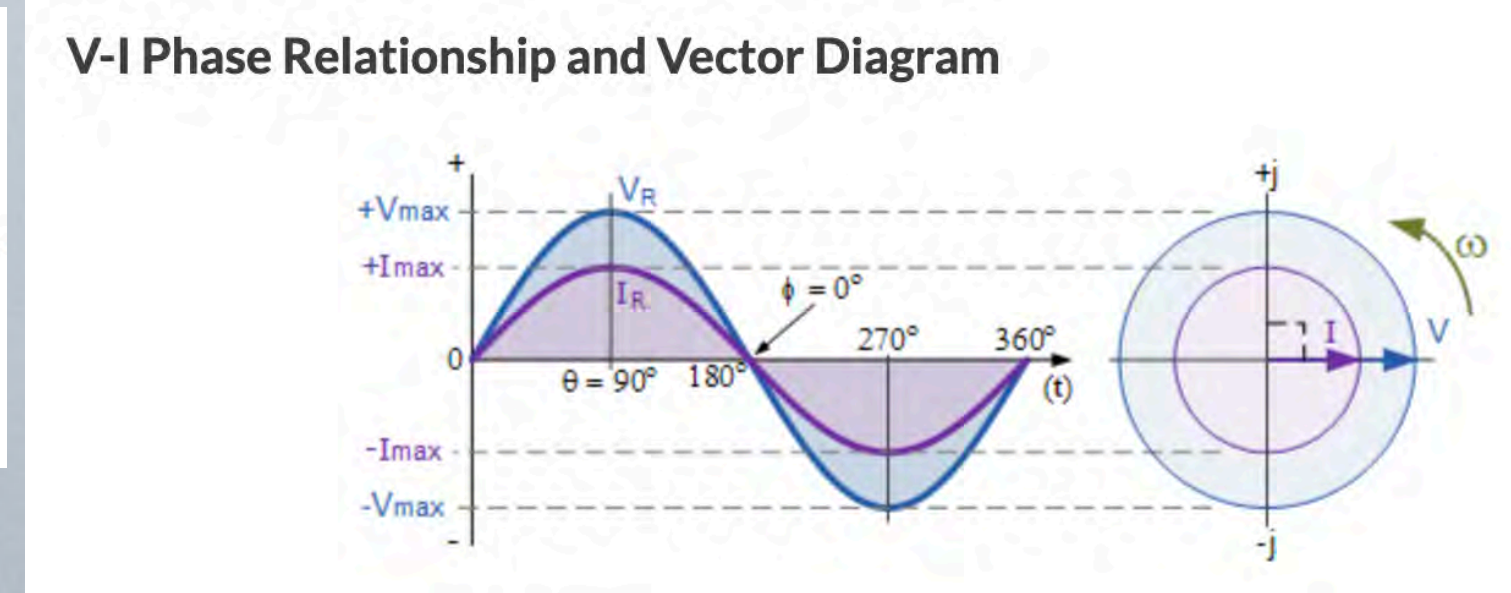
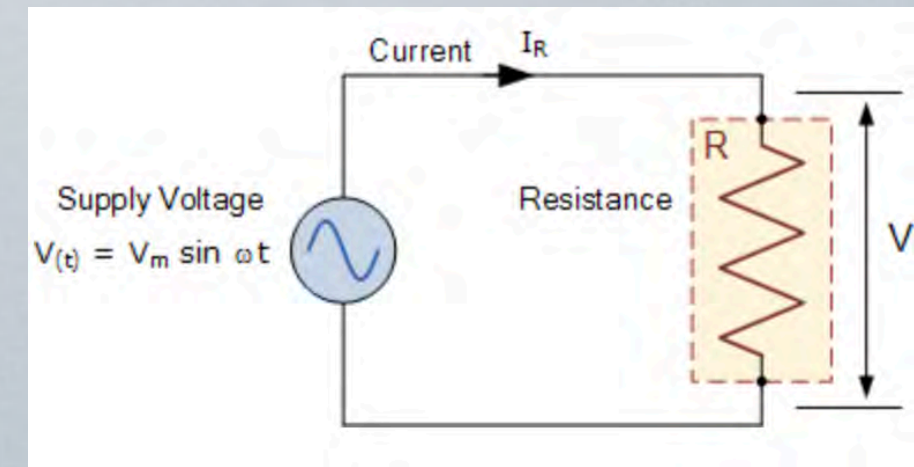
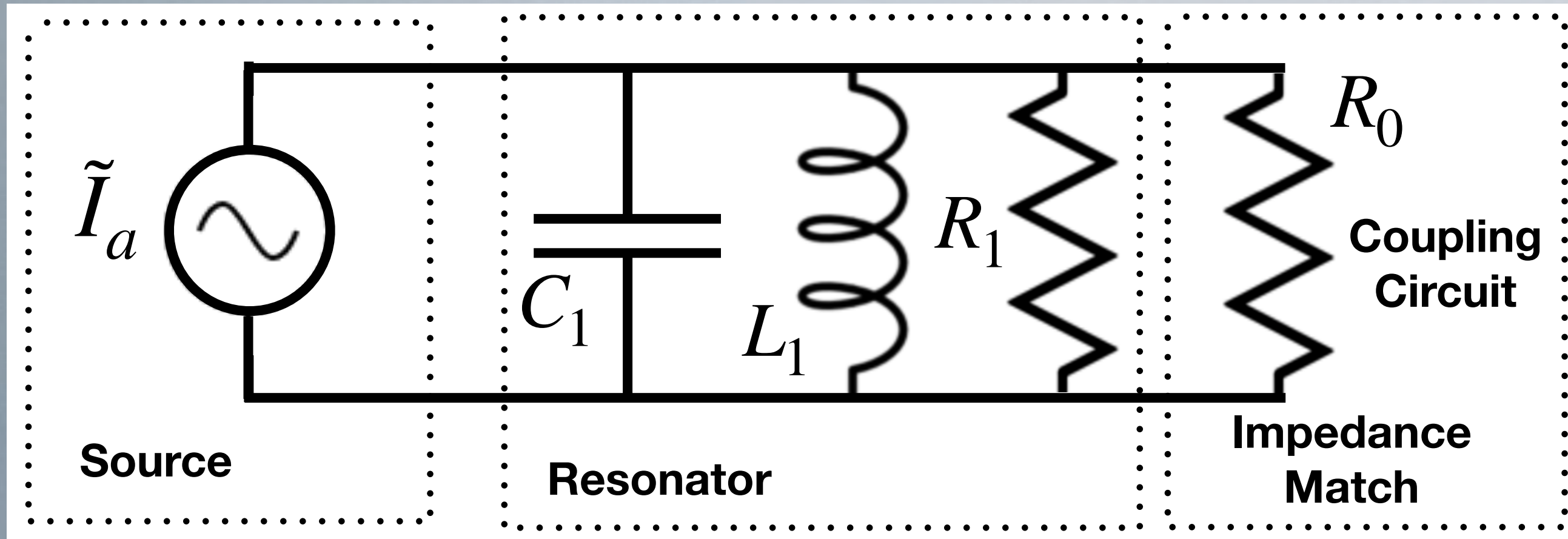
AC Capacitor Phasor Diagram



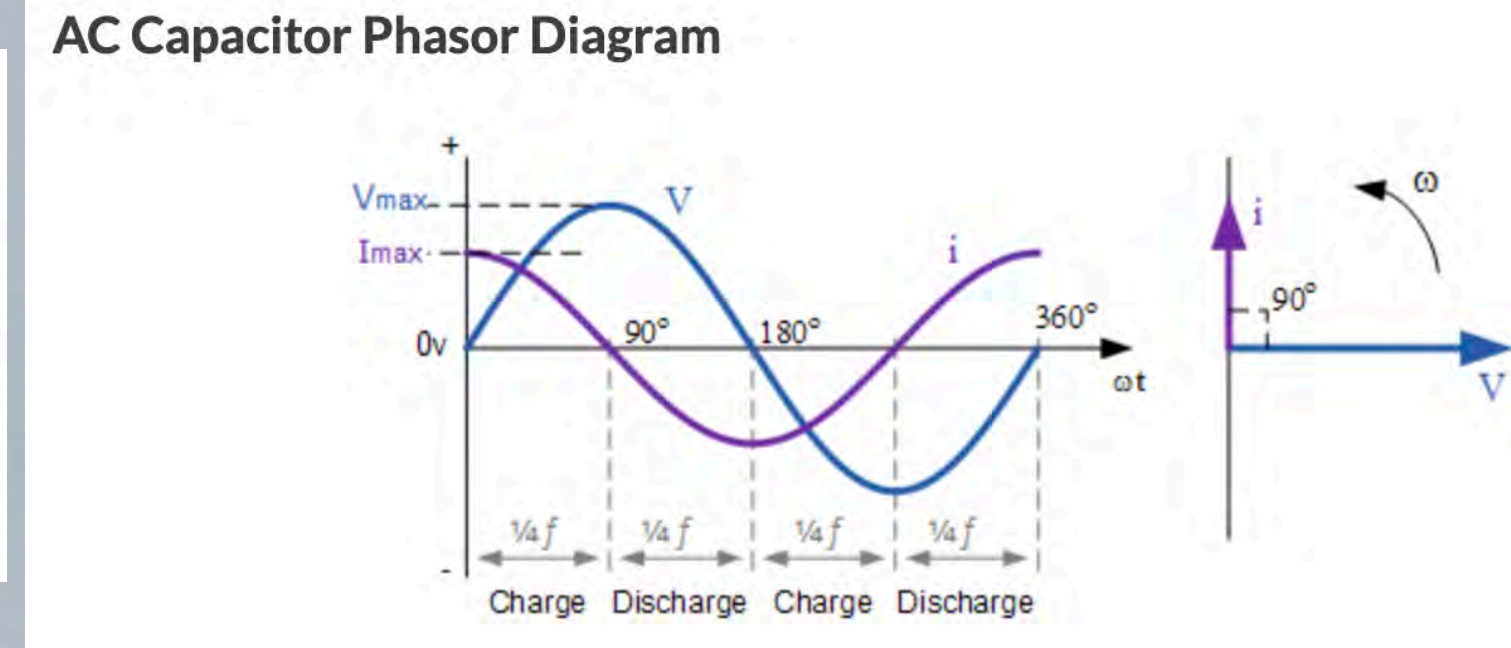
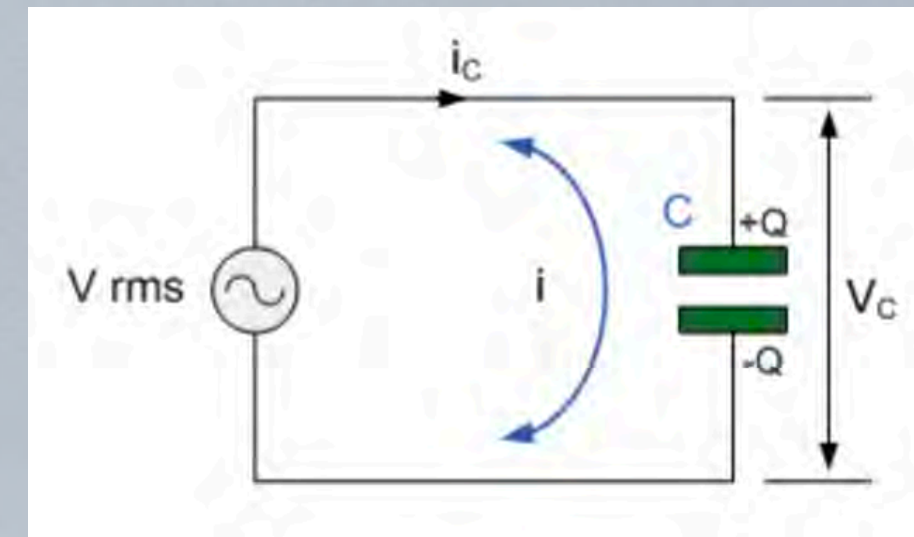
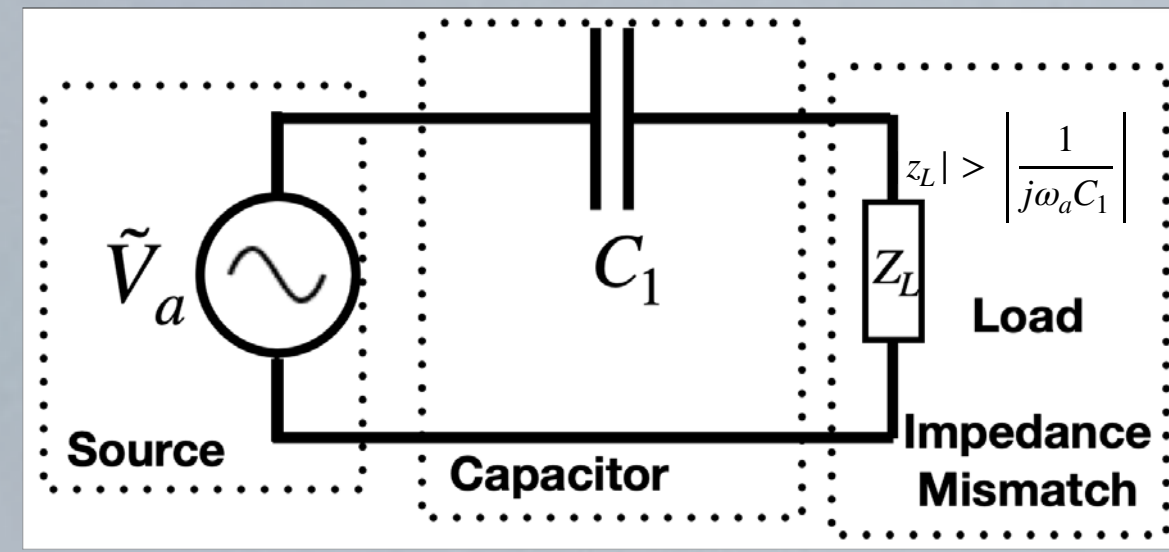
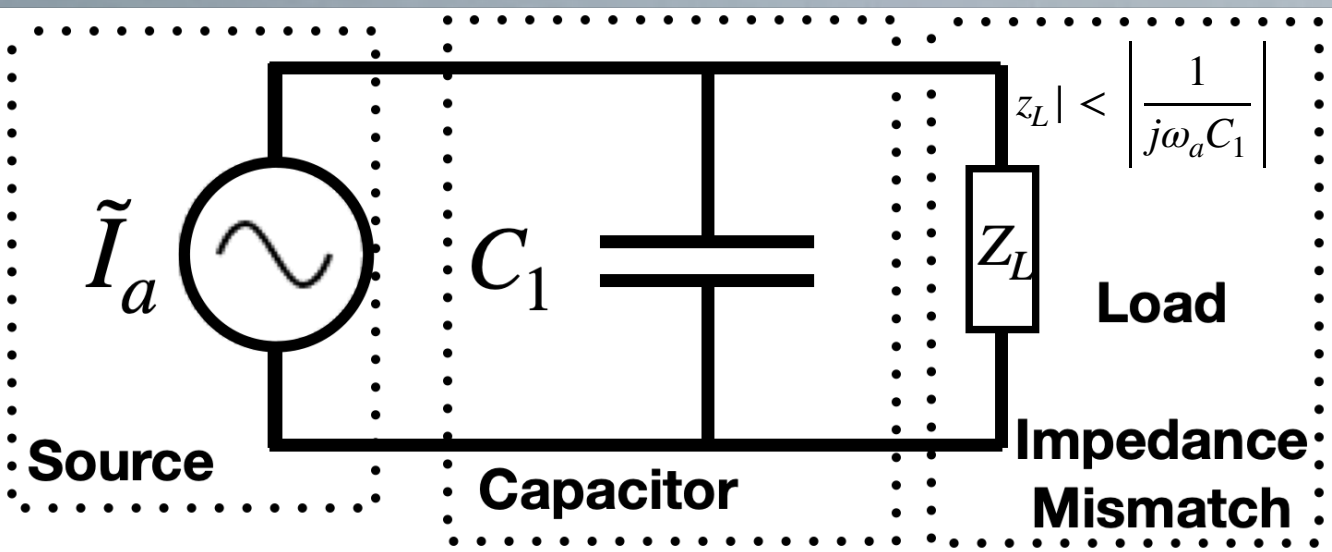
Reactive Power Measurement, Does Not Absorb Energy:

Left eg. Inductive couple SQUID Amplifier (Current of Mag Flux)

Resonator Measurement: Impedance match; set coupling =1; Take Photons from Source



Real Power Measurement, Absorbs Energy: $P_a = I_0^2 R_o = \frac{V_0^2}{R_0}$

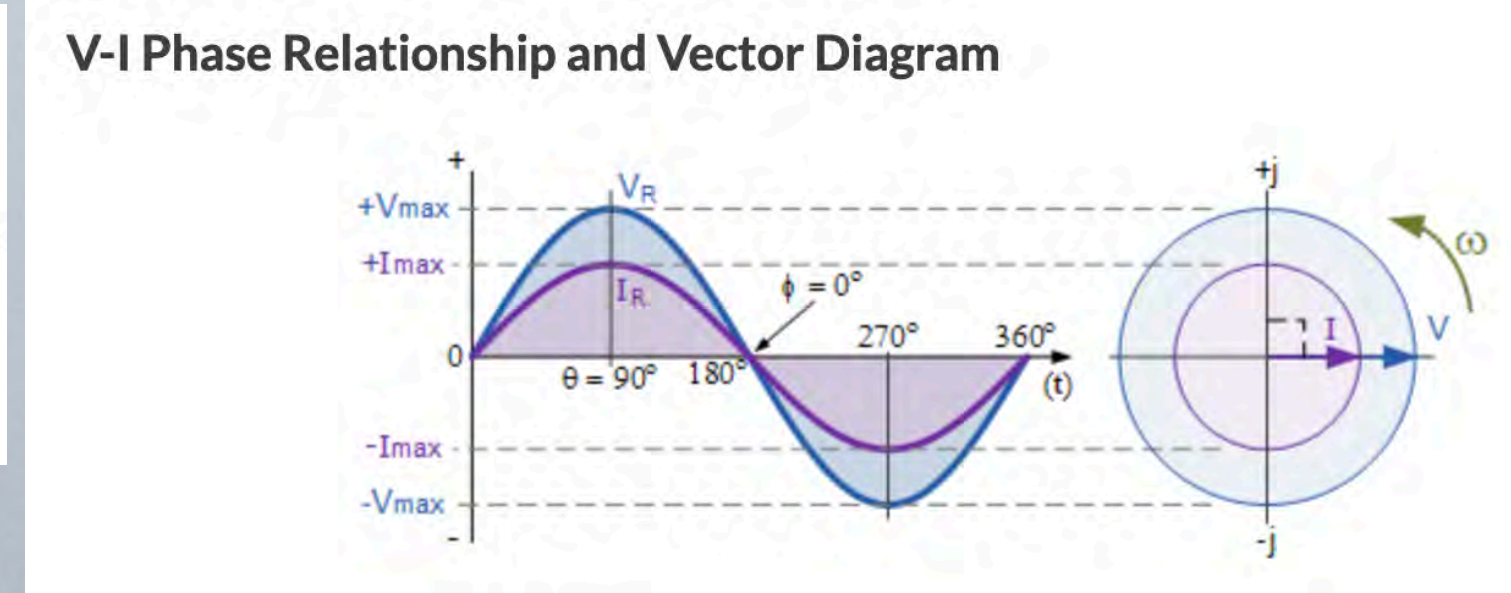
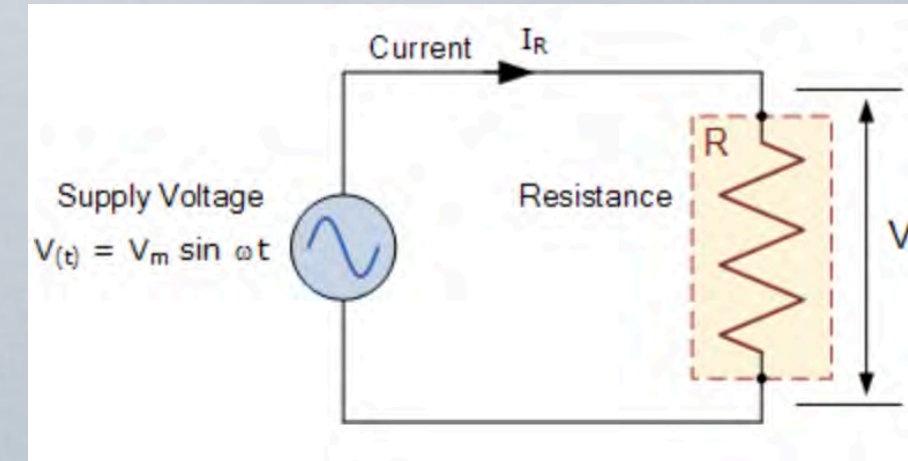
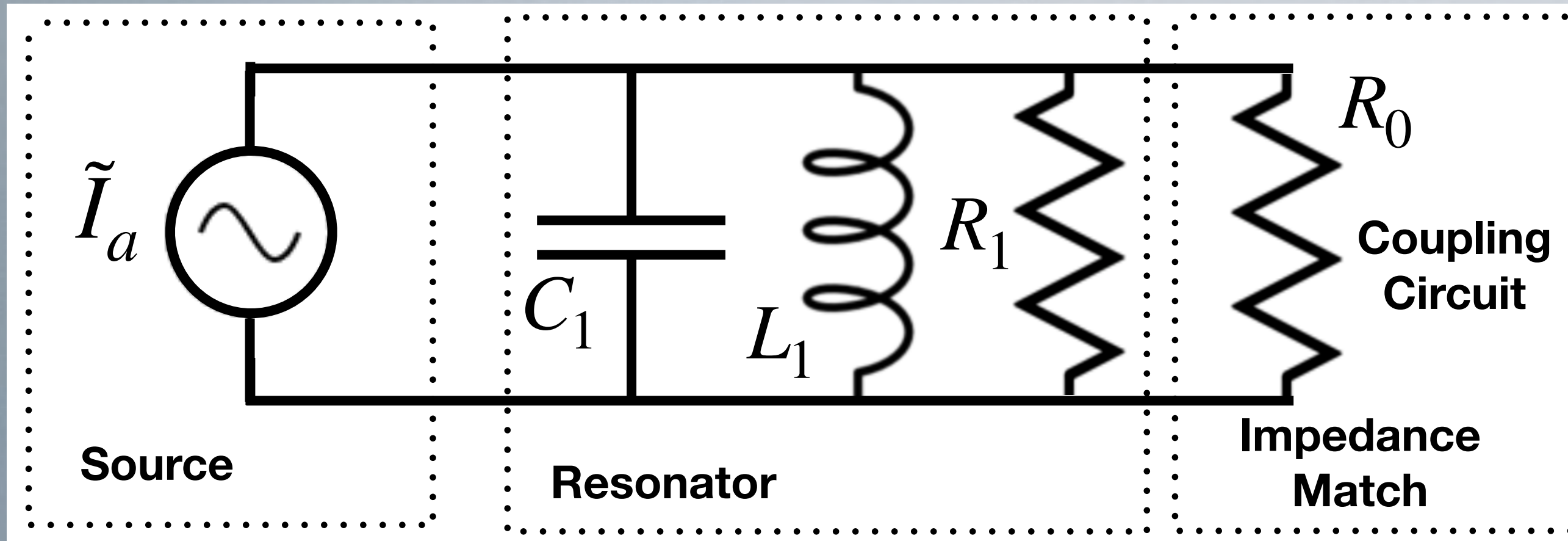


Reactive Power Measurement, Does Not Absorb Energy:

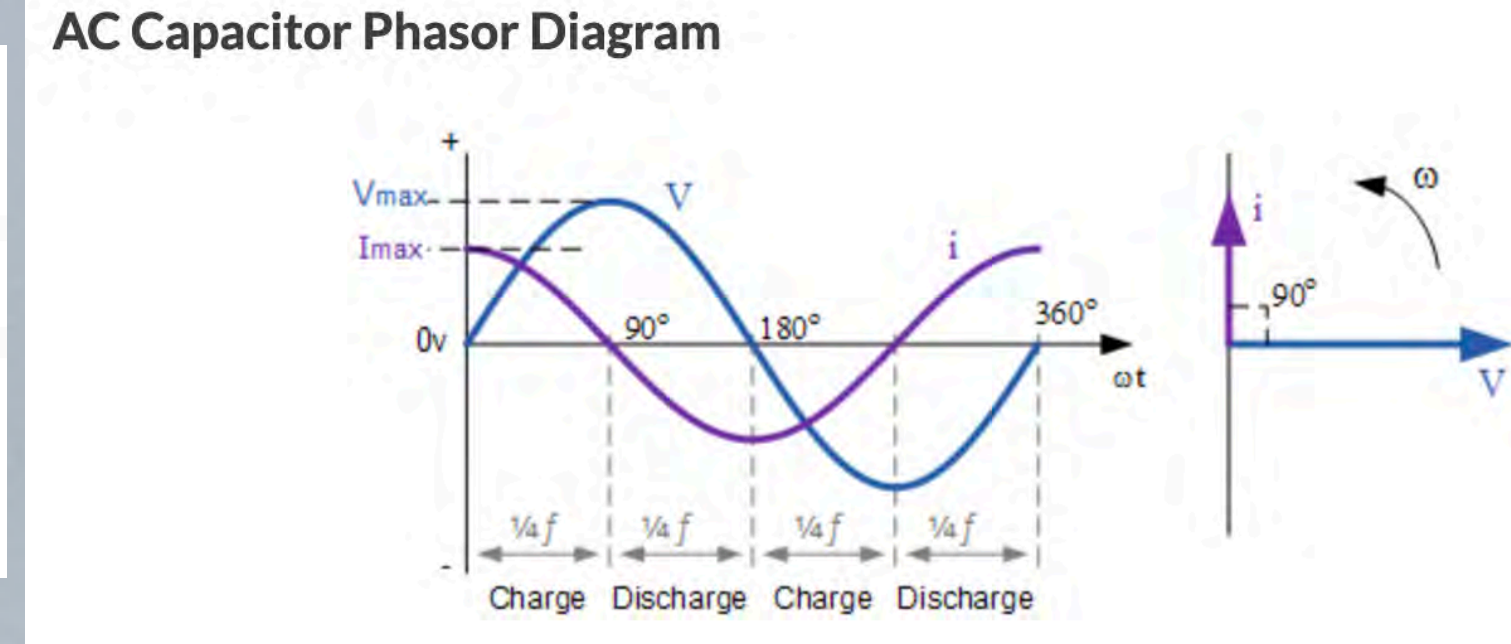
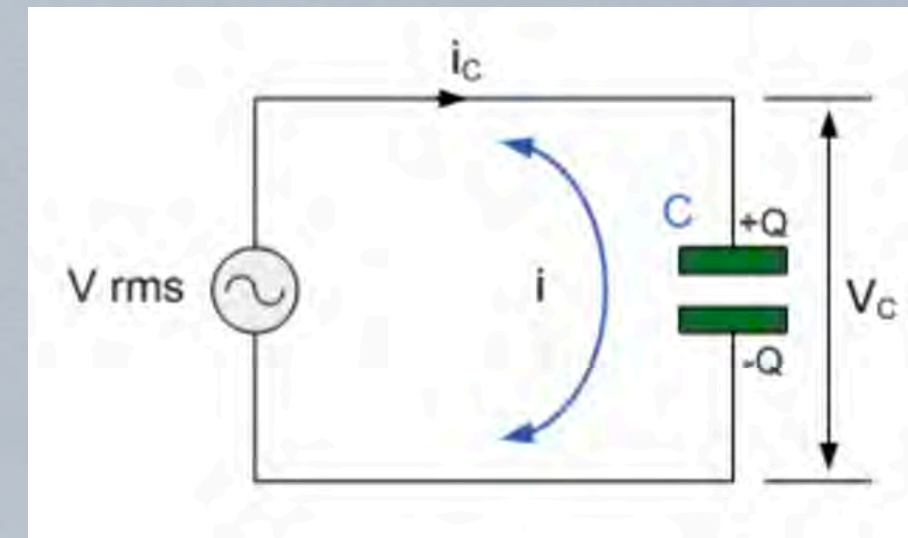
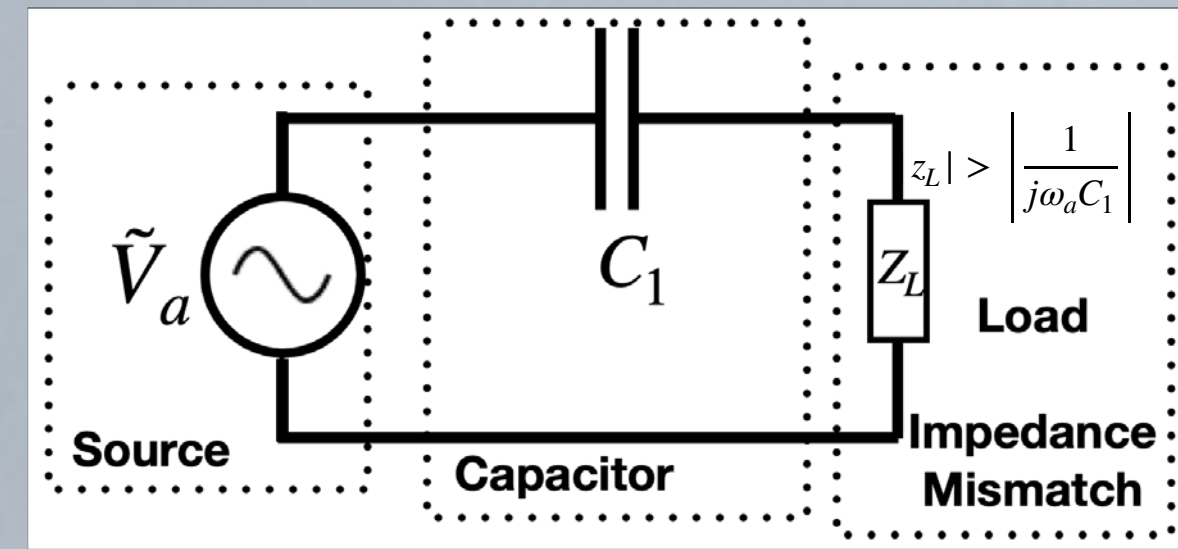
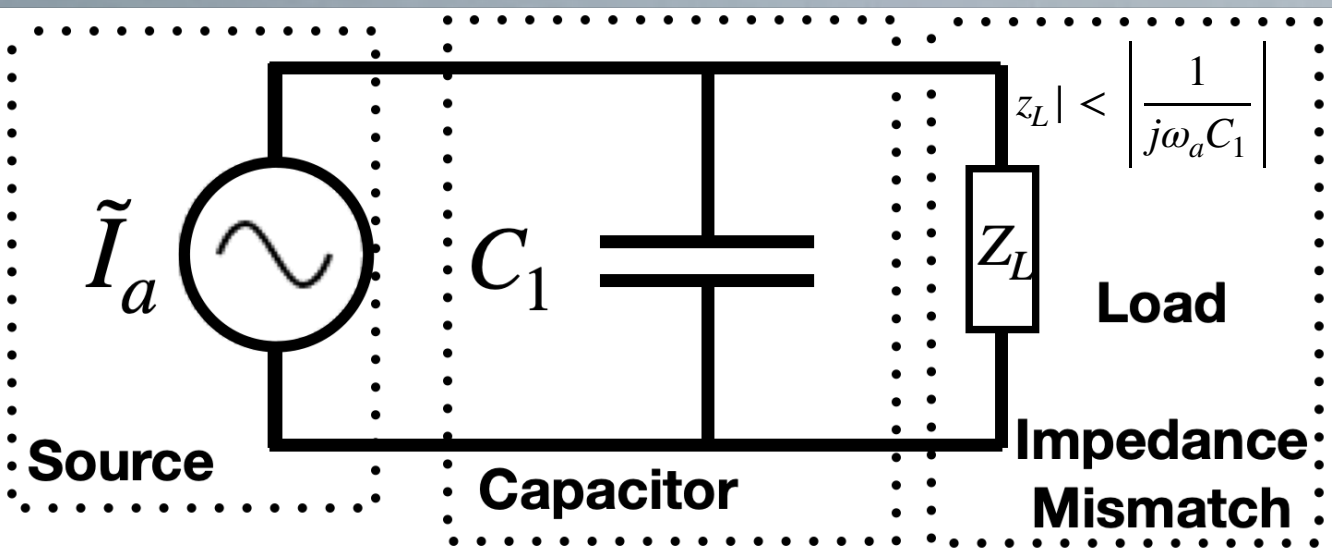
Left eg. Inductive couple SQUID Amplifier (Current of Mag Flux)

Right eg. Capacitive coupled High Impedance Amplifier (Voltage)

Resonator Measurement: Impedance match; set coupling = 1; Take Photons from Source



Real Power Measurement, Absorbs Energy: $P_a = I_0^2 R_o = \frac{V_0^2}{R_0}$



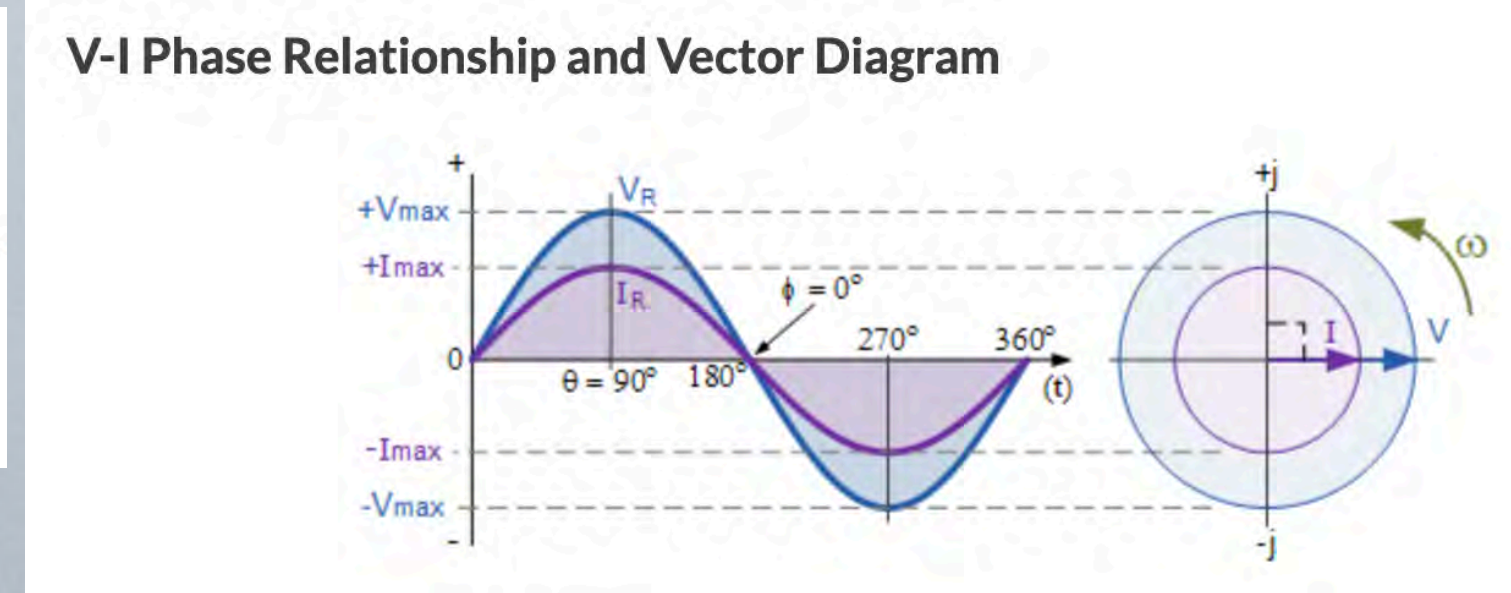
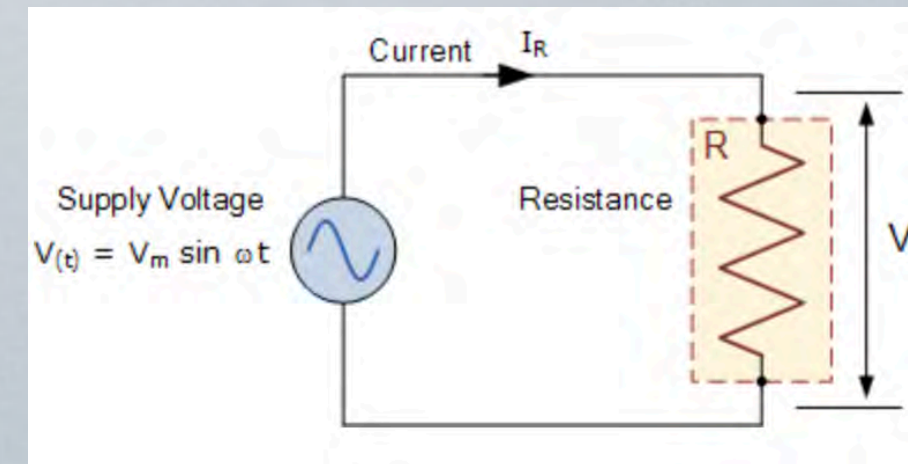
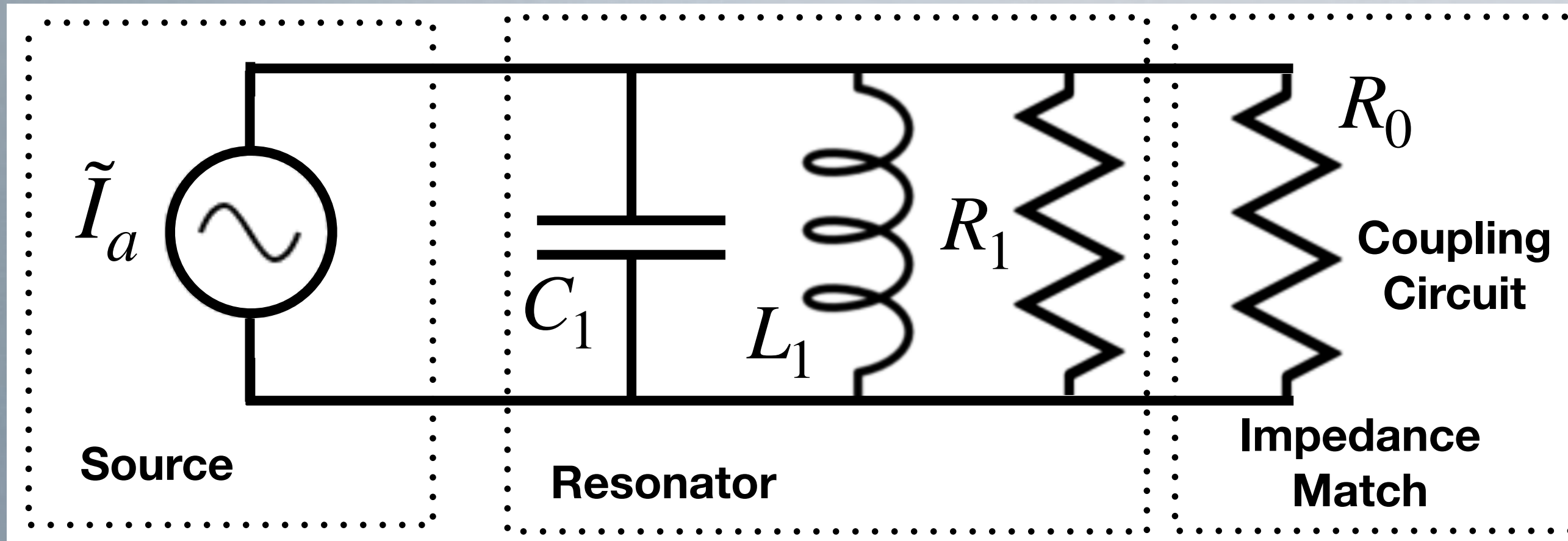
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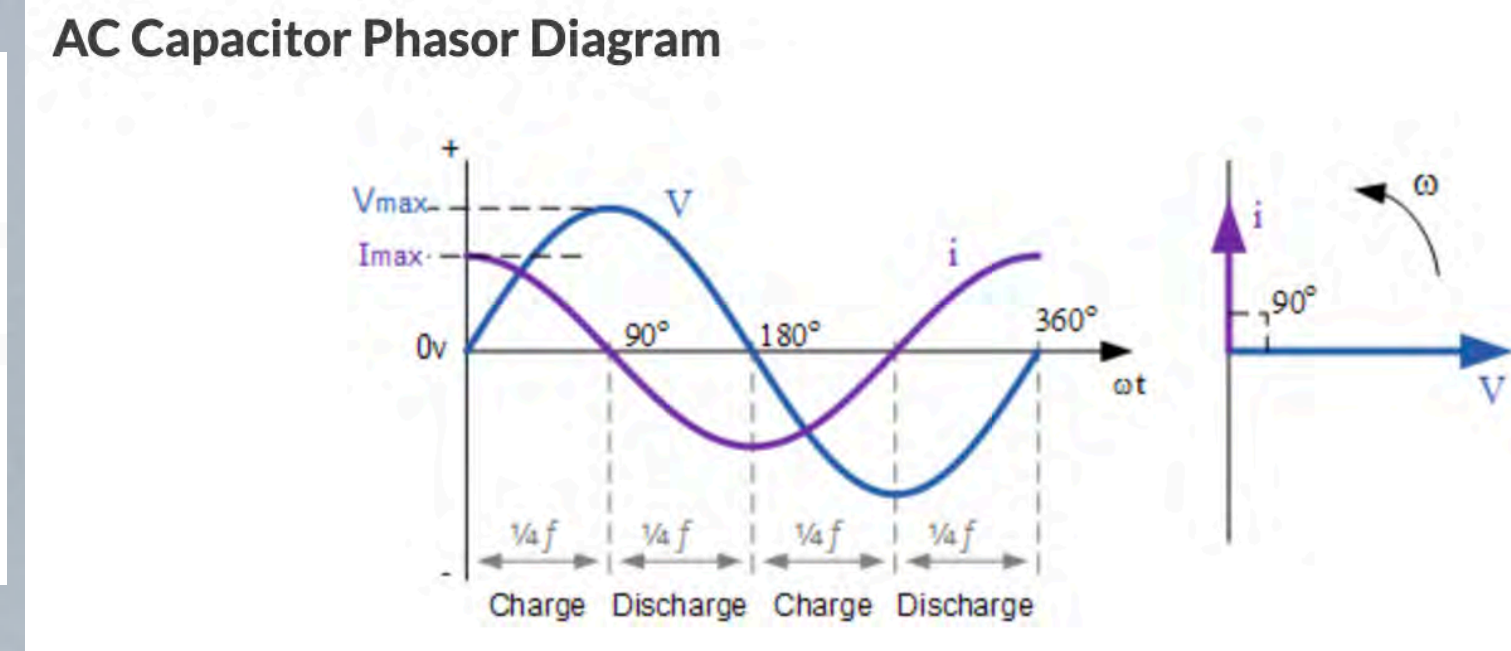
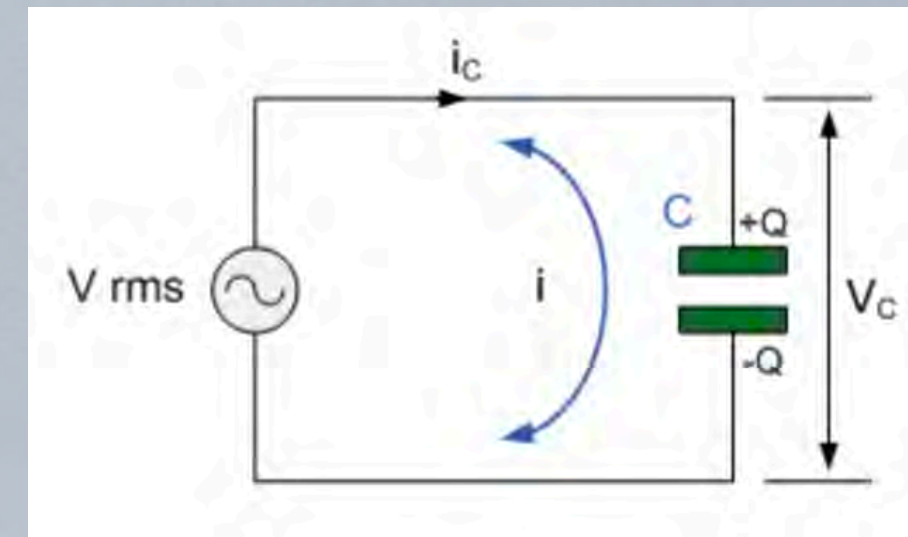
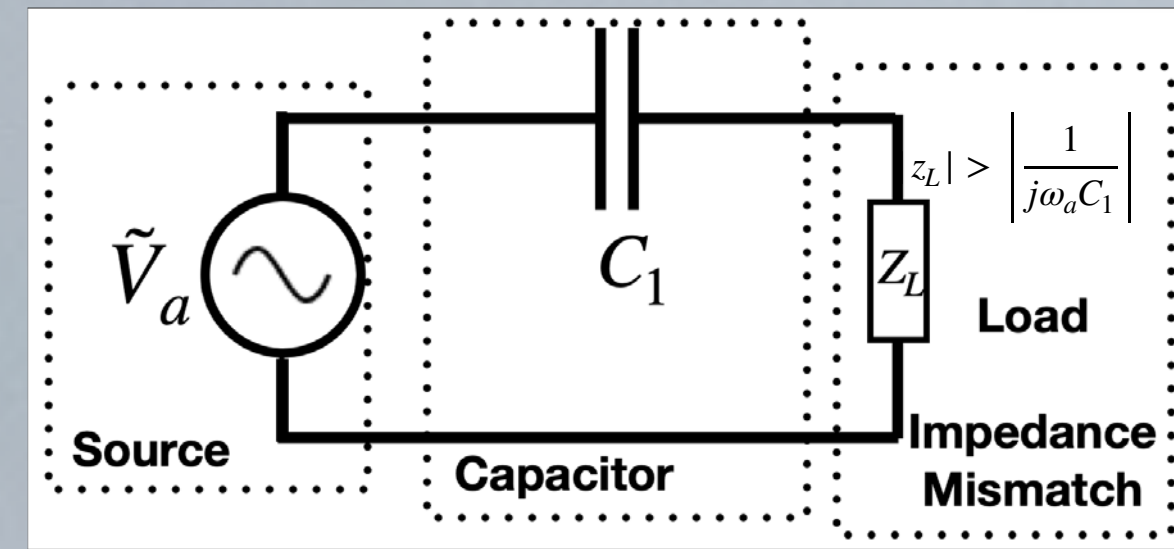
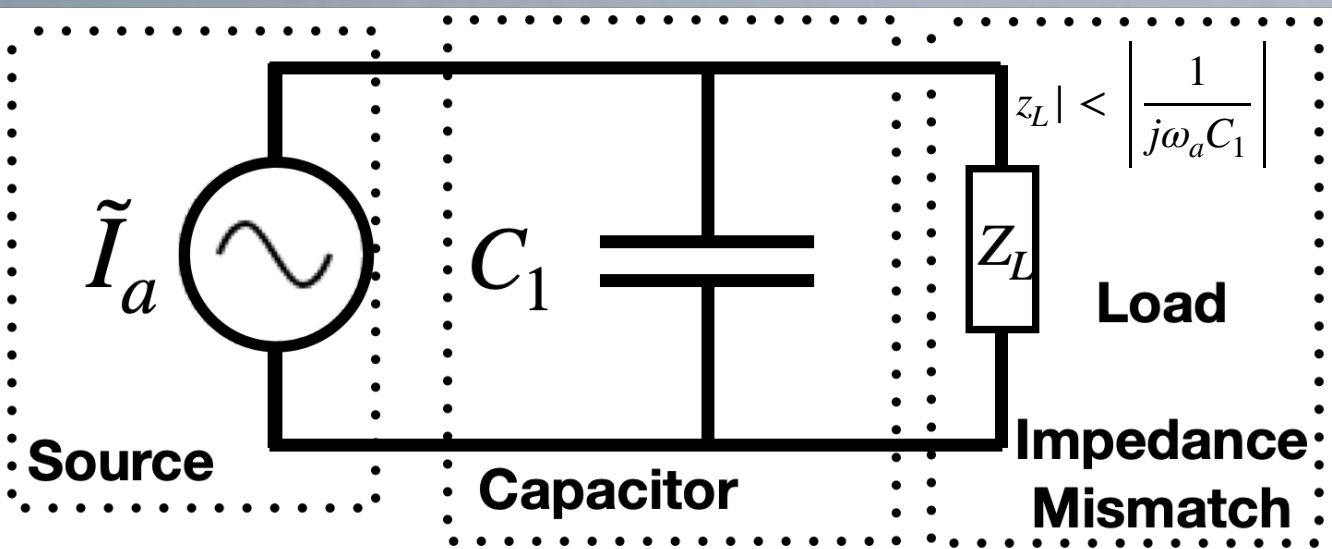
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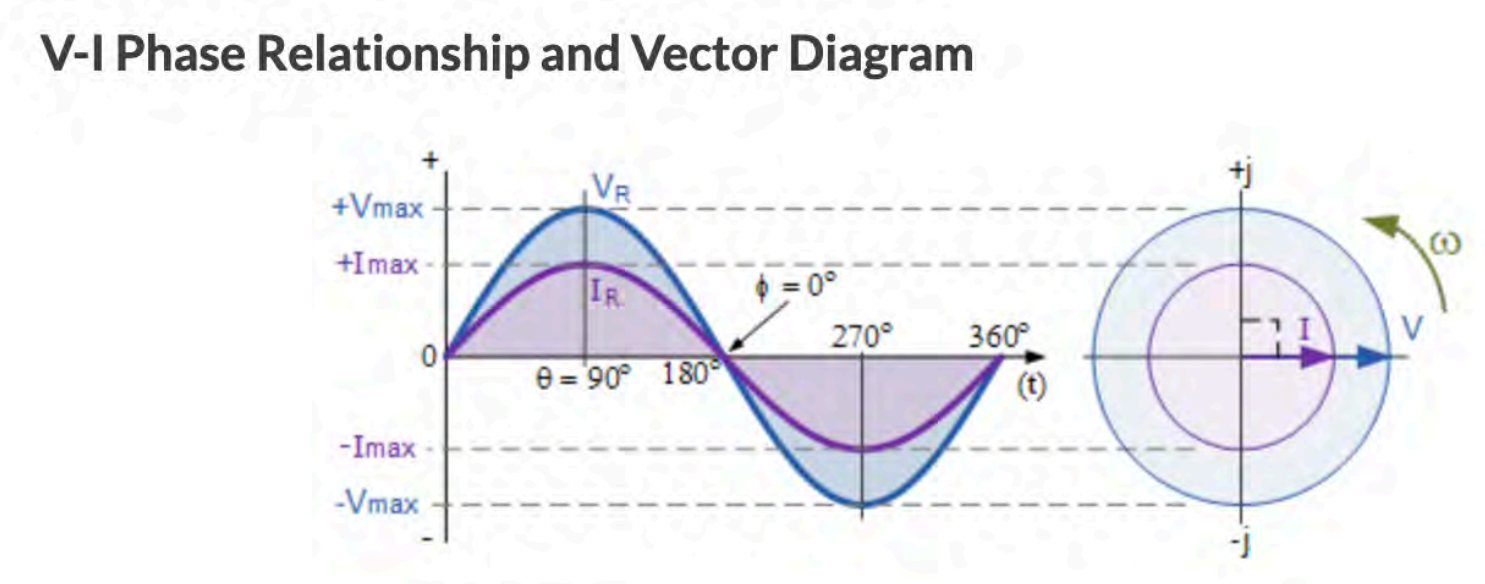
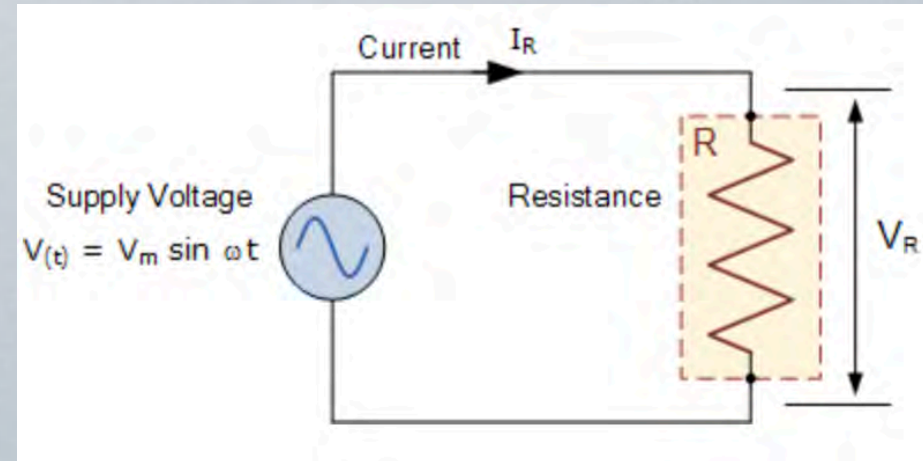
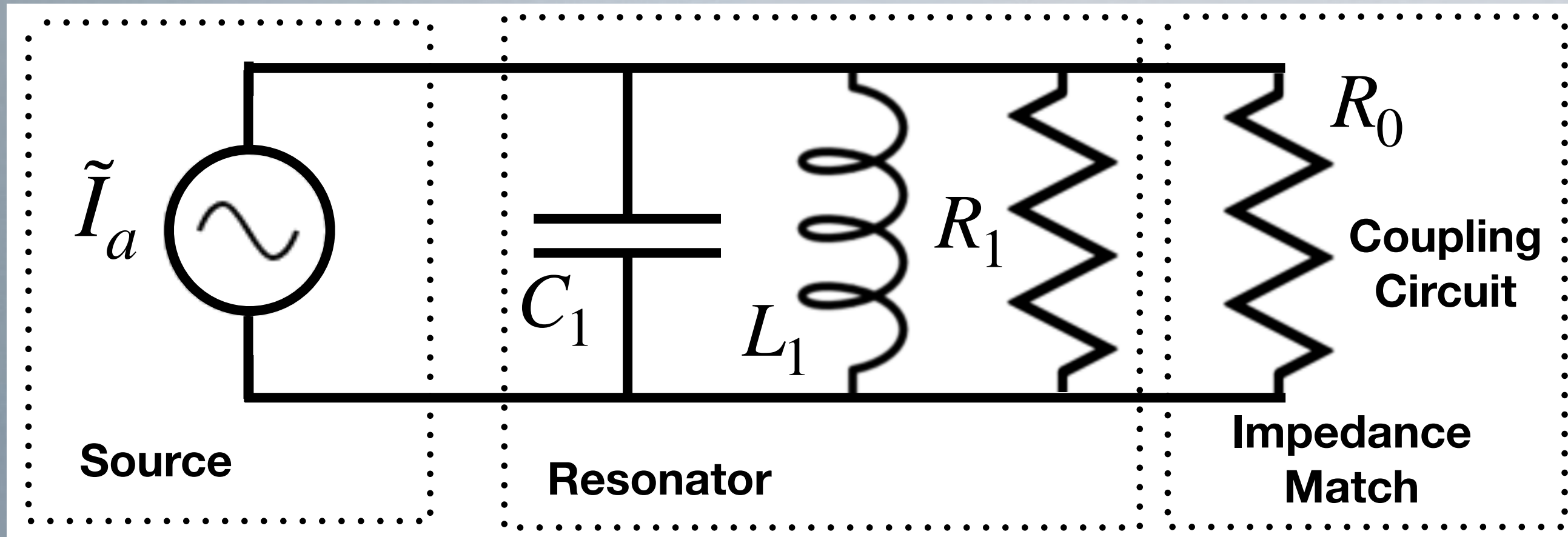
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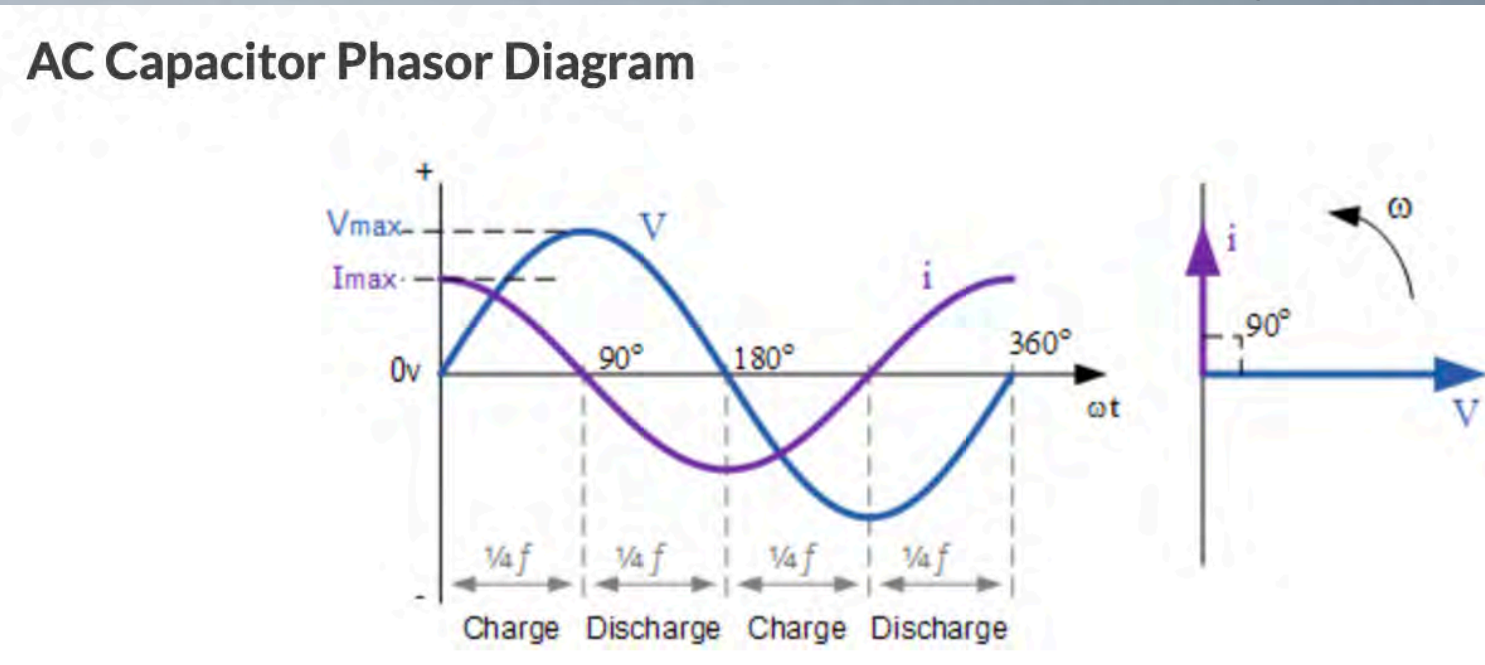
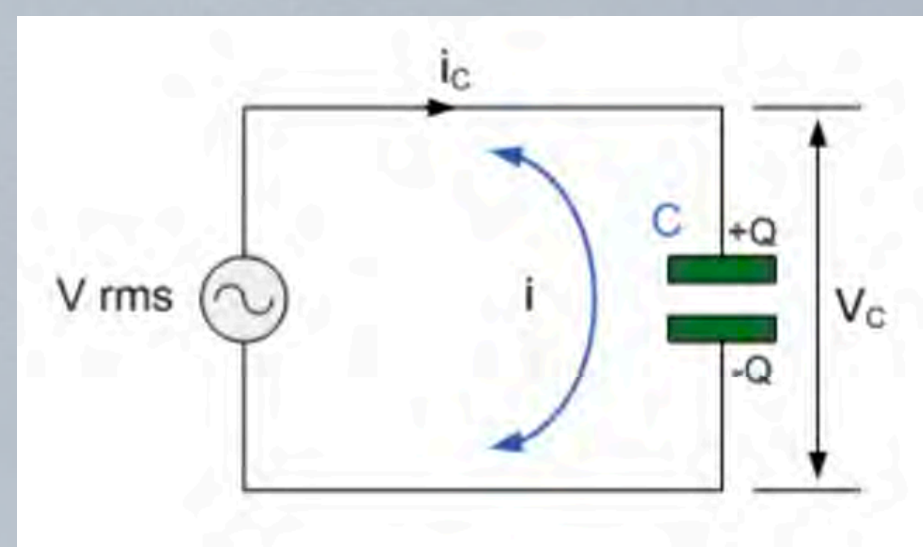
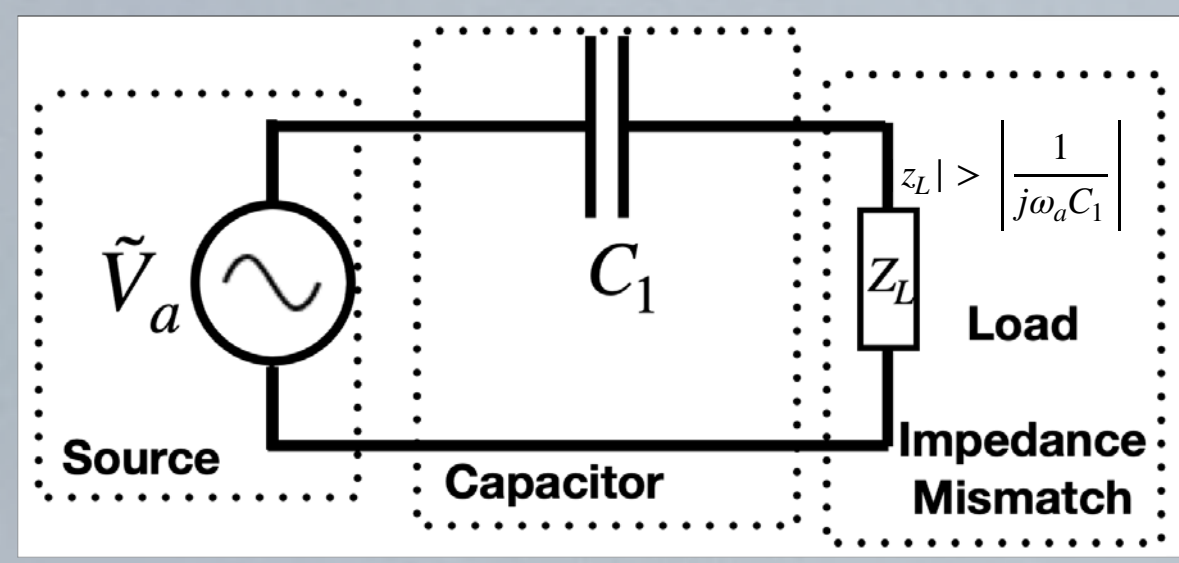
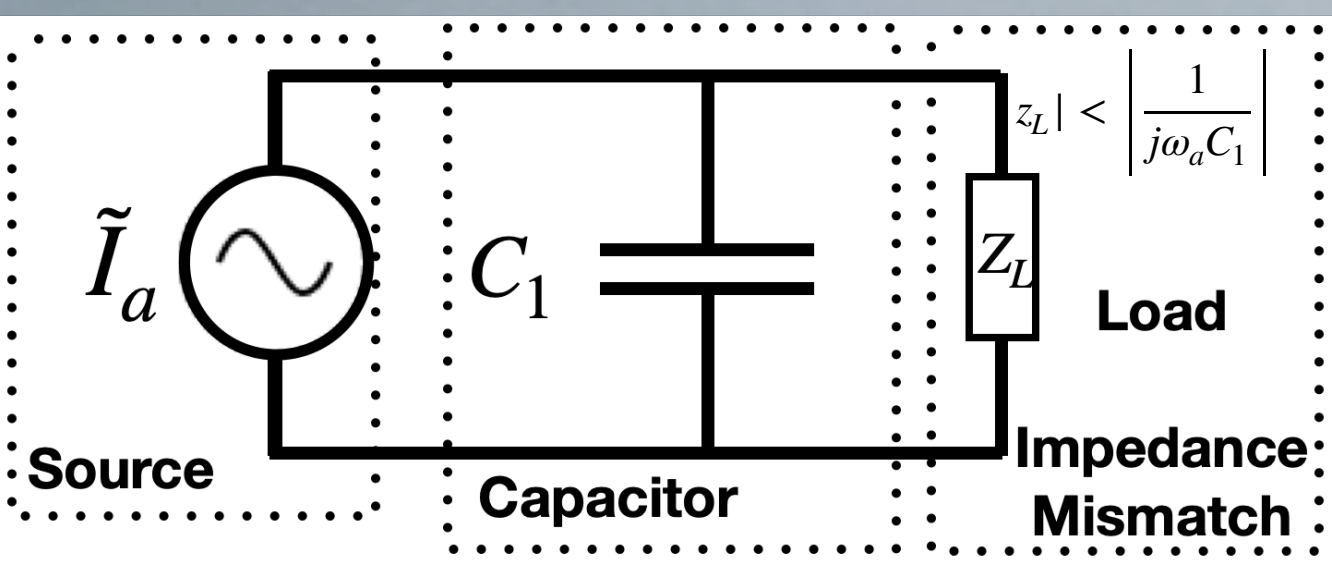
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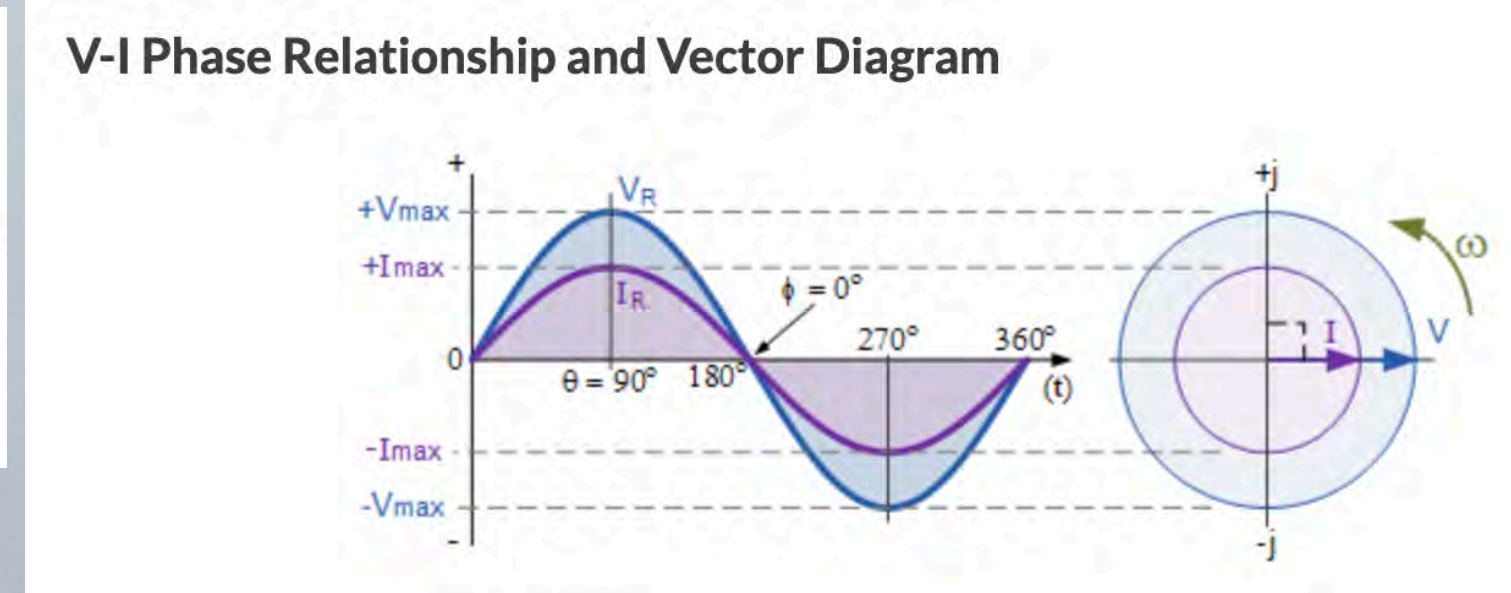
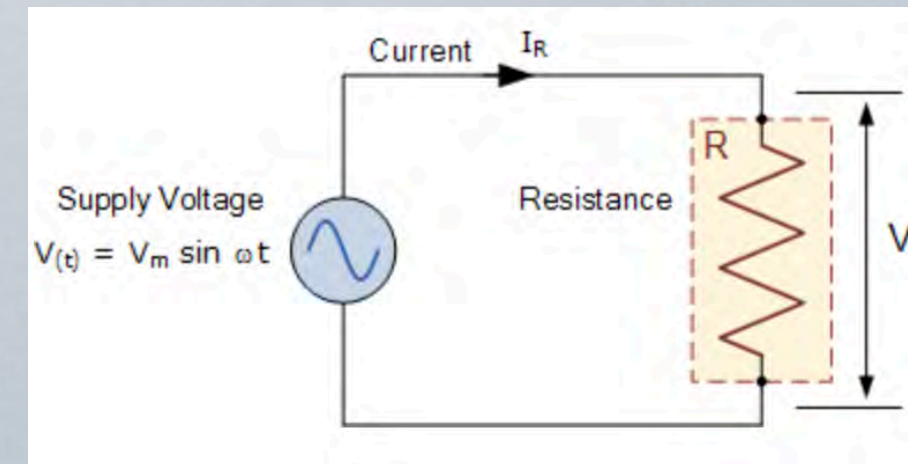
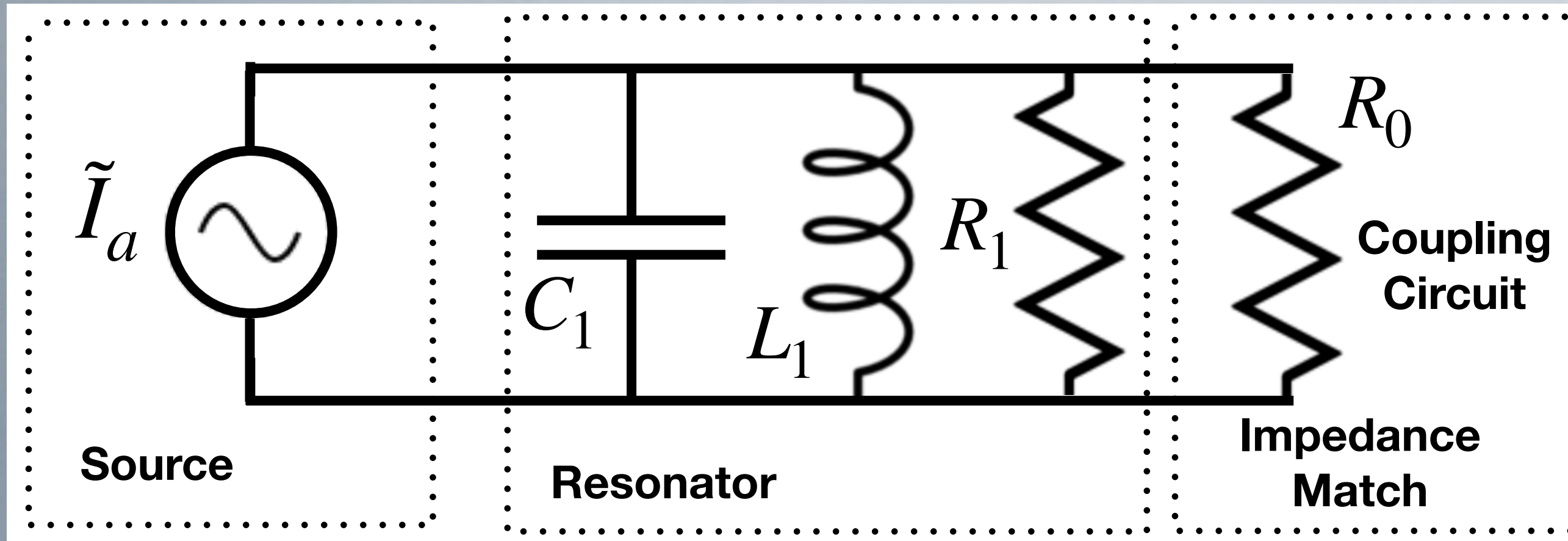
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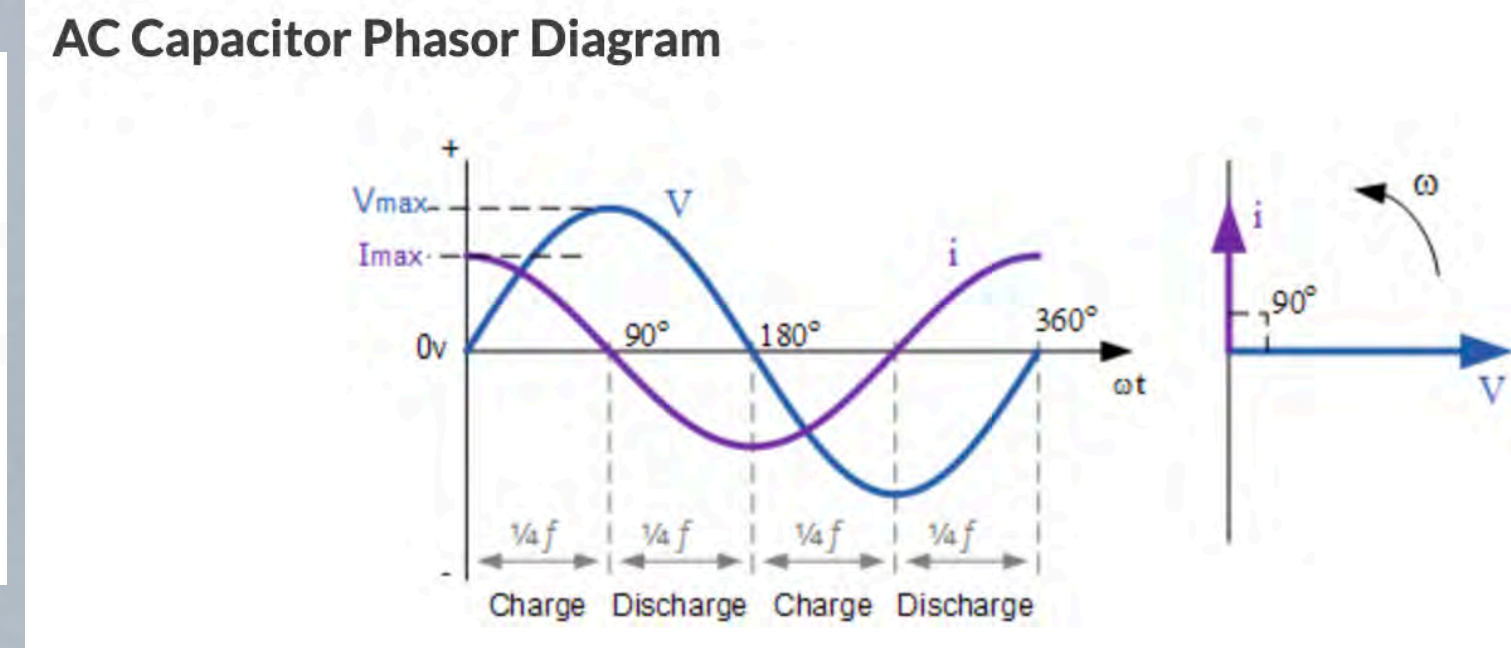
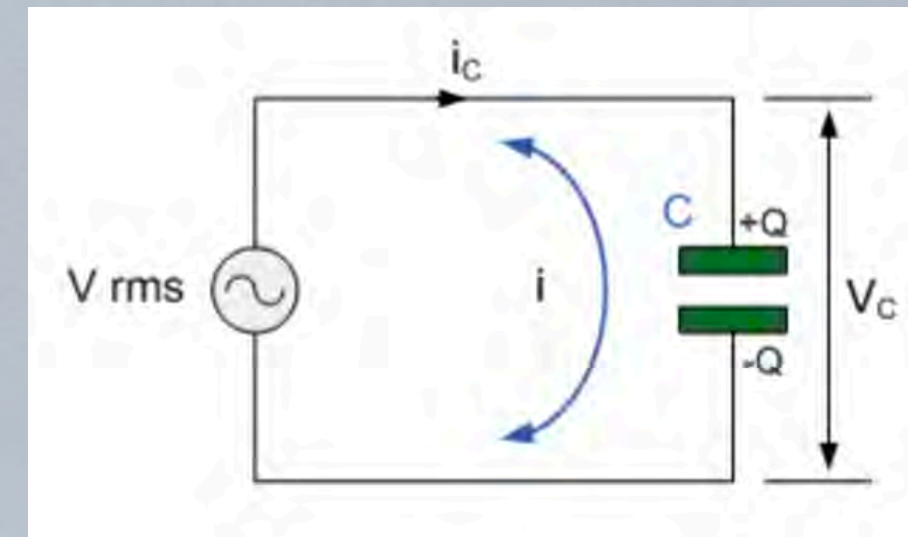
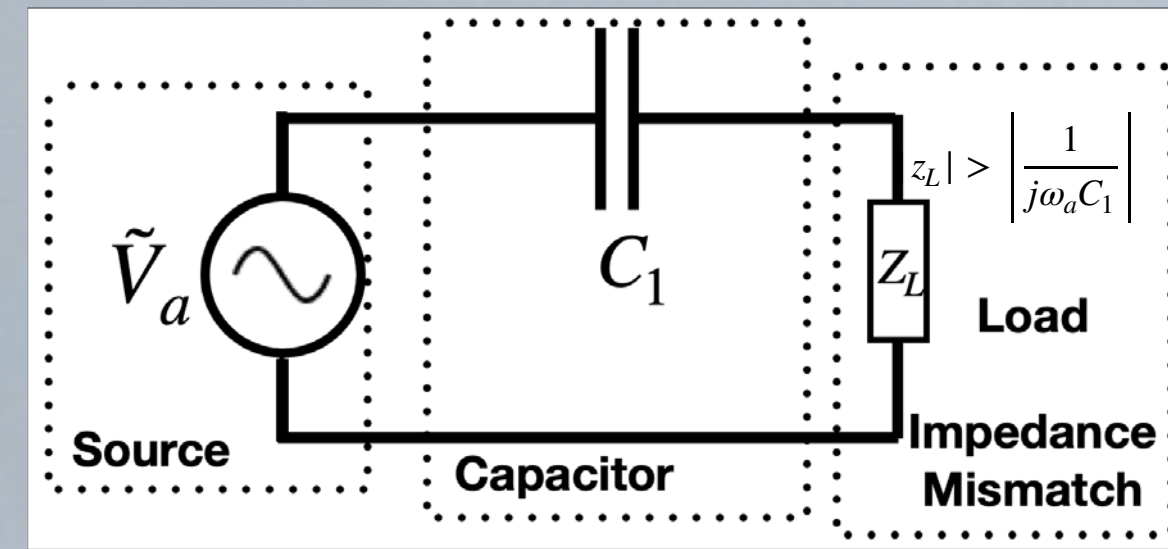
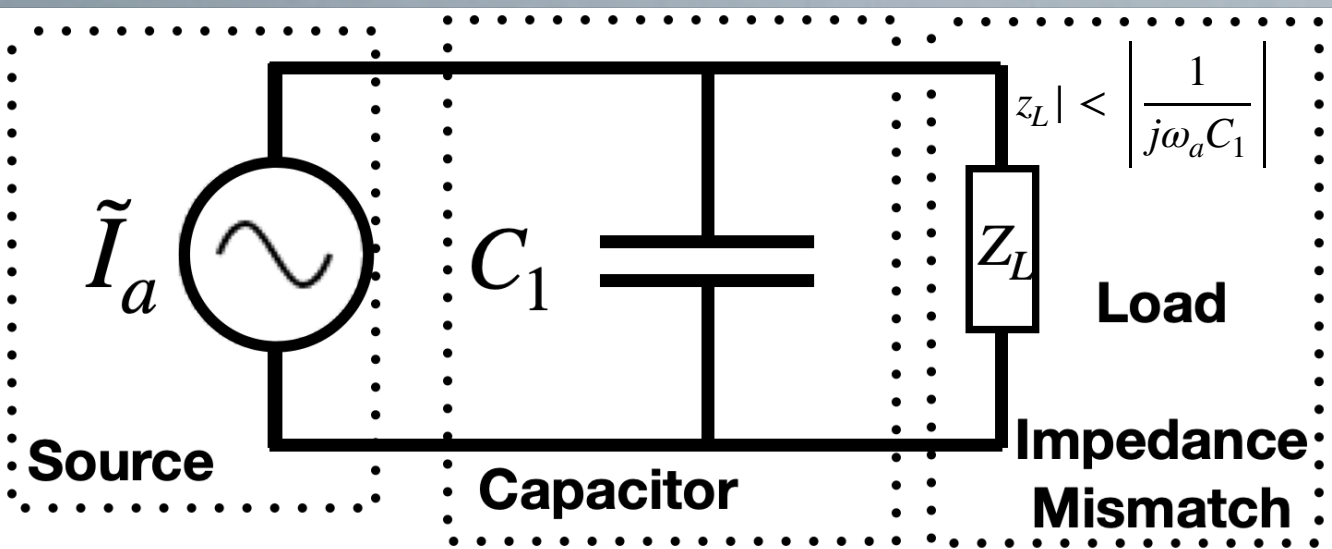
**Energy oscillates between Source and Capacitor
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Reactive power does not propagate or dissipate out of the volume of the detector (ie. no loss): Oscillates in and out of volume

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**Energy oscillates between Source and Capacitor
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Reactive power does not propagate or dissipate out of the volume of the detector (ie. no loss): Oscillates in and out of volume
Does not need to be the order of the Compton wavelength in size (sub wavelength phenomena)

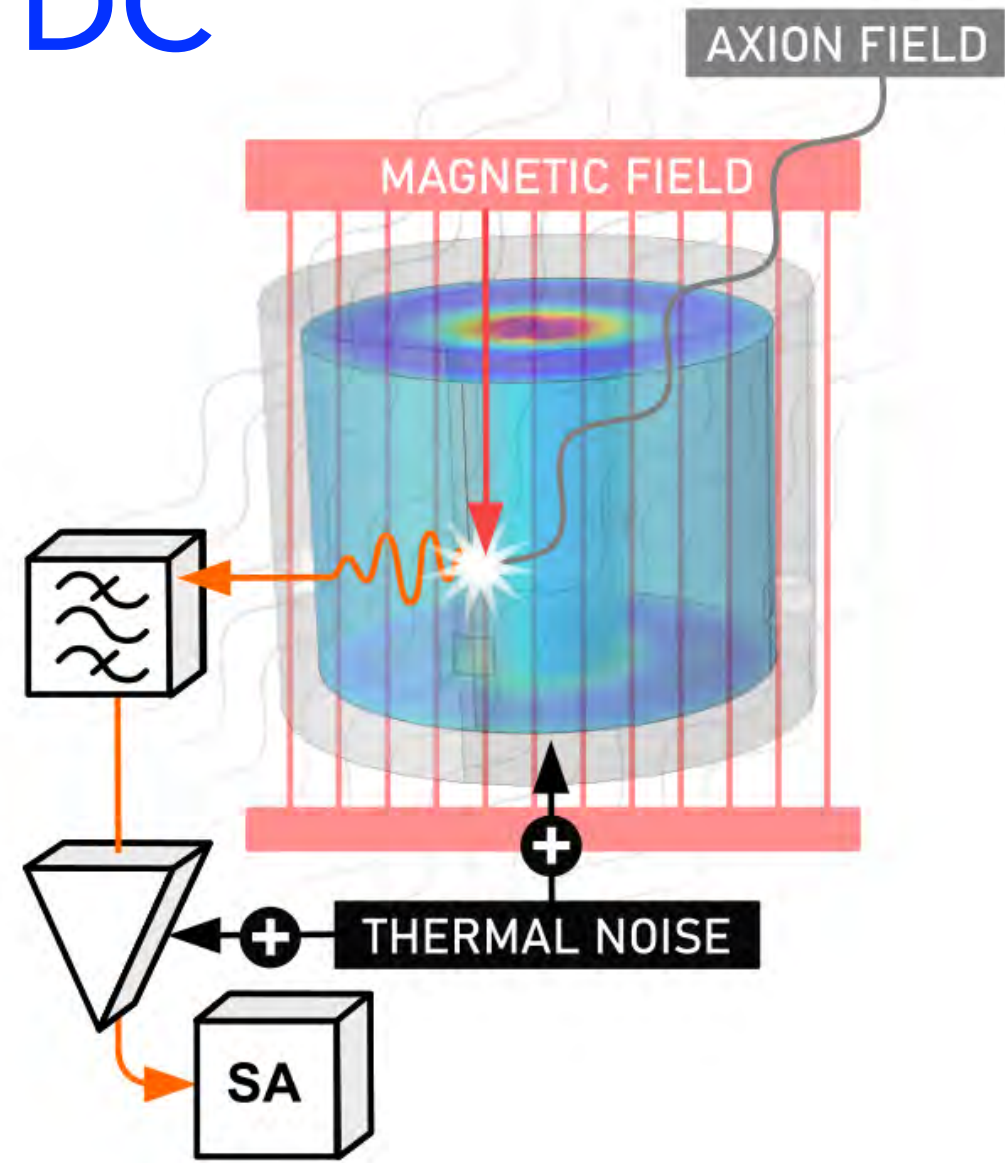
Resonant Axion Haloscopes @ UWA

$$\mathcal{H}_{int} = \epsilon_0 c g_{a\gamma\gamma} a \mathbf{E} \cdot \mathbf{B}$$

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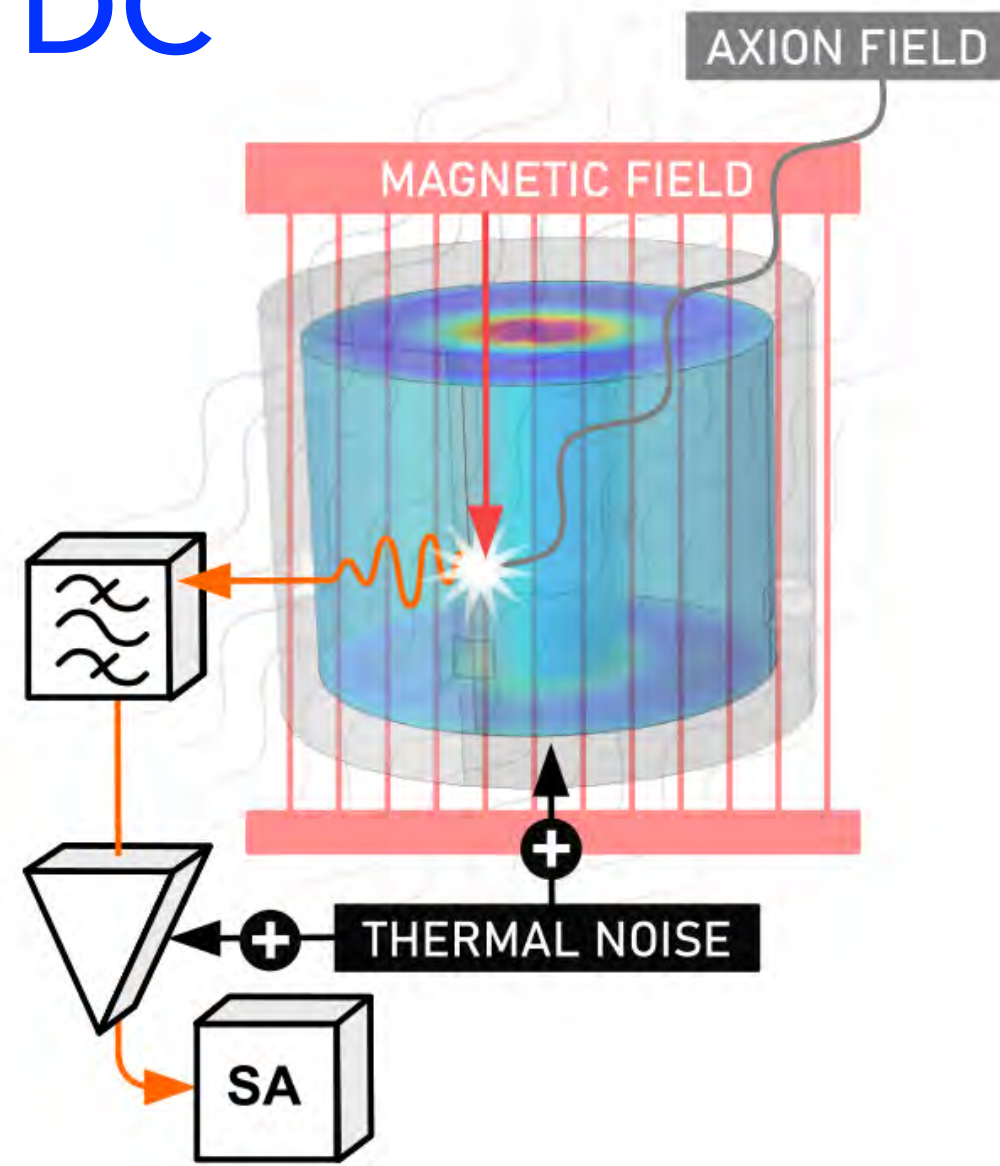
DC



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DC

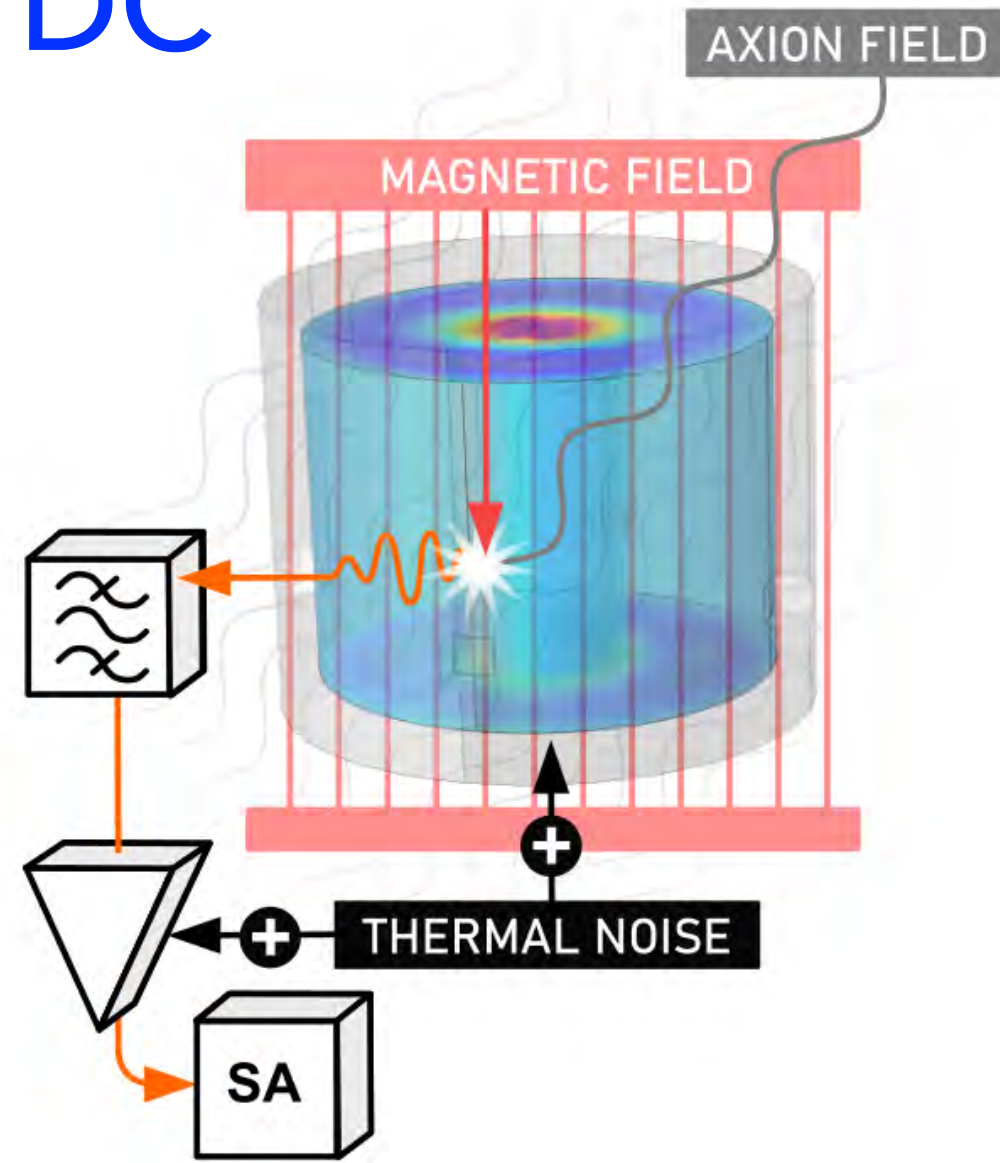


Photon 1: E field of cavity's resonant transverse magnetic mode, $m_a = f_1 + \delta f$

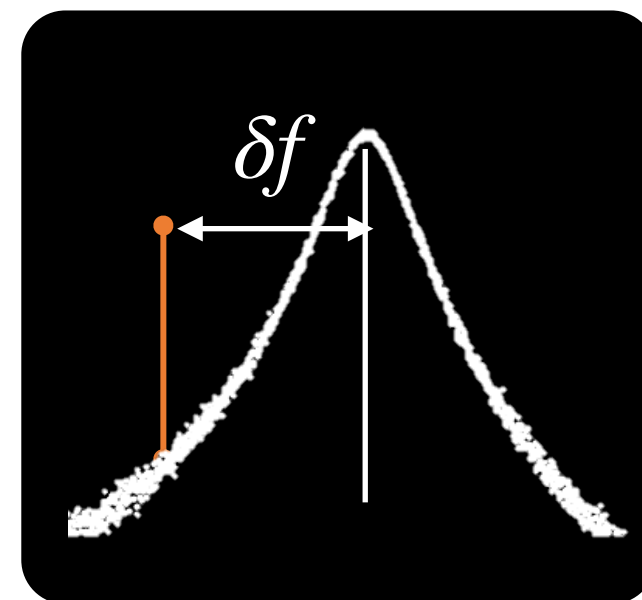
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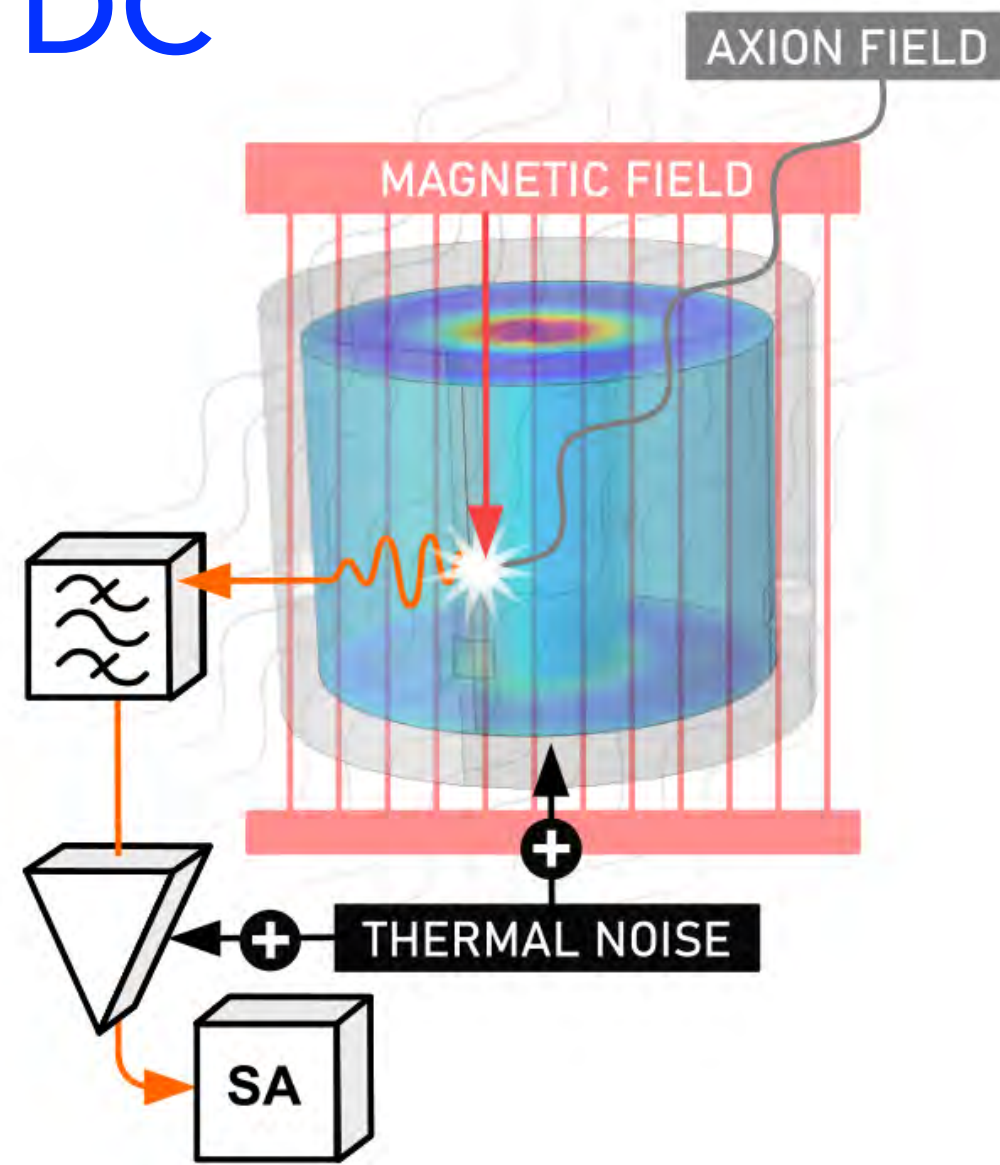
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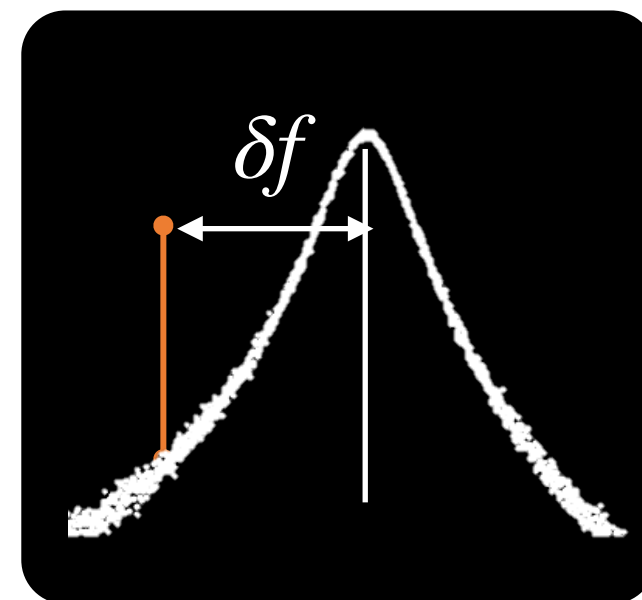
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DC



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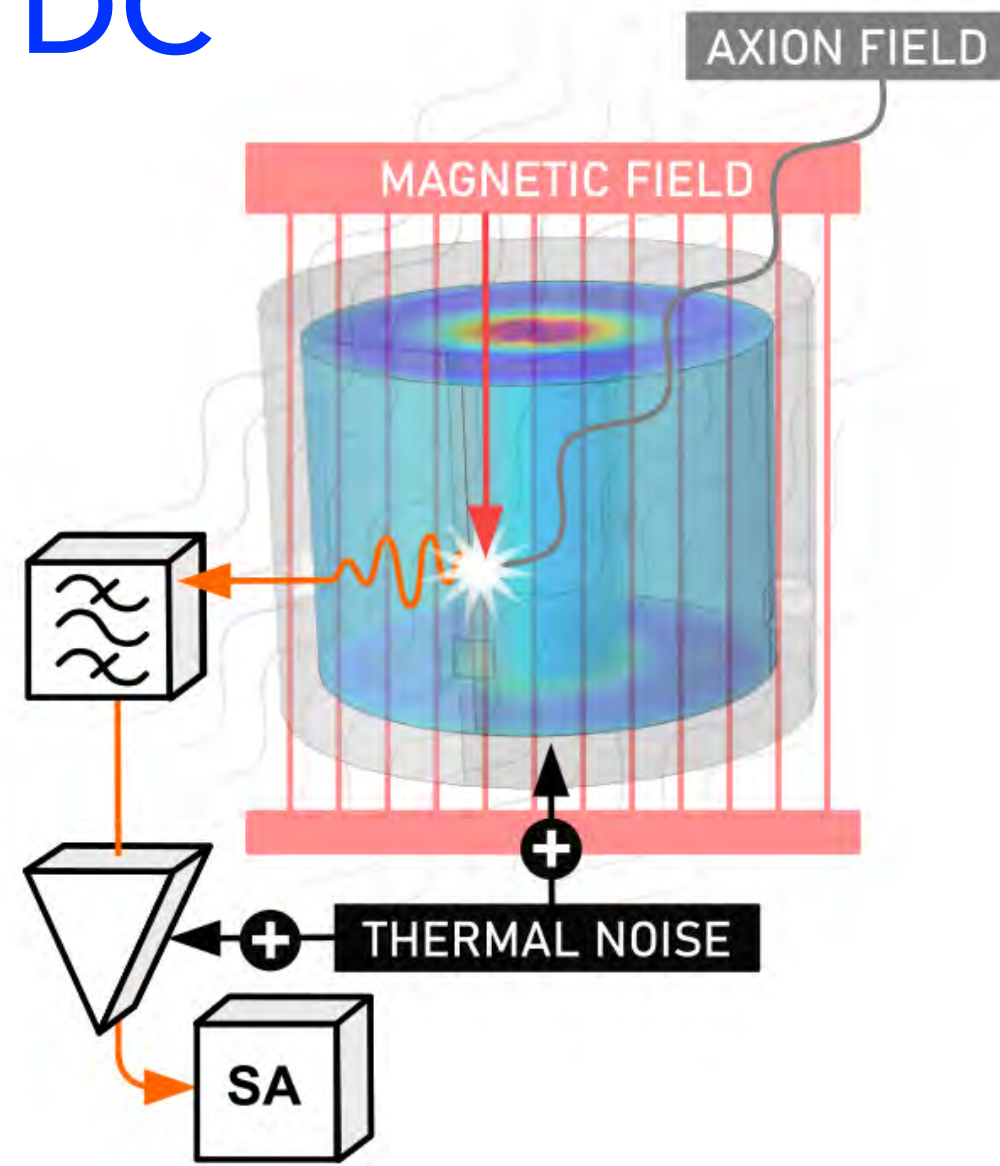
Photon 0, Back ground DC B field of surrounding magnet



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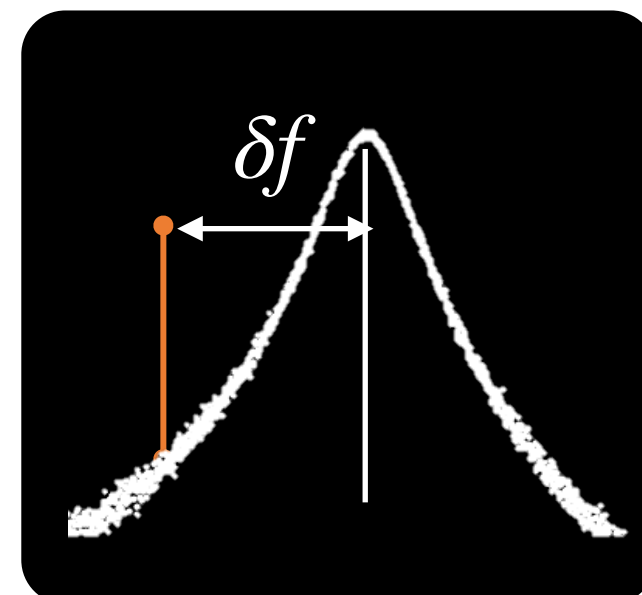


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eg.

- ADMX
- ORGAN (UWA)
- CAPP
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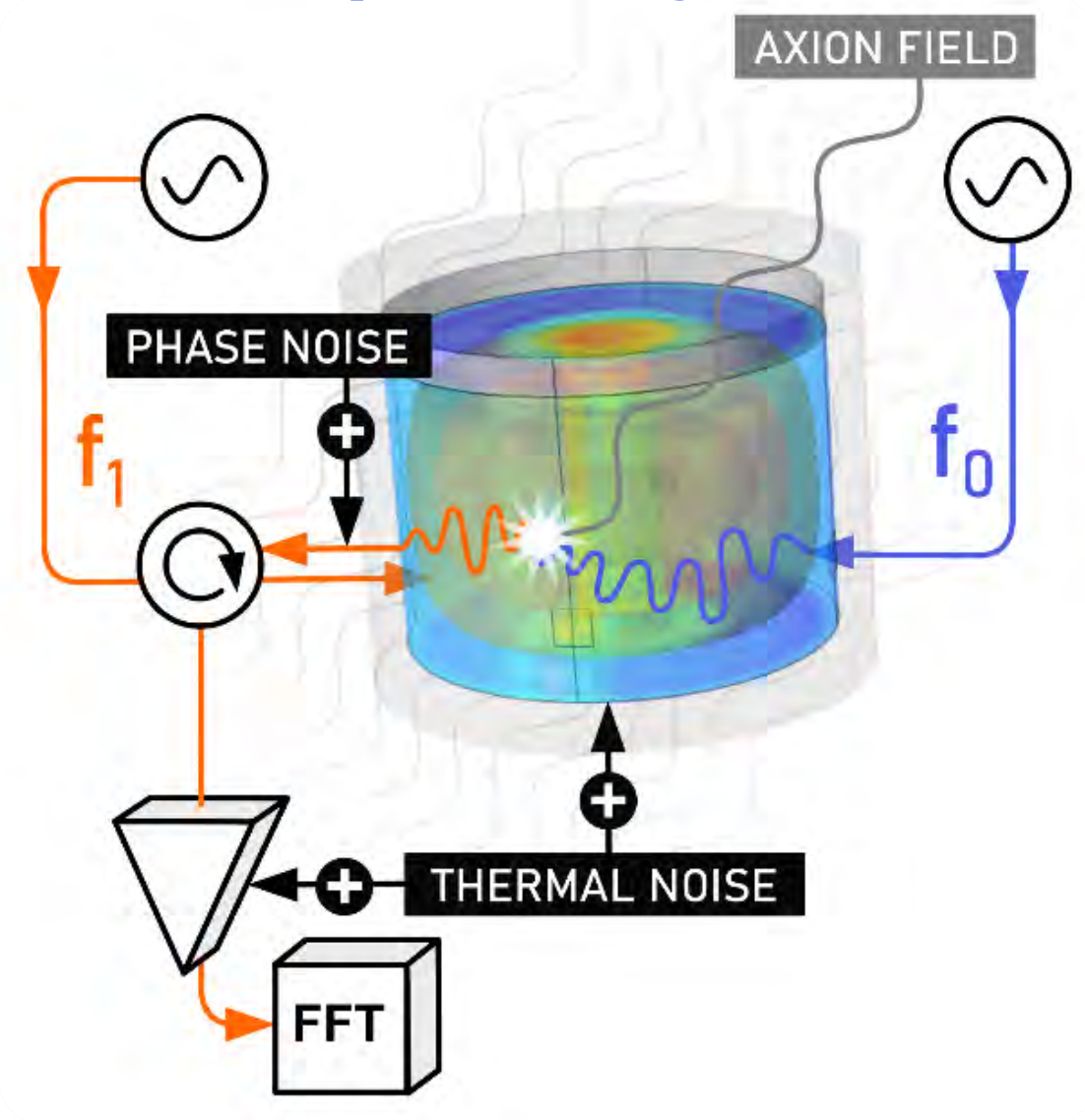
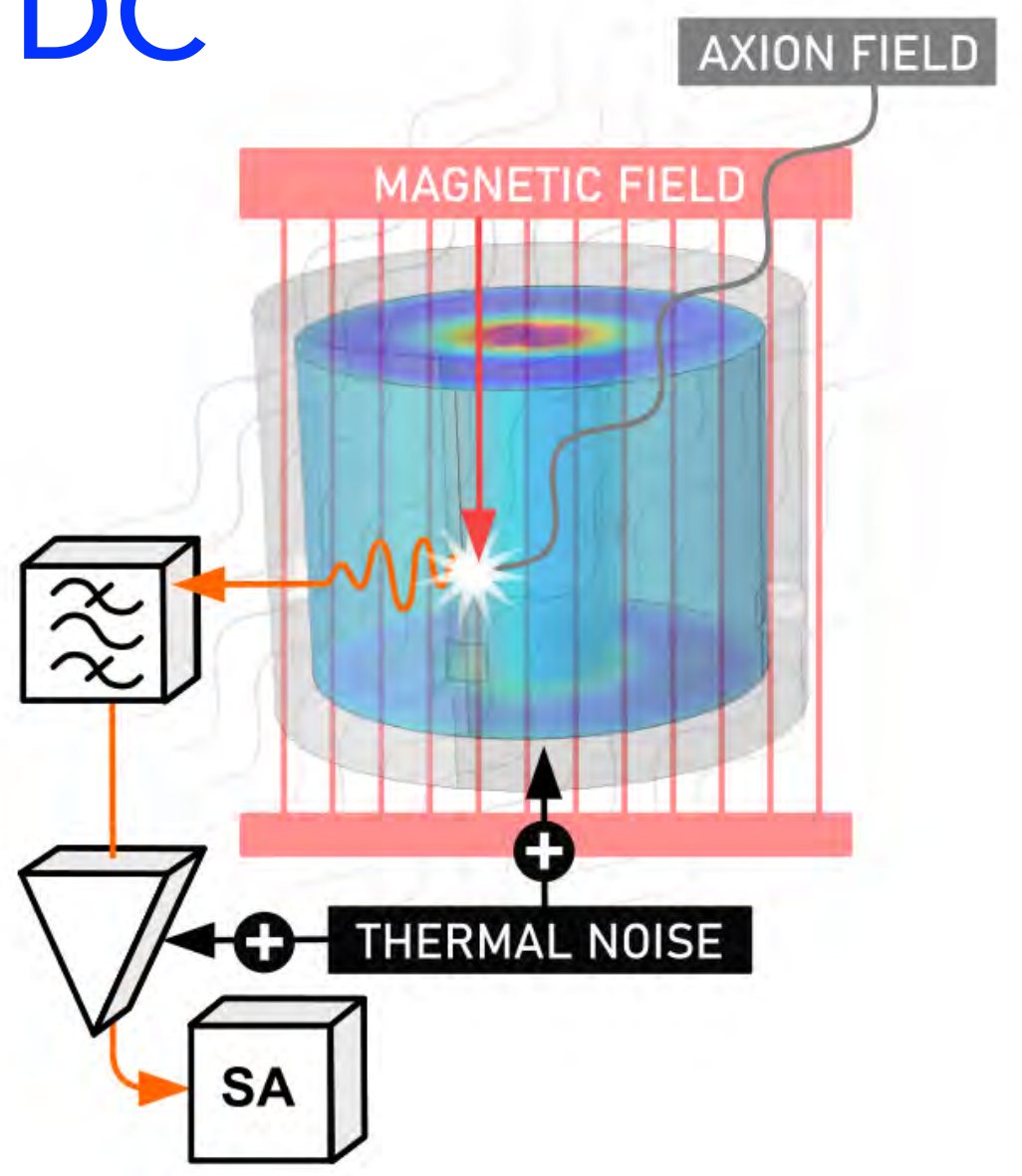


Resonant Axion Haloscopes @ UWA

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AC Frequency

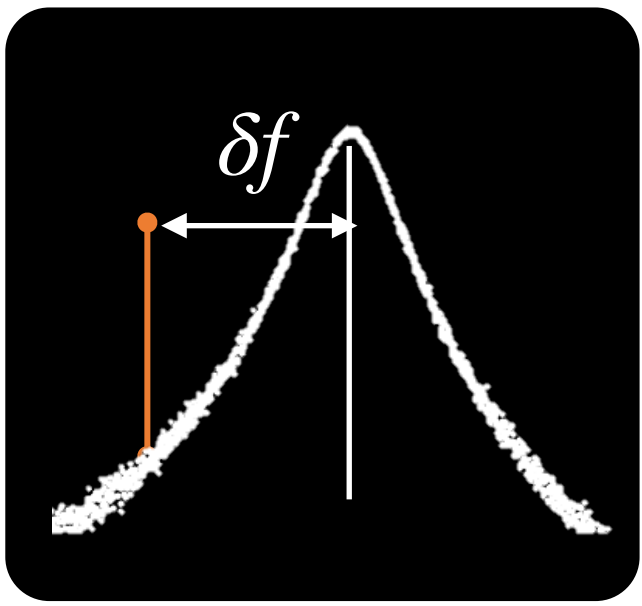
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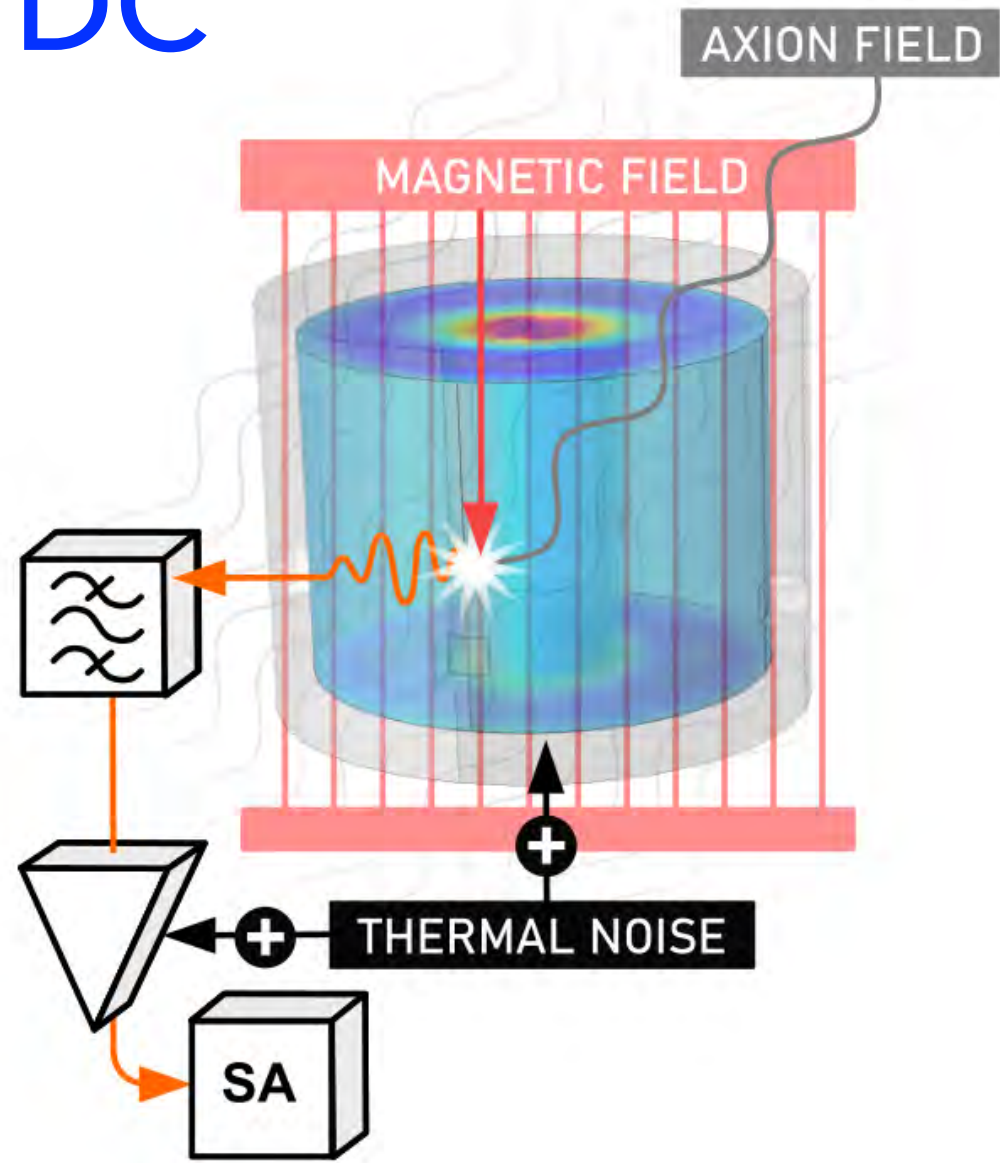
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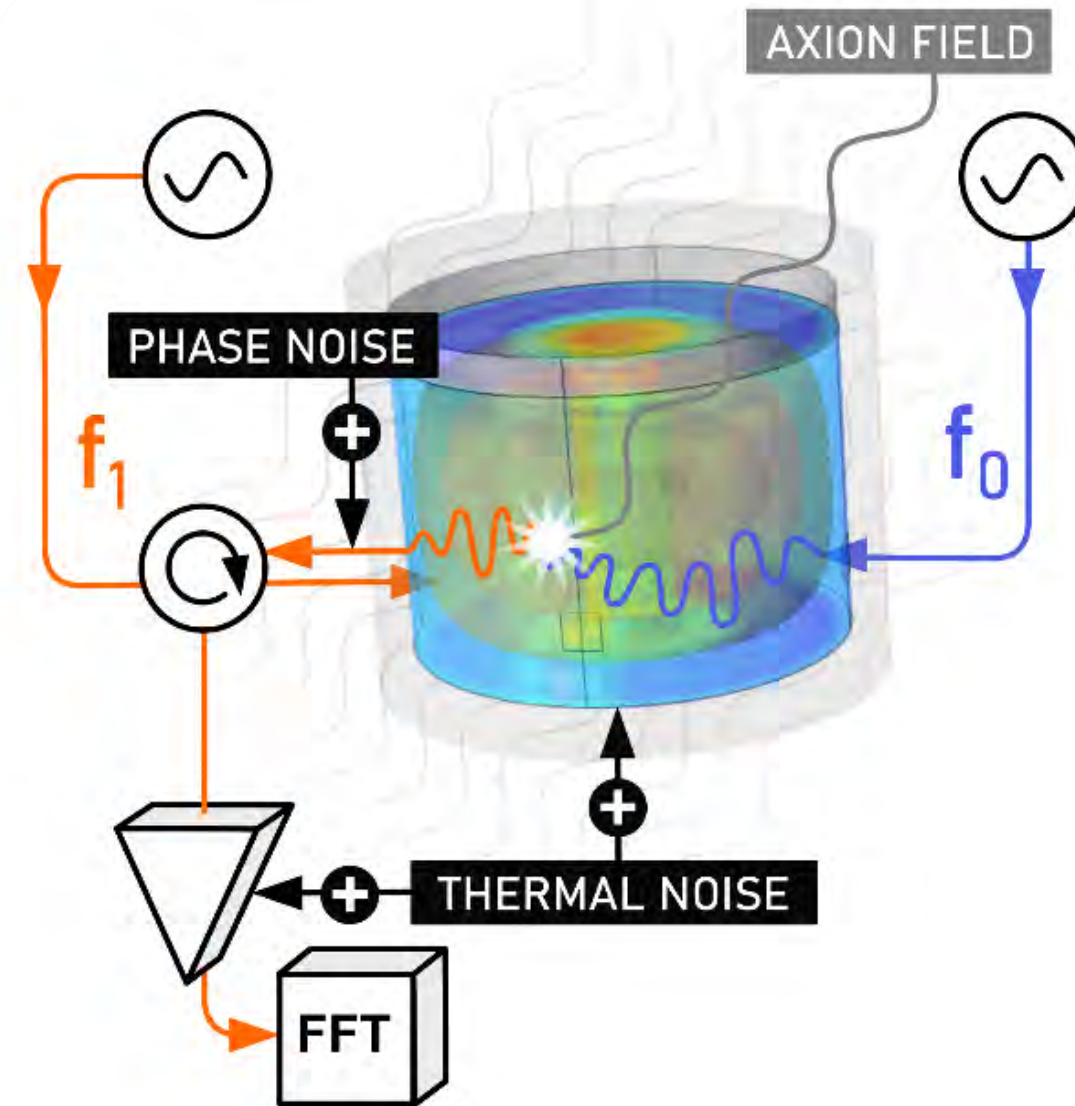
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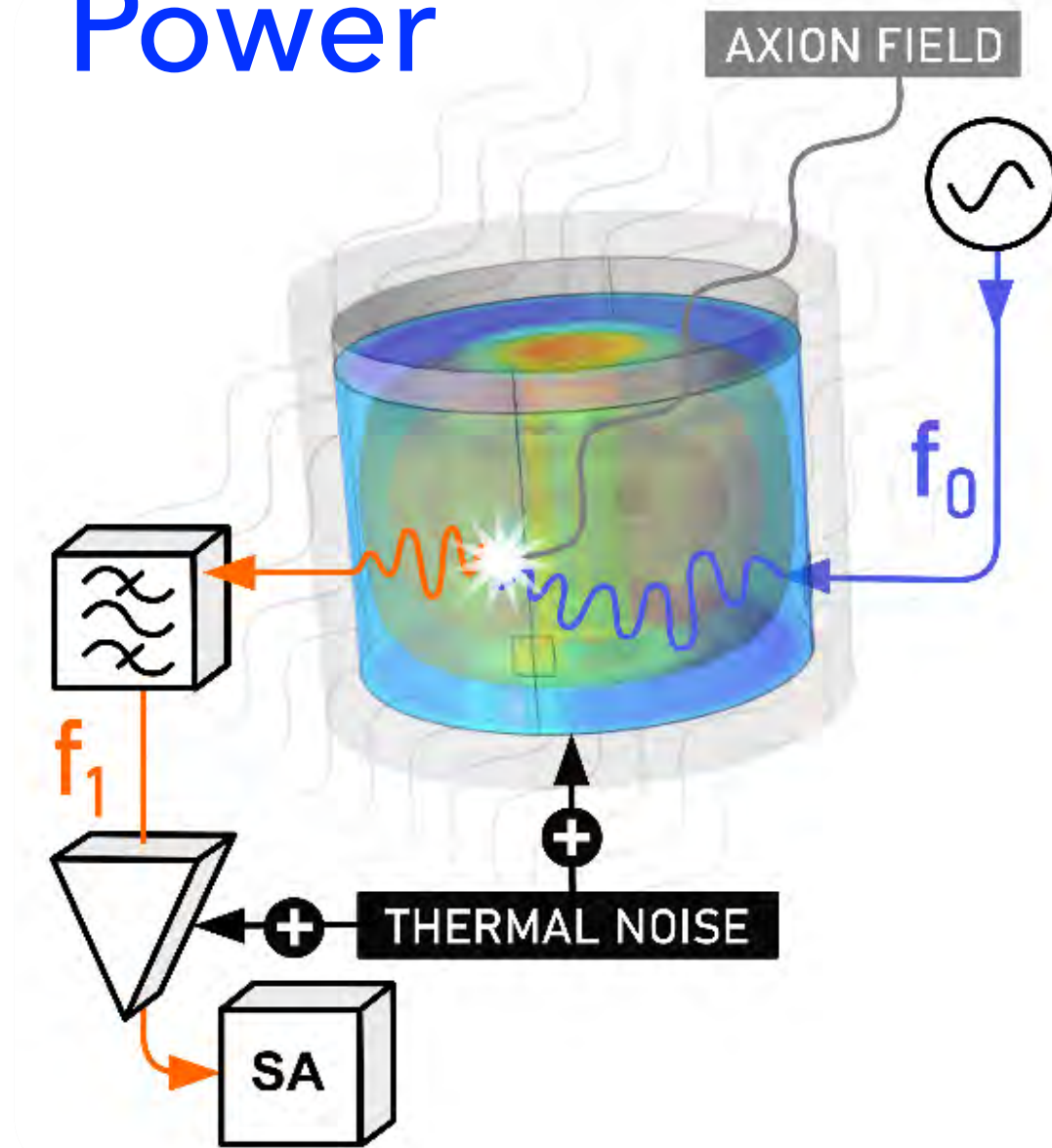
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AC Frequency



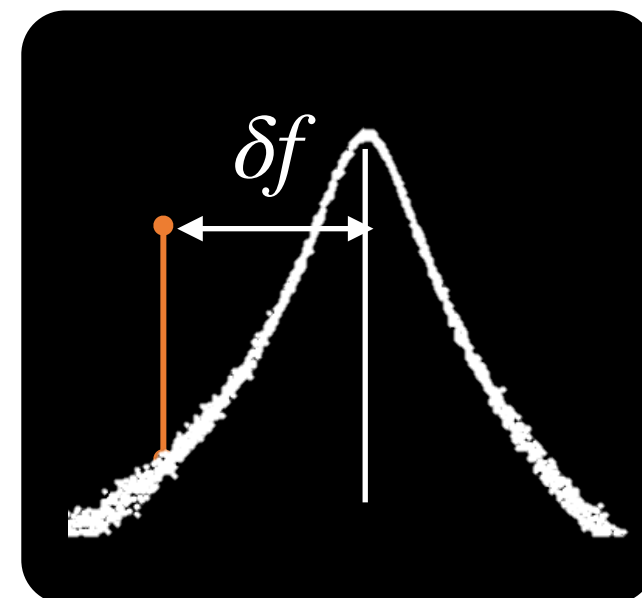
AC Power



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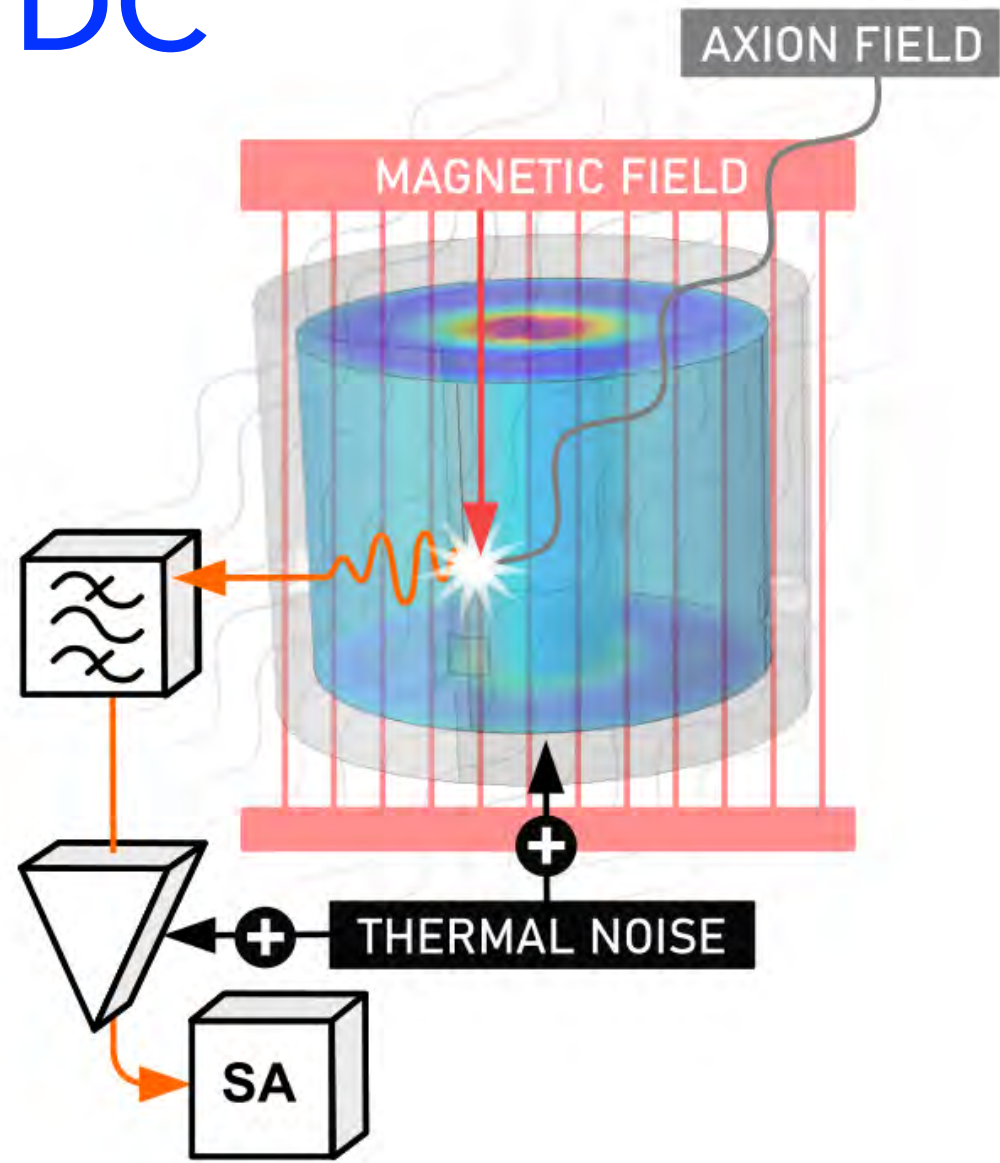
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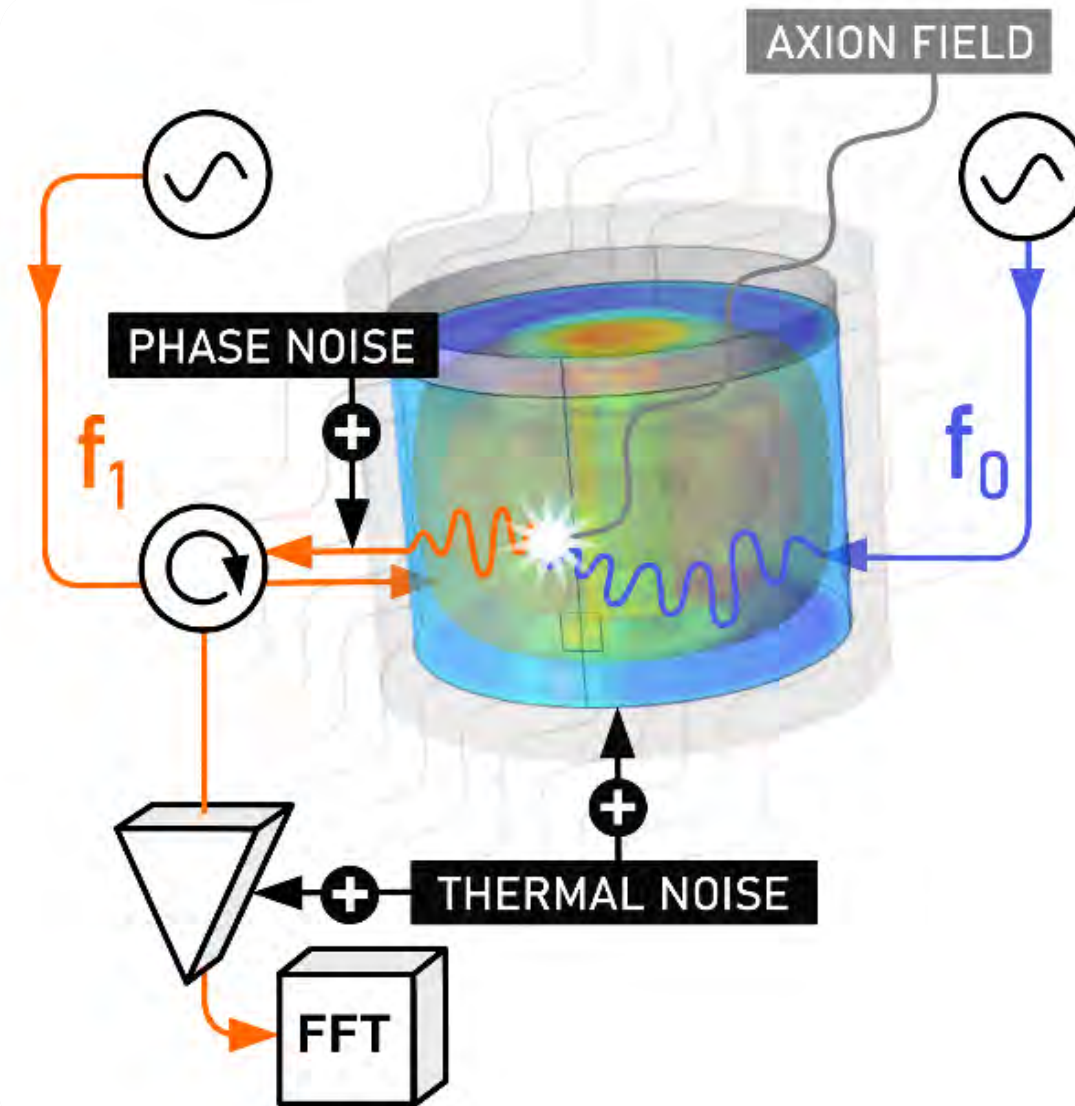
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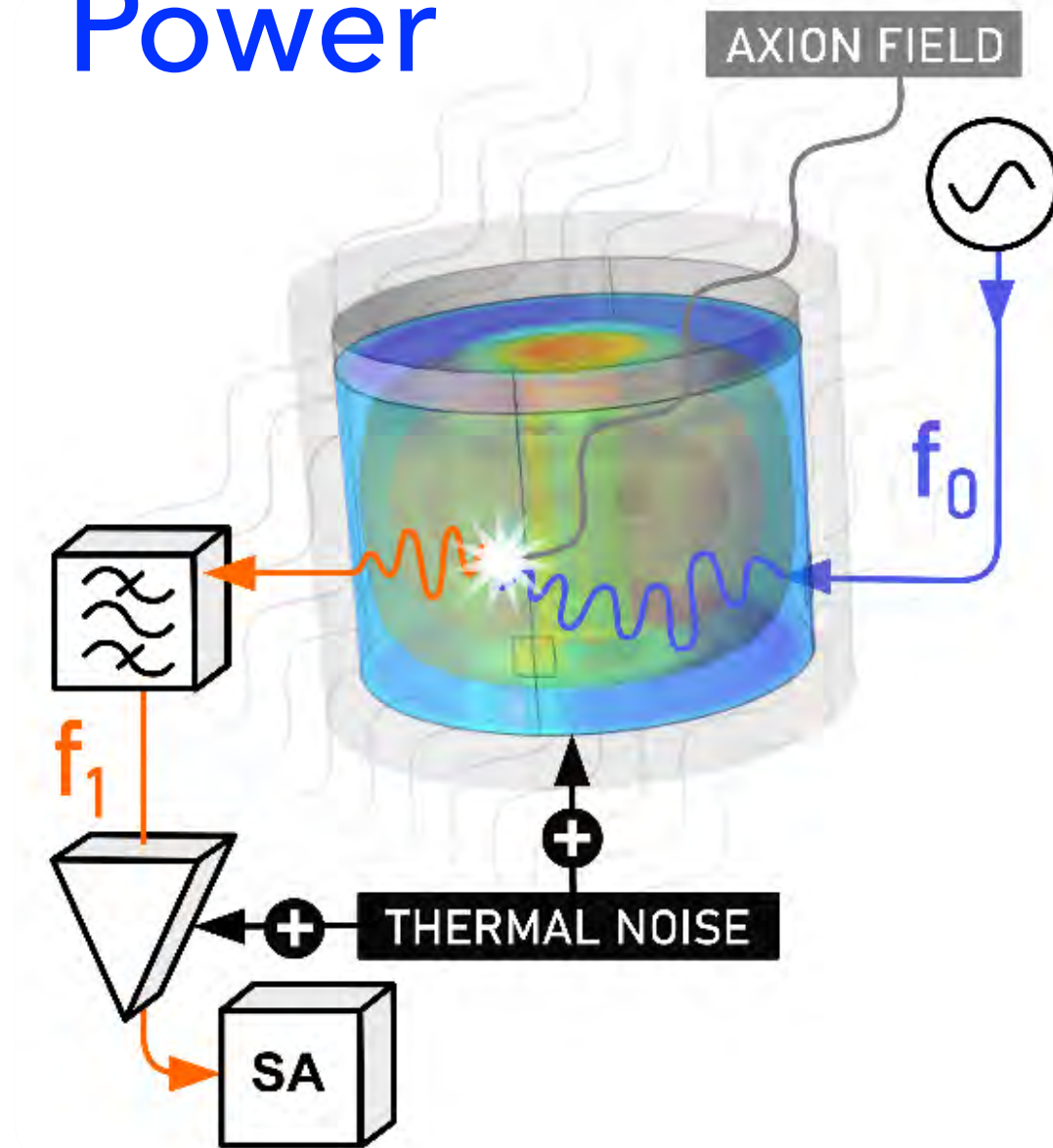
DC



AC Frequency



AC Power

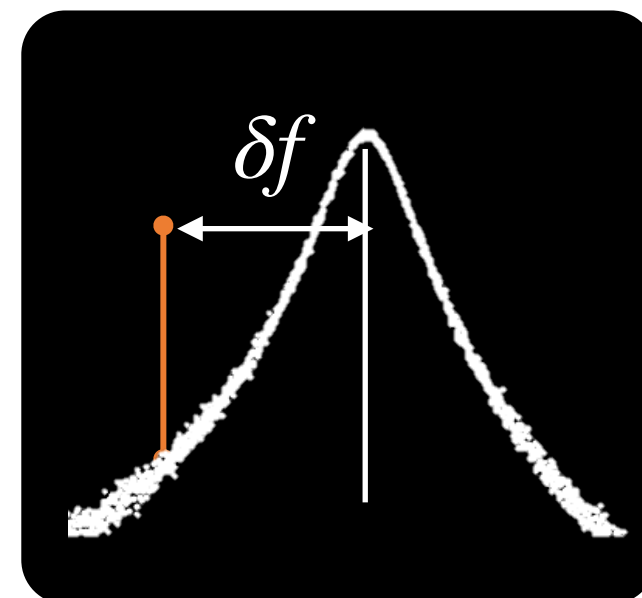


• Use a mode 0 as the background “magnetic field” AC source

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Photon 0, Back ground DC B field of surrounding magnet

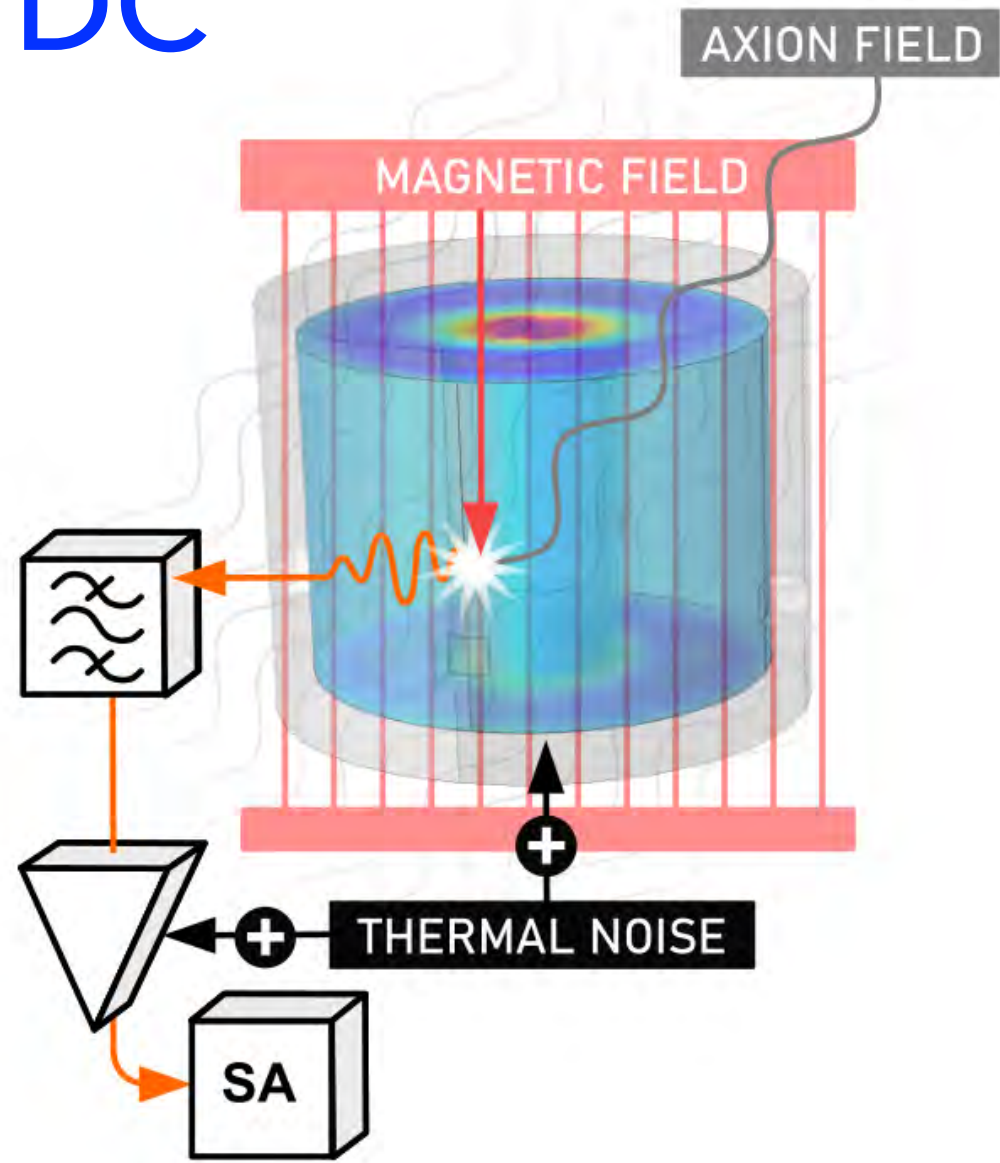
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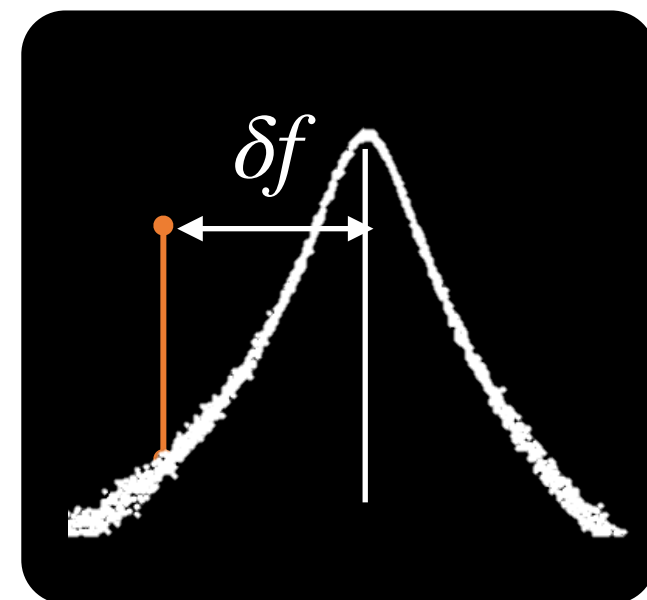
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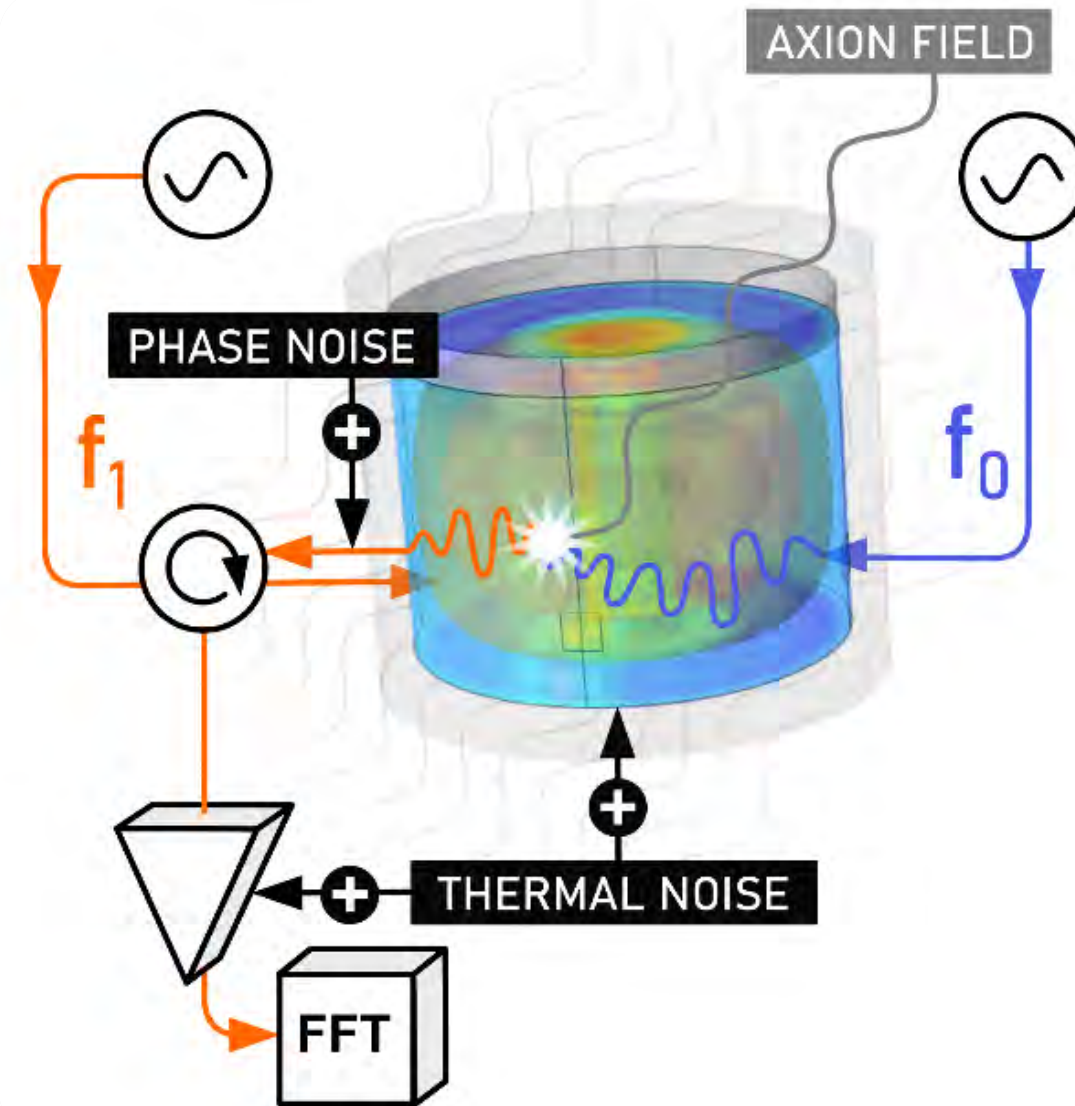
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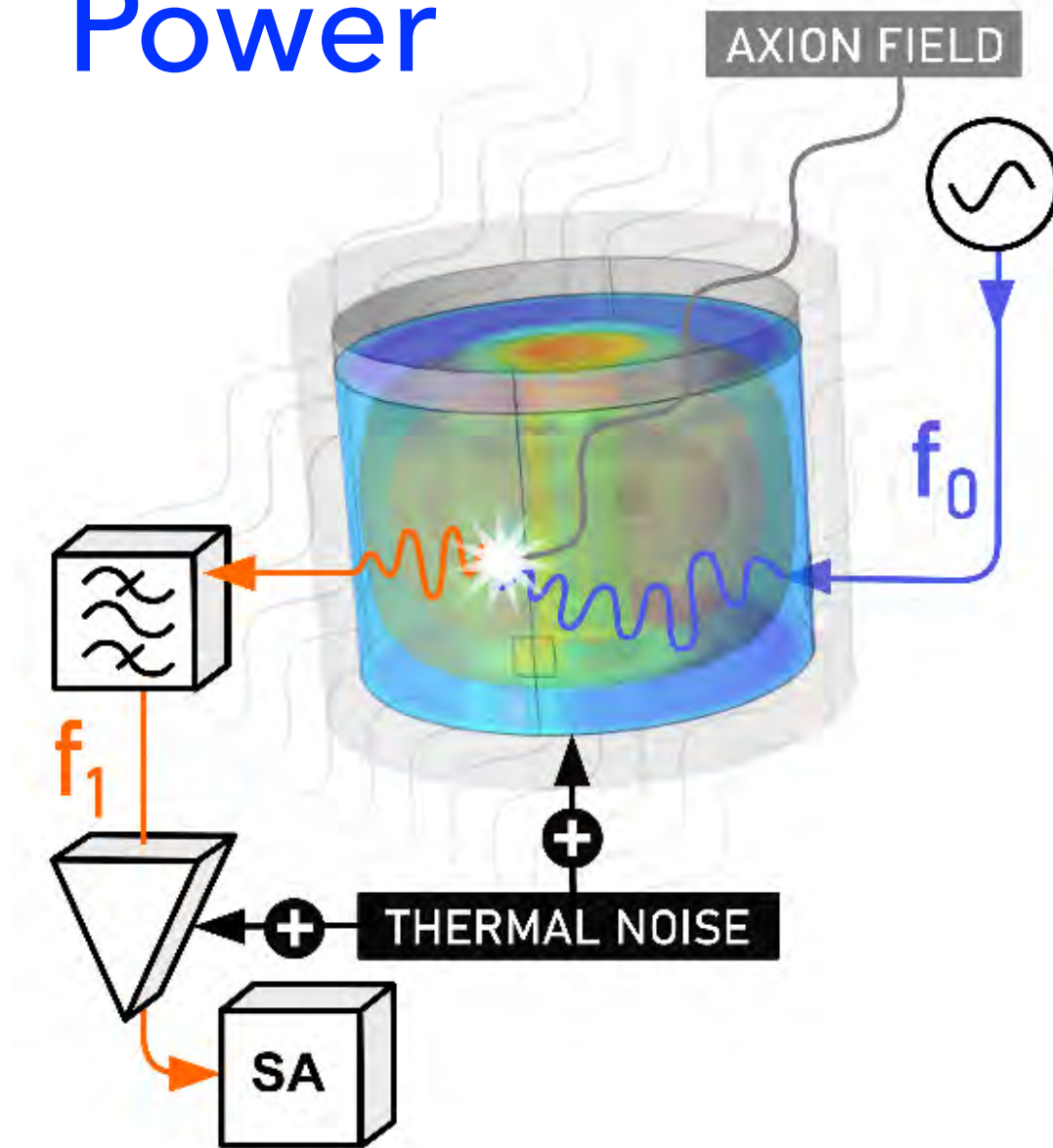


AC Frequency



- Use a mode 0 as the background “magnetic field” AC source
- Two modes in one cylindrical cavity

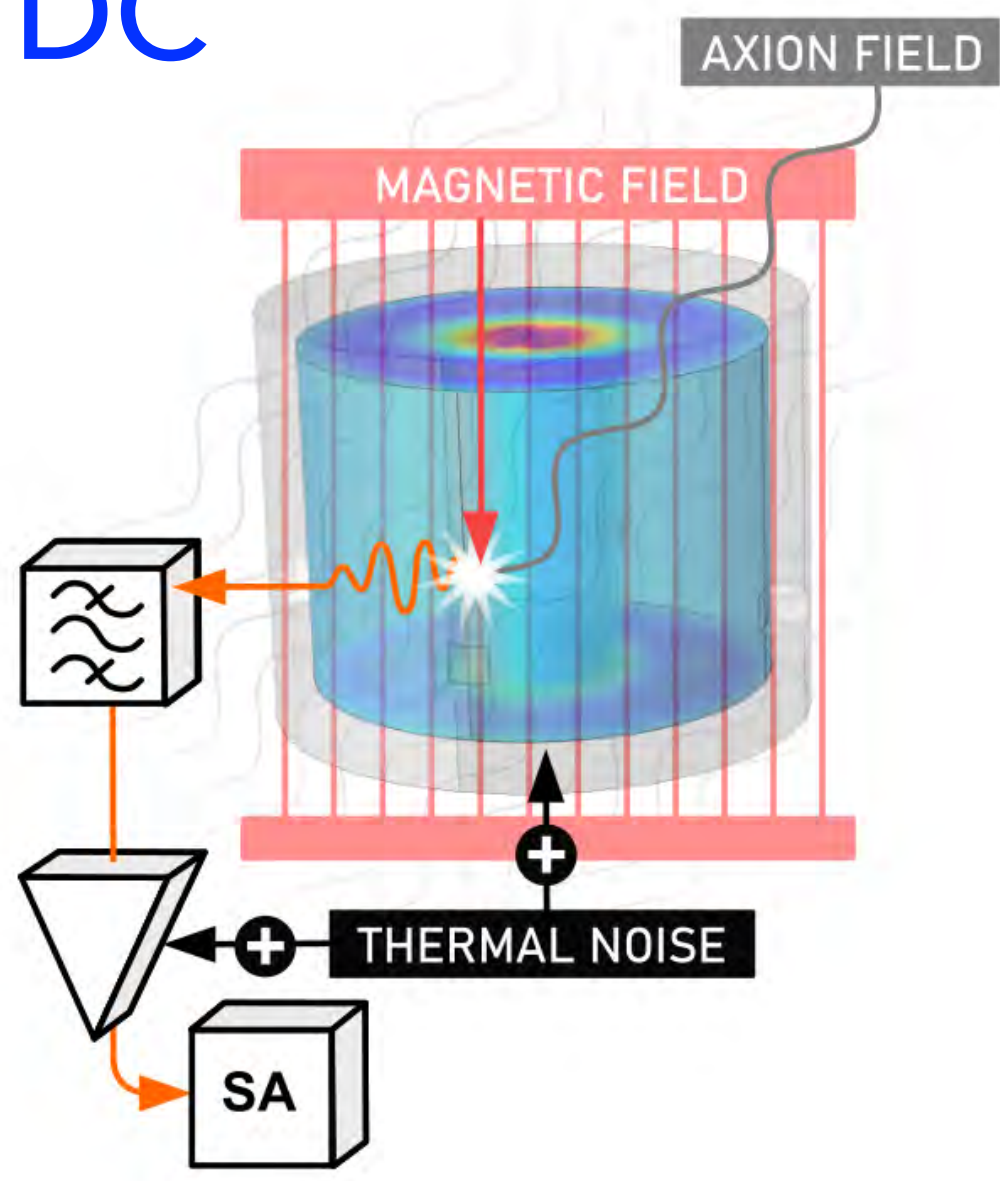
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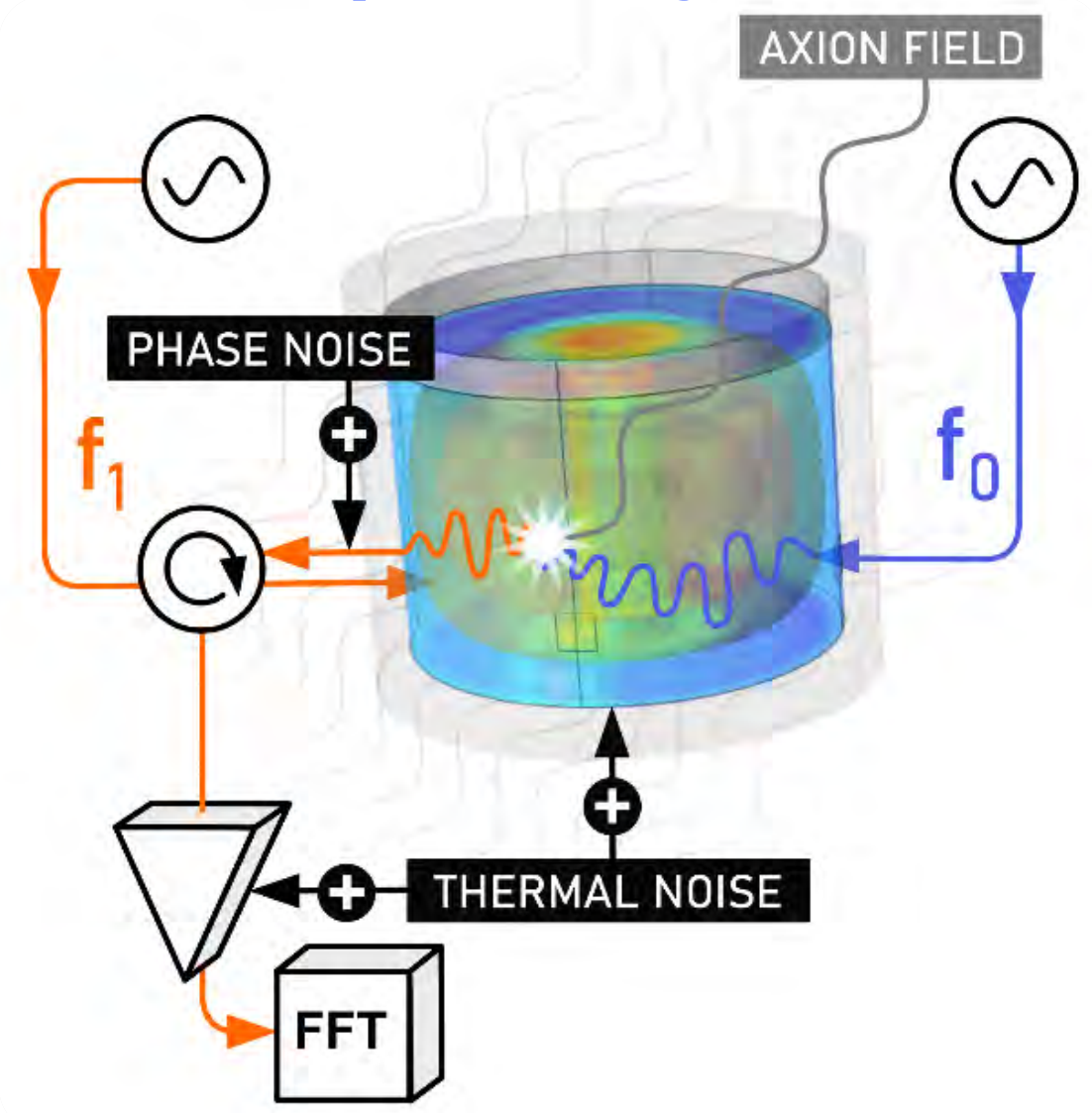
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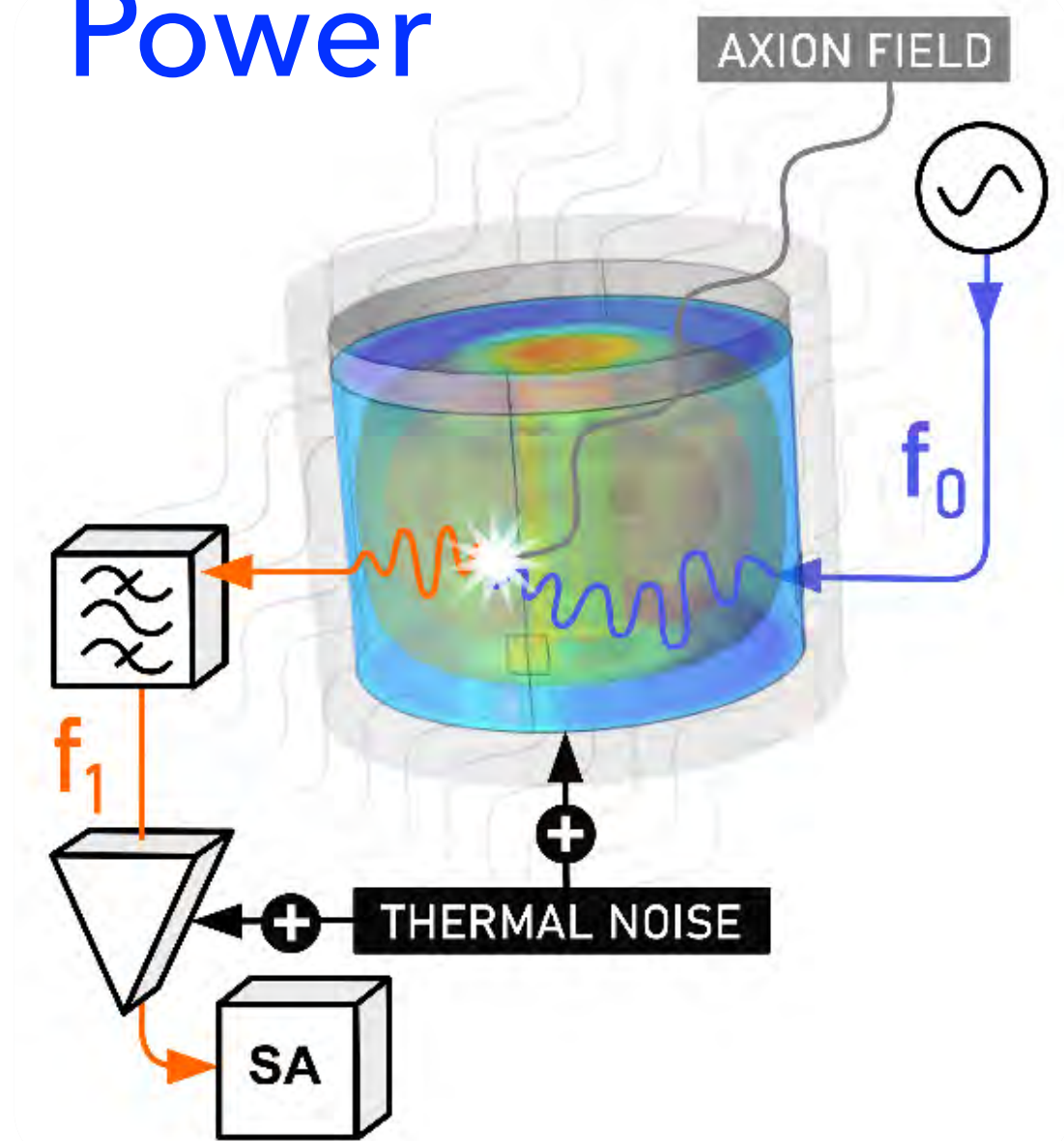
DC



AC Frequency



AC Power

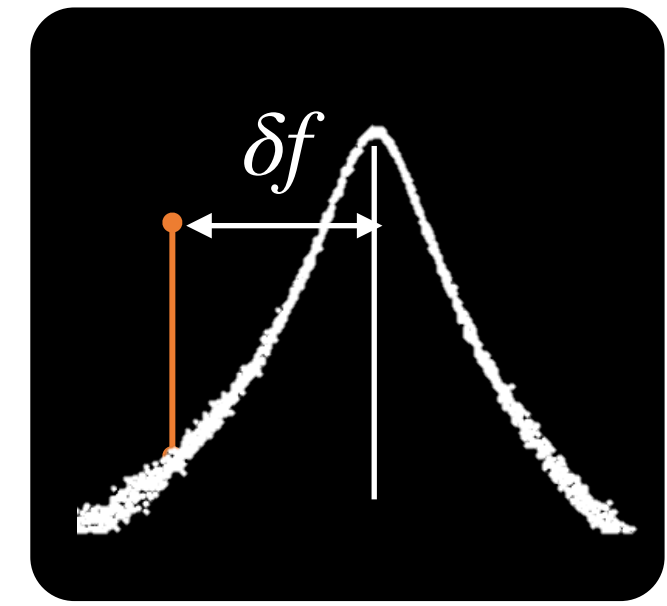


Photon 1: E field of cavity's resonant transverse magnetic mode, $m_a = f_1 + \delta f$

Photon 0, Back ground DC B field of surrounding magnet

- Use a mode 0 as the background "magnetic field" AC source
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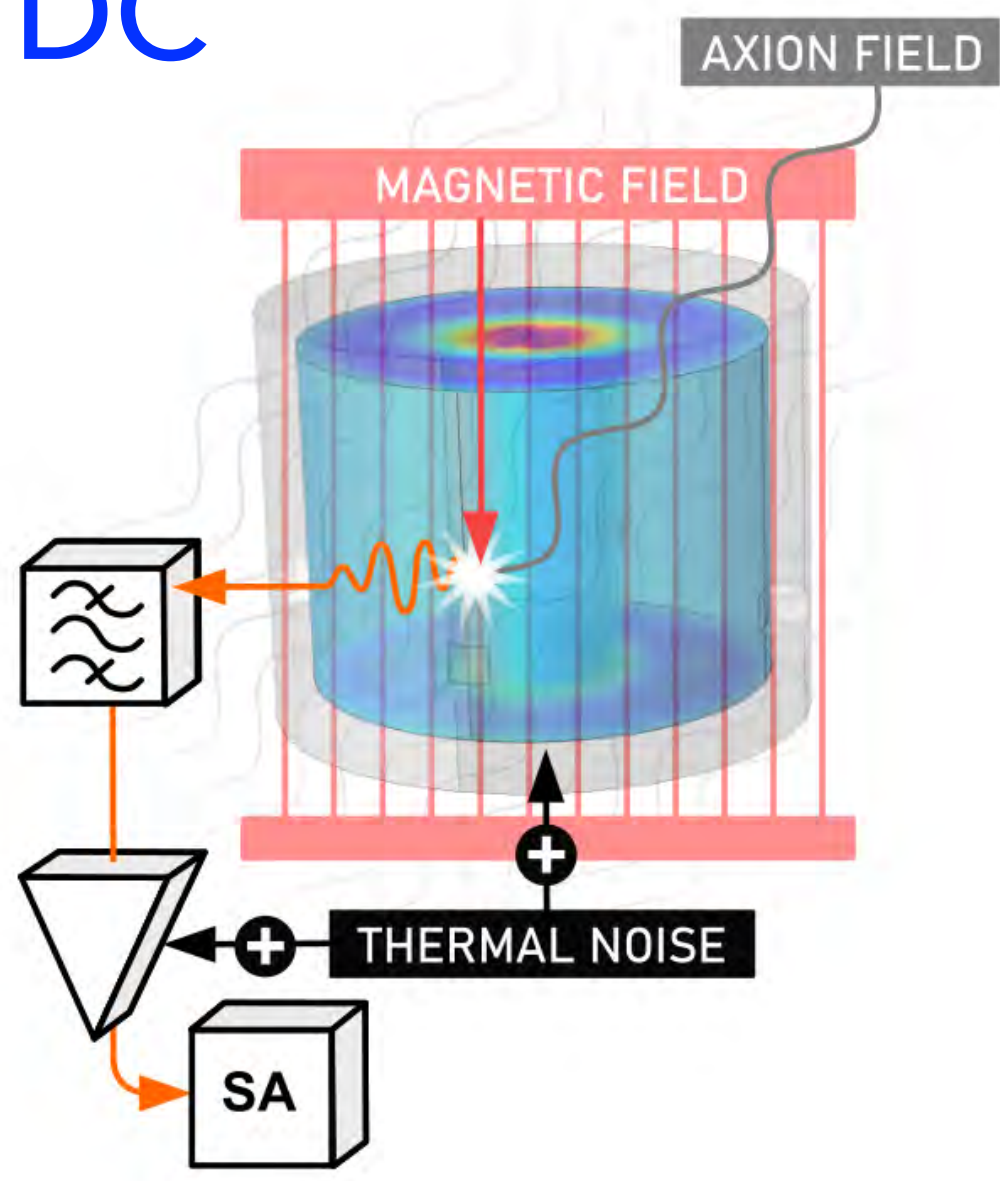
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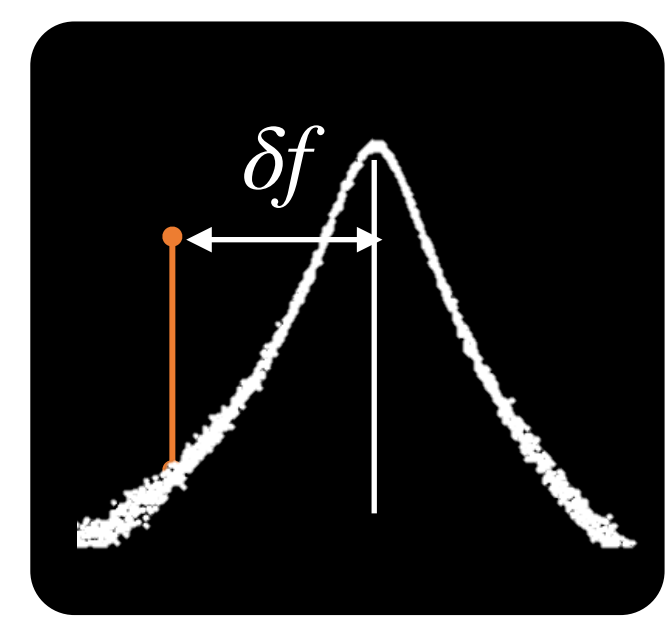
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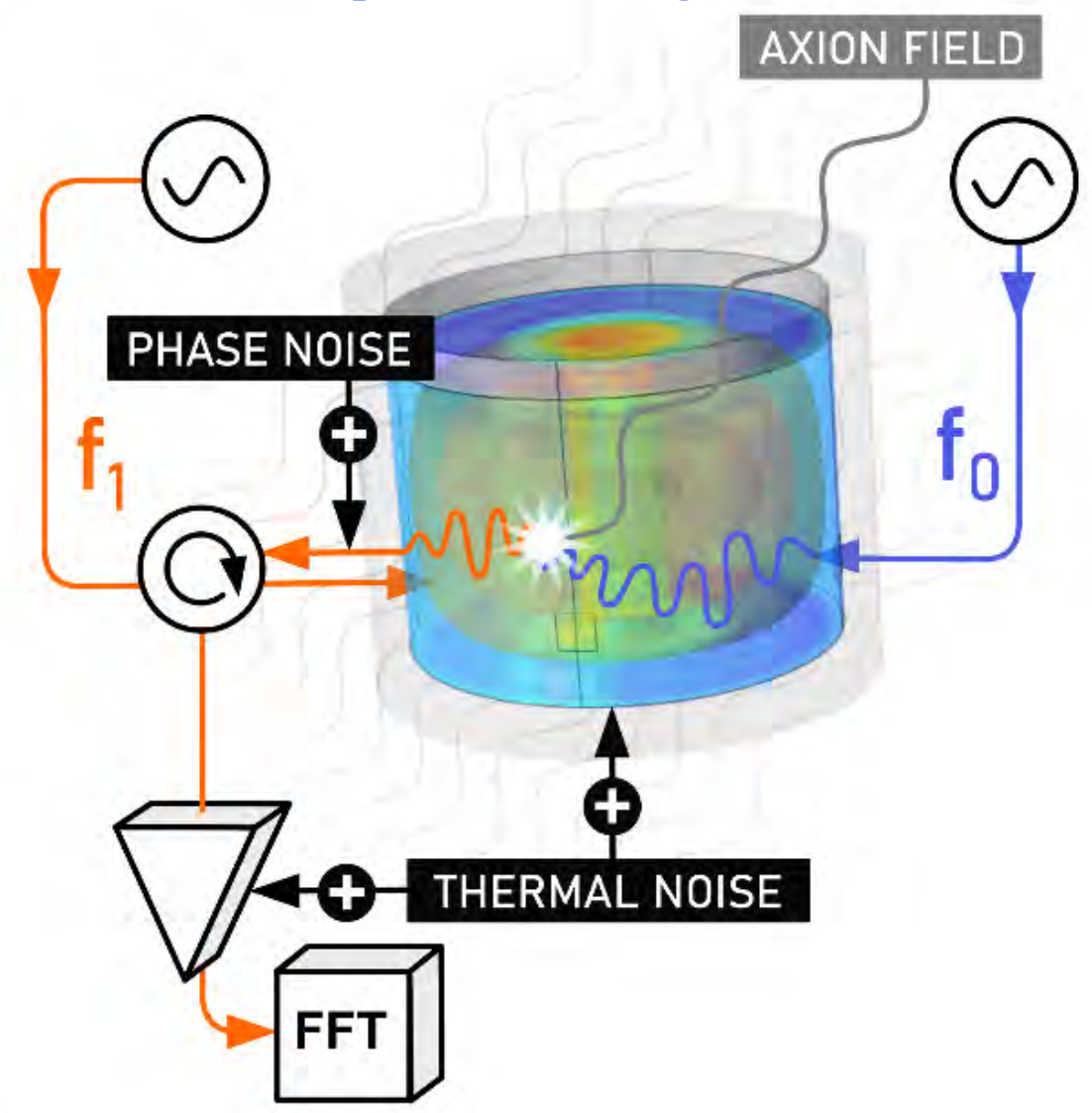
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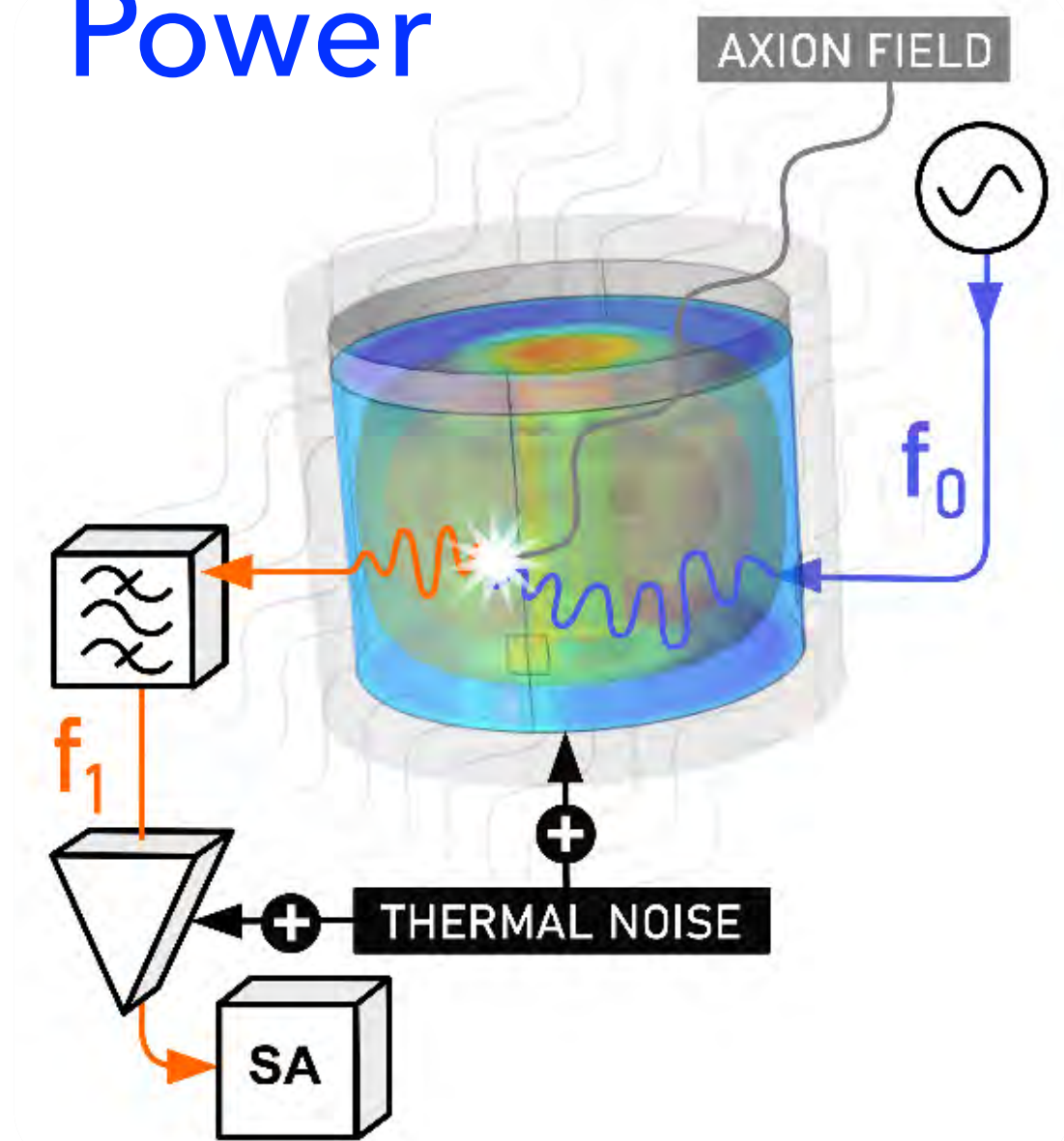


- Use a mode 0 as the background "magnetic field" AC source
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Photon 1: Transverse Magnetic Mode

(Longitudinal Electric)

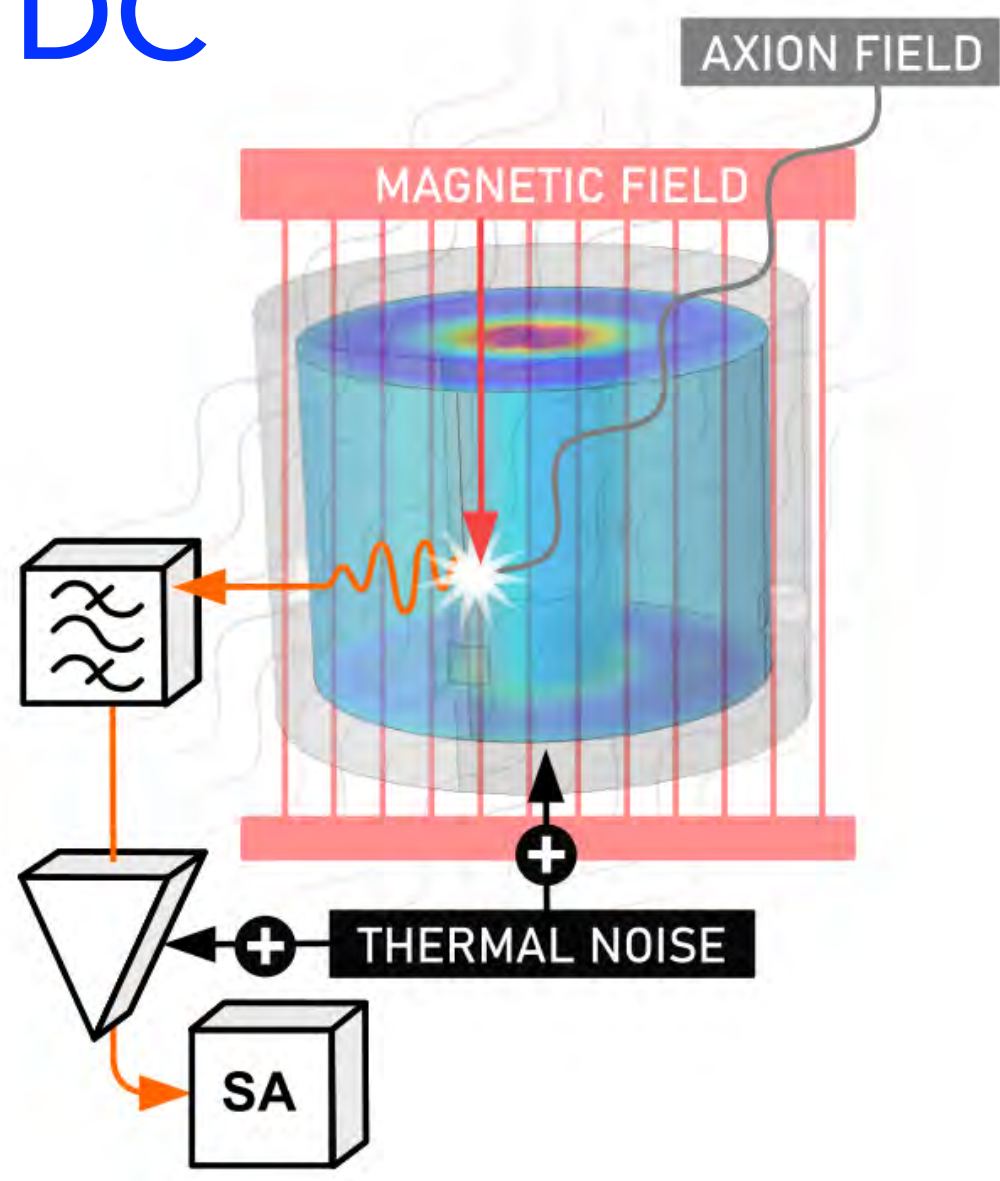
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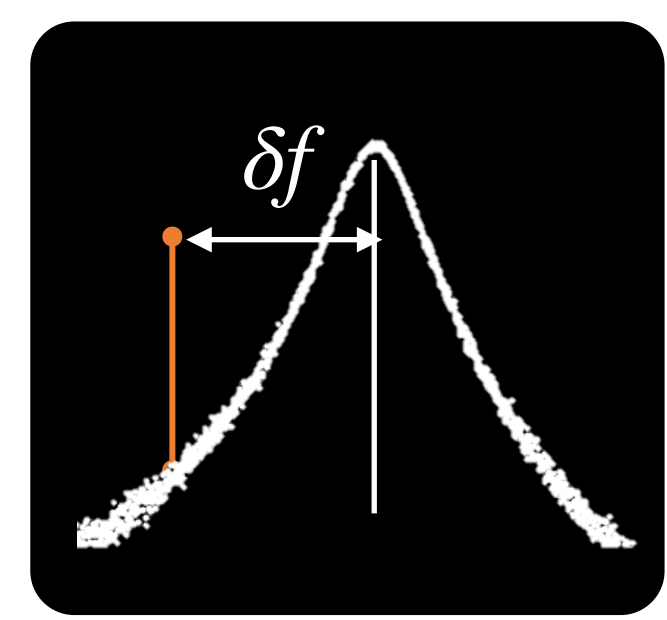
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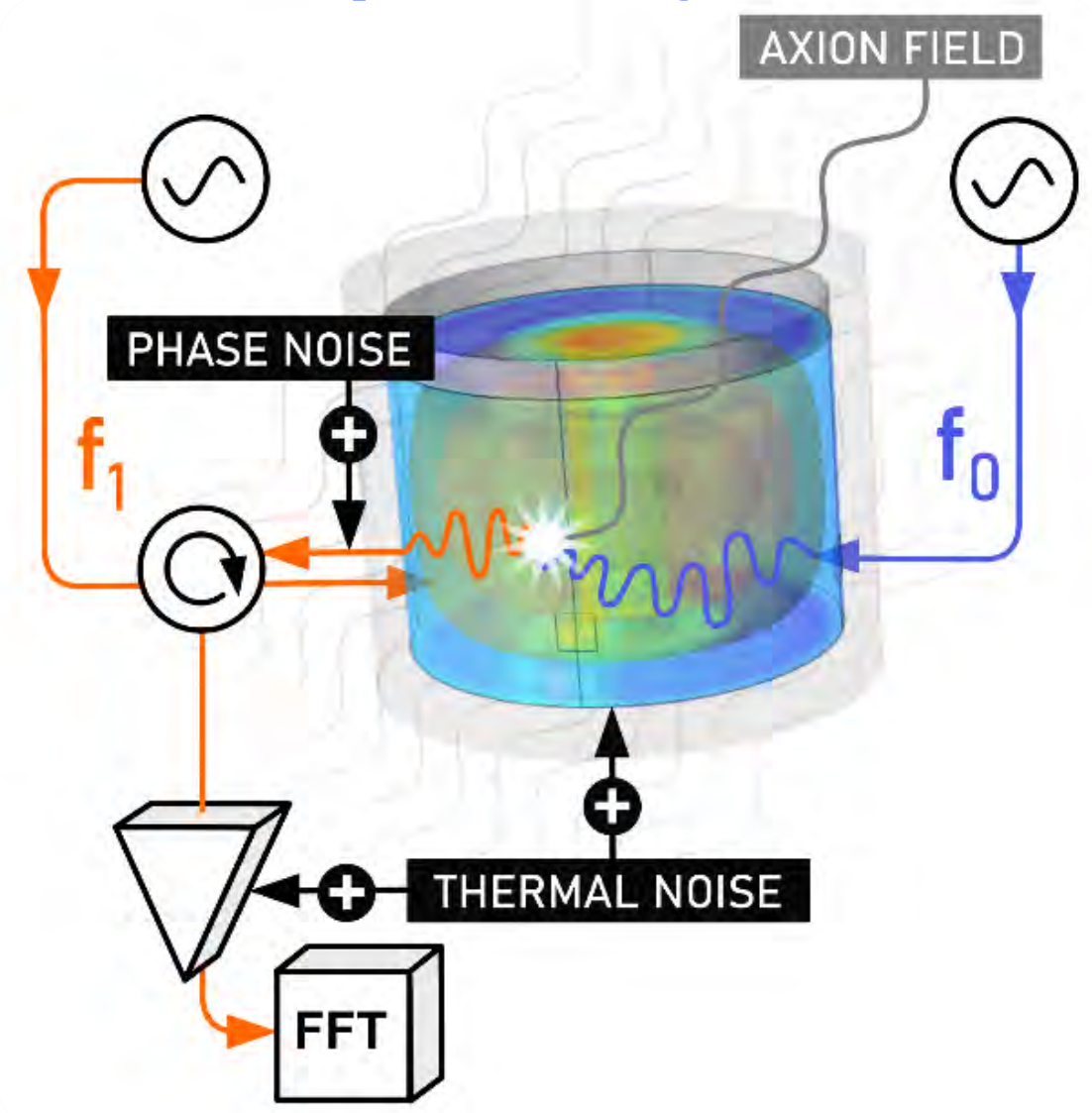
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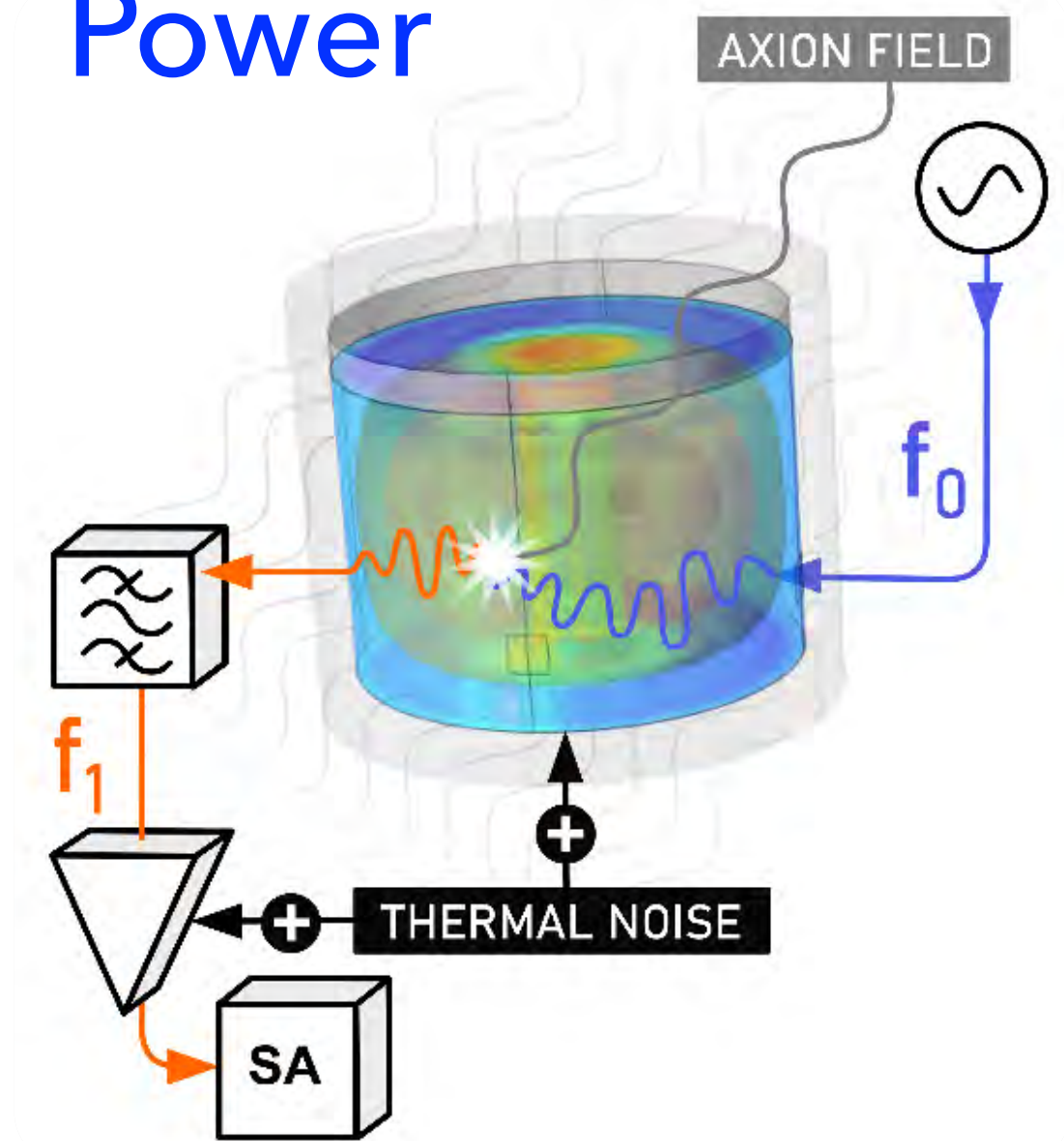
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AC Power

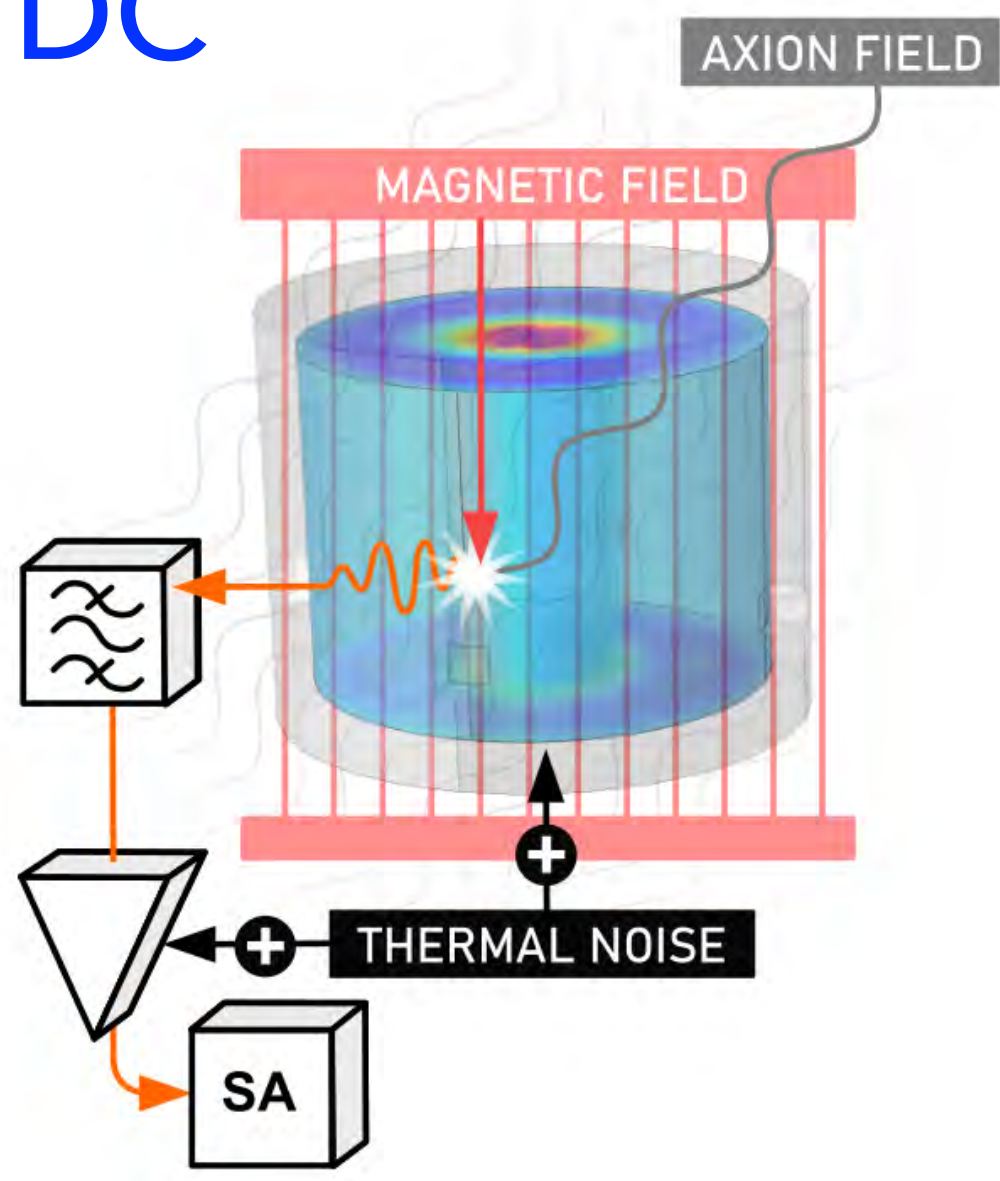


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Resonant Axion Haloscopes @ UWA

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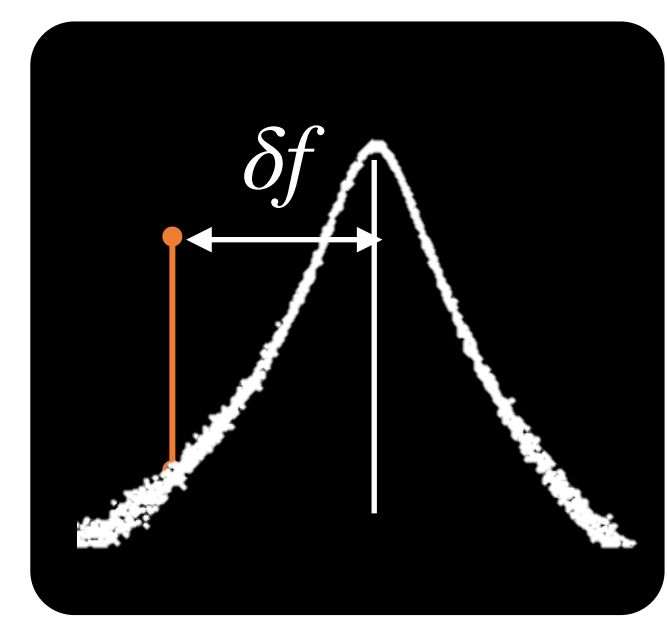
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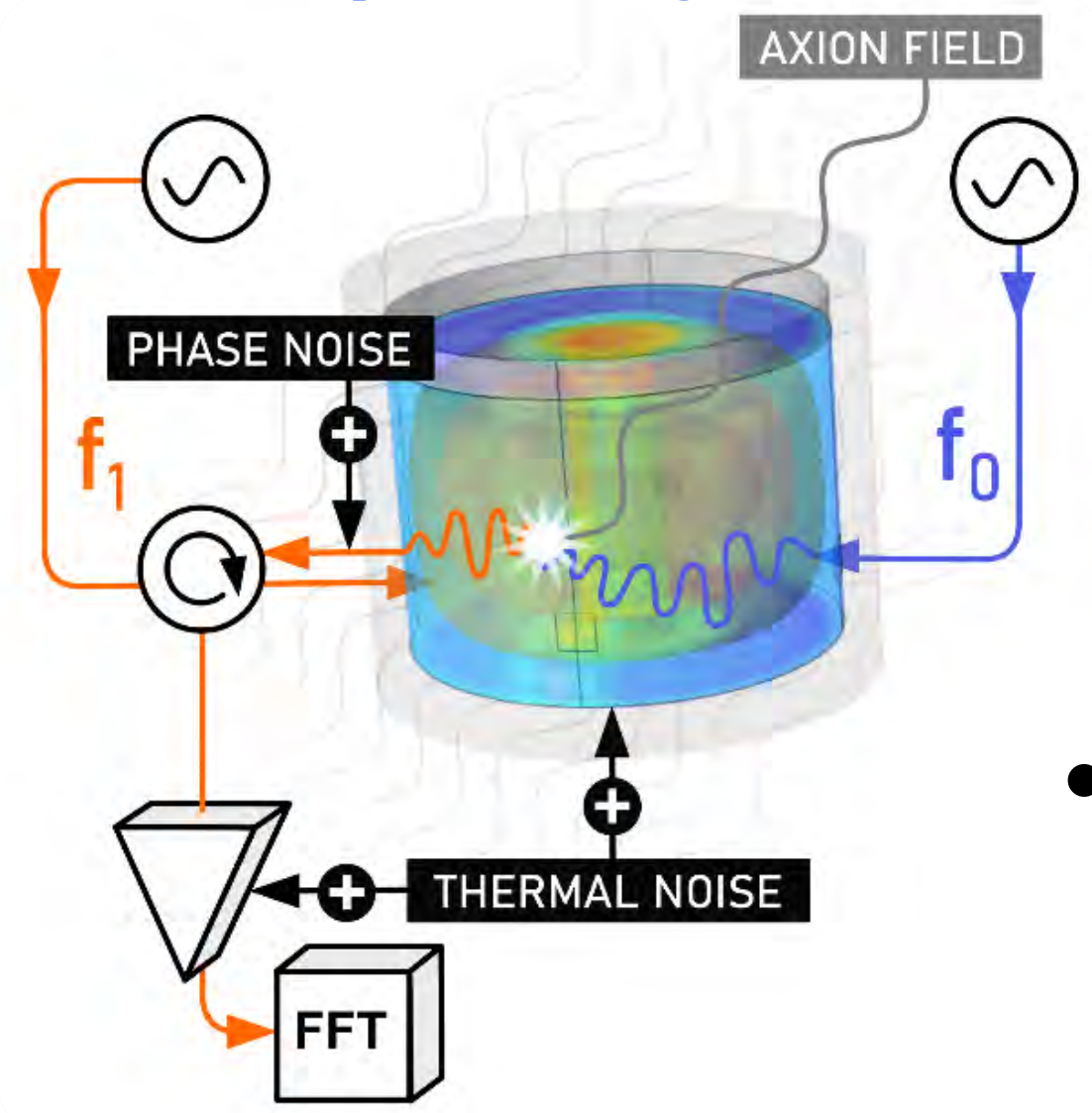
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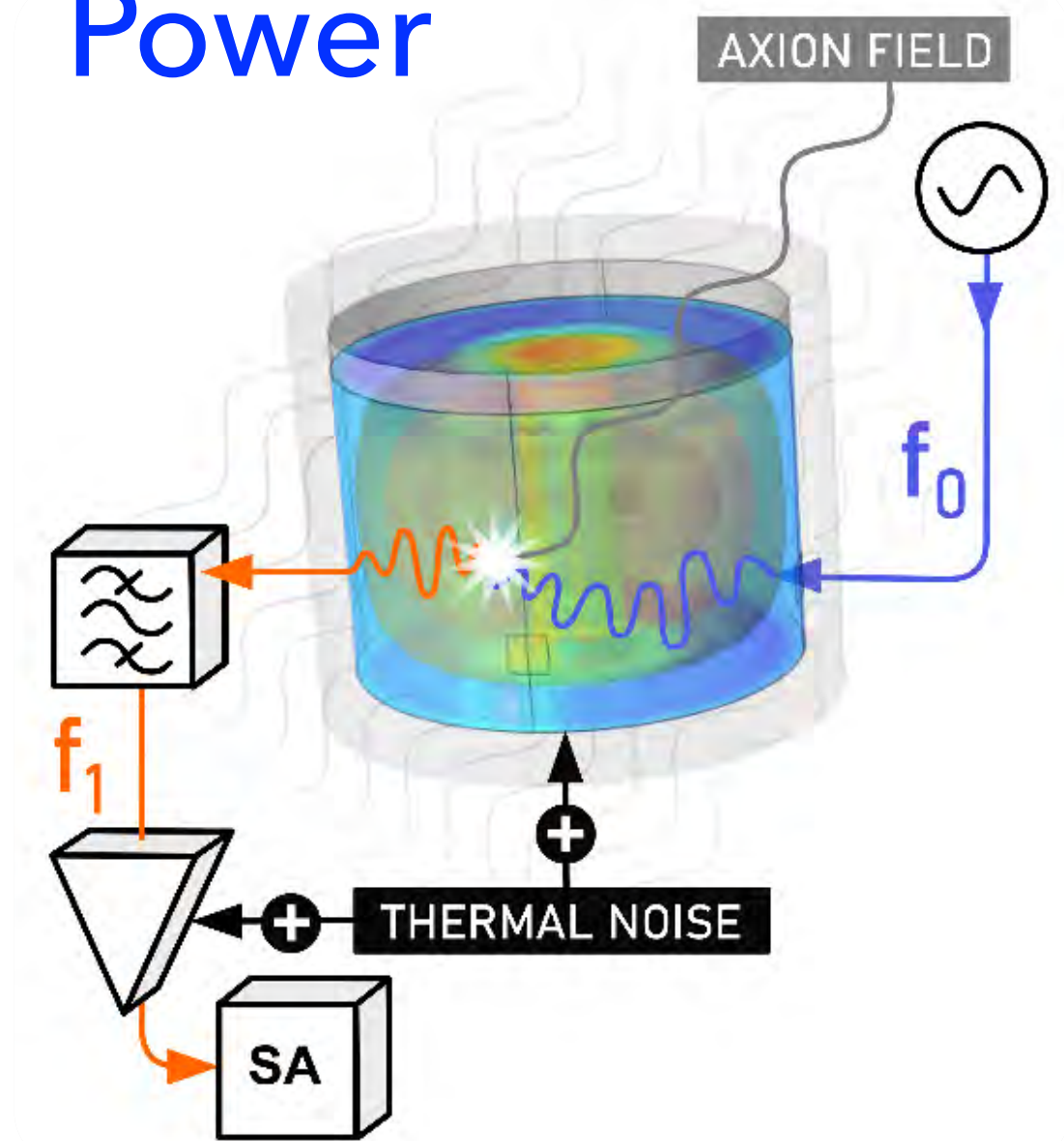
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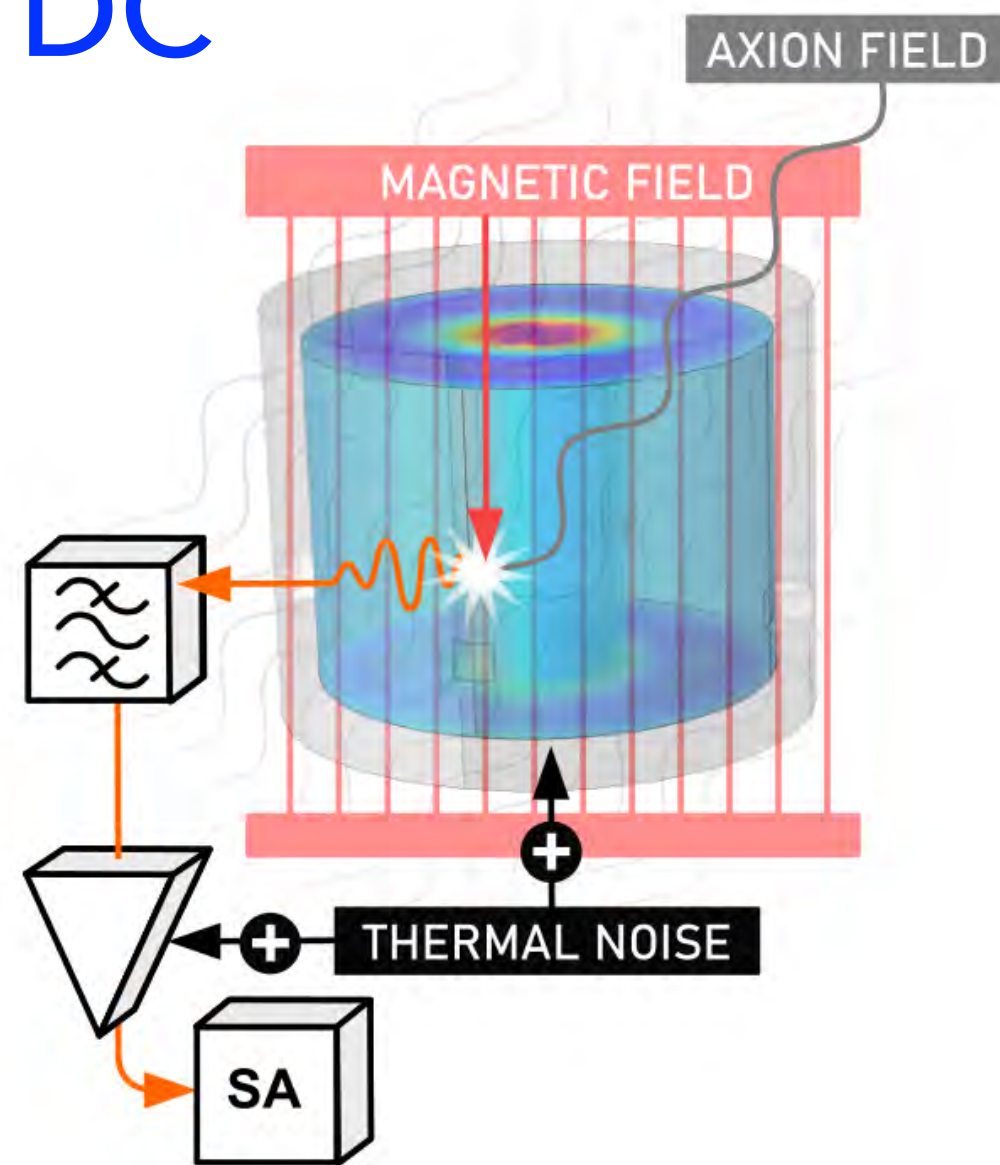
Photon 0: Transverse Electric Mode
(Longitudinal Magnetic)

• UPLOAD

Resonant Axion Haloscopes @ UWA

$$\mathcal{H}_{int} = \epsilon_0 c g_{a\gamma\gamma} a \mathbf{E} \cdot \mathbf{B}$$

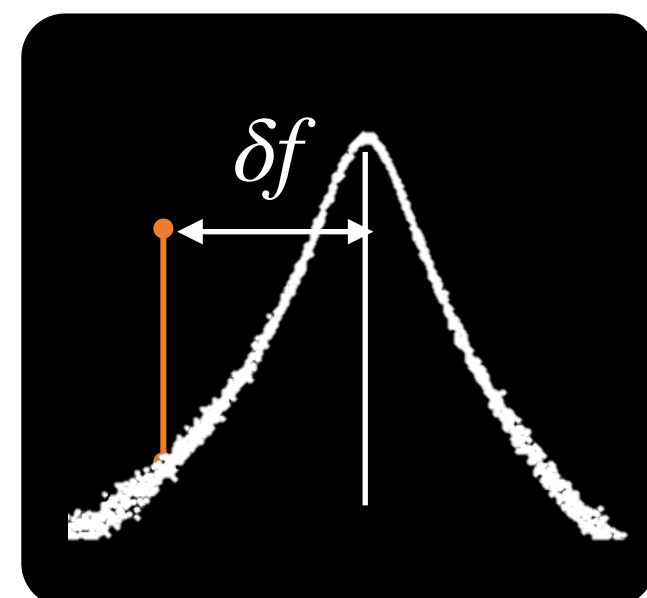
DC



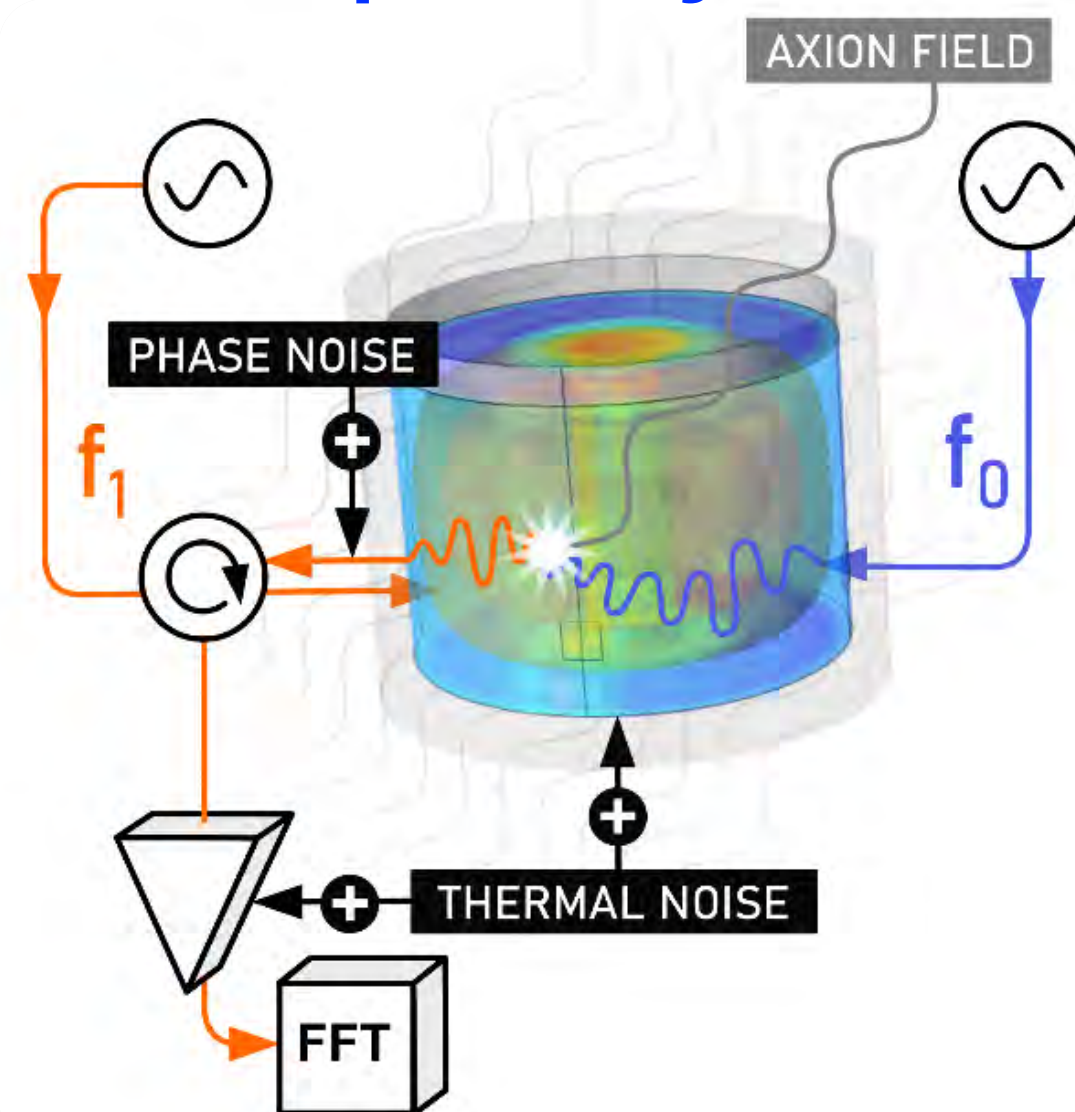
Photon 1: E field of cavity's resonant transverse magnetic mode, $m_a = f_1 + \delta f$

Photon 0, Back ground DC B field of surrounding magnet

- eg.
- ADMX
 - ORGAN (UWA)
 - CAPP
 - HAYSTAC



AC Frequency

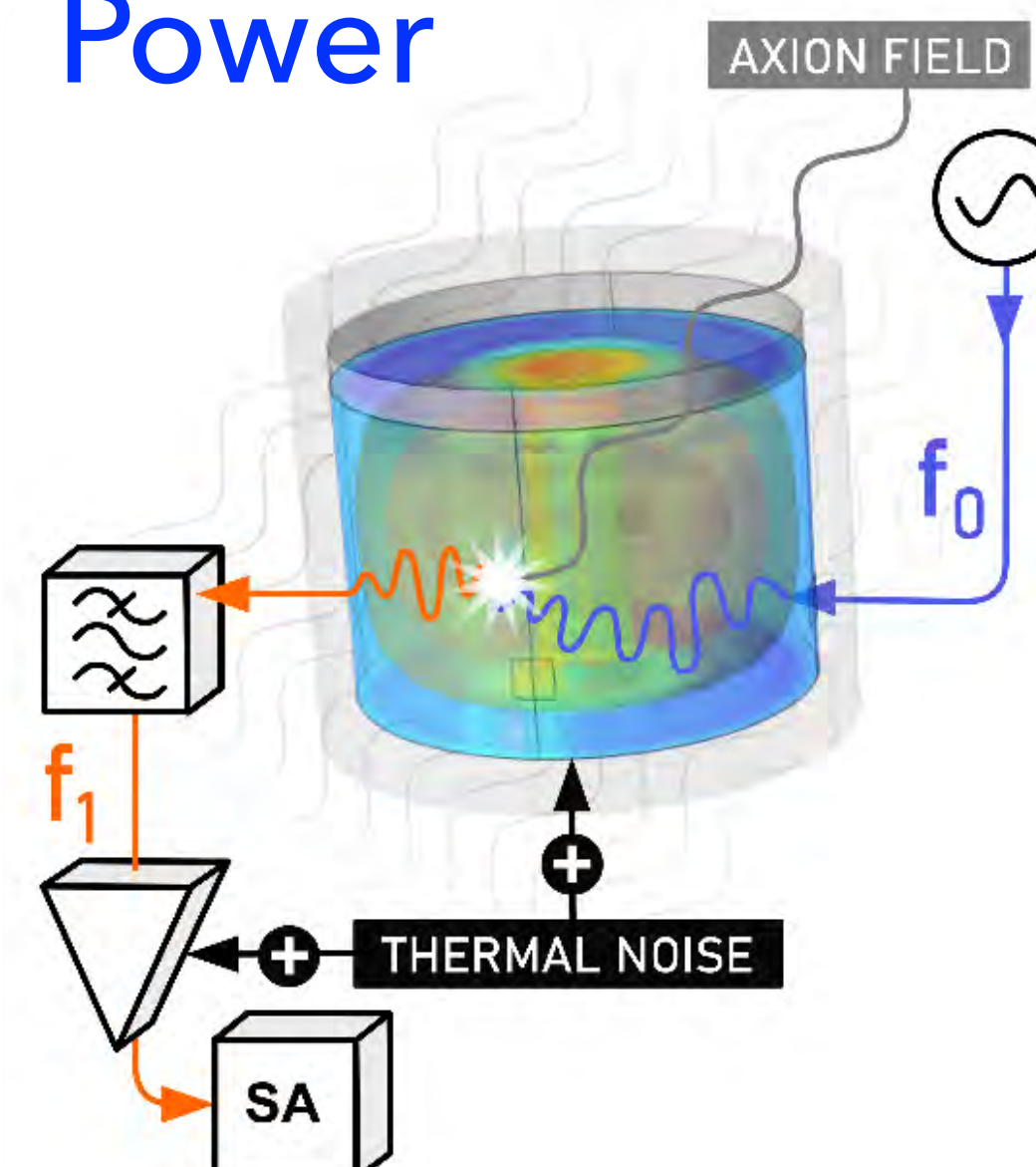


- Use a mode 0 as the background "magnetic field" AC source
- Two modes in one cylindrical cavity
- Upconversion limit $m_a = |f_1 - f_0| + \delta f$

Photon 1: Transverse Magnetic Mode

(Longitudinal Electric)

AC Power



Photon 0: Transverse Electric Mode

(Longitudinal Magnetic)

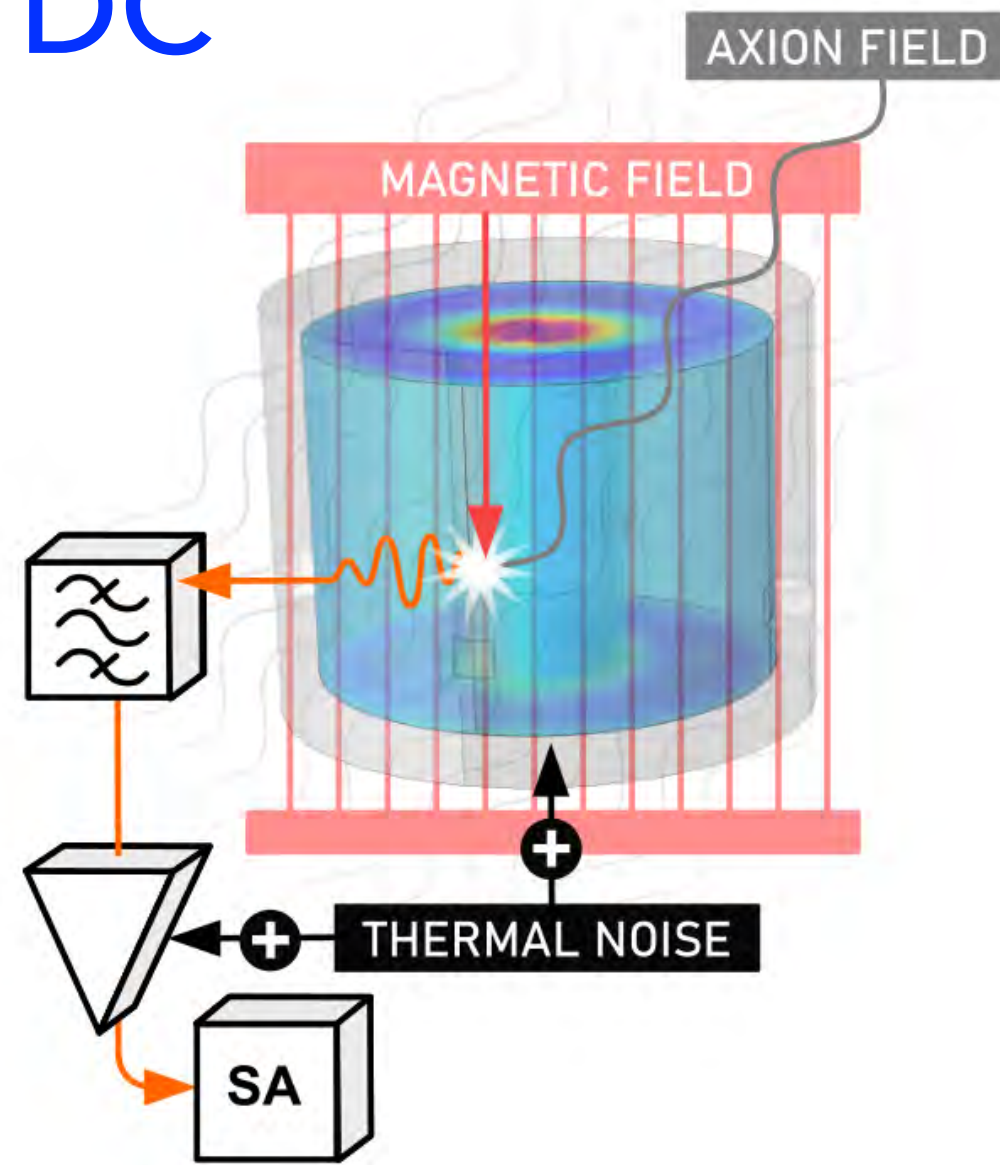
• UPLOAD

AC Frequency: Excite two modes: Measure f_1 Frequency Fluctuation Spectrum

Resonant Axion Haloscopes @ UWA

$$\mathcal{H}_{int} = \epsilon_0 c g_{a\gamma\gamma} a \mathbf{E} \cdot \mathbf{B}$$

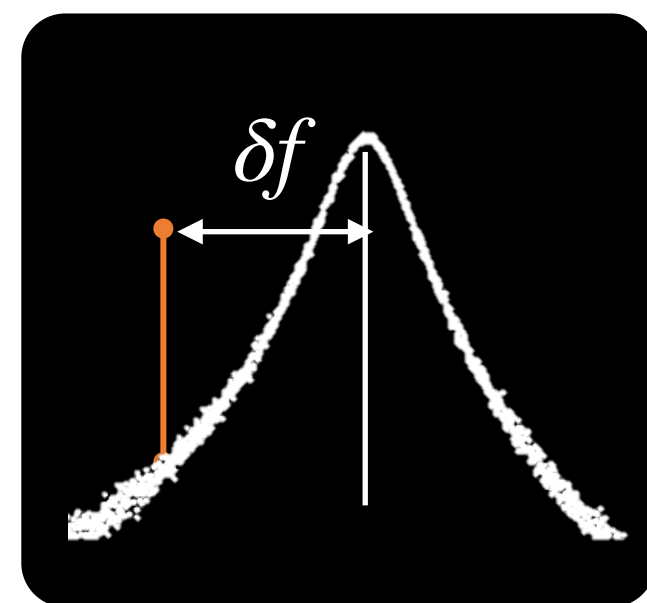
DC



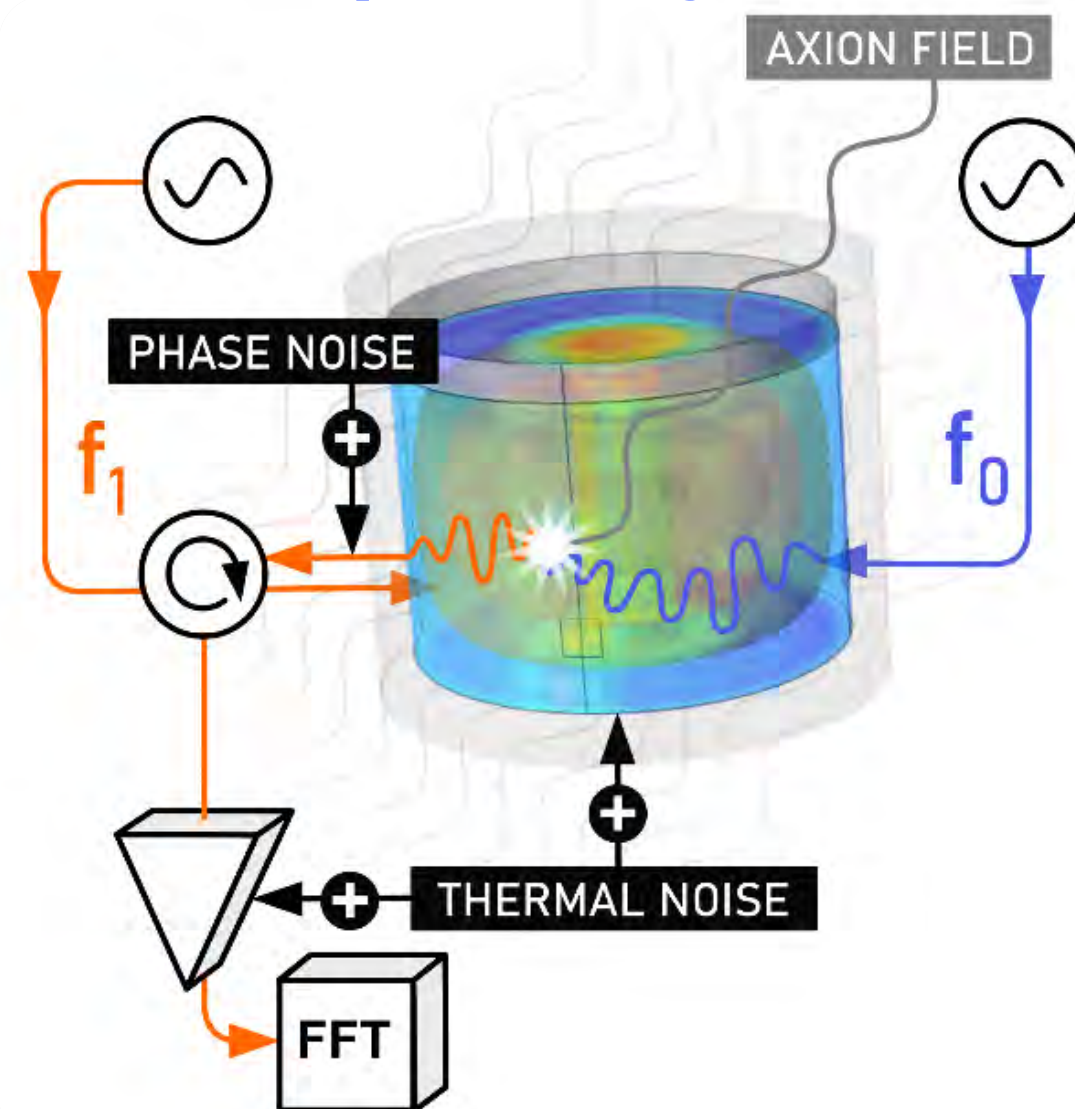
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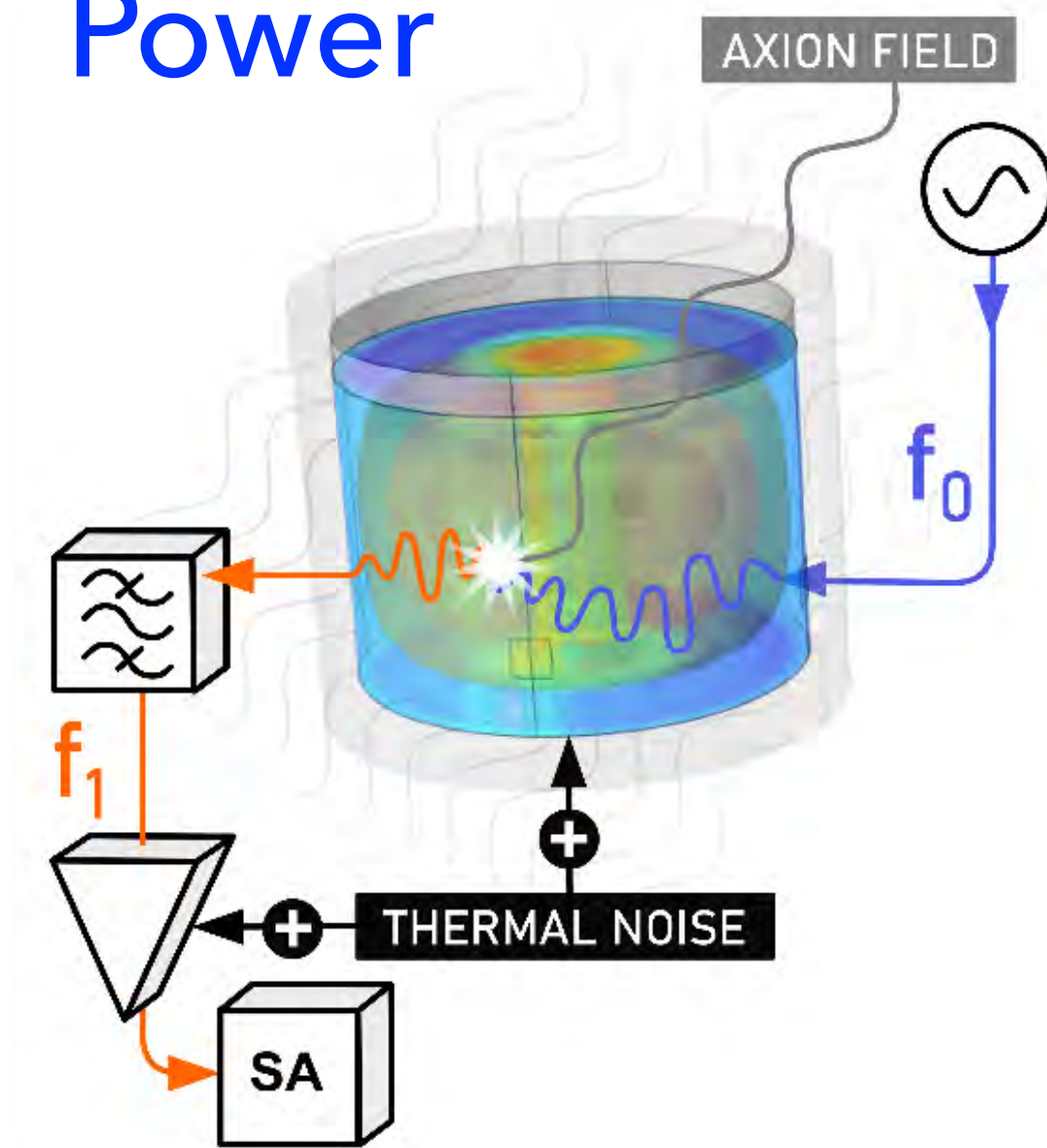
AC Frequency



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Photon 1: Transverse Magnetic Mode
(Longitudinal Electric)

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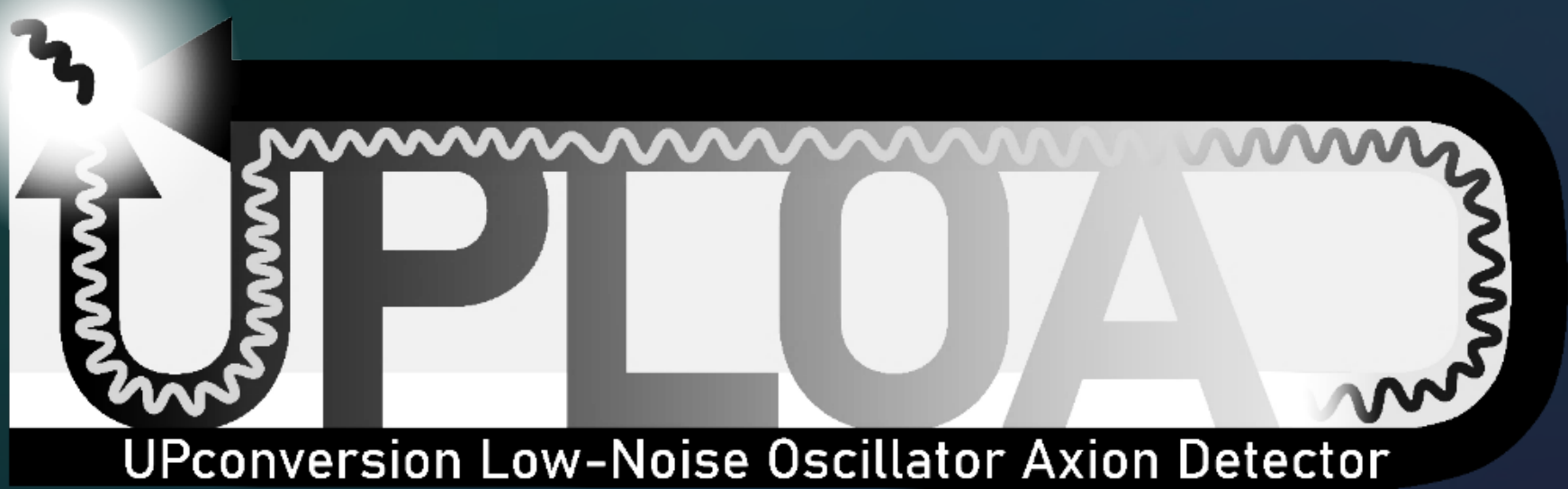


Photon 0: Transverse Electric Mode
(Longitudinal Magnetic)

AC Frequency: Excite two modes: Measure f_1 Frequency Fluctuation Spectrum

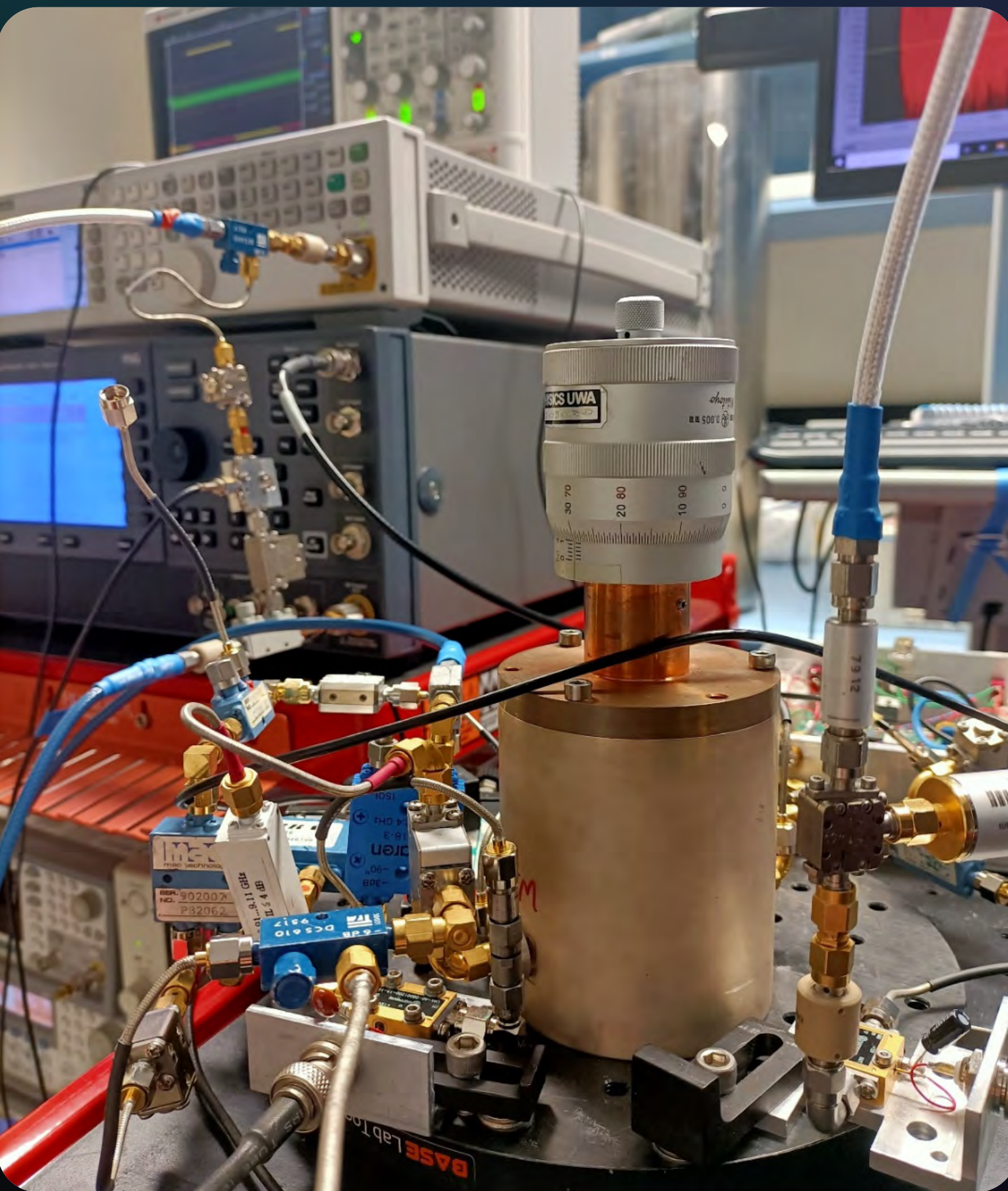
AC Power: Excite f_0 : Measure f_1 Power Fluctuation Spectrum

• UPLOAD



UPconversion Low-Noise Oscillator Axion Detection Experiment

- Cavity resonator haloscope
- No externally applied magnetic field
- TM and TE modes (~ 9 GHz modes)
- Height Tunable
- Accessing MHz axions via upconversion



PHYSICAL REVIEW D **107**, 112003 (2023)

Searching for low-mass axions using resonant upconversion

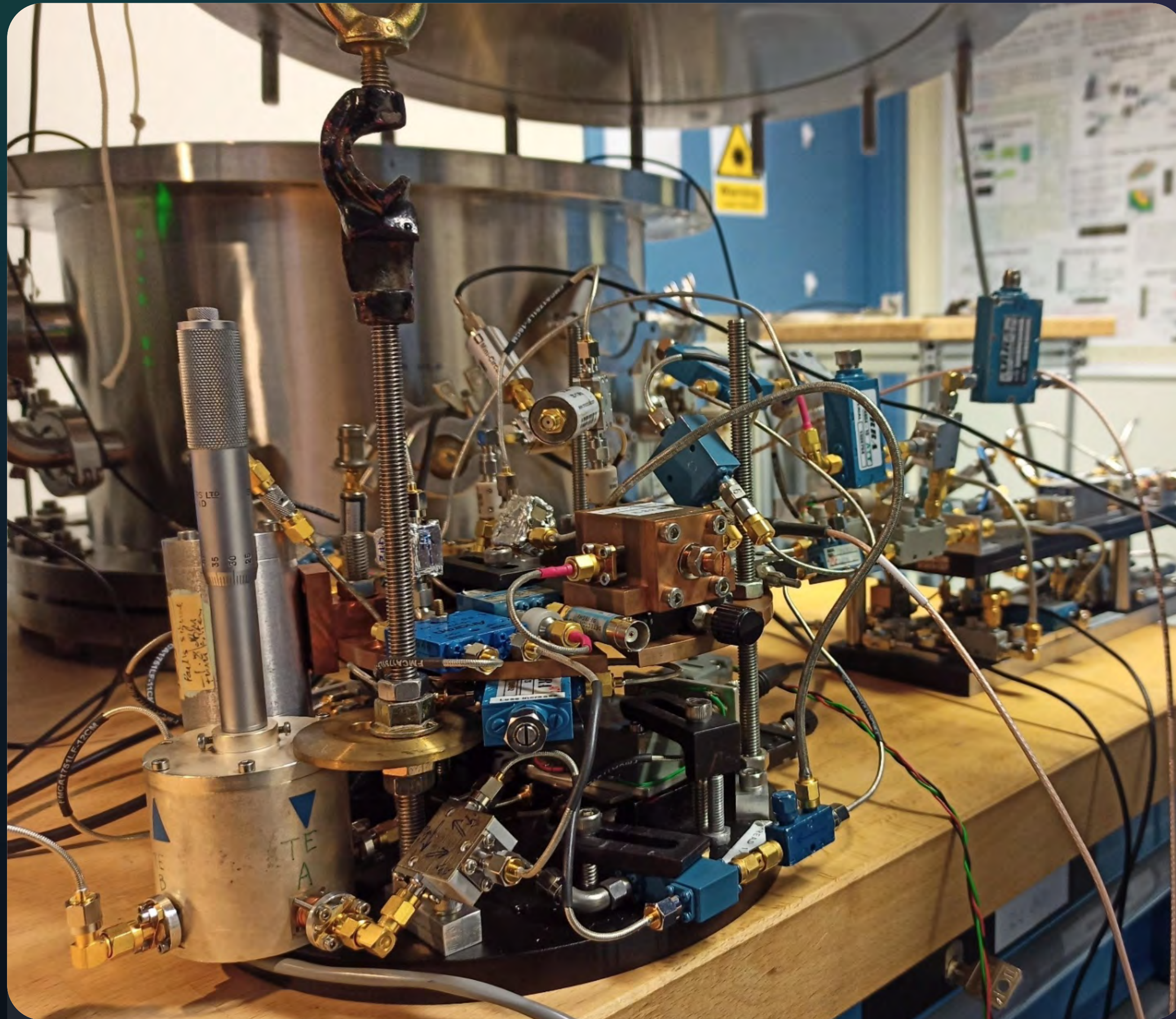
Catriona A. Thomson^{1,*}, Maxim Goryachev,¹ Ben T. McAllister,^{1,2} Eugene N. Ivanov,¹
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¹*Quantum Technologies and Dark Matter Labs, Department of Physics, University of Western Australia,
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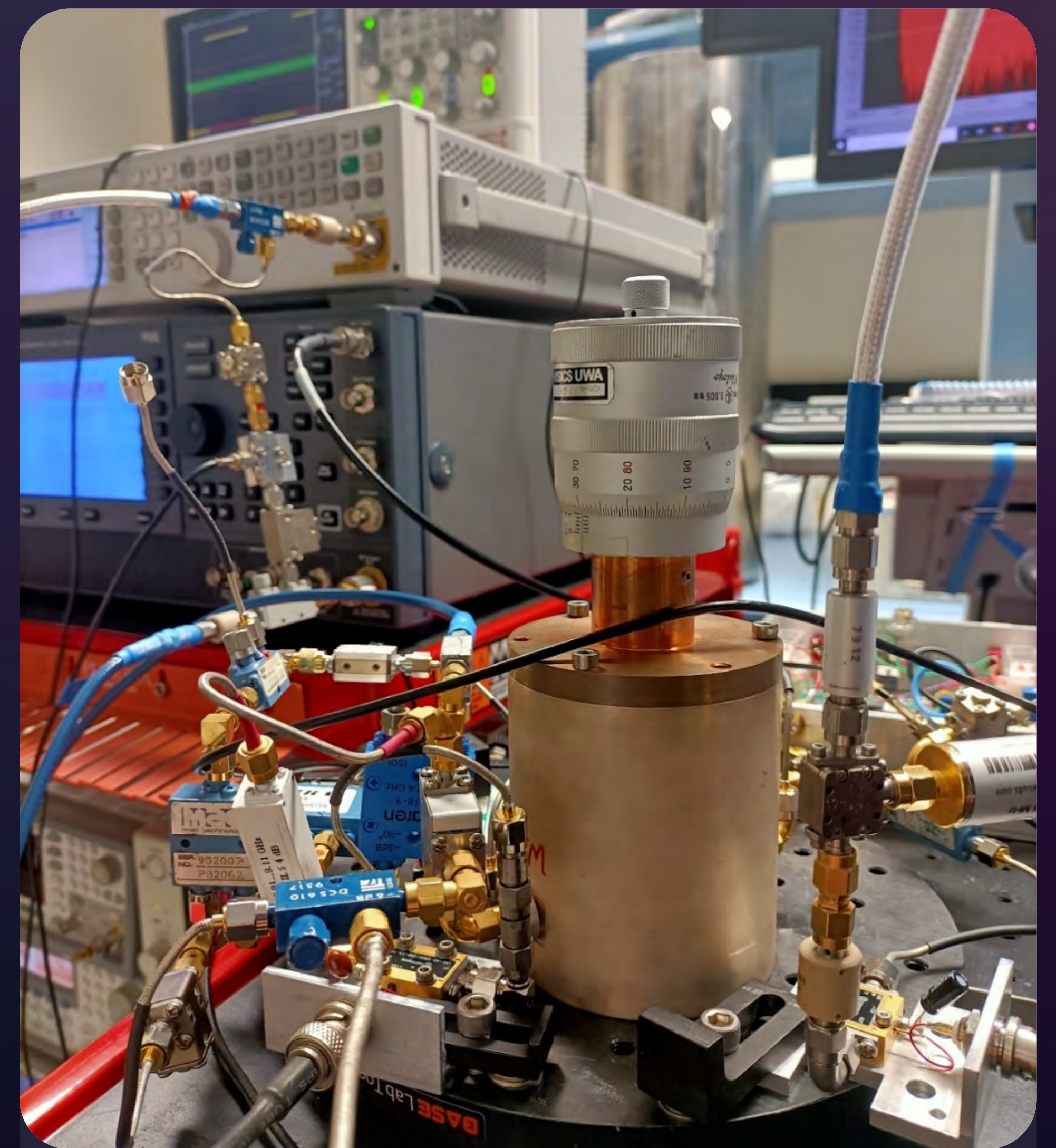
²*Centre for Astrophysics and Supercomputing, Swinburne University of Technology,
John St, Hawthorn, Victoria 3122, Australia*

³*ARC Centre of Excellence For Engineered Quantum Systems, The Australian National University,
Canberra, Australian Capital Territory 2600 Australia*

(Received 17 January 2023; accepted 5 May 2023; published 5 June 2023)

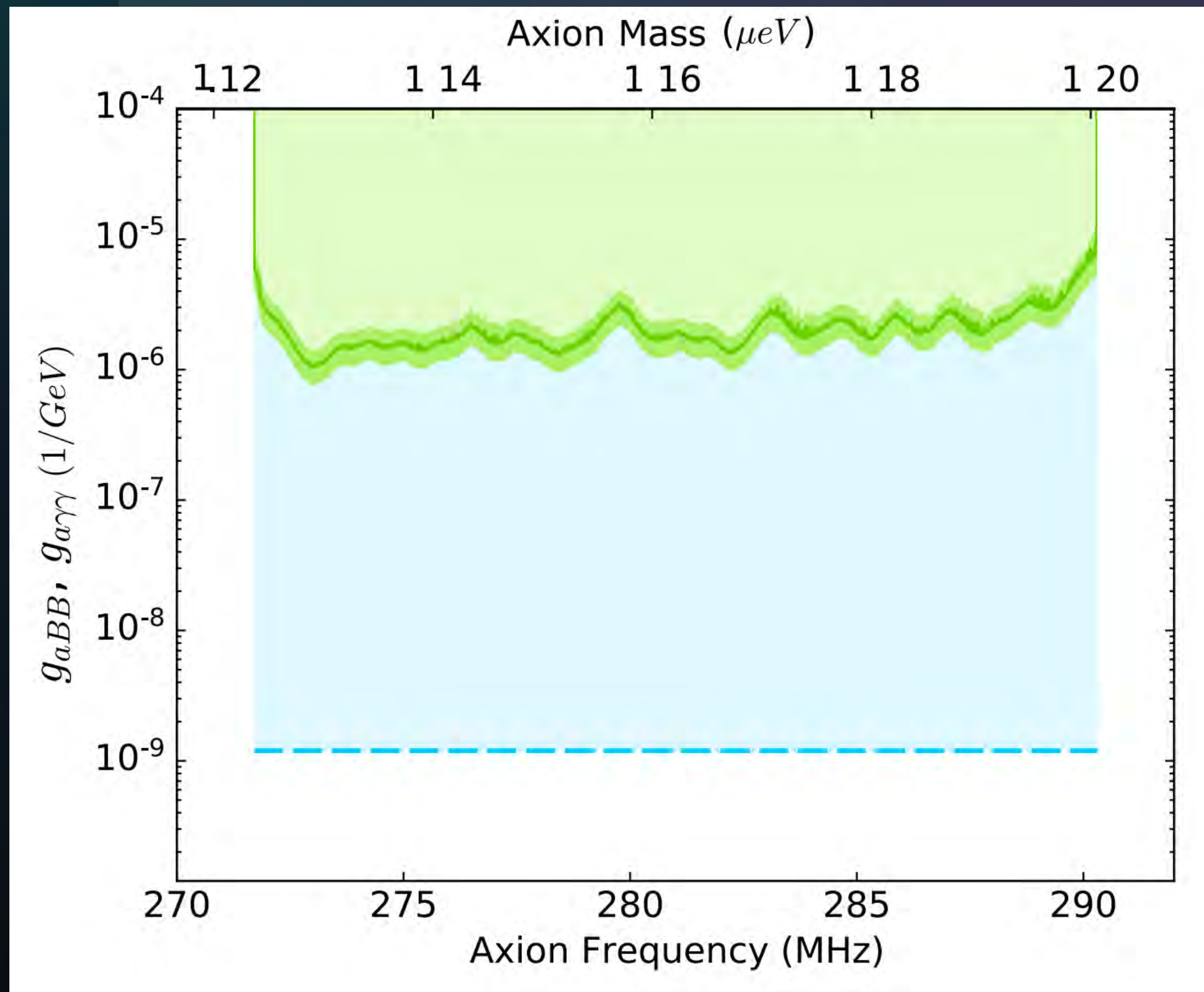


V1: readout via frequency metrology



V2: readout via thermal noise peak (power)

UPLOAD V2: Exclusion limits



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FIG. 7. In green, the 95% confidence axion exclusion zone for both $g_{a\gamma\gamma}$ and g_{aBB} for the measured mass range between 1.12 – 1.20 μeV (271.7 MHz—290.3 MHz) for a measurement period of 30 days, which is an improvement of 3 orders of magnitude over our previous result [29]. The bright green region represents the uncertainty on excluded $g_{a\gamma\gamma}$, which is detailed in Appendix C. The blue dashed line represents the approximate sensitivity achievable with a niobium resonator of loaded quality factors around 10^7 and cooled to a temperature of 4 K, measuring for a period of 30 days, and using a cryogenic amplifier of noise temperature 4 K. Construction for this setup is underway.

UPLOAD V3: Cryogenic Niobium

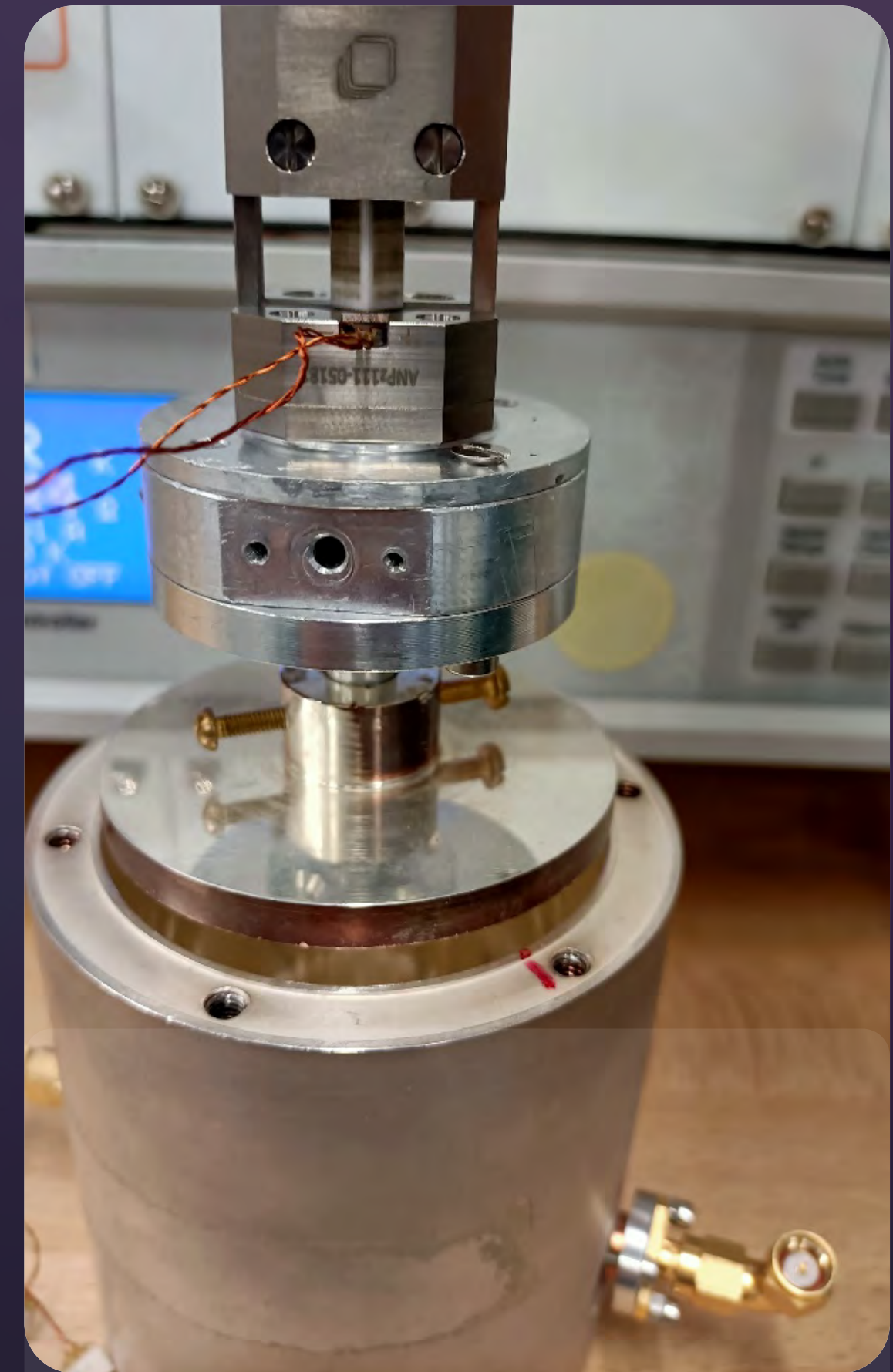
An experiment targeting 350 MHz axions with a dual mode cavity (~12 GHz), height tuning with a piezo actuated lid. Gain in noise temperature and quality factor.

290 K → 4 K

$$\langle H \rangle = k_B T$$

$$g_{a\gamma\gamma} = \frac{\frac{f_a}{\sqrt{f_1 f_0}} \frac{(2\sqrt{2}\sqrt{\beta_1\beta_0})}{\sqrt{1+\beta_1(\beta_0+1)}} \sqrt{P_a}}{\sqrt{1+4(Q_{L1})^2 \left(\frac{f_a+f_0-f_1}{f_1}\right)^2}} \frac{2\pi f_a}{\sqrt{\rho c^3}} \sqrt{Q_{L1} Q_{L0} FFP_{0inc}}$$

Q ~ 13,000 → > 20,000,000



Trialing attocube actuator in silver plated cavity

arXiv > hep-ph > arXiv:2303.10170

High Energy Physics – Phenomenology

[Submitted on 17 Mar 2023]

Generic axion Maxwell equations: path integral approach

Anton V. Sokolov, Andreas Ringwald

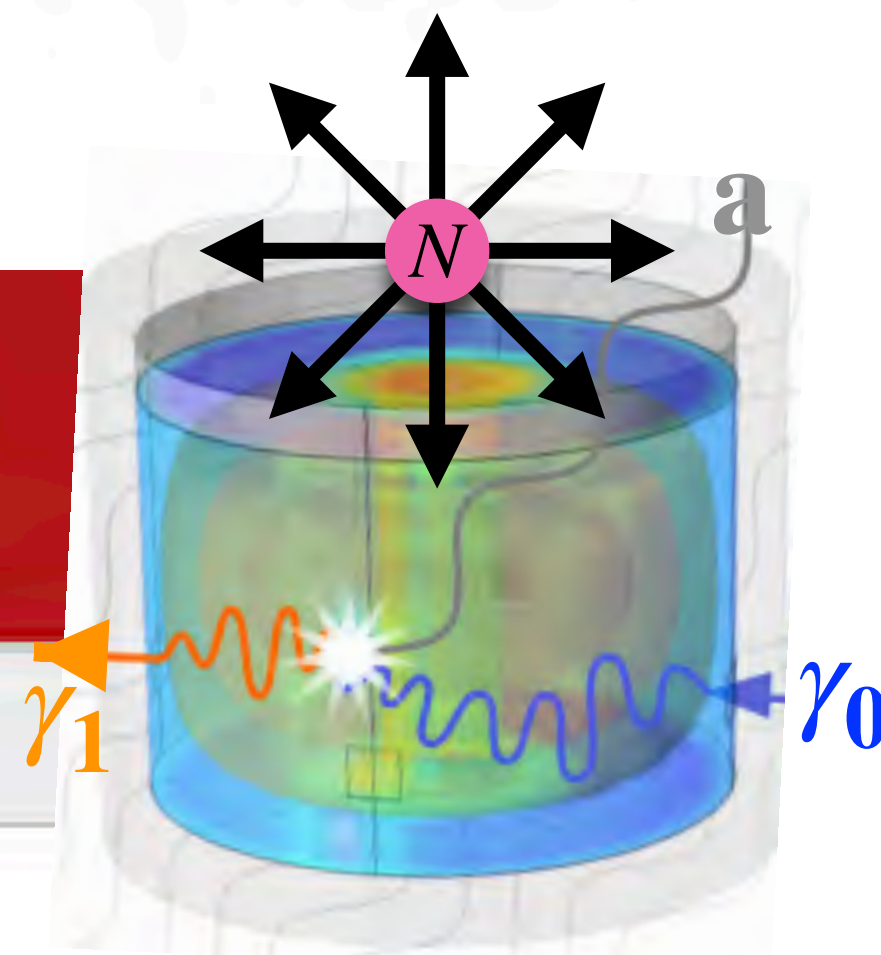
arXiv > hep-ph > arXiv:2205.02605

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Electromagnetic Couplings of Axions

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If Magnetic Charge Exist at High Energy

arXiv > hep-ph > arXiv:2303.10170

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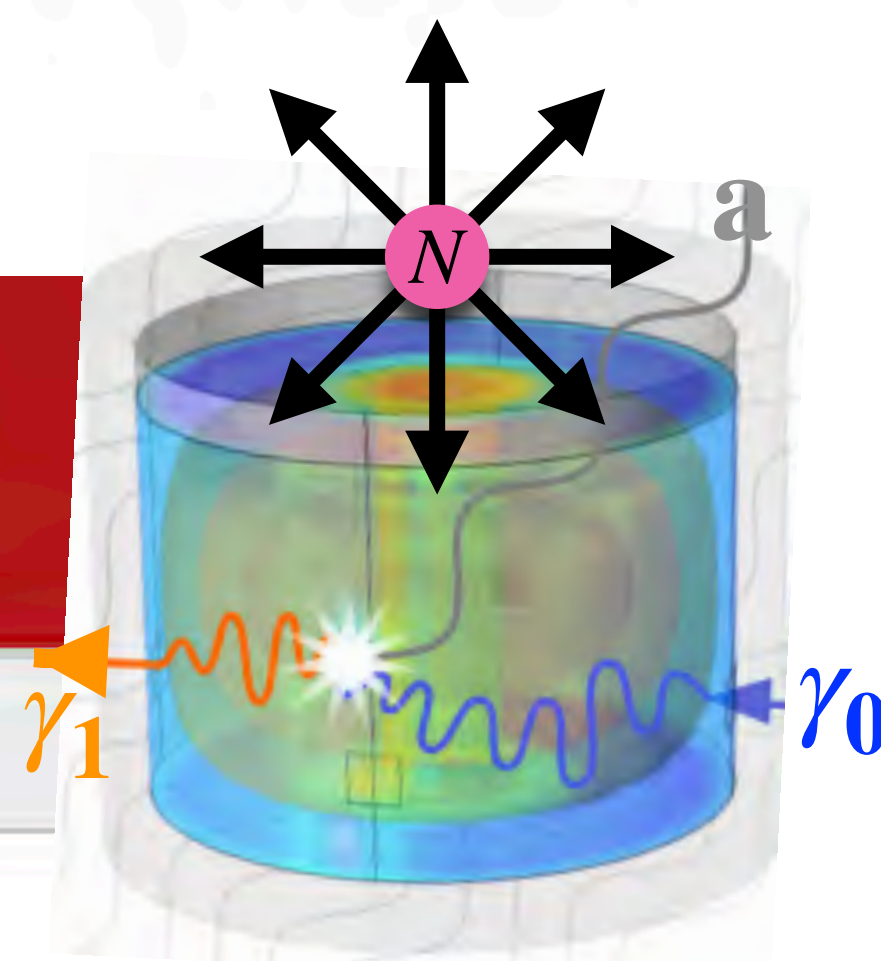
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-> Further Modifications to Axion Electrodynamics

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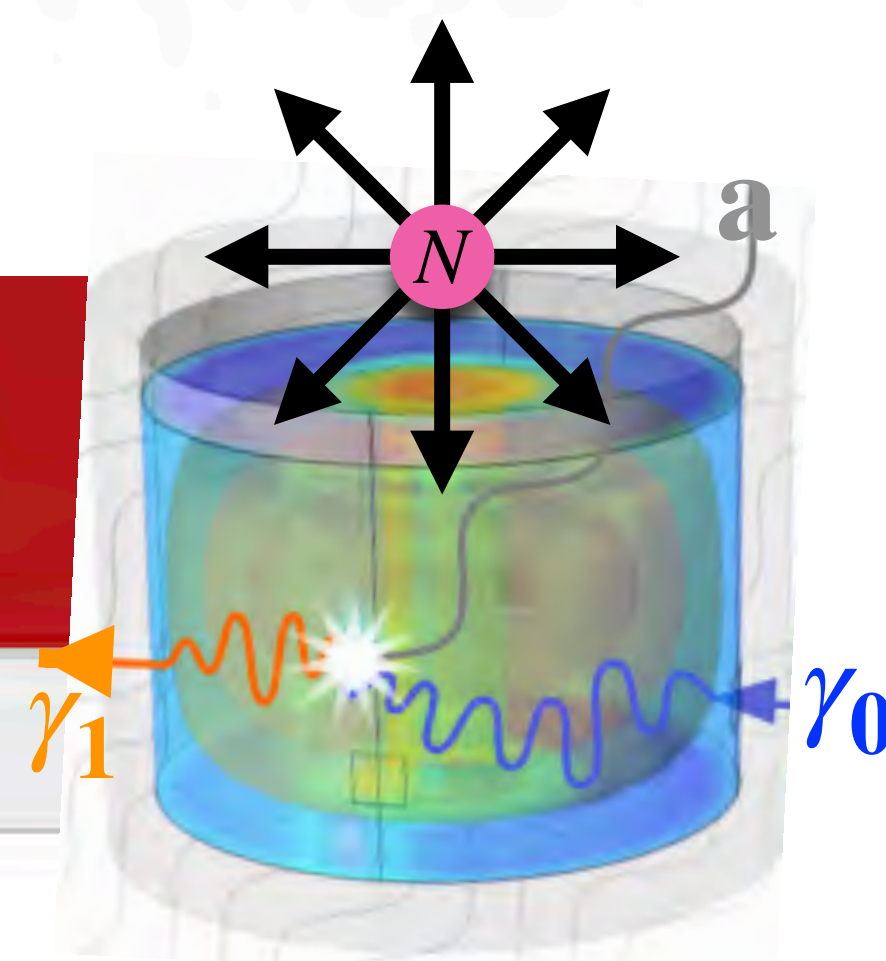
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-> Can test the existence of Magnetic Charge through Axions

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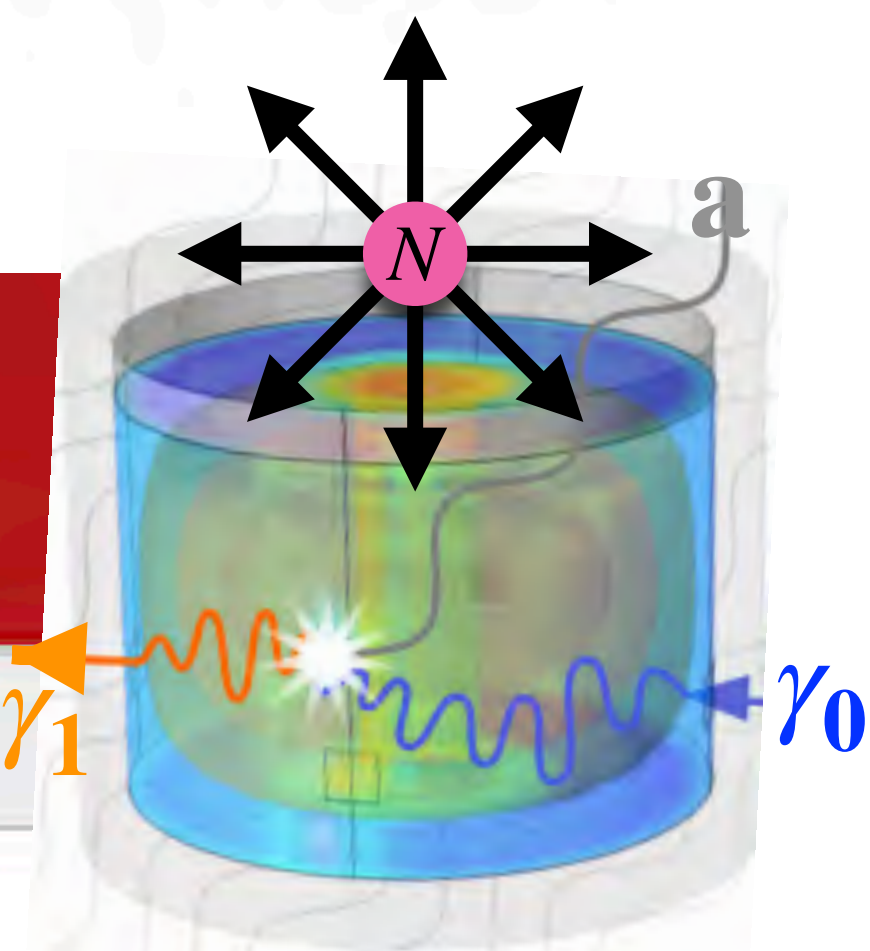
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The diagram shows a cylindrical container with a blue liquid inside. At the top center, there is a pink circle labeled 'N' with eight black arrows pointing outwards in all directions. Below this, a bright white starburst is shown, with two wavy lines extending from it: an orange one labeled γ_1 pointing left and a blue one labeled γ_0 pointing right. A small grey 'a' is located at the top right edge of the container.

If Magnetic Charge Exist at High Energy

-> Further Modifications to Axion Electrodynamics

-> Can test the existence of Magnetic Charge through Axions

Axion-photon coupling parameter space is expanded from one parameter to three

$$g_{a\gamma\gamma} \rightarrow (g_{a\gamma\gamma}, g_{aEM}, g_{aMM})$$

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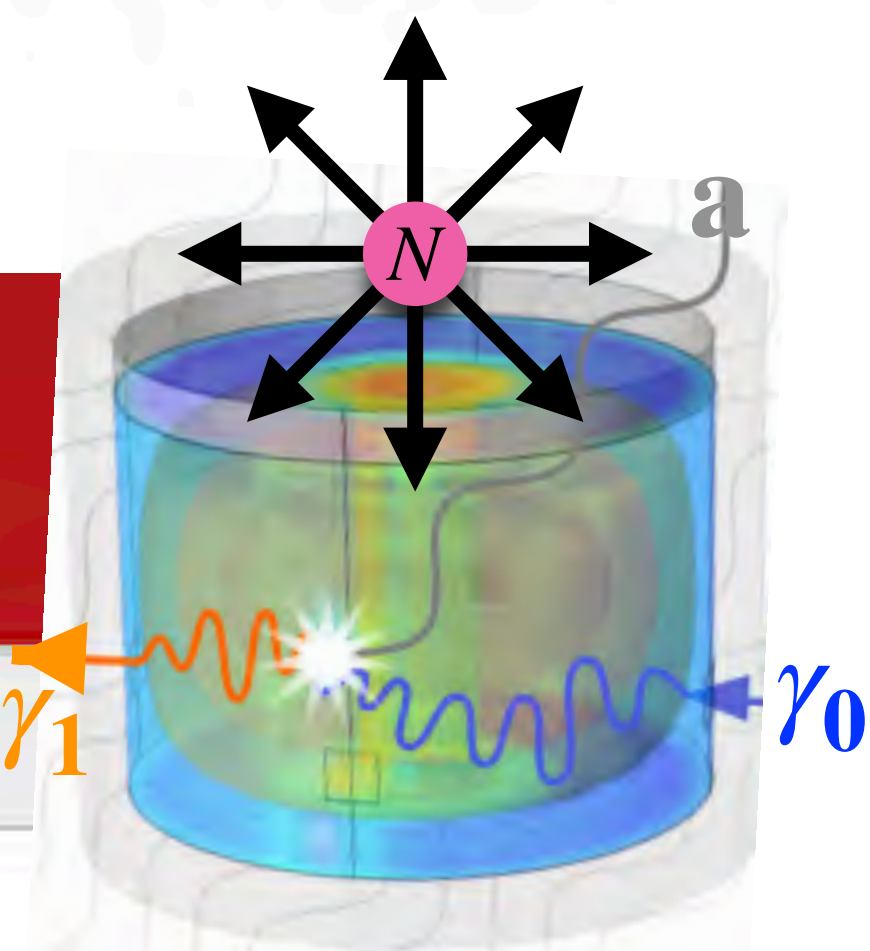
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$$g_{a\gamma\gamma} \rightarrow (g_{a\gamma\gamma}, g_{aEM}, g_{aMM})$$

$$\vec{\nabla} \cdot \vec{E}_1 = g_{a\gamma\gamma} c \vec{B}_0 \cdot \vec{\nabla} a - g_{aEM} \vec{E}_0 \cdot \vec{\nabla} a + \epsilon_0^{-1} \rho_{e1},$$

$$\begin{aligned} \mu_0^{-1} \vec{\nabla} \times \vec{B}_1 &= \epsilon_0 \partial_t \vec{E}_1 + \vec{J}_{e1} \\ &+ g_{a\gamma\gamma} c \epsilon_0 \left(-\vec{\nabla} a \times \vec{E}_0 - \partial_t a \vec{B}_0 \right) \\ &+ g_{aEM} \epsilon_0 \left(-\vec{\nabla} a \times c^2 \vec{B}_0 + \partial_t a \vec{E}_0 \right), \end{aligned}$$

$$\vec{\nabla} \cdot \vec{B}_1 = -\frac{g_{aMM}}{c} \vec{E}_0 \cdot \vec{\nabla} a + g_{aEM} \vec{B}_0 \cdot \vec{\nabla} a,$$

$$\begin{aligned} \vec{\nabla} \times \vec{E}_1 &= -\partial_t \vec{B}_1 + \frac{g_{aMM}}{c} \left(c^2 \nabla a \times \vec{B}_0 - \partial_t a \vec{E}_0 \right) \\ &+ g_{aEM} \left(\nabla a \times \vec{E}_0 + \partial_t a \vec{B}_0 \right). \end{aligned}$$

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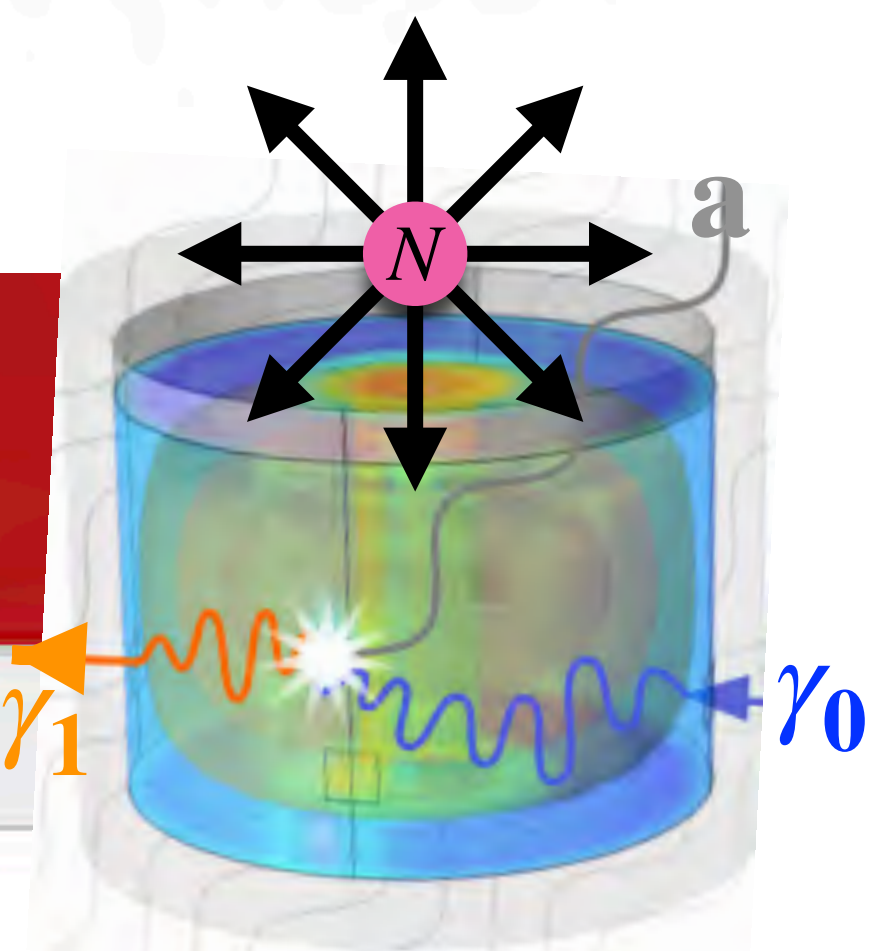
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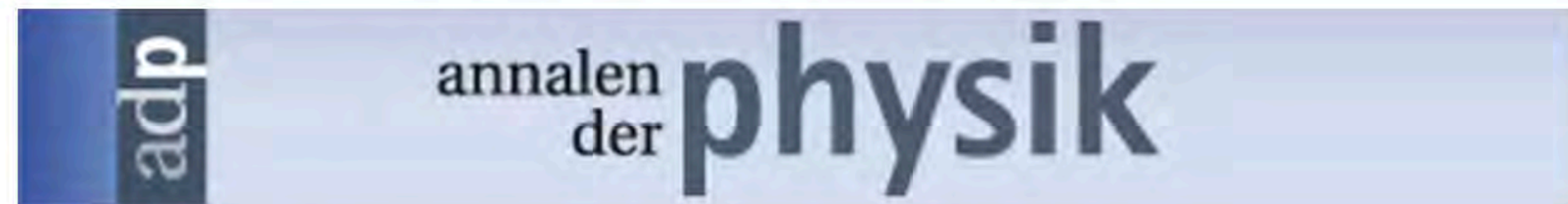


Calculate Form Factors for Resonant Experiment with Static and Time varying Background Electric and Magnetic Fields -> Poynting Theorem

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First published: 22 April 2023 | <https://doi.org/10.1002/andp.202200594>

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Reactive Experiment with Static Background Electric and Magnetic Field -> Imaginary Poynting Theorem

PHYSICAL REVIEW D **108**, 035024 (2023)

Searching for GUT-scale QCD axions and monopoles with a high-voltage capacitor

Michael E. Tobar ,^{1,*} Anton V. Sokolov ,² Andreas Ringwald ,³ and Maxim Goryachev¹

¹Quantum Technologies and Dark Matter Labs, Department of Physics, University of Western Australia, 35 Stirling Highway, Crawley, Western Australia 6009, Australia

²Department of Mathematical Sciences, University of Liverpool, Liverpool, L69 7ZL, United Kingdom

³Deutsches Elektronen-Synchrotron DESY, Notkestraße 85, 22607 Hamburg, Germany

(Received 20 June 2023; accepted 2 August 2023; published 17 August 2023)

arXiv:2306.13320v1 [hep-ph] 23 Jun 2023

SENSITIVITY OF AXION RESONANT HALOSCOPES UNDER DC MAGNETIC FIELDS

$$P_{s1} = P_d = \frac{\omega_1 U_1}{Q_1} = g_{a\gamma\gamma} \frac{\omega_a \epsilon_0 \langle a_0 \rangle}{\sqrt{2} Q_1} \int \vec{B}_0 \cdot \text{Re}(\mathbf{E}_1) dV + g_{aEM} \frac{\omega_a \epsilon_0 \langle a_0 \rangle c}{\sqrt{2} Q_1} \int \vec{B}_0 \cdot \text{Re}(\mathbf{B}_1) dV$$

$$\sqrt{P_1} = \sqrt{\omega_a Q_1 U_1} = (g_{a\gamma\gamma} \sqrt{C_{1a\gamma\gamma}} + g_{aEM} \sqrt{C_{1aEM}}) \langle a_0 \rangle c B_0 \sqrt{\omega_a Q_1 \epsilon_0 V_1} = (g_{a\gamma\gamma} \sqrt{C_{1a\gamma\gamma}} + g_{aEM} \sqrt{C_{1aEM}}) B_0 \sqrt{\frac{\rho_a Q_1 \epsilon_0 c^5 V_1}{\omega_a}}$$

Form Factors

$$C_{1a\gamma\gamma} = \frac{(\int \vec{B}_0 \cdot \text{Re}(\mathbf{E}_1) dV)^2}{B_0^2 V_1 \int \mathbf{E}_1 \cdot \mathbf{E}_1^* dV} \quad C_{1aEM} = \frac{(\int \vec{B}_0 \cdot \text{Re}(\mathbf{B}_1) dV)^2}{B_0^2 V_1 \int \mathbf{B}_1 \cdot \mathbf{B}_1^* dV}$$

SENSITIVITY OF AXION RESONANT HALOSCOPES UNDER DC ELECTRIC FIELDS

$$\sqrt{P_1} = \sqrt{\omega_a Q_1 U_1} = (g_{aMM} \sqrt{C_{1aMM}} + g_{aEM} \sqrt{C_{1aEMm}}) \langle a_0 \rangle E_0 \sqrt{\omega_a Q_1 \epsilon_0 V_1} = (g_{aMM} \sqrt{C_{1aMM}} + g_{aEM} \sqrt{C_{1aEMm}}) E_0 \sqrt{\frac{\rho_a Q_1 \epsilon_0 c^3 V_1}{\omega_a}},$$

Form Factors

$$C_{1aEMm} = \frac{(\int \vec{E}_0 \cdot \text{Re}(\mathbf{E}_1) dV)^2}{E_0^2 V_1 \int \mathbf{E}_1 \cdot \mathbf{E}_1^* dV} \quad C_{1aMM} = \frac{(\int \vec{E}_0 \cdot \text{Re}(\mathbf{B}_1) dV)^2}{E_0^2 V_1 \int \mathbf{B}_1 \cdot \mathbf{B}_1^* dV},$$

Searching for GUT-scale QCD axions and monopoles with a high-voltage capacitor

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The QCD axion has been postulated to exist because it solves the strong- CP problem. Furthermore, if it exists axions should be created in the early Universe and could account for all the observed dark matter. In particular, axion masses of order 10^{-10} eV to 10^{-7} eV correspond to axions in the vicinity of the grand unified theory scale (GUT-scale). In this mass range many experiments have been proposed to search for the axion through the standard QED coupling parameter $g_{a\gamma\gamma}$. Recently axion electrodynamics has been expanded to include two more coupling parameters, g_{aEM} and g_{aMM} , which could arise if heavy magnetic monopoles exist. In this work we show that both g_{aMM} and g_{aEM} may be searched for using a high-voltage capacitor. Since the experiment is not sensitive to $g_{a\gamma\gamma}$, it gives a new way to search for effects of heavy monopoles if the GUT-scale axion is shown to exist, or to simultaneously search for both the axion and the monopole at the same time.

DOI: [10.1103/PhysRevD.108.035024](https://doi.org/10.1103/PhysRevD.108.035024)

arXiv:2306.13320v1 [hep-ph] 23 Jun 2023

AC Capacitor: Apply Poynting Theorem: Sensitive to g_{aEM}

Vector Phasor Amplitudes

$$\oint \text{Im} (\mathbf{S}_1) \cdot \hat{n} ds = \omega_a \int \left(\left(\frac{1}{2\mu_0} \mathbf{B}_1^* \cdot \mathbf{B}_1 - \frac{\epsilon_0}{2} \mathbf{E}_1 \cdot \mathbf{E}_1^* \right) - \frac{g_{aEM} a_0 \epsilon_0}{4} (\mathbf{E}_1 + \mathbf{E}_1^*) \cdot \vec{E}_0 + \frac{g_{aMM} a_0 \epsilon_0}{4} (\mathbf{B}_1 + \mathbf{B}_1^*) \cdot \vec{E}_0 \right) dV.$$

AC Capacitor: Apply Poynting Theorem: Sensitive to g_{aEM}

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$$U_1 = \frac{\epsilon_0 a_0^2 \left(\int \left(g_{aEM} (\mathbf{E}_1^* + \mathbf{E}_1) - g_{aMM} c (\mathbf{B}_1^* + \mathbf{B}_1) \right) \cdot \vec{E}_0 dv \right)^2}{8 \int \left(c^2 \mathbf{B}_1^* \cdot \mathbf{B}_1 - \mathbf{E}_1 \cdot \mathbf{E}_1^* \right) dv}$$

AC Capacitor: Apply Poynting Theorem: Sensitive to g_{aEM}

Vector Phasor Amplitudes

$$\oint \text{Im} (\mathbf{S}_1) \cdot \hat{n} ds = \omega_a \int \left(\left(\frac{1}{2\mu_0} \mathbf{B}_1^* \cdot \mathbf{B}_1 - \frac{\epsilon_0}{2} \mathbf{E}_1 \cdot \mathbf{E}_1^* \right) - \frac{g_{aEM} a_0 \epsilon_0}{4} (\mathbf{E}_1 + \mathbf{E}_1^*) \cdot \vec{E}_0 + \frac{g_{aMM} a_0 \epsilon_0}{4} (\mathbf{B}_1 + \mathbf{B}_1^*) \cdot \vec{E}_0 \right) dV.$$

$$U_1 = \frac{\epsilon_0 a_0^2 \left(\int \left(g_{aEM} (\mathbf{E}_1^* + \mathbf{E}_1) - g_{aMM} c (\mathbf{B}_1^* + \mathbf{B}_1) \right) \cdot \vec{E}_0 dv \right)^2}{8 \int \left((c^2 \mathbf{B}_1^* \cdot \mathbf{B}_1 - \mathbf{E}_1 \cdot \mathbf{E}_1^*) \right) dv} \quad \mathbf{B}_1 + \mathbf{B}_1^* \sim 0 \quad \mathbf{E}_1 + \mathbf{E}_1^* \sim 2\mathbf{E}_1$$

AC Capacitor: Apply Poynting Theorem: Sensitive to g_{aEM}

Vector Phasor Amplitudes

$$\oint \text{Im} (\mathbf{S}_1) \cdot \hat{n} ds = \omega_a \int \left(\left(\frac{1}{2\mu_0} \mathbf{B}_1^* \cdot \mathbf{B}_1 - \frac{\epsilon_0}{2} \mathbf{E}_1 \cdot \mathbf{E}_1^* \right) - \frac{g_{aEM} a_0 \epsilon_0}{4} (\mathbf{E}_1 + \mathbf{E}_1^*) \cdot \vec{E}_0 + \frac{g_{aMM} a_0 \epsilon_0}{4} (\mathbf{B}_1 + \mathbf{B}_1^*) \cdot \vec{E}_0 \right) dV.$$

$$U_1 = \frac{\epsilon_0 a_0^2 \left(\int \left(g_{aEM} (\mathbf{E}_1^* + \mathbf{E}_1) - g_{aMM} c (\mathbf{B}_1^* + \mathbf{B}_1) \right) \cdot \vec{E}_0 dv \right)^2}{8 \int \left(c^2 \mathbf{B}_1^* \cdot \mathbf{B}_1 - \mathbf{E}_1 \cdot \mathbf{E}_1^* \right) dv} \quad \mathbf{B}_1 + \mathbf{B}_1^* \sim 0 \quad \mathbf{E}_1 + \mathbf{E}_1^* \sim 2\mathbf{E}_1 \quad U_1 \approx - \frac{g_{aEM}^2 a_0^2 \epsilon_0 \left(\int \mathbf{E}_1 \cdot \vec{E}_0 dv \right)^2}{2 \int \mathbf{E}_1 \cdot \mathbf{E}_1^* dv}$$

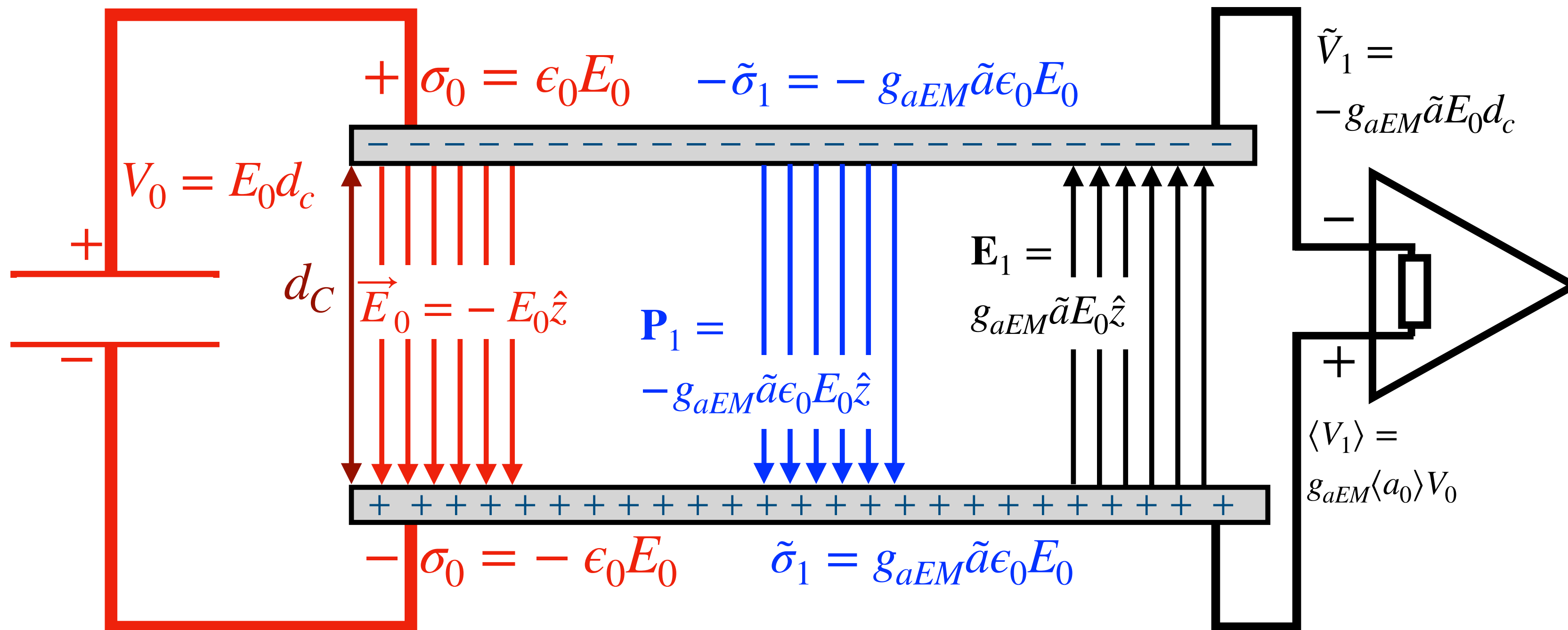
AC Capacitor: Apply Poynting Theorem: Sensitive to g_{aEM}

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Axion generated Electric Field



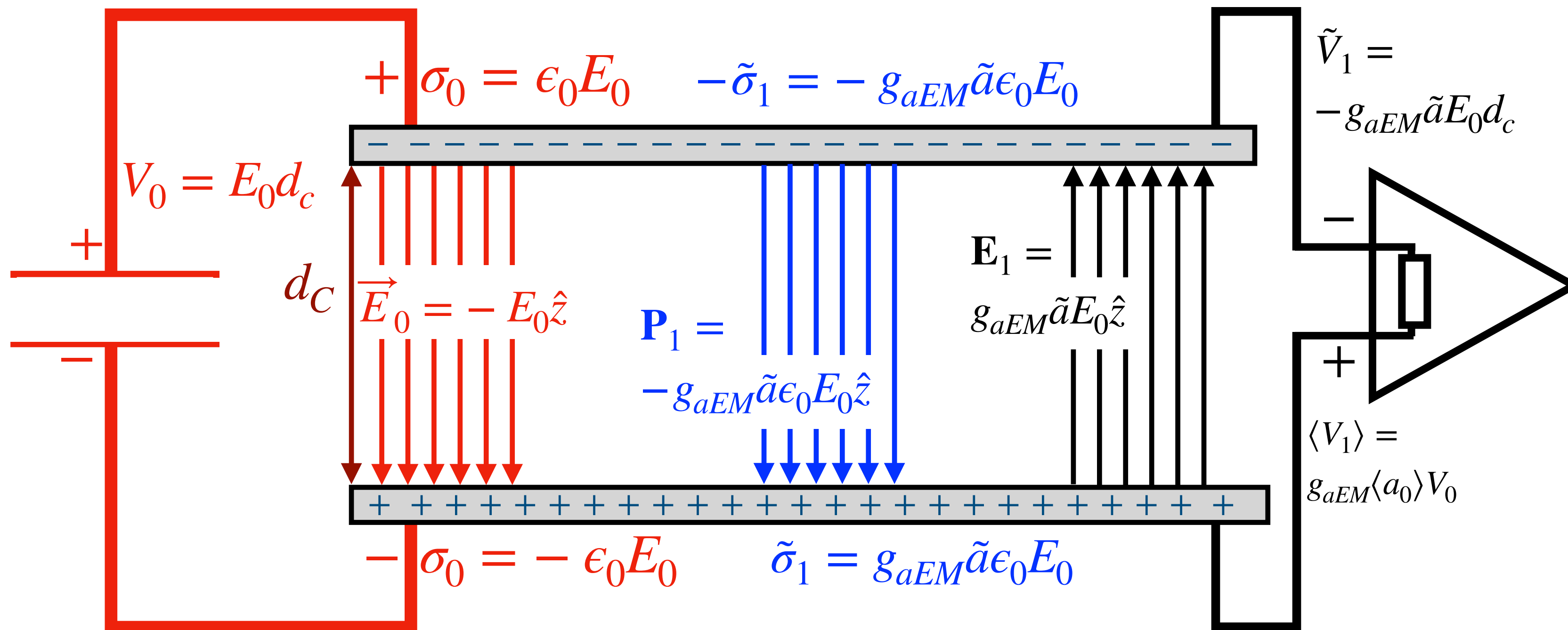
AC Capacitor: Apply Poynting Theorem: Sensitive to g_{aEM}

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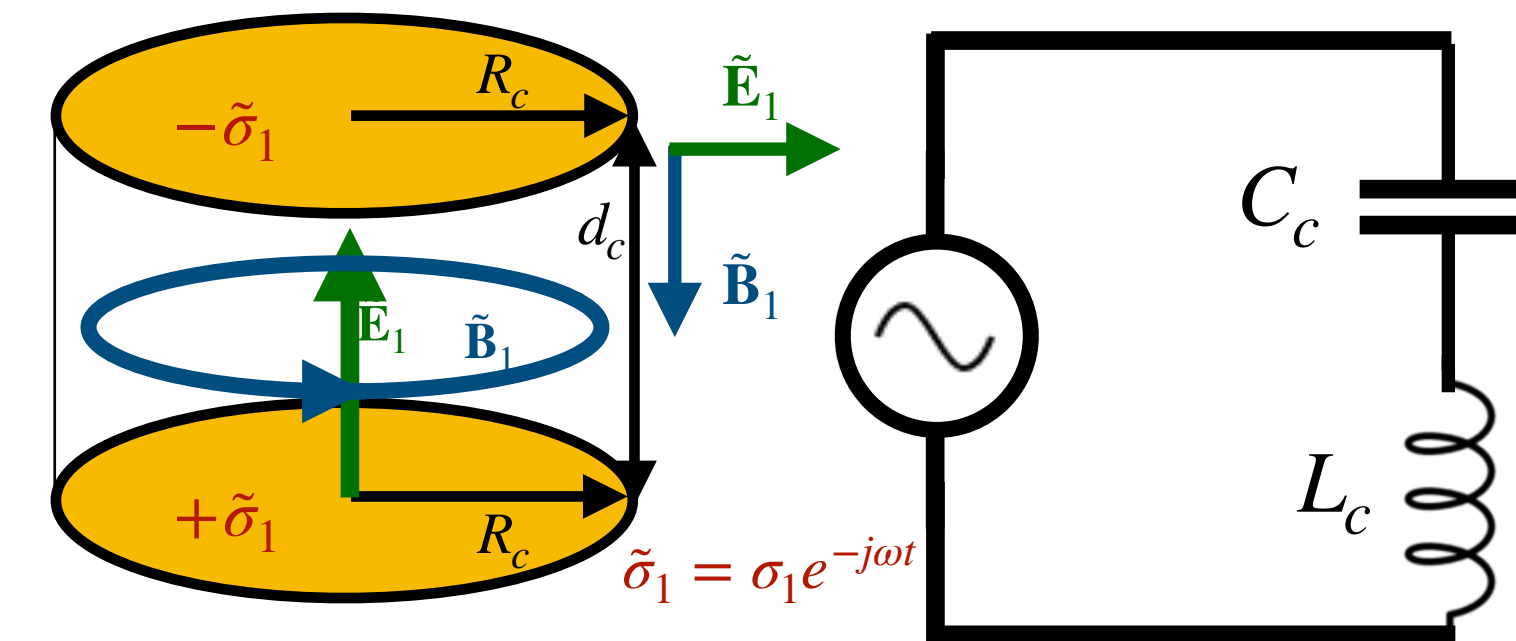
Axion generated Electric Field



Cylindrical // Plate Capacitor

$$\tilde{\mathbf{E}}_1 = \tilde{E}_{01} J_0 \left(\frac{\omega_1 r}{c} \right) e^{-j\omega_1 t \hat{z}}$$

$$\tilde{\mathbf{B}}_1 = -j \frac{\tilde{E}_{01}}{c} J_1 \left(\frac{\omega_1 r}{c} \right) e^{-j\omega_1 t \hat{\phi}} \quad \tilde{E}_{01} = \frac{\tilde{q}_1}{\pi R_c^2 \epsilon_0}$$



Axion Generated Magnetic Field-> Magnetic Circuit Readout Sensitive to g_{aMM}

$$\frac{\oint \text{Im}(\mathbf{S}_1) \cdot \hat{n} ds}{\omega_a} = \int \left(\left(\frac{1}{2\mu_0} \mathbf{B}_1^* \cdot \mathbf{B}_1 - \frac{\epsilon_0}{2} \mathbf{E}_1 \cdot \mathbf{E}_1^* \right) - \frac{g_{aEM} a_0 \epsilon_0}{4} (\mathbf{E}_1 + \mathbf{E}_1^*) \cdot \vec{E}_0 + \frac{g_{aMM} a_0 \epsilon_0 c}{4} (\mathbf{B}_1 + \mathbf{B}_1^*) \cdot \vec{E}_0 \right) dV$$

$$\mathbf{E}_1 + \mathbf{E}_1^* \sim 0 \quad \mathbf{B}_1 + \mathbf{B}_1^* \sim 2\mathbf{B}_1$$

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$$U_1 = \frac{\left(\frac{g_{aMM} a_0 \epsilon_0 c}{2} \int \mathbf{B}_1 \cdot \vec{E}_0 dV \right)^2}{\int \left(\frac{1}{2\mu_0} \mathbf{B}_1^* \cdot \mathbf{B}_1 - \frac{\epsilon_0}{2} \mathbf{E}_1 \cdot \mathbf{E}_1^* \right) dV}$$

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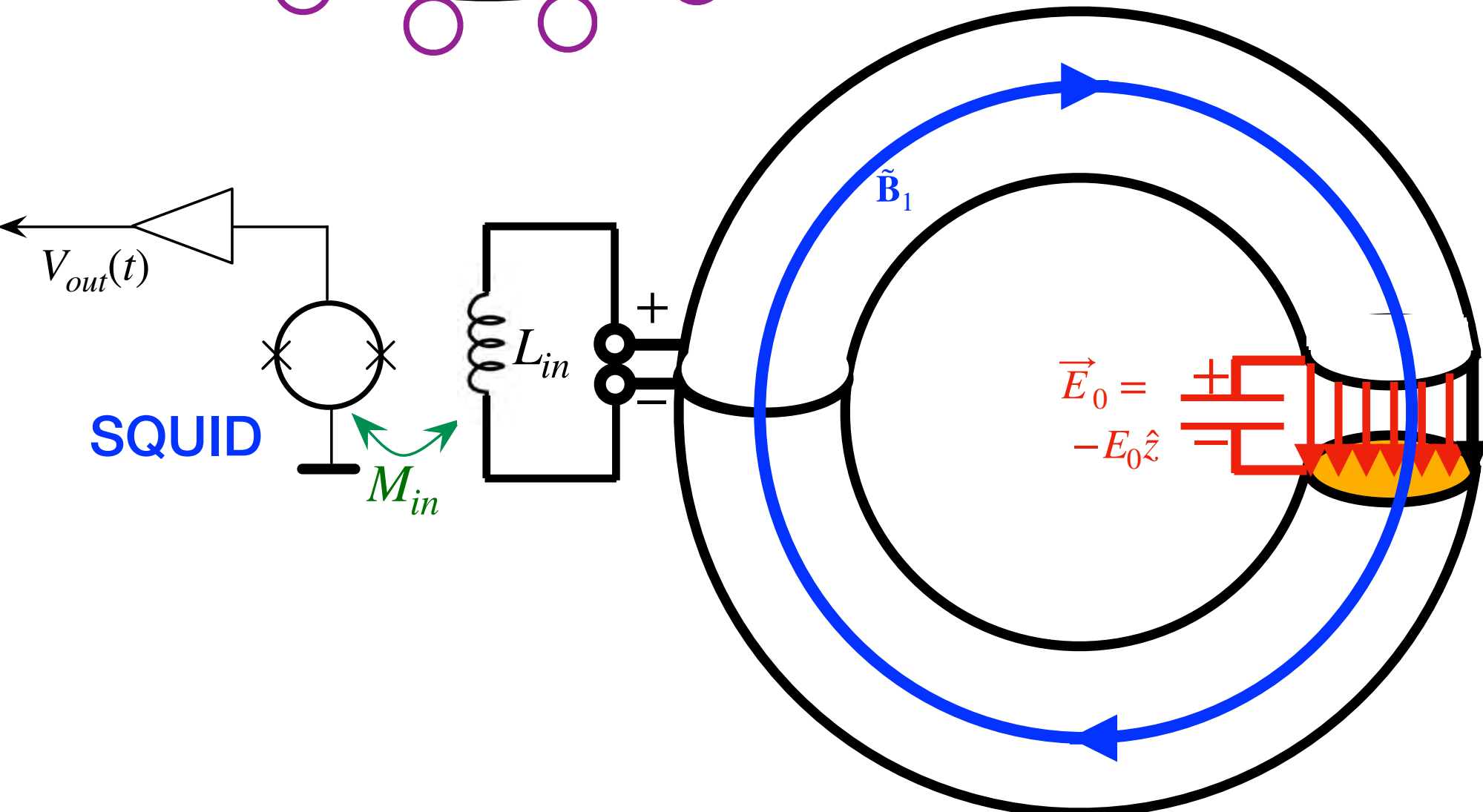
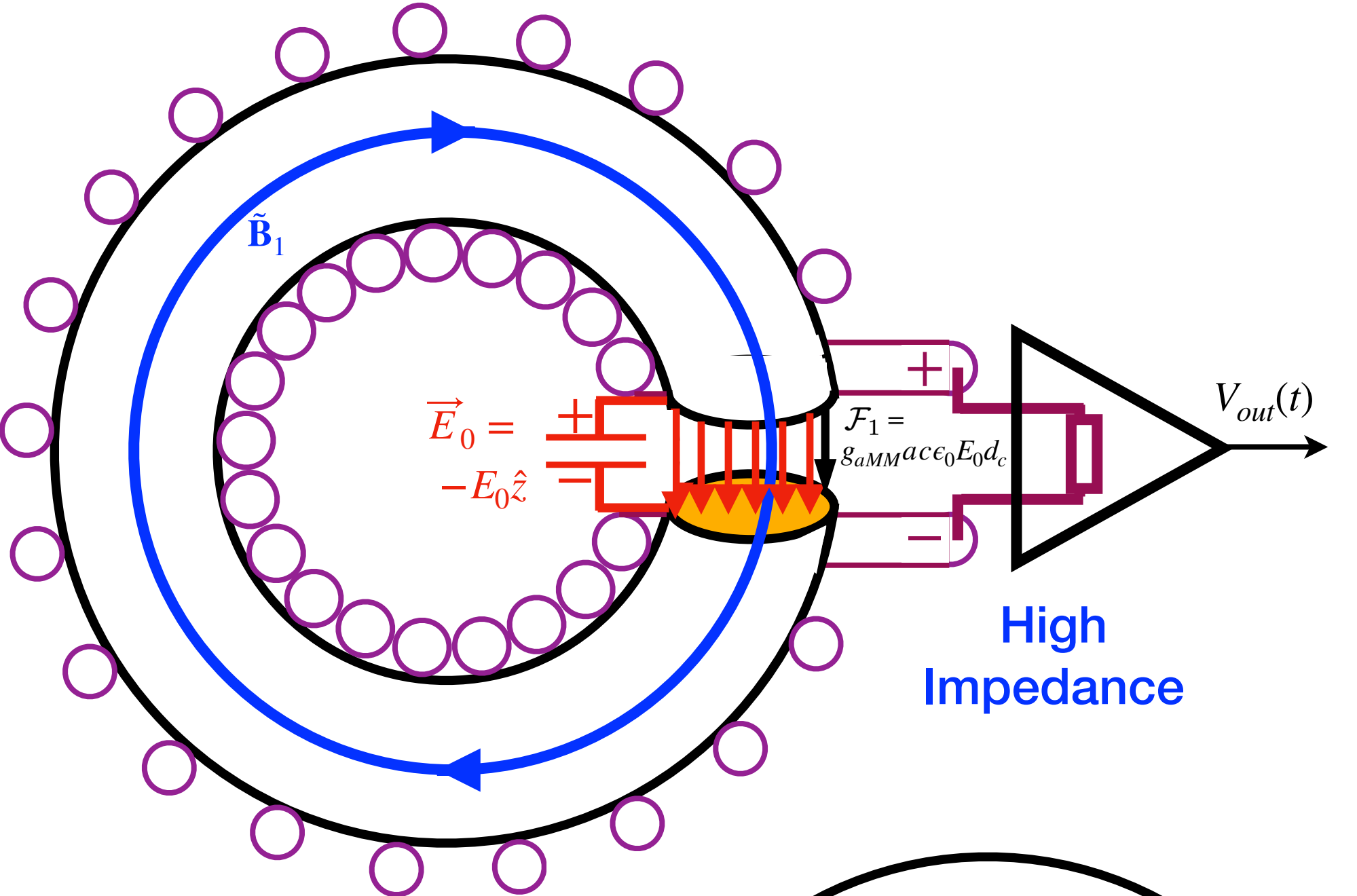
Axion Generated Magnetic Field -> Magnetic Circuit Readout Sensitive to g_{aMM}

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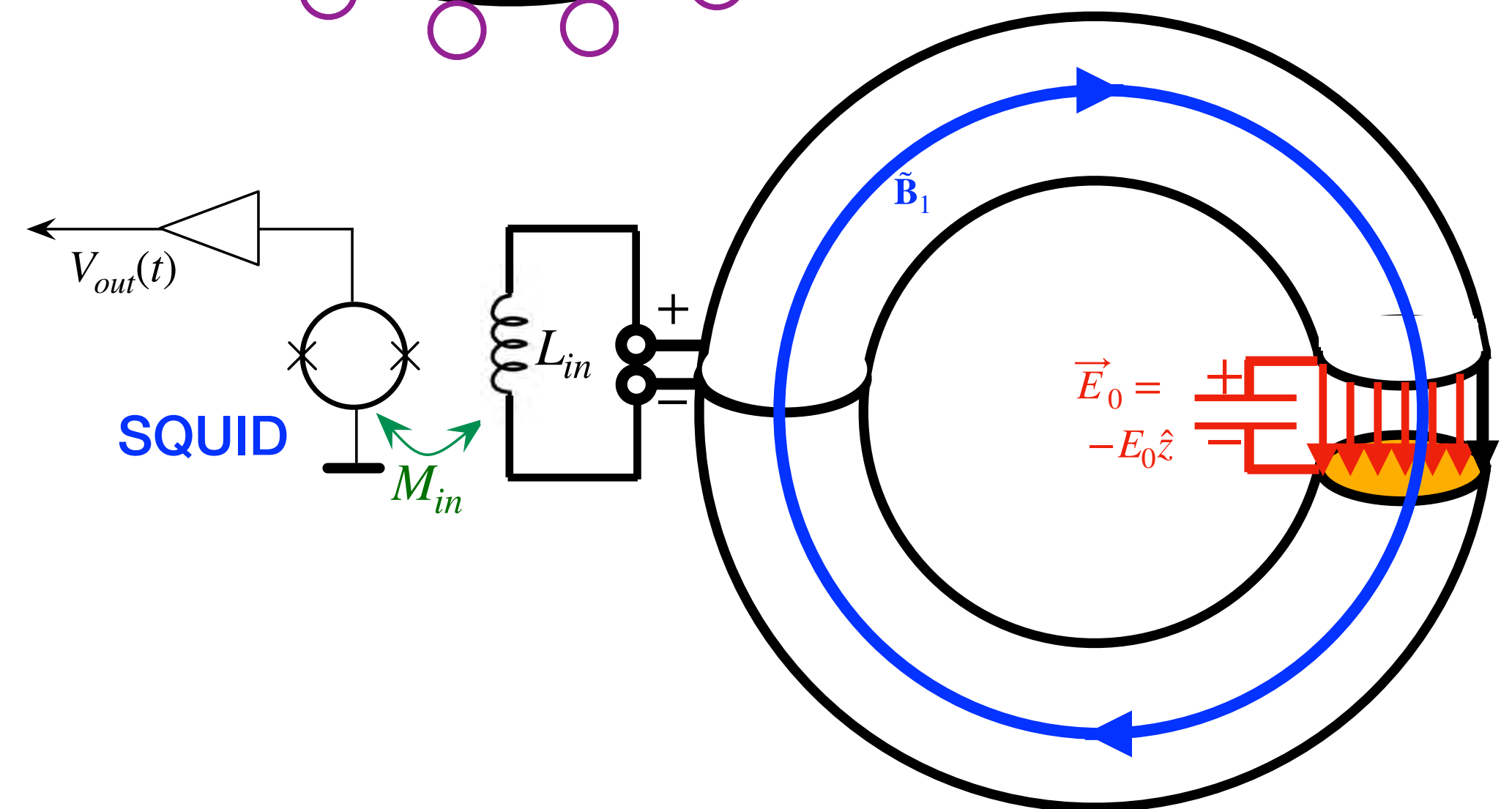
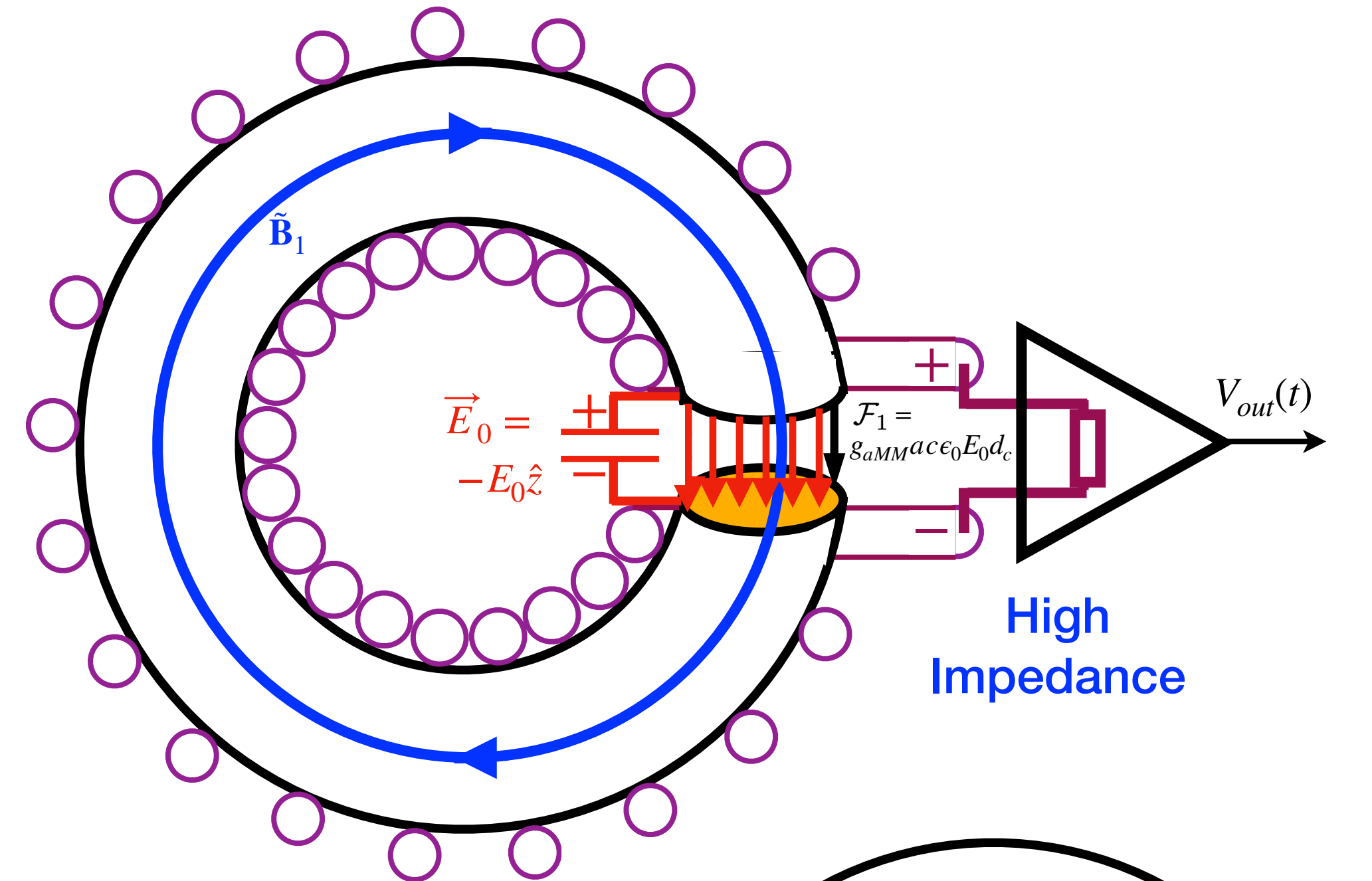
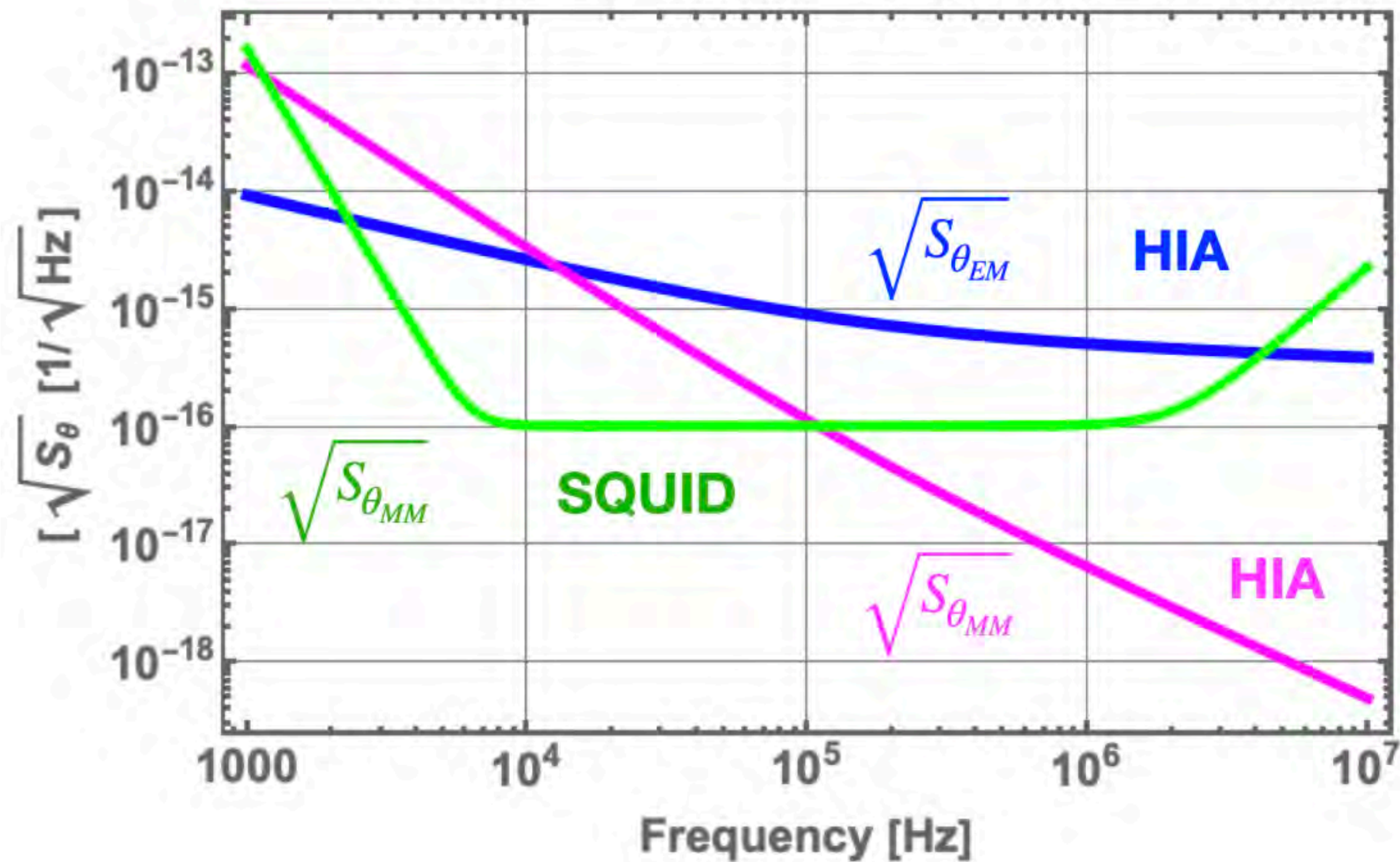


Axion Generated Magnetic Field -> Magnetic Circuit Readout Sensitive to g_{aMM}

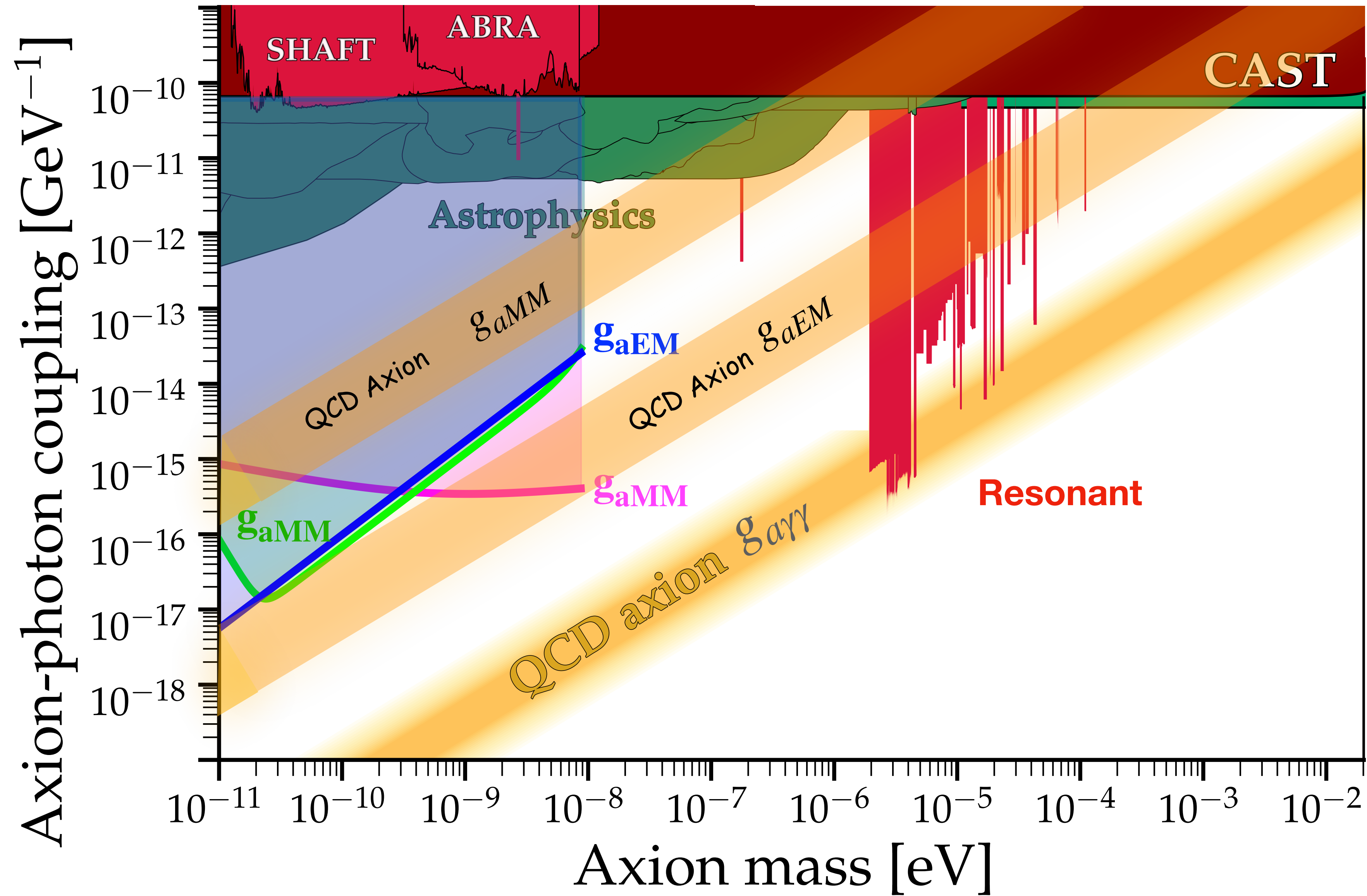
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Low-Mass Sensitivity to the QCD Axion



18 days of continuous data taking

SCALAR DARK MATTER: ELECTROMAGNETIC TECHNIQUES

PHYSICAL REVIEW D **106**, 055037 (2022)

Searching for scalar field dark matter using cavity resonators and capacitors

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³*ARC Centre of Excellence for Dark Matter Particle Physics, Centre for Astrophysics and Supercomputing, Swinburne University of Technology, John St, Hawthorn VIC 3122, Australia*

$$g_{aEM} \equiv g_{\phi\gamma\gamma}$$

The Team



Professor Michael Tobar
Director—QDM Lab, EQUUS Node Director, CDM Node Director



Dr Maxim Goryachev
Lecturer—Research Intensive, EQUUS Chief Investigator, CDM Chief Investigator



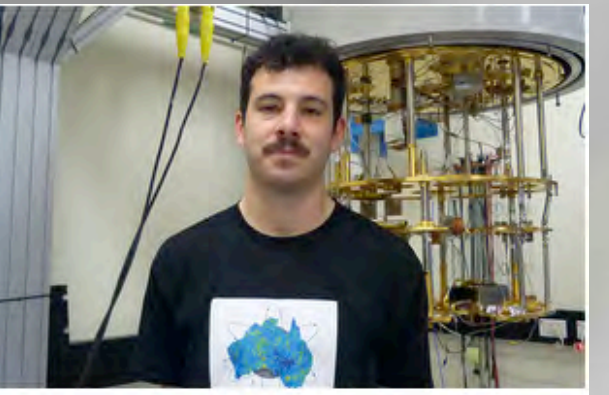
Dr Ben McAllister
Forrest Prospect Fellow



Professor Alexey Veryaskin
Adjunct Professor



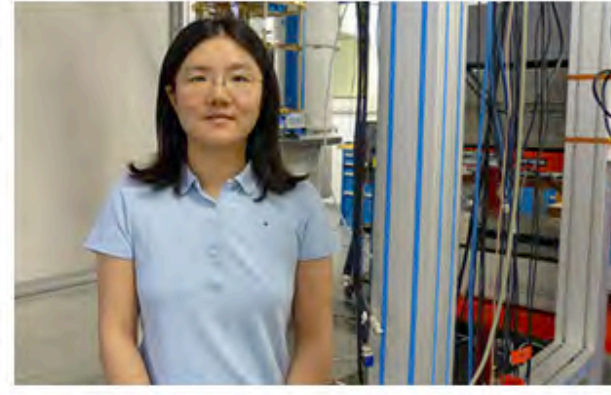
Graeme Flower
Research Associate



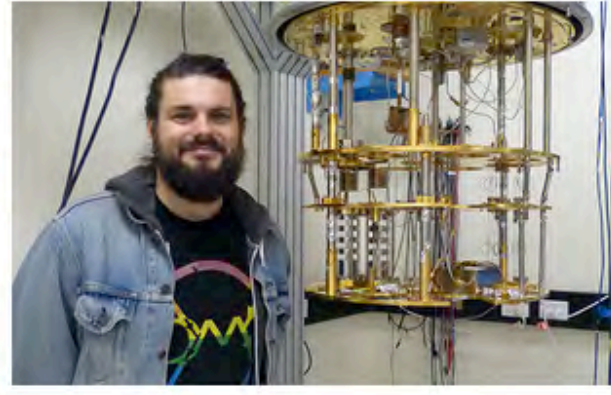
Will Campbell
PhD



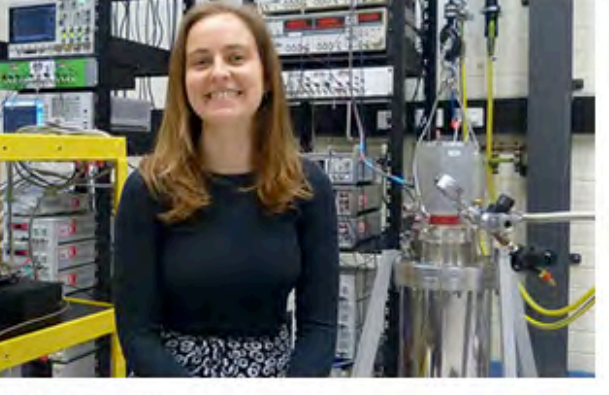
Winthrop Professor Eugene Ivanov
Senior Principle Research Fellow



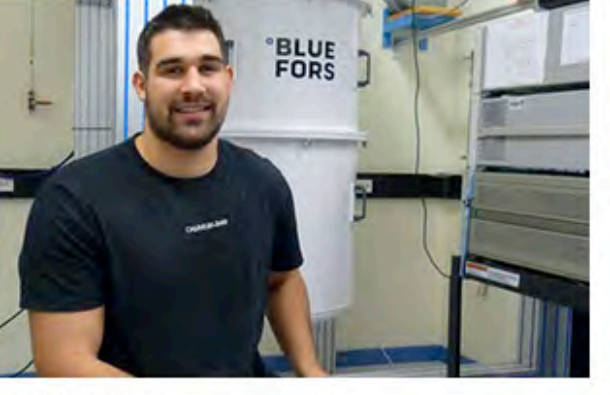
Dr Cindy Zhao
Deborah Jin Fellow—EQUUS



Dr Jeremy Bourhill
Postdoctoral Research Associate



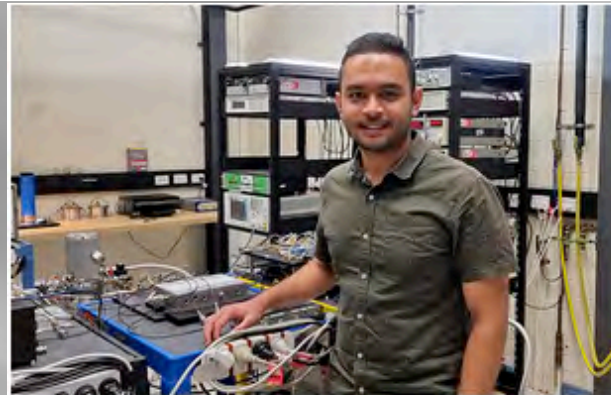
Catriona Thomson
PhD



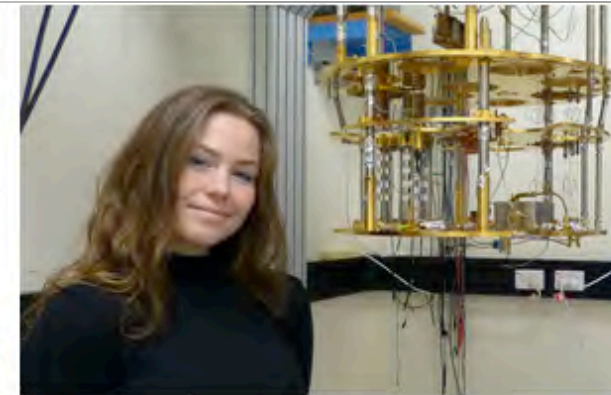
Aaron Quiskamp
PhD



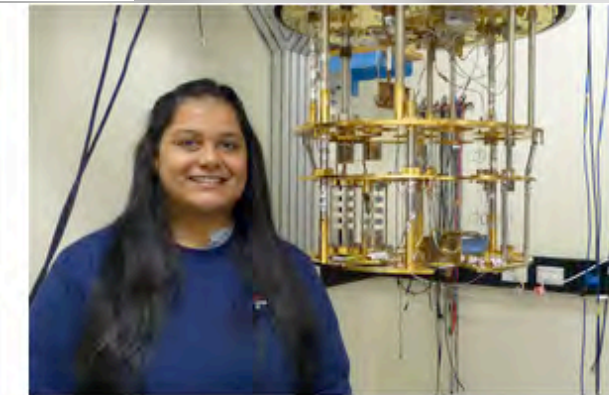
Elina Hartman
PhD



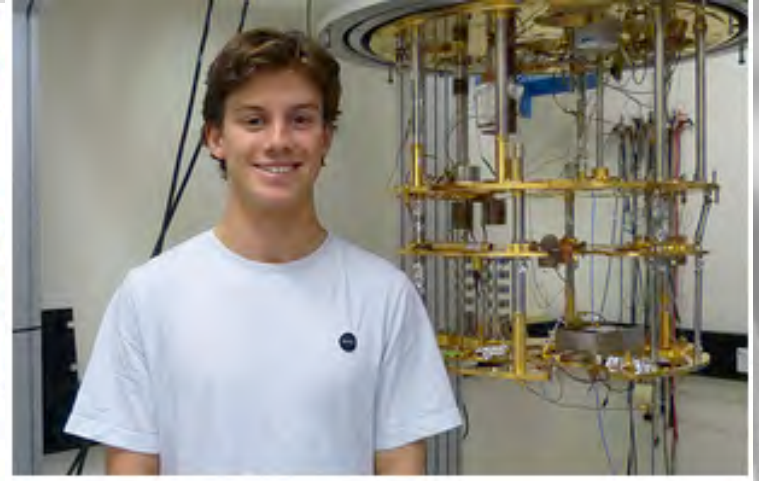
Steven Samuels
PhD



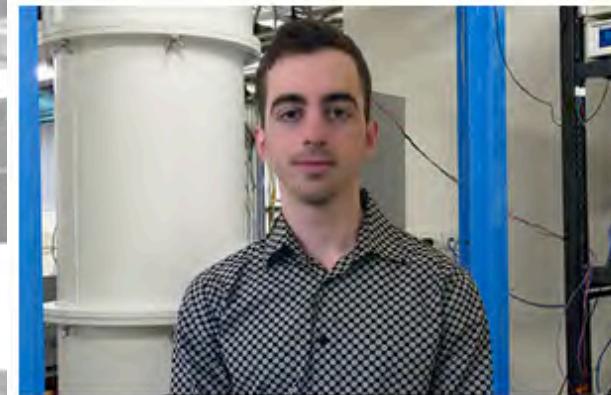
Emma Paterson
BPhil (Hons) Honours Dissertation



Sonali Parashar
Master of Physics—Coursework and Dissertation



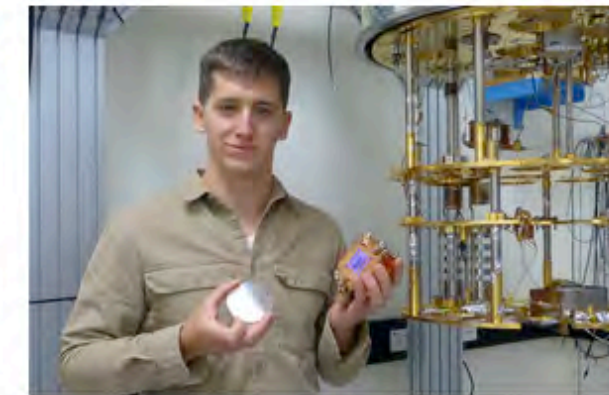
Hugh Mitchell
BPhil (Hons) Honours Placement



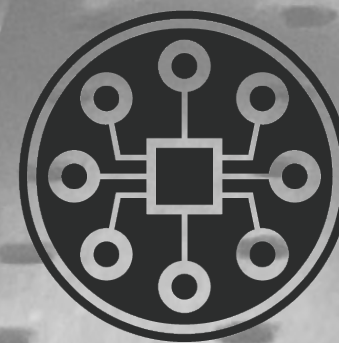
Michael Hatzon
BPhil (Hons) Honours Dissertation



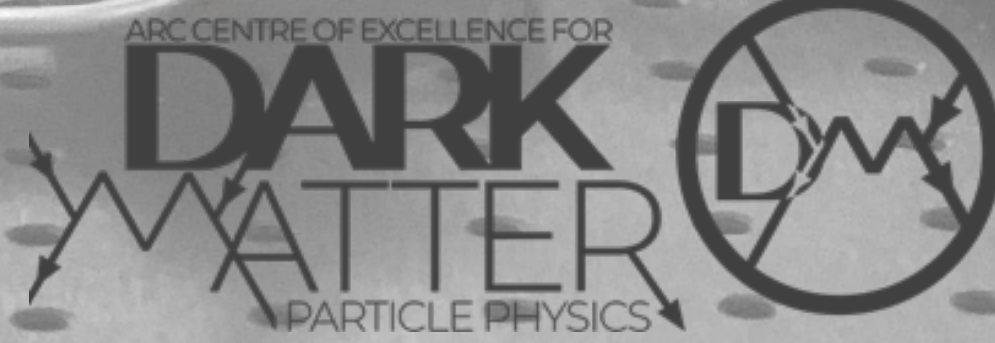
Robert Crew
BPhil (Hons) Honours Dissertation



Jerzy Cuper
Visiting Research Student, Warsaw University of Technology
1 October 2022 - 1 October 2023



EQUUS
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